



Homework for Module 3 Part 1

Quiz, 9 questions

1
point

1.
(Difficulty: ★) Write out the phase of the complex numbers $a_1 = 1 - j$ and $a_2 = -1 - j$.

Express the phase in degrees and separate the two phases by a single white space. Each phase should be a number in the range $[-180, 180]$.

-45 -135

1
point

2.
(Difficulty: ★) Let $W_N^k = e^{-j\frac{2\pi}{N}k}$ and $N > 1$. Then $W_N^{N/2}$ is equal to...

- ☒ -1
- ☐ 1
- ☐ -j
- ☐ $e^{-j(2\pi/N)+N}$

1
point

3.
(Difficulty: ★) Which of the following signals (continuous- and discrete-time) are periodic signals?

Note that $t \in \mathbb{R}$ and $n \in \mathbb{Z}$.

- ☒ $x(t) = \cos(2\pi f_0 t + \phi)$ with $f_0 \in \mathbb{R}$.
- ☒ $x[n] = (-1)^n$.
- ☐ $x[n] = \sin(n)$.
- ☐ $x(t) = (t + 2\pi)^2$.
- ☒ $x(t) = t - \text{floor}(t)$.

2
points

4.
(Difficulty: ★ ★ ★) Choose the correct statements from the choices below.

- ☐ If we apply the DFT twice to a signal $x[n]$, we obtain the signal itself scaled by N , i.e. $Nx[n]$.
- ☒ Consider the length- N signal $x[n] = (-1)^n$ with N even. Then $X[k] = 0$ for all k except $k = N/2$
- ☐ Consider the length- N signal $x[n] = \cos(\frac{2\pi}{N}Ln + \phi)$, where N is even and $L = N/2$. Then
$$X[k] = \begin{cases} \frac{N}{2}e^{j\phi} & \text{for } k = L \\ 0 & \text{otherwise} \end{cases}.$$

1
point

5.
(Difficulty: ★) Consider the Fourier basis $\{\mathbf{w}^k\}_{k=0,\dots,N-1}$, where $\mathbf{w}^k[n] = e^{-j\frac{2\pi}{N}nk}$ for $0 \leq n \leq N-1$.

Select the correct statement below.

- ☐ The orthogonality of the vectors depends on the length N of the elements of the basis.
- ☒ The orthogonality of the vectors depends on the length N of the elements of the basis.



The elements of the basis are orthogonal:



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$\langle \mathbf{w}^i, \mathbf{w}^j \rangle = \begin{cases} 1 & \text{for } i = j \\ 0 & \text{otherwise.} \end{cases}$

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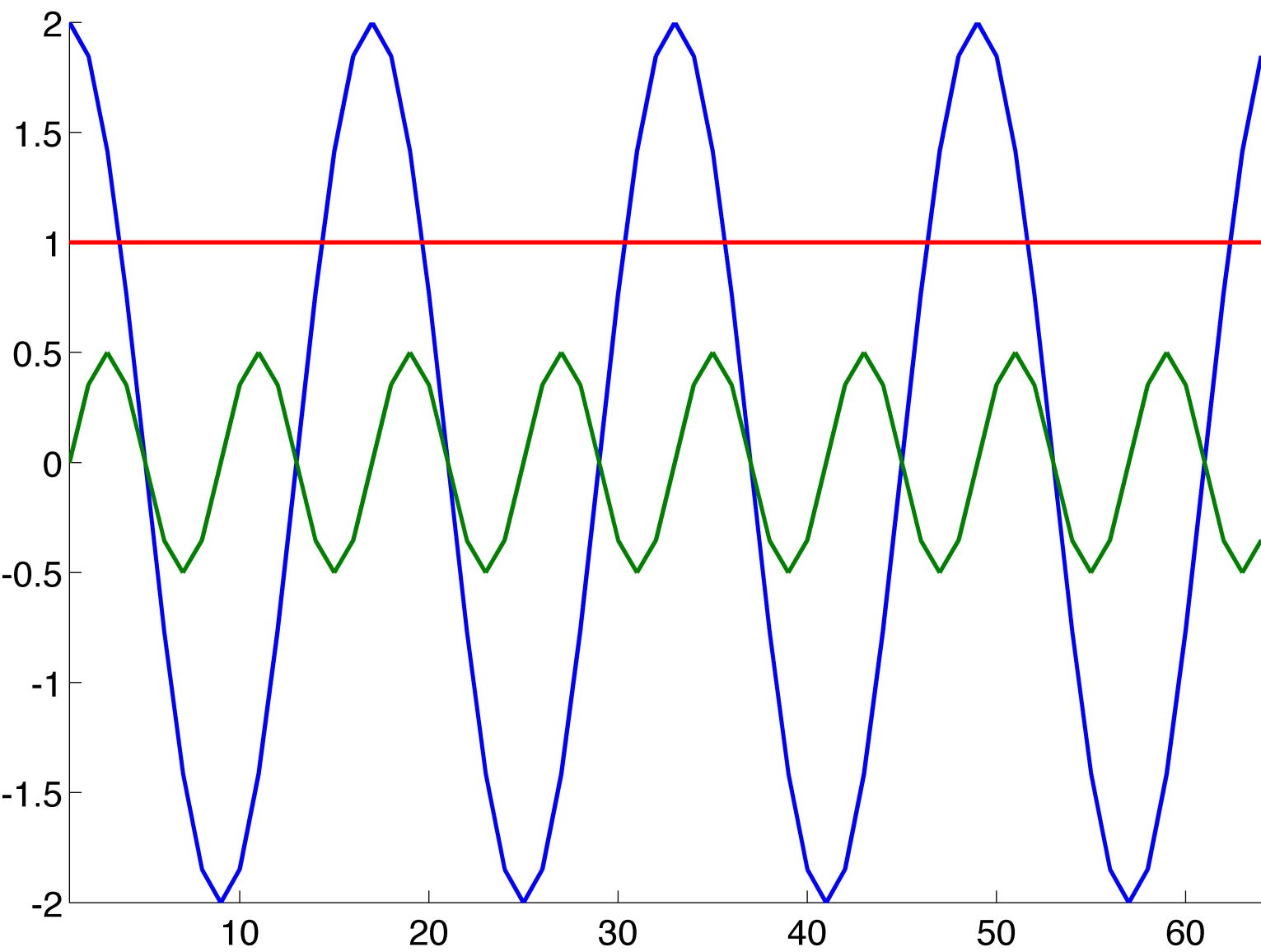


