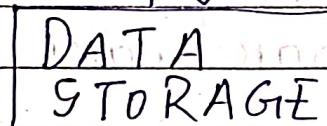
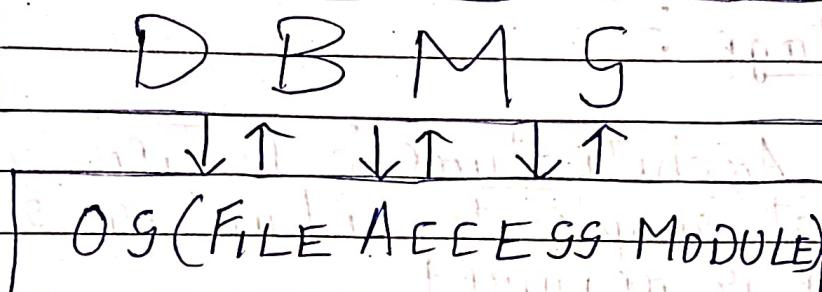
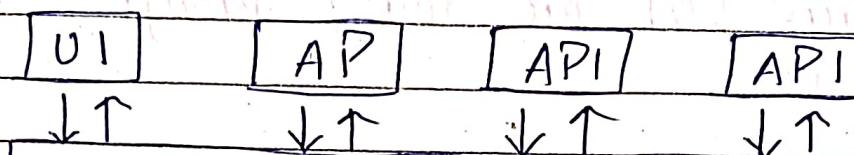


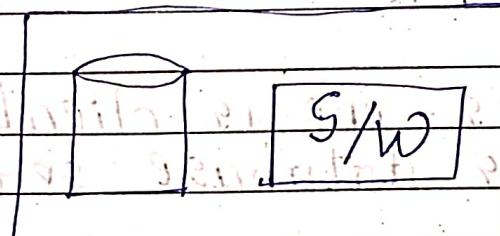
- \* DBMS → i) Collection of inter-related data.
- ii) Set of software tools / program which access & process the data in an easy & effective manner.



### \* key Features of Database

- ⇒ Data storage & retrieval
- ⇒ Concurrency control
- ⇒ Backup & recovery
- ⇒ Data integrity & security

### \* 1-Tier Architecture



M I

- ⇒ In 1-Tier Architecture, The database is directly available to the user.
- ⇒ Client & server present in same machine
- ⇒ To learn SQL or doing project in machine.

### Advantage :-

- Simple Architecture :- 1-Tier architecture is most simple to set up as single machine is required.
- Easy to implement
- Cost-effective
- No additional hardware is required.

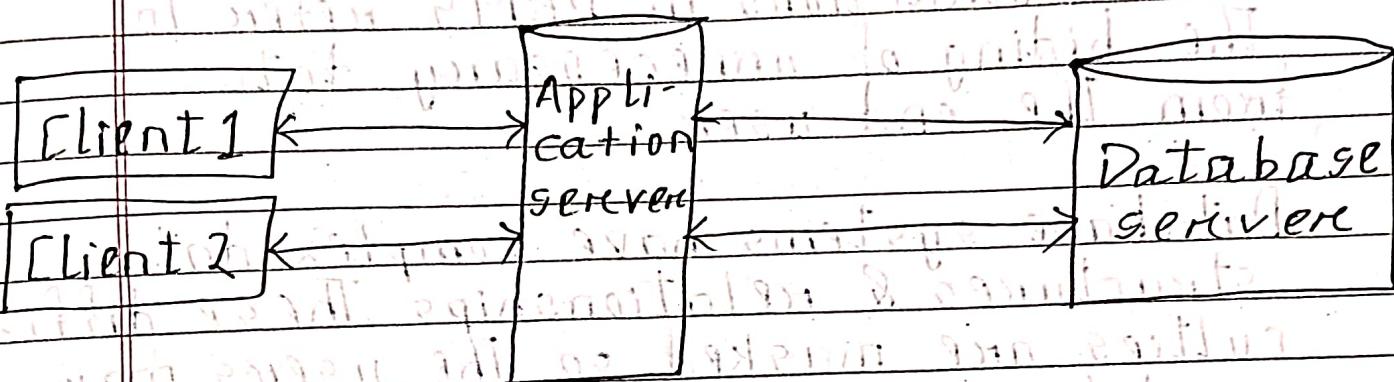
### \* 2-Tier Architecture

#### Advantage :-

- ⇒ Easy to access :- 2 Tier architecture makes easy access to the database which makes fast retrieval
- ⇒ Scalable :- Can scale the database easily by adding clients or hardware.
- ⇒ Low cost than 3 Tier
- Specifically 2 tiers - one is client layer & second is database server layer

→ Client layer providing interface or API & fetch data from database API using 'jdbc', 'odbc' to connect with database.

### \* 3-Tier Architecture



Advantages:

→ Enhanced Scalability: Scalability is enhanced due to distributed deployment of application server.

→ Data integrity: 3-Tier architecture maintains data integrity. Since there is a middle layer between client & server data corruption can be avoided.

Security: Improves security. This model prevent direct interaction of the client with server thereby reducing access to unauthorised data.

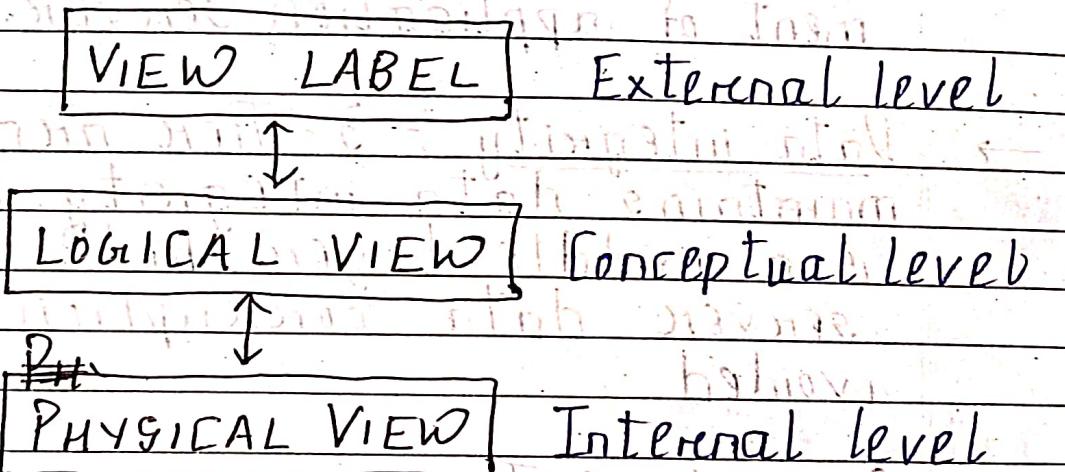
## Disadvantages

→ Complex than 1-Tier & 2-Tier

## \* Data Abstraction & Data Independence

⇒ Data abstractions in DBMS refer to The hiding of unnecessary data from The end user.

⇒ Database systems have complex data structures & relationships. These difficulties are masked so The users may readily access the data & only The relevant section of The database is made accessible Through The data abstraction.



05/09/24

Page No. \_\_\_\_\_

Date: / /

## Physical / Internal Level

⇒ Lowest level of abstractions for DBMS.

How data is stored.

- Data structures for storing data.
- Database access mechanisms.
- Define physical storage.
- Data will be stored in blocks.
- B-Tree or Hash are defined in this level.

## Logical / Conceptual Level

⇒ Next higher level are intermediate.

⇒ It describes which data are stored & how they are related.

■ Defines what table, what will be attributes & how the tables are connected.

■ Primary key ( $P_k$ ) & Foreign key ( $F_k$ ) are defined.

■ Internal data structures (DS) are hidden.

## View / External Level

⇒ This is the top level.

- ⇒ Various views are present & it is the part of database.
- ⇒ Facilitates numerous views of a single database.
- Eg.: Student view, Faculty view, Accountant view.

## Data Independence

- ⇒ Primary goal of data abstractions in DBMS is to obtain data independence in order to save time & money while modifying or altering a database.
- ⇒ Ability to change the schema without impacting the programmers & applications to be rewritten.
- ⇒ Data is isolated from programs so that changes to the data do not influence program.
- ⇒ Data independence are 2 types:
  - Physical level
  - Logical level

a) Physical level Independence

⇒ It refers to the ability to change the physical schema without changing the logical/conceptual schema.

b) Logical level Independence

⇒ This feature is referred to has the ability to change the logical schema without changing the external schema or application programs.

⇒ Any modifications to the conceptual representation of the data wouldn't affect user's perception of the data.

FILE PROCESSING SYSTEM

DBMS

1) The problem of redundancy & inconsistency are present in FPS.

No redundancy & inconsistency.

2) Accessing file is not easy.

Very easy in DBMS.

3) No data independence in FPS.

