

# QCBM Documentation

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## 1 Model Description

**Training Data:** Gaussian Distribution

**Pre-training:** Particle number distribution

**Number of qubits:** 4

**Loss Function:** MMD Loss

**Kernel:** Gaussian RBF kernel

**Accuracy:** KL Divergence

**Learning rate:** 1.0

**Optimizer:** optax.adam

## 2 Observations

### 2.1 Pre-Training

QCBM Circuit = RZ + IsingXY gates

| S.No | Initialized State                        | Model            |
|------|--|------------------|
| 1    | ['0000', '0001', '0011', '0111', '1111'] | Converges        |
| 2    | ['0000', 'randomly chosen' × 3, '1111']  | Doesn't Converge |
| 3    | ['0000', 'superposition', '1111']        | Converges        |

Table 1: Model convergence based on different initial states

## 2.2 Superposition Pre - Training

| S.No | qcbm circuit           | Layers                | min KL Div | Model     |
|------|------------------------|-----------------------|------------|-----------|
| 1    | RZ + Ising XY          | $\geq 2\text{layers}$ | $10^{-1}$  | Converges |
| 2    | RX + RZ + CNOT         | $\geq 3\text{layers}$ | $10^{-4}$  | Converges |
| 3    | RY + RZ + CNOT         | $\geq 3\text{layers}$ | $10^{-3}$  | Converges |
| 4    | RZ + IsingZZ           | $\geq 1\text{layer}$  | $10^0$     | Converges |
| 5    | RZ + IsingXY + IsingZZ | $\geq 2\text{layers}$ | $10^{-4}$  | Converges |

Table 2: Model convergence based on different qcbm circuits

## 2.3 No Pre - Training

| S.No | qcbm circuit           | Layers                | min KL Div | Model            |
|------|------------------------|-----------------------|------------|------------------|
| 1    | RZ + Ising XY          | -                     | $10^{38}$  | Doesn't Converge |
| 2    | RX + RZ + CNOT         | $\geq 3\text{layers}$ | $10^{-4}$  | Converges        |
| 3    | RY + RZ + CNOT         | $\geq 3\text{layers}$ | $10^{-3}$  | Converges        |
| 4    | RZ + IsingZZ           | -                     | $10^{38}$  | Doesn't Converge |
| 5    | RZ + IsingXY + IsingZZ | -                     | $10^{38}$  | Doesn't Converge |

Table 3: Model convergence based on different qcbm circuits

## 3 Conclusion

Pre-training the QCBM circuit with the superposition of all the states with amplitudes corresponding to the particle number distribution of the target Gaussian distribution doesn't help the model when using the maximally entangling circuit i.e., with CNOT gates. Whereas using IsingXY or IsingZZ

entangling operation instead requires pre-training for the model to converge.

The other conclusion is that the QCBM circuit with RZ and IsingZZ operations in the presence of pre-training leads to very minimal to no learning.