

← Homework for Module 3 Part 1

Quiz, 9 questions

1  
point

1.  
(Difficulty: ★) Write out the phase of the complex numbers  $a_1 = 1 - j$  and  $a_2 = -1 - j$ .

Express the phase in degrees and separate the two phases by a single white space. Each phase should be a number in the range  $[-180, 180]$ .

-45 -135

1  
point

2.  
(Difficulty: ★) Let  $W_N^k = e^{-j\frac{2\pi}{N}k}$  and  $N > 1$ . Then  $W_N^{N/2}$  is equal to...

- ☒ -1
- ☐ 1
- ☐ -j
- ☐  $e^{-j(2\pi/N)+N}$

1  
point

3.  
(Difficulty: ★) Which of the following signals (continuous- and discrete-time) are periodic signals?

Note that  $t \in \mathbb{R}$  and  $n \in \mathbb{Z}$ .

- ☒  $x(t) = t - \text{floor}(t)$ .
- ☐  $x[n] = \sin(n)$ .
- ☒  $x[n] = (-1)^n$ .
- ☐  $x(t) = (t + 2\pi)^2$ .
- ☒  $x(t) = \cos(2\pi f_0 t + \phi)$  with  $f_0 \in \mathbb{R}$ .

2  
points

4.  
(Difficulty: ★ ★ ★) Choose the correct statements from the choices below.

- ☐ Consider the length- $N$  signal  $x[n] = (-1)^n$  with  $N$  odd. Then  $X[k] = 0$  for all  $k$  except  $k = N/2$
- ☐ If we apply the DFT twice to a signal  $x[n]$ , we obtain the time reversed signal, i.e.  $x[N - n]$ .
- ☒ Consider the length- $N$  signal  $x[n] = \cos(\frac{2\pi}{N}Ln + \phi)$  where  $L$  is an integer and  $L \neq N/2$ . Then 
$$X[k] = \begin{cases} \frac{N}{2}e^{i\phi} & \text{for } k = L \\ \frac{N}{2}e^{-i\phi} & \text{for } k = N - L \\ 0 & \text{otherwise} \end{cases}$$

1  
point

5.  
(Difficulty: ★) Consider the Fourier basis  $\{\mathbf{w}^k\}_{k=0,\dots,N-1}$ , where  $\mathbf{w}^k[n] = e^{-j\frac{2\pi}{N}nk}$  for  $0 \leq n \leq N-1$ .

Select the correct statement below.

- ☐ The orthogonality of the vectors depends on the length  $N$  of the elements of the basis.

☐

The elements of the basis are orthonormal:



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$$\langle \mathbf{w}^i, \mathbf{w}^j \rangle = \begin{cases} 1 & \text{for } i = j \\ 0 & \text{otherwise.} \end{cases}$$