Data independence are present in DBMS.

4) Less Security

More Security.

## Advantages of Data Abstractions

- ⇒ It reduces the complexity for the user.
- ⇒ Increases the code reusability.
- ⇒ Increases the security aspect of the applications.

## Disadvantages of Data Abstractions

- ⇒ Might be confusing for developers as there are complexities at multiple levels of the database abstraction.
- ⇒ Whenever extra layer is there, navigation becomes challenging.

## \* Data Model

- ⇒ Data modelling is the consistency constraint of the data & modelling w.r.t. the data description.
- ⇒ Provides the conceptual tool for describing the design of database at each level of the abstractions.

## Types of Data Model

- 1) Relational Data Model
- 2) ER Model
- 3) Object based Model
- 4) Semi-structured Model
- 5) Network Data Model
- 6) Hierarchical Data Model

### 1) Relational Data Model

- ⇒ Most widely used model by DBMS.
- ⇒ It uses collection of tables for representing data & relationship.
- ⇒ Each Table is a group of rows & columns.

### 2) ER Model (Entity Relationship)

- ⇒ High level Data Model.
- ⇒ Blueprint or actual representation of data.
- ⇒ Logical representations of data as objects & relationships among them. These objects are known as entities.

### 3) Object Based Data Model

⇒ Also known as Object Oriented Table Data Model.

⇒ Object based data model is an extension of ER Model with some encapsulation, object identity.

#### 4) Semi Structured Data Model

⇒ Semi-structured modeling is the modified form of relational model.

⇒ Allows data specifications at places where the individual data item may have a different set of attributes.

⇒ Represented by XML (Extended Markup Language).

#### 5) Hierarchical Data Model

⇒ This is the old form of data model.

⇒ This model uses a tree like structure.

⇒ Each entity has a single parent.

University

Student

UG

PG

Staff

I

Teaching

Non-Teaching

Teaching

Non-Teaching

Faculty

Programmer

Executive

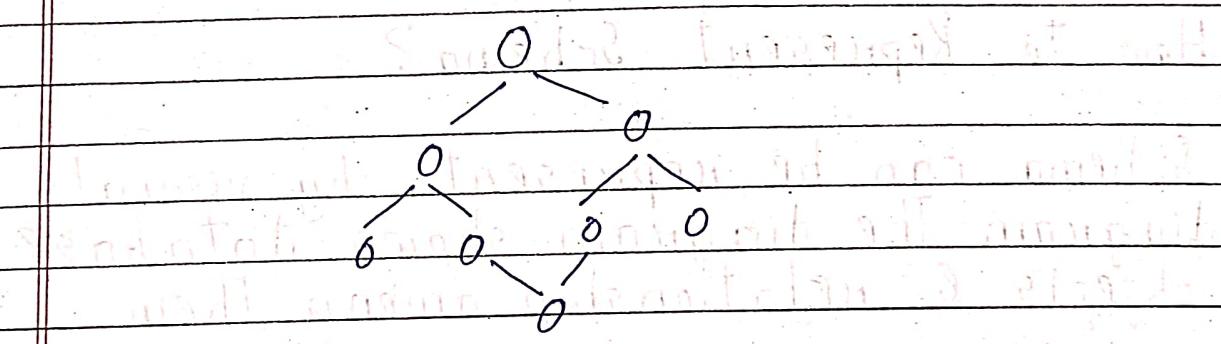
Non-executive

## 6) Network Data Model

⇒ Modified version of Hierarchical data model.

⇒ Represented by using a graph.

⇒ Unlike hierarchical model, more than one parent can exist.



## \* Data Model Schema & Instance

⇒ Overall design of a database is called schema.

⇒ A database schema is the skeleton structure of the database. It represents logical view of data.

⇒ A schema contains objects like table,

- a) Table
- b) Primary key
- c) Foreign key
- d) View
- e) Columns
- f) Datatype
- g) Stored procedure
- h) Trigger

Instance :

⇒ The data which is stored in a database at a particular moment of time is called The instance of The database.

How To Represent Schema?

Schema can be represented by visual diagram. The diagram shows database objects & relationship among them.

Why we have to draw schema and who will draw it.

Database schema drawn by database designers usually team leaders or middle level managers to help programmers whose SW will interact with database. The process of database creation is called data modelling.

Student	Roll	Name	Course	DOB
---------	------	------	--------	-----

College	College	Course name	Credit	Dept
---------	---------	-------------	--------	------

Prerequisite	Course Id	Requirement
--------------	-----------	-------------

### ER MODEL

⇒ ER Model stands for Entity Relationship model.

⇒ This model is used to define The data elements & relationships for a specified system.

⇒ The ~~be~~ diagram to represent ~~for~~ entity relationship is known as ER diagram.

### Entity

It is a Thing or object in real world.  
 It is something which has a permanent existence in an enterprise and with an entity some set of attributes are connected depending on some value.

# ER Model

Entity

Weak

Strong

Attributes

Simple Vs

Multivalue

Simple Vs

Composite

Stored Vs

Derived

key Vs Non-

key

Relation

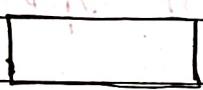
1 to 1

1 to many

Many to 1

Many to many

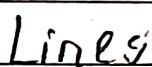
Symbols



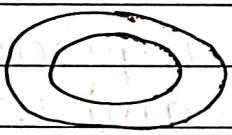
→ Entity



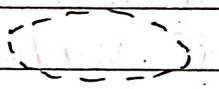
→ Attribute



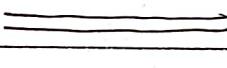
→ Link bet<sup>n</sup> Entity & Relationship



→ Multi valued Attribute



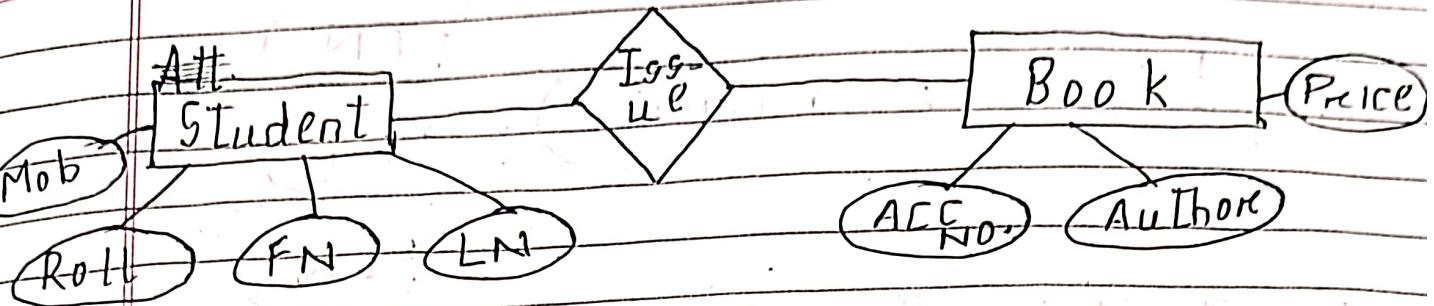
→ Derived attribute



→ Merging bet<sup>n</sup> relationship & entity



→ Weak entity



### Attributes

#### 1) Single Vs Multivalue

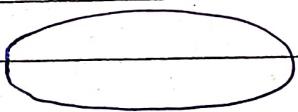
→ Single → One value for that attribute.  
 Multiple value → More than one value for attribute.

#### → Representation :-

Multivalue



Single



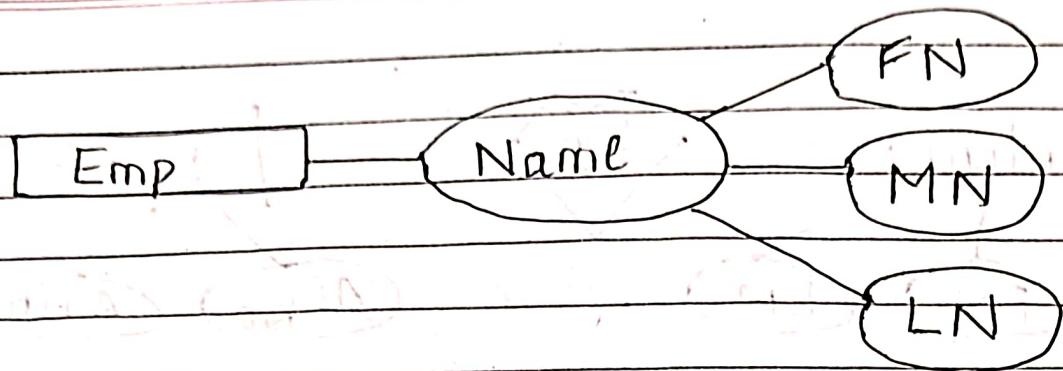
#### 2) Simple Vs Composite

→ Composite → Can be divided into further part.