The elements of the basis are orthonormal:

$\langle \mathbf{w}^i, \mathbf{w}^j \rangle = \begin{cases} 1 & \text{for } i = j \\ 0 & \text{otherwise.} \end{cases}$

1 point

6.



(Difficulty: ★★) Consider the three sinusoids of length $N = 64$ as illustrated in the above figure; note that the signal values are shown from $n = 0$ to $n = 63$.

Call $y_1[n]$ the blue signal, $y_2[n]$ the green and $y_3[n]$ the red. Further, define $x[n] = y_1[n] + y_2[n] + y_3[n]$.

Choose the correct statements from the list below. Note that the capital letters indicate the DFT vectors.



$Y_3[k] = \begin{cases} 32 & \text{for } k = 0 \\ 32 & \text{for } k = 64 \\ 0 & \text{otherwise} \end{cases}$



$Y_2[k] = \begin{cases} -16j & \text{for } k = 8 \\ 16j & \text{for } k = 56 \\ 0 & \text{otherwise} \end{cases}$



$Y_1[k] = \begin{cases} 2 & \text{for } k = 4, 60 \\ 0 & \text{otherwise} \end{cases}$



$\|x\|_2^2 = \|X\|_2^2 = 12800$

1 point

7.

(Difficulty: ★ ★ ★) Consider the length- N signal

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where M and L are integer parameter with $0 < L \leq N - 1, 0 < M \leq N$.

Choose the correct statements among the choices below.

- ☒ If $M = N$ and $2L < N$, the signal has exactly L periods for $0 \leq n < N$
- ☐ In general, it will be easier to compute the norm of the signal $\|\mathbf{x}\|_2$ in the Fourier domain, using the Parseval's Identity.
- ☒ The DFT $X[k]$ has two elements different from zero if $N = M$ and $N \neq 2L$.
- ☒ Consider the circularly shifted signal $y[n] = x[(n - D) \bmod N]$. In the Fourier domain, the two DFTs related by a modulation factor: $Y[k] = X[k]e^{-j2\pi k \frac{D}{N}}$.

1 point

8.
(Difficulty: ★) Consider an orthogonal basis $\{\phi_i\}_{i=0,\dots,N-1}$ for \mathbb{R}^N . Select the statements that hold for any vector $\mathbf{x} \in \mathbb{R}^N$.

- ☐ $\|\mathbf{x}\|_2^2 = \sum_{i=0}^{N-1} |\langle x, \phi_i \rangle|^2$.
- ☒ $\|\mathbf{x}\|_2^2 = \sum_{i=0}^{N-1} |\langle x, \phi_i \rangle|^2$ if and only if $\|\phi_i\|_2 = 1 \ \forall i$.
- ☒ $\|\mathbf{x}\|_2^2 = \frac{1}{P} \sum_{i=0}^{N-1} |\langle x, \phi_i \rangle|^2$ if and only if $\|\phi_i\|_2^2 = P \ \forall i$.
- ☐ $\|\mathbf{x}\|_2^2 = \frac{1}{P} \sum_{i=0}^{N-1} |\langle x, \phi_i \rangle|^2$
if and only if $\|\phi_i\|_2 = P \ \forall i$.

1 point

9.
(Difficulty: ★★) Pick the correct sentence(s) among the following ones regarding the DFT \mathbf{X} of a signal \mathbf{x} of length N , where N is odd.

Remember the following definitions for an arbitrary signal (asterisk denotes conjugation):

hermitian-symmetry: $x[0]$ real and $x[n] = x[N - n]^*$ for $n = 1, \dots, N - 1$.

hermitian-antisymmetry: $x[0] = 0$ and $x[n] = -x[N - n]^*$ for $n = 1, \dots, N - 1$.

- ☒ If the signal \mathbf{x} is hermitian-symmetric, then its DFT is real.
- ☐ If the signal \mathbf{x} is hermitian-symmetric, then the DFT \mathbf{X} is also hermitian-symmetric.
- ☐ If the signal \mathbf{x} is purely real, then the DFT \mathbf{X} is purely imaginary.
- ☒ If the signal \mathbf{x} is hermitian antisymmetric, then its DFT \mathbf{X} is purely imaginary.

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