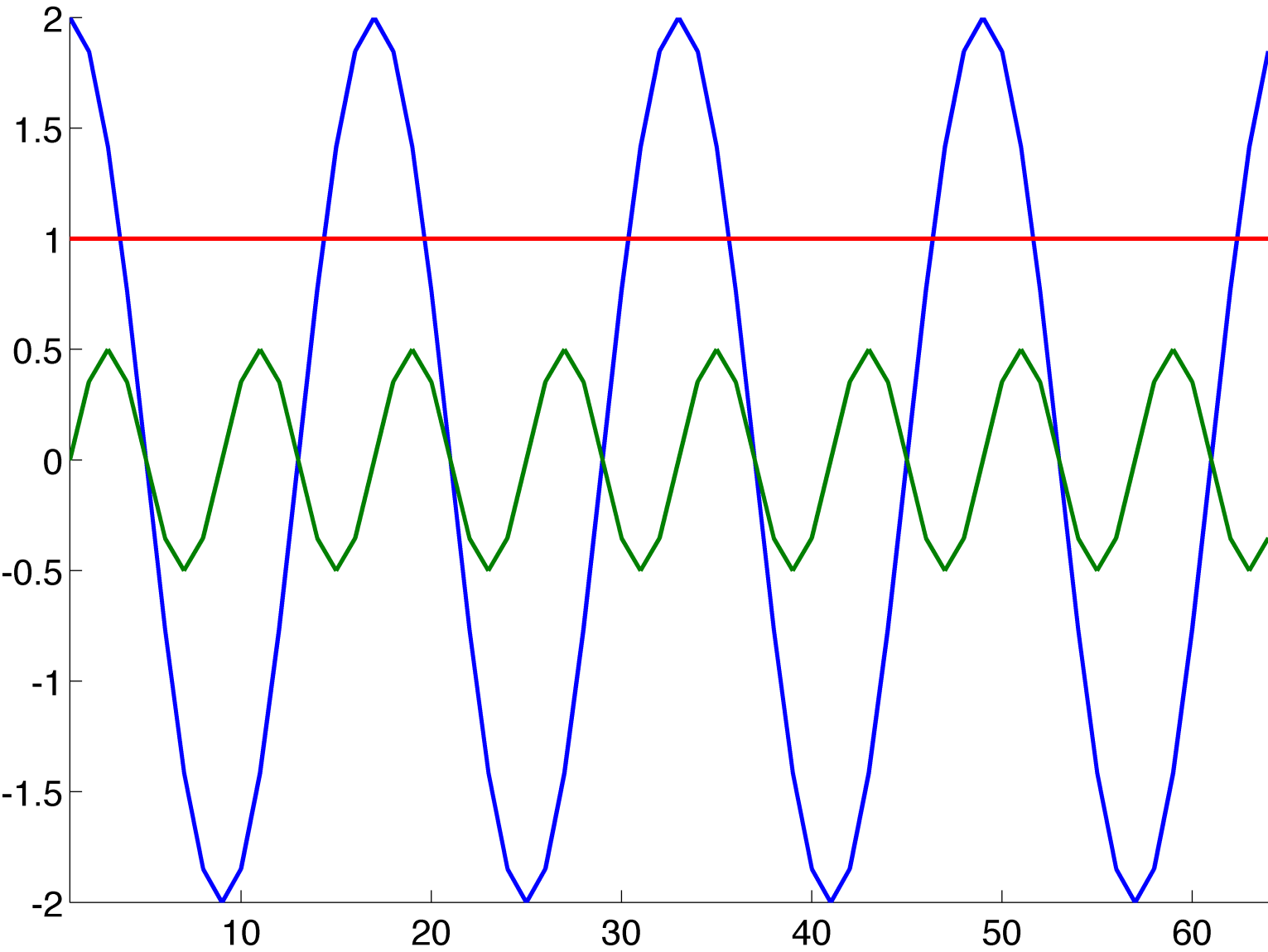
☒

The elements of the basis are orthogonal:

$$\langle \mathbf{w}^i, \mathbf{w}^j \rangle = \begin{cases} N & \text{for } i = j \\ 0 & \text{otherwise.} \end{cases}$$

1 point

6.



(Difficulty: ★★) Consider the three sinusoids of length  $N = 64$  as illustrated in the above figure; note that the signal values are shown from  $n = 0$  to  $n = 63$ .

Call  $y_1[n]$  the blue signal,  $y_2[n]$  the green and  $y_3[n]$  the red. Further, define  $x[n] = y_1[n] + y_2[n] + y_3[n]$ .

Choose the correct statements from the list below. Note that the capital letters indicate the DFT vectors.

- ☐
- $$Y_3[k] = \begin{cases} 32 & \text{for } k = 0 \\ 32 & \text{for } k = 64 \\ 0 & \text{otherwise} \end{cases}$$
- ☒
- $$Y_1[k] = \begin{cases} 64 & \text{for } k = 4, 60 \\ 0 & \text{otherwise} \end{cases}$$
- ☒
- $$Y_2[k] = \begin{cases} -16j & \text{for } k = 8 \\ 16j & \text{for } k = 56 \\ 0 & \text{otherwise} \end{cases}$$
- ☐
- $$\|x\|_2^2 = 200 \text{ and } \|X\|_2^2 = 12800$$

1 point

7.

(Difficulty: ★ ★ ★) Consider the length- $N$  signal

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where  $M$  and  $L$  are integer parameter with  $0 < L \leq N - 1, 0 < M \leq N$ .

Choose the correct statements among the choices below.

- ☐ In general, it will be easier to compute the norm of the signal  $\|\mathbf{x}\|_2$  in the Fourier domain, using the Parseval's Identity.
- ☒ Consider the circularly shifted signal  $y[n] = x[(n - D) \bmod N]$ . In the Fourier domain, the two DFTs related by a modulation factor:  $Y[k] = X[k]e^{-j2\pi k \frac{D}{N}}$ .
- ☒ If  $M = N$  and  $2L < N$ , the signal has exactly  $L$  periods for  $0 \leq n < N$
- ☒ The DFT  $X[k]$  has two elements different from zero if  $N = M$  and  $N \neq 2L$ .

1 point

8.  
(Difficulty: ★) Consider an orthogonal basis  $\{\phi_i\}_{i=0,\dots,N-1}$  for  $\mathbb{R}^N$ . Select the statements that hold for any vector  $\mathbf{x} \in \mathbb{R}^N$ .

- ☐  $\|\mathbf{x}\|_2^2 = \sum_{i=0}^{N-1} |\langle x, \phi_i \rangle|^2$ .
- ☒  $\|\mathbf{x}\|_2^2 = \frac{1}{P} \sum_{i=0}^{N-1} |\langle x, \phi_i \rangle|^2$  if and only if  $\|\phi_i\|_2^2 = P \forall i$ .
- ☐  $\|\mathbf{x}\|_2^2 = \frac{1}{P} \sum_{i=0}^{N-1} |\langle x, \phi_i \rangle|^2$   
if and only if  $\|\phi_i\|_2 = P \forall i$ .
- ☒  $\|\mathbf{x}\|_2^2 = \sum_{i=0}^{N-1} |\langle x, \phi_i \rangle|^2$  if and only if  $\|\phi_i\|_2 = 1 \forall i$ .

1 point

9.  
(Difficulty: ★★) Pick the correct sentence(s) among the following ones regarding the DFT  $\mathbf{X}$  of a signal  $\mathbf{x}$  of length  $N$ , where  $N$  is odd.

Remember the following definitions for an arbitrary signal (asterisk denotes conjugation):

hermitian-symmetry:  $x[0]$  real and  $x[n] = x[N - n]^*$  for  $n = 1, \dots, N - 1$ .

hermitian-antisymmetry:  $x[0] = 0$  and  $x[n] = -x[N - n]^*$  for  $n = 1, \dots, N - 1$ .

- ☐ If the signal  $\mathbf{x}$  is hermitian-symmetric, then the DFT  $\mathbf{X}$  is also hermitian-symmetric.
- ☐ If the signal  $\mathbf{x}$  is purely real, then the DFT  $\mathbf{X}$  is purely imaginary.
- ☒ If the signal  $\mathbf{x}$  is hermitian-symmetric, then its DFT is real.
- ☒ If the signal  $\mathbf{x}$  is hermitian antisymmetric, then its DFT  $\mathbf{X}$  is purely imaginary.

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