Simple → Cannot be divided further.

Eg. Name → Composite  
 Address → Composite

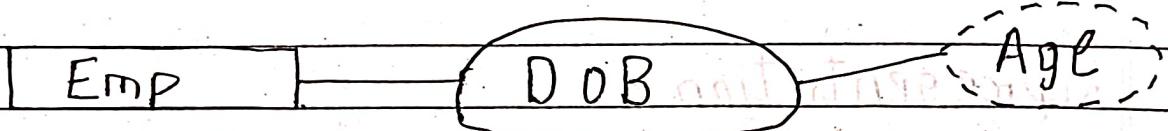
Gender → Simple  
 Salary → Simple



### 3) Stored Vs Derived

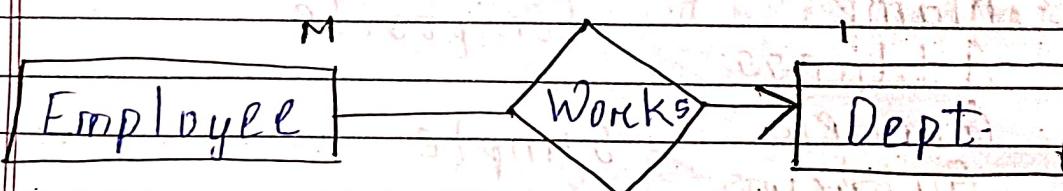
- Stored → Data are explicitly entered & saved
- Derived → Calculated from other attributes

Eg. DOB —> Age



### Relationship

- Relationship can be defined as how 2 entities can be associated with each other.
- It can be one-to-one, one-to-many, many-to-many & many-to-many.



## \* Cardinality

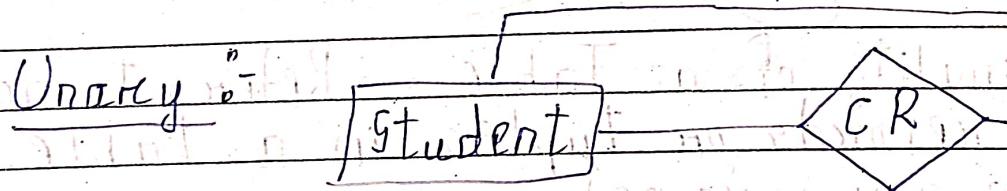
⇒ Mapping cardinality refers to the relationship b/w 2 entities in a database.

⇒ It specifies how many instances of one entity can be linked to instance of another entity - 1:1, 1:m, m:1, m:n.

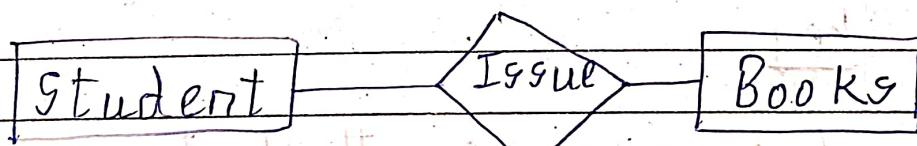
## \* Degree of a Relationship

⇒ It defines no. of entity that associate in a relationship.

1) Unary:



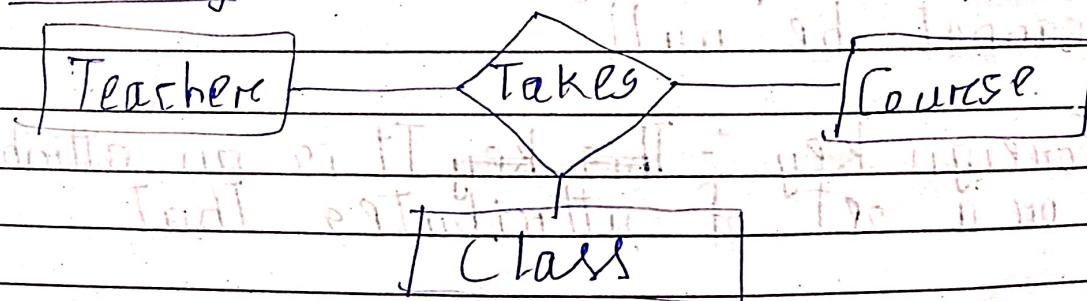
2) Binary:



→ Consists of 2 entities that are related.

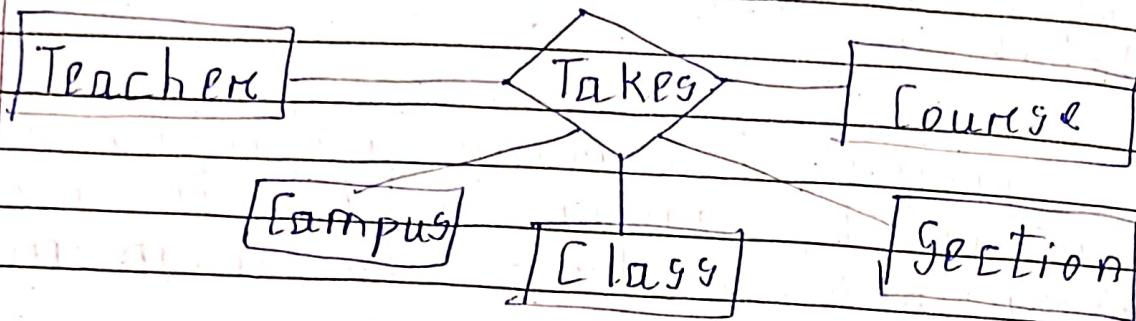
→ Relationship is connected with 2 entities

3) Tertiary:



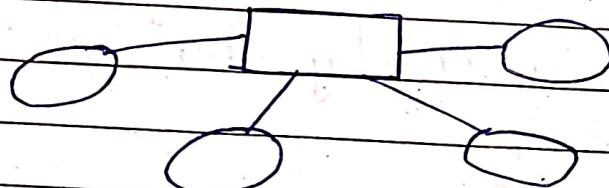
## 4) N-ARY:

n type of entities are connected with  
1 relation



~~25/09/24~~

- Degree of a Table → How many attributes are there in a table (column)



Degree = 4

- Cardinality of a Table → Refers to no. of records or tuples in a table (how many rows)

key

- One or more attributes which can uniquely identify tuple.

Primary key : This key uniquely identifies each row & value of that attribute cannot be null.

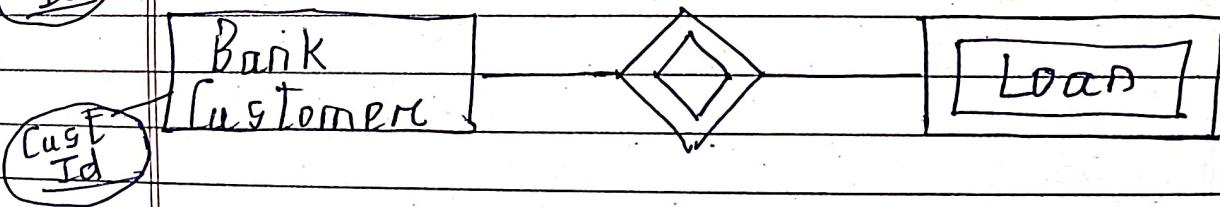
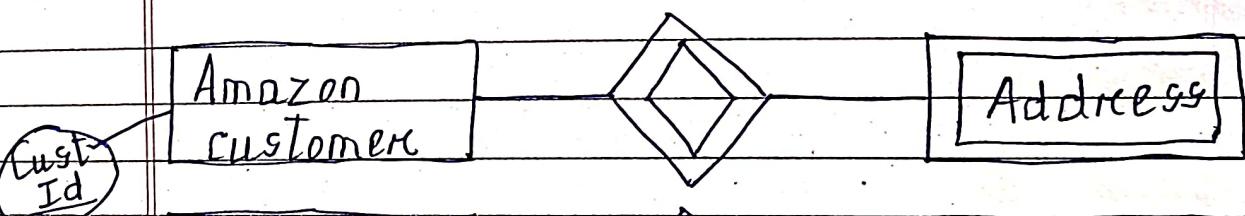
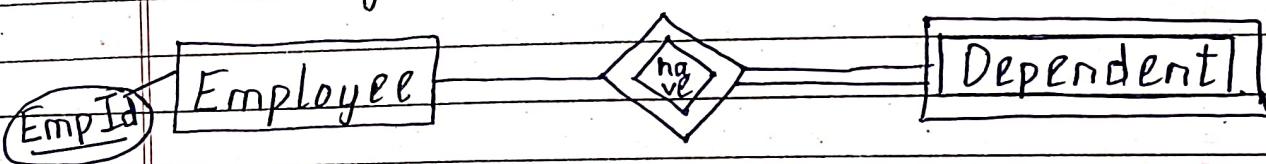
Foreign key : This key It is an attribute or a set of attributes that

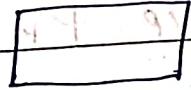
- References to a primary key of some table or any relationship.
- It maintains Referential integrity.

