

Consider mathematical dynamical system model, described by following differential equations:

$$\dot{v} = -5 \cdot v + \omega + 0.1 \cdot |F|,$$

$$\dot{\omega} = v - \omega,$$

where  $F$  [Nm] is a force acting on the system, which we can manipulate,  $\omega$  [rad/s] is angular velocity and  $v$  [m/s] is linear velocity, which we measure.

### Tasks:

- 1) Decide state variables, inputs, and outputs of the system.
- 2) Implement mathematical model in Simulink. Do not forget about static nonlinearities.
- 3) Create linear approximation of the model in an operating point, where  $v = 0 \text{ m/s}$ :
  - a) Find analytical condition for the operating point to be an equilibrium. **(0.2 b)**
  - b) Linearize the system in said point:
    - i) Consider the static nonlinearity at the system input **(0.2 b)**
    - ii) Neglect the static nonlinearity at the system input **(0.2 b)**
  - c) Compare responses of the original and the linearized model. Discuss suitable signal shapes for validating your linearization.
    - i) Consider the static nonlinearity at the system input **(0.2 b)**
    - ii) Neglect the static nonlinearity at the system input **(0.2 b)**
- 4) Create linear approximation of the model in an operating point, where  $v = 10 \text{ m/s}$ :
  - a) Find analytical condition for the operating point to be an equilibrium. **(0.2 b)**
  - b) Linearize the system in said point:
    - i) Consider the static nonlinearity at the system input **(0.2 b)**
    - ii) Neglect the static nonlinearity at the system input **(0.2 b)**
  - c) Compare responses of the original and the linearized model. Discuss suitable signal shapes for validating your linearization.
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### Tasks:

Repeat tasks 1 – 4