Longest Palindromic Subsequence

Given a string s, find the longest palindromic subsequence's length in s. You may assume that the maximum length of s is 1000.

Example 1: Input:
"bbbab"
Output: 4
One possible longest palindromic subsequence is "bbbb". Example 2: Input:
"cbbd"
Output:

One possible longest palindromic subsequence is "bb".

2

```
dp[i][j]: the longest palindromic subsequence's length of substring(i, j)
State transition:
dp[i][j] = dp[i+1][j-1] + 2 \text{ if s.charAt}(i) == s.charAt(j)
otherwise, dp[i][j] = Math.max(dp[i+1][j], dp[i][j-1])
Initialization: dp[i][i] = 1
 public class Solution {
     public int longestPalindromeSubseq(String s) {
         int[][] dp = new int[s.length()][s.length()];
         for (int i = s.length() - 1; i >= 0; i--) {
             dp[i][i] = 1;
             for (int j = i+1; j < s.length(); j++) {</pre>
                 if (s.charAt(i) == s.charAt(j)) {
                     dp[i][j] = dp[i+1][j-1] + 2;
                 } else {
                     dp[i][j] = Math.max(dp[i+1][j], dp[i][j-1]);
                 }
             }
         }
         return dp[0][s.length()-1];
     }
 }
```

Top bottom recursive method with memoization

```
public class Solution {
    public int longestPalindromeSubseq(String s) {
        return helper(s, 0, s.length() - 1, new Integer[s.length()][s.length()]);
    }
    private int helper(String s, int i, int j, Integer[][] memo) {
        if (memo[i][j] != null) {
            return memo[i][j];
        if (i > j)
                        return 0;
        if (i == j)
                        return 1;
        if (s.charAt(i) == s.charAt(j)) {
            memo[i][j] = helper(s, i + 1, j - 1, memo) + 2;
        } else {
            memo[i][j] = Math.max(helper(s, i + 1, j, memo), helper(s, i, j - 1, j))
memo));
        return memo[i][j];
    }
}
```

written by tankztc original link here

```
public class Solution {
    public int longestPalindromeSubseq(String s) {
        int len = s.length();
        int[][] dp = new int[len][len];
        for(int i = 0;i < len;i++){</pre>
            dp[i][i] = 1;
        //for each interval length
        for(int l = 2; l <= len; l++) {</pre>
            //for each interval with the same length
            for(int st = 0;st <= len-l;st++){</pre>
                 int ed = st+l-1;
                 //if left end equals to right end or not
                 dp[st][ed] = s.charAt(st) == s.charAt(ed)? dp[st+1][ed-1]+2 : Math.
max(dp[st+1][ed], dp[st][ed-1]);
            }
        return dp[0][len-1];
}
```

written by Ryan777 original link here

Solution 3

Idea:

```
dp[i][j] = longest palindrome subsequence of s[i to j].

If s[i] == s[j], dp[i][j] = 2 + dp[i+1][j-1]

Else, dp[i][j] = max(dp[i+1][j], dp[i][j-1])
```

Rolling array O(2n) space

Further improve space to O(n)

written by jedihy original link here