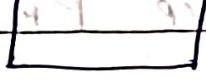
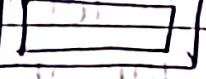
### Entity

Strong Entity : It is ~~do~~ not dependent on any other entity in the schema. It will always have Pk & represented by a rectangle.

Weak Entity : It is dependent on strong entity. Unlike strong entity, weak entity does not have a Pk. Relation bet<sup>n</sup> Weak entity & Strong entity is represented by double diamond. Weak entity represented by double rectangle.



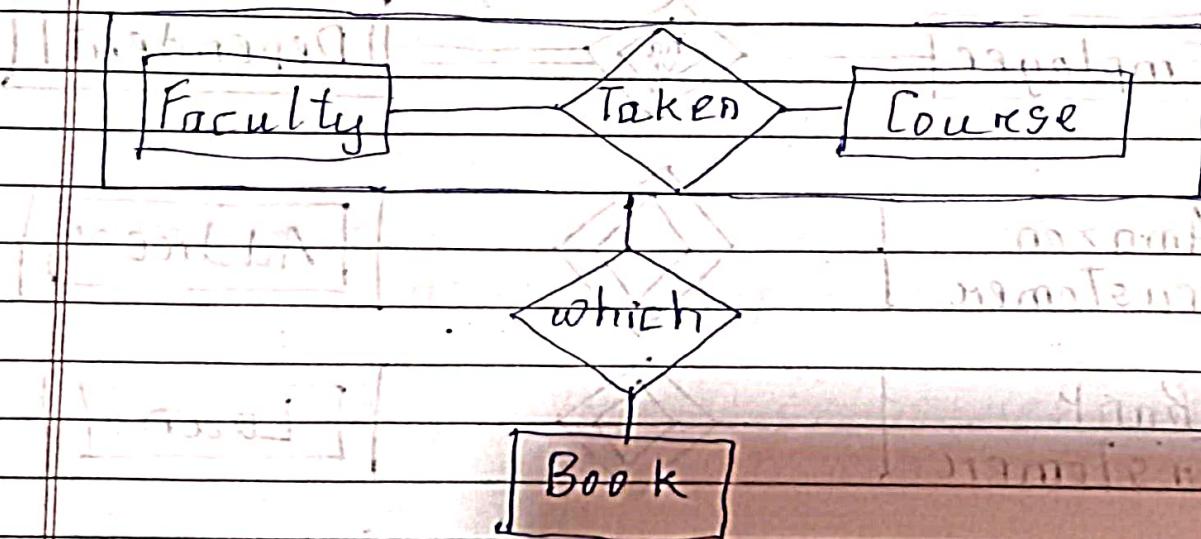
	Strong Entity	Weak Entity
1	Has Primary Key	Has partial discrimination key
2	Not dependent on other entity	Depend on strong entity.
3	Represented by 	Represented by 

	Strong Entity	Weak Entity
1	Has Primary key	Has partial discrimination key
2	Not dependent on other entity	Depend on strong entity.
3	Represented by 	Represented by 

### ~~03/00/24~~ Extended ER Diagram

- Generalisation
- Specialization
- Aggregation

### Aggregation

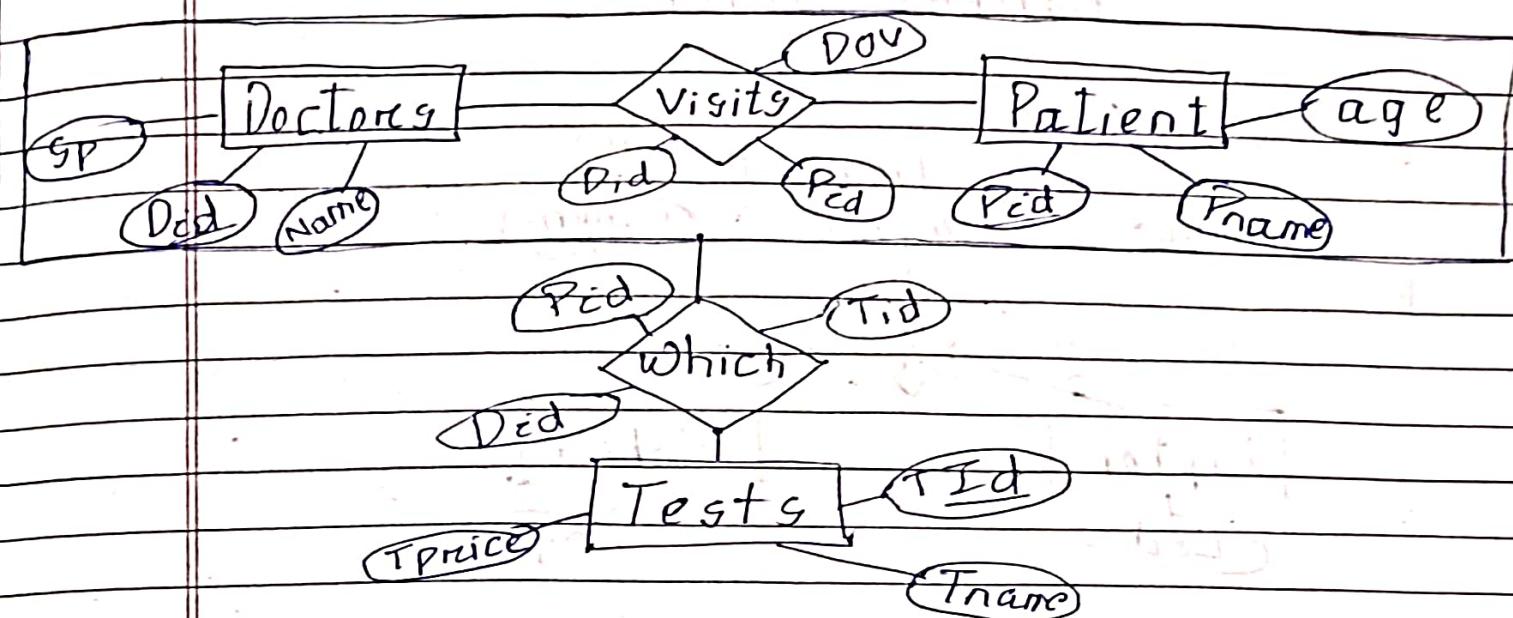


⇒

Aggregation in DBMS is a process of combining 2 or more entities do not make sense on their own without applying the aggregation process.

⇒

In order to create aggregation b/w 2 entities which cannot be used for its individual quantities rather a relationship is established & the resultant product is created into new entities.



Generalization & Sp

It is known as extended ER-diagram

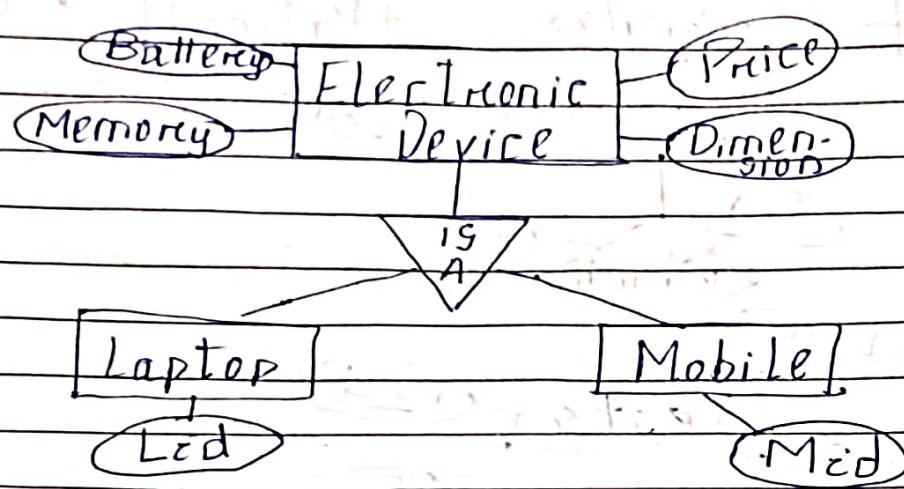
- For generalization, it is a bottom up approach

- In generalization, lower level Func's are combined to form higher level entities

- In The generalized process, we simplify The entities.

Mobile (Mobile-id, Dimension, Memory, Battery, Price)

Laptop (Laptop-id, Dimension, Memory, Battery, Price)



Rule Table → Leaf node

- Specialization means opp. of generalization

- Broken into smaller parts to simplify it further.

- It is a top down approach.

## Relational Algebra

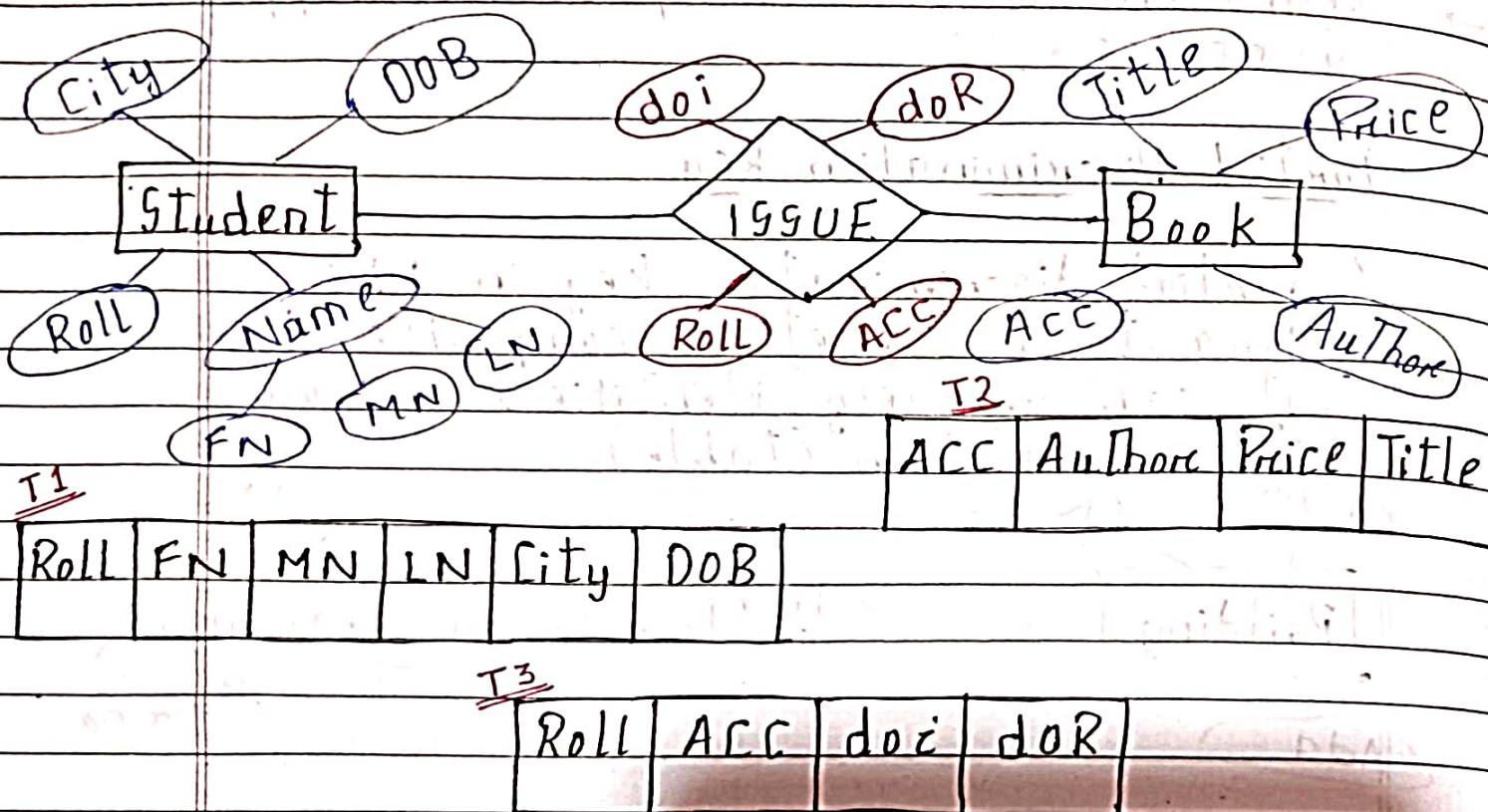
⇒ It is a procedural language for manipulating relations.

### Fundamental Operators

Unary → Select, Project, Rename  
 Binary → Union, set diff, cartesian product

### Secondary Operators

Intersection, Natural join, Division & Assignment



## 1) Select Operator ( $\sigma$ )

Chooses the subset of rows from the relation that satisfies the given condition mentioned in the syntax of selection.

`select * from student (query)`

Relation  $\rightarrow \sigma(\text{student})$

`select * from student where city = "kolkata".`

Relation  $\rightarrow \sigma(\text{student})$   
city = "kolkata"

`select * from books where price > 500`

Relation  $\rightarrow \sigma(\text{Book})$   
price > 500

Note: Select in query selects the column from the given table but the 'select' ( $\sigma$ ) operator selects the row of the same.

## 2) Projection Operator ( $\pi$ )

Chooses the specific column from a table while excluding the other columns from a selected table.

select \* from issue where doc > 1-Sep-2024

Relation  $\rightarrow \pi_{\text{roll}} (\sigma_{\text{issue}} (\text{doc} > 1-\text{Sep}-2024))$

select roll from student where city = "kolkata"  
or city = "BBGR"

Relation  $\rightarrow \pi_{\text{roll}} (\sigma_{\text{student}} (\text{city} = \text{"kolkata"} \vee \text{city} = \text{"BBGR"}))$

### 3) Join Operators ( $\bowtie$ )

Combine the tables according to the cond<sup>n</sup>

Eg.

P	Q	R
P <sub>1</sub>	Q <sub>1</sub>	R <sub>1</sub>
P <sub>2</sub>	Q <sub>2</sub>	R <sub>2</sub>

M	N
M <sub>1</sub>	N <sub>1</sub>
M <sub>2</sub>	N <sub>2</sub>

P	Q	R	M	N
P <sub>1</sub>	Q <sub>1</sub>	R <sub>1</sub>	M <sub>1</sub>	N <sub>1</sub>
P <sub>1</sub>	Q <sub>1</sub>	R <sub>1</sub>	M <sub>2</sub>	N <sub>2</sub>
P <sub>2</sub>	Q <sub>2</sub>	R <sub>2</sub>	M <sub>1</sub>	M <sub>1</sub>
P <sub>2</sub>	Q <sub>2</sub>	R <sub>2</sub>	M <sub>2</sub>	N <sub>2</sub>

Find FN, city of student who issued books after 1 Sep 2024

A-  $\pi_{FN, city, issue\_roll} (\sigma_{issue\_date > 1 Sep 2024} (student \bowtie issue))$   
 $student\_roll = issue\_roll$

29/10/24

1) Find the student roll no. & books they have issued

A- select roll, from issue ACC from issue  
 $\pi_{roll, ACC} (\sigma_{ACC} (issue))$

2) Find out the roll no. who issued the book ADO10.

A- select roll from issue where ACC = "ADO10"  
 $\pi_{roll} (\sigma_{ACC = "ADO10"} (issue))$

3) Find the roll no. & ACC who issued the books after 1 Sep 2024.

A- select roll, ACC from issue where date >  
 $1 Sep 2024$

$\pi_{roll, ACC} (\sigma_{date > '1 Sep 2024} (issue))$

4) Find out ACC, title of the books which author's name is kanit kari.

A- select ACC, title from book where author = "kanit kari"

$\pi ( \sigma (Book) )$   
ACC, title(Author = "kanit kari")

5) Find roll, FN who issue the book A0010.

A- select student.roll, FN from student, issue where student.roll = issue.roll  
and ACC = "A0010"

$\pi ( \sigma (Student \times Issue) )$   
student.roll, ACC = "A0010"  $\wedge$   
FN student.roll = issue.roll

6) Find student roll & city who issue book after 1st Sep 2024.

A- select student.roll, city from student, issue where date > 1 Sep 2024 and  
student.roll = issue.roll

$\pi ( \sigma (Student \times Issue) )$   
student.roll, student.roll = issue.roll  $\wedge$   
city issue. ACC = b

7) Find student roll, city who issue the book of kanit kare.

A- select student.roll, city from student, issue, book where student.roll = issue.roll and issue.ACC = book.ACC and author = "kanit kare".

$\pi$  (student  $\times$  Issue  $\times$  Book)  
 student.roll = issue.roll  $\wedge$   
 student.roll issue.ACC = book.ACC  $\wedge$  author = "kanit kare"  
 city

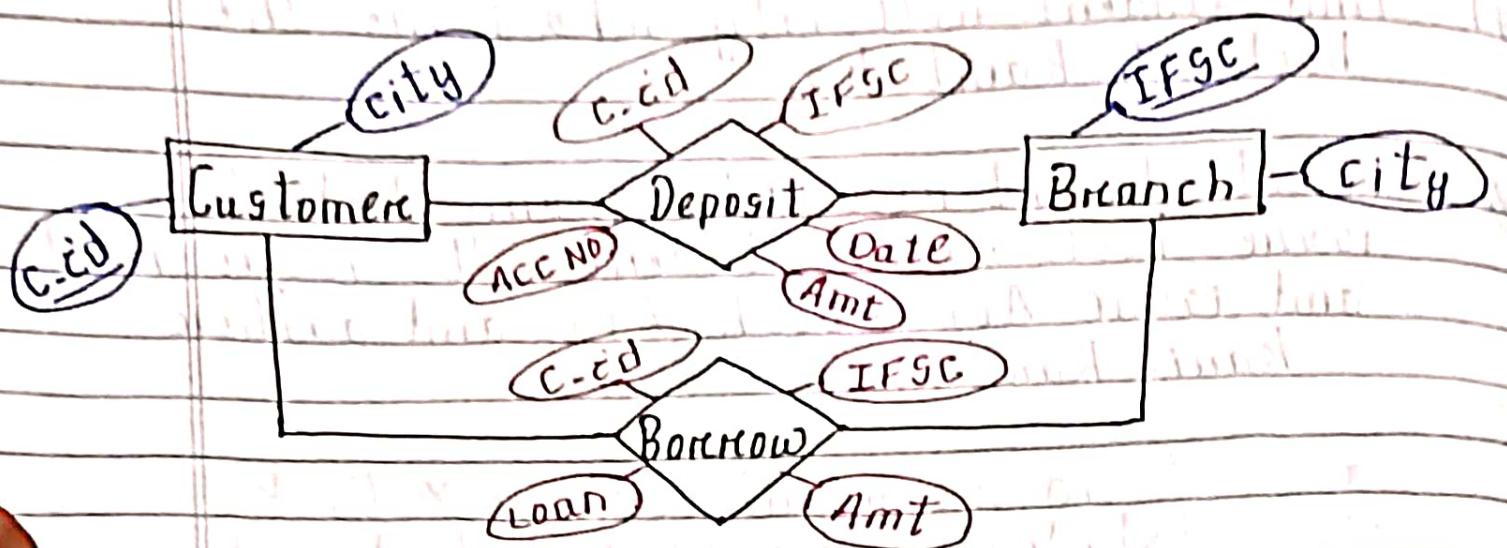
8) Find the author of the book which is issued by students of Calcutta & Jamshedpur.

A- select book.author from student, issue, book where student.roll = issue.roll and issue.ACC = book.ACC and city = "Calcutta" and city = "Jamshedpur".

$\pi$  (student  $\times$  Issue  $\times$  Book)  
 student.roll = issue.roll  $\wedge$   
 issue.ACC = book.ACC  $\wedge$   
 city = "CALCUTTA"  $\wedge$  city = "JAMSHEDPUR"

07/11/24

Page No. / /  
Date: / /



## Total Tables

- 1) Deposit (**C-id**, **IFSC**, **ACC NO**, **Date**, **Amt**)
- 2) Branch (**IFSC**, **city**)
- 3) Customer (**C-id**, **city**)
- 4) Borrow (**C-id**, **IFSC**, **Loan**, **Amt**)

- 1) list all data from deposit.  
A-  $\delta$  (Deposit)
- 2) list all data from borrow where amount is greater than 4000.  
A-  $\delta$  (Borrow)  
amt > 4000
- 3) List the ACC no & amt from deposit

A-  $\pi$  (deposit)  
ACC no, amt

4) List the ACC No. & C-id from deposit who deposited more than 2000.

A-  $\pi_{ACC\text{ no.}, C\text{-id}} \sigma_{(Deposit)} (amt > 2000)$

5) Find the branch name in city BBSR & CALCUTTA.

A-  $\pi_{IFSC} \left( \begin{array}{l} \sigma_{(Branch)} \\ \text{city} = 'BBSR' \vee \\ \text{city} = 'CALCUTTA' \end{array} \right)$

6) Find the customer info where customer name is Anil.

A-  $\sigma_{Customer} (c\text{-id} = 'Anil')$

7) Find out all the customer name, who are living in same city where is branch city exist.

A-  $\pi_{c.c\text{-id}} \left( \begin{array}{l} \sigma_{Customer \times Deposit \times Branch} \\ c.c\text{-id} = d.c\text{-id} \\ d.IFSC = b.IFSC \\ c.city = b.city \end{array} \right)$

8) List customer name, amount whence branch city = Mumbai. <sup>min balance</sup>

A-  $\pi \left( \sigma \left( \text{Deposit} \times \text{Branch} \right) \text{deposit.b-name} = \text{branch.b-name} \wedge \text{c-name} = \text{branch.city} = 'MUMBAI' \wedge \text{amt} \right)$

select c-name, amt from Deposit, Branch  
where deposit.b-name = branch.b-name  
and branch.city = 'MUMBAI'.

9) Find out customers who have deposited but never taken loan.

A-  $\pi_{\text{c-cd}} \left( \text{Deposit} \right) - \pi_{\text{c-cd}} \left( \text{Borrow} \right)$

### Self Join

Find out all the emp\_id who are working in same dept. where Chinmay Gir is working.

A-  $\pi_{\text{M.EmpId}} \left( \sigma_M \left( \text{Emp} \right) \times \sigma_N \left( \text{Emp} \right) \right)$   
 $M.\text{dept} = N.\text{dept} \wedge N.\text{EmpId} = 'EM'$   
 $\wedge M.\text{EmpId} \neq N.\text{EmpId}$

## Set Operations

- Union
- Intersection
- Minus

### Union

- ⇒ The union operation is used to combine data from 2 relations.
- ⇒ Denoted by union ( $\cup$ ) symbol.

$R_1 \cup R_2$  is a relation that includes all tuples that are either present in  $R_1$  or  $R_2$  or in both.

### Intersection

- ⇒ The intersection operation is used to identify the rows that are common to 2 relations.
- ⇒ Denoted by ( $\cap$ ) symbol.

$R_1 \cap R_2$  is a relation that includes all tuples that are present both in  $R_1$  &  $R_2$ .

### Difference

- ⇒ The difference operation is used to identify the rows that are in one relation & not in another.

⇒ Denoted as (-) symbol.

$R_1 - R_2$  is a relation that includes all tuples that are in  $R_1$ , but not in  $R_2$

### Division Operator ( $\div$ )

⇒ The division operation creates a new relation by selecting the rows in one relation that match every row in another relation.

⇒ Denoted by ( $\div$ ) symbol.

⇒ Division operator is suited to queries that include the phrase "every" or "all" as part of the cond"

	Rollno	Cid	Troll	Cid	CName
	1	C <sub>2</sub>		C <sub>1</sub>	C++
	2	C <sub>3</sub>		C <sub>2</sub>	C#
	3	C <sub>1</sub>	Java	C <sub>3</sub>	JAVA
	3	C <sub>2</sub>		C <sub>4</sub>	PHP
	4	C <sub>3</sub>			
	3	C <sub>3</sub>			
	3	C <sub>4</sub>			

Q- List the roll no. of the student who have registered in all the courses.

$\pi$  ( $\sigma$  (Student))  
roll, rid

$\pi$  ( $\sigma$  (course))  
cid.

### Rename Operators

Denoted by  $\delta$ .

$\delta$  ( $\sigma$  (Customer))  
c.city = 'Mumbai'

A- Find out the customer name who stays  
in the same city where Anil stays -

A-	C Name	City	C Name	City	C Name	City
	Barun	Delhi	Barun	Delhi	Barun	Delhi
	Anil	BBSR	Barun	Delhi	Anil	BBSR
	Ram	BBSR	Barun	Delhi	Ram	BBSR
			Anil	BBSR	Barun	Delhi
			Anil	BBSR	Anil	BBSR
			Anil	BBSR	Ram	BBSR
			Ram	BBSR	Barun	Delhi
			Ram	BBSR	Anil	BBSR
			Ram	BBSR	Ram	BBSR

$\pi$  ( $\delta$  ( $\sigma$  (Customer)  $\times$   $\sigma$  (Customer)))

M.CName  
M.city = N.city  $\wedge$  N.Cname = 'ANIL'  
 $\wedge$  M.CName  $\neq$  N.CName

13/11/24

Page No. \_\_\_\_\_

Date: / /

### \* Super key

→ It is a comb<sup>n</sup> of one or more than one attribute using which we can identify one entity among a entity set.

Roll	Class	Sec	Name	Dob
1	5	A	AB	1993
2	6	B	CD	1997
3	10	A	EF	1998
4	5	B	GH	1997

SK = {Roll, {Roll, Class, Sec}, {Roll, Class}}

SK = {Roll, Class, Sec, Name, Dob}

### \* Candidate key

Minimal subset of a super key.

CK = {Roll, Class, Sec} is The subset

of Super key

CK = {Roll}

CK = {Name}

All other candidate key are super key but all super key are not super key

14/11/24

Page No.

Date / /

## FUNCTIONAL DEPENDENCY

### AND NORMALISATION

- ⇒ A functional dependency occurs when one attribute uniquely identifies another attribute within a relation.
- ⇒ Describes how attributes in a table relate to each other.

$A \rightarrow B$  (A determines B)

Roll	Name	Marks	Dept	Course
1	a	78	CS	C1
2	b	60	EE	C1
3	a	78	CS	C2
4	b	60	EE	C3
5	c	80	IT	C3
6	d	80	EC	C2

Roll → Name (Roll determines Name) ✓

Name → Roll (Name is not unique) ✗

Roll → Marks ✓

Dept → Course ✗

Marks → Dept ✗

Roll, No → Marks ✓

\* Types of Functional Dependency

## 1) Trivial FD

⇒ A dependent is always a subset of the determinant.

i.e. If  $X \rightarrow Y$  and  $Y$  is subset of  $X$  then it is called Trivial FD.

Eg.  $\{ \text{Roll, Name} \} \rightarrow \underbrace{\text{Name}}_{Y}$

The dependent is a subset of the determinant set.

Eg.  $\text{Roll} \rightarrow \text{Roll}$

## 2) Non-Trivial FD

⇒ The dependent is strictly not a subset of the determinant.

i.e. If  $X \rightarrow Y$  and  $Y$  is not a subset of  $X$ .

Then it is called non-Trivial FD.

Eg.  $\{ \text{Roll, Name} \} \rightarrow \underbrace{\text{Marks}}_Y$

The dependent is not subset of the determinant set.

## \* Armstrong Axioms (Inference Rules)

Primary

### 1) Reflexivity

If  $A \rightarrow B$  Then  $A \rightarrow A$ .

### 2) Transitivity

If  $A \rightarrow B$  and  $B \rightarrow C$

Then  $A \rightarrow C$

### 3) Augmentation

If  $X \rightarrow Y$  and  $A$  is an attribute

Then  $XA \rightarrow YA$

Secondary

### 4) Union

If  $X \rightarrow Y$  and  $X \rightarrow Z$

Then  $X \rightarrow YZ$

### 5) Decomposition / Split

If  $X \rightarrow YZ$  Then  $X \rightarrow Y$  and  $X \rightarrow Z$ .

(Vice-versa is not true)

### 6) Pseudo Transitivity

If  $X \rightarrow Y$  and  $YZ \rightarrow A$

Then  $XZ \rightarrow A$

## 7) Composition

If  $X \rightarrow Y$  and  $A \rightarrow B$   
Then  $XA \rightarrow YB$

Eg.  $R(ABCDE)$

$A \rightarrow B$ ,  $B \rightarrow D$ ,  $F \rightarrow A$

$$S_K = (ABCFDE)^+$$

$$(ACE)^+$$

$\downarrow$   
 $C_K$

$$(AB) = \{A, B, D\} \quad S_K \times$$

$$(CD)^+ = \{C, D\} \quad S_K \times$$

$$(ABCDEF)^+ = \{A, B, C, D\} \quad S_K \times$$

$$(CE)^+ = \{C, E, A, B, D\} \quad S_K \checkmark$$

$\downarrow$   
 $C_K$

$$2^3 S_K$$

How to Method Find Candidate key?

$R(A B C D E F)$

$$A \rightarrow B \quad C \rightarrow D \quad D \rightarrow E$$

RULE 1 Attribute not present in the right hand side in this dependency.

$A \sqsubset F$  is not present in RHS.  
So, essential attribute is  $A, C, F$ .

Rule 2 Remaining attribute are non-essential.  
 $B, D, E$  is non-essential.

CASE ① IF ALL ESSENTIAL ATTRIBUTE CAN DETERMINE ALL REMAINING NON-ESSENTIAL THEN COMB<sup>N</sup> OF ESSENTIAL =  $C_k$

$$(A \sqsubset F)^+ = \{A, B, C, D, E, F\}$$

↓

$C_k$

CASE ② IF ESSENTIAL ATTRIBUTE CANNOT BE DETERMINED THE SET OF NON-ESSENTIAL THEN COMB<sup>N</sup> OF ESSENTIAL & PARTICULAR NON-ESSENTIAL =  $C_k$

Q-

$$R(ABCDE)$$

$$AB \rightarrow C \quad BC \rightarrow D \quad CD \rightarrow E \quad EA \rightarrow B$$

A-

$$\text{Essential} \rightarrow \{A, B\}$$

$$(AB)^+ = \{A, B, C, D, E\}$$

 $C_K$ 

5/11/24

Q-

$$R(ABCDE)$$

$$A \rightarrow B \quad B \rightarrow C \quad C \rightarrow D \quad D \rightarrow E$$

A-

$$\text{Essential} \rightarrow \{A\}$$

 $C_K \rightarrow A^+$ 

$$= \{A, B, C, D, E\}$$

Q-

$$R(ABCDEF)$$

$$A \rightarrow BC \quad BC \rightarrow DE \quad D \rightarrow F \quad CF \rightarrow G$$

A-

$$\text{Essential} \rightarrow \{A\}$$

 $C_K \rightarrow A^+$ 

$$= \{A, B, C, D, E, F, G\}$$

 $S_K$ 

$$2^6 \rightarrow S_K$$

Q-

$$R(ABCD)$$

$$AB \rightarrow CD \quad D \rightarrow A$$

A- Essential  $\rightarrow \{B\}$

$B^+ = \{B\}$  Not a superkey

$C_K \rightarrow (AB)^+ = \{A, B, C, D\}$

$\downarrow$

$S_K$

Prime attribute =  $\{A, B\}$

$C_K \rightarrow (DB)^+ = \{B, D, A, C\}$

$\downarrow$

$S_K$

Prime attribute =  $\{A, D, B\}$

R (ABCDF)

$A \rightarrow B$      $D \rightarrow E$

A- Essential  $\rightarrow \{A, C, D\}$

$C_K \rightarrow (ACD)^+ = \{A, C, D, B, E\}$

$\downarrow$

$S_K$

Prime attribute =  $\{A, C, D\}$  One CK

R (ABCD)

$A \rightarrow B$      $B \rightarrow C$      $C \rightarrow A$

A- Essential  $\rightarrow \{D\}$

$D^+ = \{D\}$  Not superkey

$$C_K \rightarrow (AD)^+ = \{A, D, B, C\}$$

↓

$S_K$

$$\text{Prime Attribute} = \{A, D\}$$

$$C_K \rightarrow (CD)^+ = \{C, D, A, B\}$$

↓

$S_K$

$$\text{Prime Attribute} = \{A, D, C\}$$

$$C_K \rightarrow (BD)^+ = \{B, D, C, A\}$$

↓

$S_K$

$$\text{Prime Attribute} = \{A, D, C, B\}$$

Q-

$$R(A B C D)$$

$$AB \rightarrow CD \quad D \rightarrow B \quad C \rightarrow A$$

A- Essential  $\rightarrow X$

$$ABC D^+ \rightarrow S_K$$

$$C_K \rightarrow AB^+ = \{A, B, C, D\}$$

↓

$S_K$

$$C_K \rightarrow CD^+ = \{C, D, A, B\}$$

↓

$S_K$

$$CD^+ = \{C, B, D, A\}$$

$$C_K \rightarrow AD^+ = \{A, D, B, C\}$$

↓

$S_K$

$C_K \rightarrow DC^+ = \{D, C, B, A\}$

↓

$G_K$  is a column IT is unique & functional dependency.

Primary Attribute = {A, B, C, D}

## NORMALIZATION

<u>Roll</u>	<u>SName</u>	<u>Credits</u>	<u>DeptName</u>	<u>Building</u>	<u>Rooms</u>
1	Rahul	6	CGE	G-15	11
2	Amit	7	CGF	F-15	11
3	Bipasha	8	IT	F-14	10
4	Rupa	6	IT	F-14	10
5	Aniket	6	EE	F-13	11

Normalization is a process of organizing the data in database.

It is used to minimize the redundancy from a relation or a set of relations.

It divides the larger table into smaller & links them using relationship.

## Why Do WE NEED NORMALIZATION ?

The main reason for normalizing the relations is removing certain anomalies. Failure to eliminate anomalies leads to data redundancy & can cause data integrity.

## Data modification Anomalies

- i) Insertion Anomaly : It refers to when one cannot insert a new tuple into a relationship due to lack of data.
- ii) Deletion Anomaly : It refers to a situation where the deletion of data results in the unintended loss of some other important data.
- iii) Updation Anomaly : The update anomaly is when an update of a single data value requires multiple rows of data to be updated.

## Types of Normal Forms

- 6 types :- i) 1NF
- ii) 2NF
- iii) 3NF
- iv) BCNF
- v) 4NF
- vi) 5NF

## 1) First Normal Form (1NF)

A relation is in 1NF if every attribute in that relation is single valued attribute.

Rules :-

- ① Atomic values for each table.
- ② Attribute type should be same.
- ③ No ordering of tuples or columns.
- ④ No duplicate records are there.

## 2) Second Normal Form (2NF)

Rules :-

- ① It must be in 1NF and transitively closed.
- ② No partial dependency in relation R.

Note: A functional dependency  $X \rightarrow Y$  is said to be in partial dependency, if  $Y$  can be determined by any proper subset of  $X$ .

- \* In 2NF, every non-prime attribute must not partially dependent on each CR of the table.

SUBSET OF  $\subseteq_K$   $\rightarrow$  Non-prime  
2NF  $\times \times$

Page No. / /  
Date: / /

$R(A B C D E F)$

$A \rightarrow B$   $B \rightarrow C$   $C \rightarrow D$   $D \rightarrow E$

Essential  $\rightarrow \{A, F\}$

$\subseteq_K$

$\subseteq_K \rightarrow (AF)^+ = \{A, F, B, C, D, E\}$

$A^+ F^+ \{F\} \times$

$\{A, B, C, D, E\} \times$

Prime  $\rightarrow \{A, F\}$

Non-Prime  $\rightarrow \{B, C, D, E\}$

$A \rightarrow B$

$\because$  As subset of  $\subseteq_K$  can determine a non-prime attribute.

Hence, it is not 2NF.

### 3) Third Normal Form (3NF)

$\Rightarrow$  The relational schema R is in 3NF if

i) FD is non-trivial and  $X \rightarrow A$

ii)  $X \rightarrow A$  and  $X$  is superkey OR  $X$  is prime attribute

iii)  $X \rightarrow A$  and  $X$  is superkey OR  $X$  is prime attribute

$A$  is prime attribute

#### 4) BCNF (Boyce-Codd Normal Form)

$\Rightarrow$  Every relation is in BCNF if:

i) ~~Every~~ It is in 3NF.

ii)  $X \rightarrow A$  ( $X$  is a superkey)

Q-  $R(A B C D)$   
 $AB \rightarrow C$     $AB \rightarrow D$     $C \rightarrow A$     $B \rightarrow D$

A- RHS      Not in RHS

$A C D$        $B C S$        $G A \leftarrow G A$

$$B^+ = \{B, D\} \rightarrow S_K \times \times$$

$$S_K \rightarrow (A B)^+ = \{A, B, C, D\}$$

$\downarrow$   
 $S_K$

Prime attribute = {A, B}

$$S_K \rightarrow (C B)^+ = \{C, B, A, D\}$$

$\downarrow$   
 $S_K$

Prime = {A, B, C}

Non-prime = {D}

$|AB \rightarrow C|$  BCNF (AB is  $S_K$ )

$|AB \rightarrow D|$  BCNF (AB is  $S_K$ )

$$C \rightarrow A$$

3NF ( $\because A$  is prime)

$$B \rightarrow D$$

1NF ( $\because D$  is non-prime)

$\therefore$  The relation  $R$  is in 1NF

Q-  $R(ABCD)$  ~~prime in RHS~~  $A \leftarrow X$

$$AB \rightarrow CD \quad D \rightarrow A$$

$$L_K AB \cdot DB \quad (G78A)$$

$$(G \leftarrow 8) \quad A \leftarrow 7 \quad R \leftarrow 8A \quad D \leftarrow 8A$$

~~A-~~

$$\text{Prime} = \{A, B, D\}$$

$$\text{Non-prime} = \{C\}$$

$$AB \rightarrow CD \quad BCNF$$

$$D \rightarrow A \quad 3NF$$

$\therefore$  The relation  $R$  is in 3NF

Q-  $R(ABCDE)$

$$A \rightarrow B \quad BC \rightarrow E \quad ED \rightarrow A$$

~~A-~~

RHS Not in RHS

$$B, E, A$$

$$CD$$

$$(CD)^+ = \{C, D\} \quad \cancel{GK XX}$$

$$L_K \rightarrow (ACD)^+ = \{A, C, D, B, E\}$$

$$L_K \rightarrow (ECD)^+ = \{B, C, D, E, A\}$$

$$L_K \rightarrow (BCD)^+ = \{B, C, D, E, A\}$$

Prime = { A, B, C, D, E }

Non-prime = { B }

\* If all the attributes are prime, Then  
the relation is in 3NF.

Q- R(ABC)

$$A \rightarrow B \quad B \rightarrow A \quad B \rightarrow C$$

A-  $(ABC)^+ = \{ A, B, C \}$

$$A^+ = \{ A, B, C \}$$

$$B^+ = \{ A, B, C \}$$

$$A \rightarrow B$$

BCNF

$$B \rightarrow A$$

BCNF

$$B \rightarrow C$$

BCNF

∴ The relation R is in BCNF.

Q- R(ABCDEFG)

$$\begin{array}{lll} AB \rightarrow C & AC \rightarrow B & AD \rightarrow E \\ B \rightarrow D & BC \rightarrow A & E \rightarrow F \end{array}$$

$$R_1(ABC) \quad R_2(ABCD) \quad R_3(ABCEF)$$

$R_1(ABC)$

$AB \rightarrow AC$     $AC \rightarrow BC$     $BC \rightarrow A$

$\cancel{AB}$

$\{ABC\}^+ = \{C\}$

$\{ACB\}^+ = \{AC, B\}$

RHS

Not in RHS

$A, B, C$

$\{ABC\}^+ = \{A, B, C\}$

$\{BAC\}^+ = \{A, B, C\}$

$\{ACB\}^+ = \{A, C, B\}$

$\{BCA\}^+ = \{B, C, A\}$

Prime  $\Rightarrow \{A, B, C\}$

$AB \rightarrow C$

$AC \rightarrow B$

$BC \rightarrow A$

(BCNF)

BCNF

BCNF

(BCNF)

∴ The relation  $R_1$  is in BCNF.

## DECOMPOSITION

The process of breaking up or dividing a single relation into 2 or more sub relations is called Decomposition.

It is of 2 types :-

i) Lossless

ii) Dependency preserving.

i) Lossless

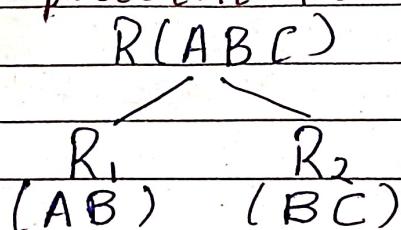
It is a decomposition of relation R into relations  $R_1$  &  $R_2$  such that, if we perform natural join of  $R_1$  &  $R_2$ , it will return the original relation R.

$$R \Leftrightarrow R_1 \times R_2$$

a	b	c	A	B	C
1	2	1	1	2	2
2	5	3	2	5	5
3	3	3	3	3	3

How to Detect if R is lossy OR lossless

RULE 1 Union of both the sub relations containing all attributes that are present in parent relation R.



$$R_1 \cup R_2 = ABC = \underline{R}$$

Rule 2 Intersection of  $R_1 \cap R_2$ , sub relations cannot be null sets

Rule 3  $R_1 \cap R_2 = \emptyset$  if either  $R_1$  or  $R_2$  is null relation.

Q-  $R(ABCD)$

$A \rightarrow B$  given  $B \rightarrow D$

$R_1(AB) \quad R_2(CD)$

Rule 1 ✓

Q-  $R(ABCD)$

$R_1(A) \quad R_2(BD)$

$R_3(A) \quad R_4(LBC)$

$A \rightarrow B \quad B \rightarrow C \quad C \rightarrow D \quad D \rightarrow B$

$R_1 \cup R_2 = \{B\}$  ✓

$B^+ = \{B, C, D\}$

∴ This is lossless.

## Lossy Decomposition

⇒ It is a decomposition of relation R into relation  $R_1$  &  $R_2$  such that if we perform natural join of  $R_1$  &  $R_2$ , it will not return the original relation R but also some additional information with it.

$R(ABC)$		
<i>original R</i>	$R(AC)$	$R(BC)$
a 1 2 3	b 2 5 3	c 1 3 3
a 1 2 3	c 1 3 3	b 2 1 3
b 2 1 3	c 1 3 3	c 1 3 3

$AC \times BC$

	a	b	c
1	2		
2	5	3	
3	3	3	
3	5	3	

*original*  $\neq AC \times BC$

$R_2(A B C D)$   
 $AB \rightarrow C \quad AC \rightarrow B \quad B \rightarrow D \quad BC \rightarrow A$

A-  $(AB)^+ \rightarrow \{A, B, C, D\}^S_{SK}$

$(BC)^+ \rightarrow \{B, C, A, D\}^S_{SK}$

$(AC)^+ \rightarrow \{A, C, B, D\}^S_{SK}$

Prime = {A, B, C}

Non-prime = {D}

$AB \rightarrow C \quad BCNF$

$AC \rightarrow B \quad BCNF$

$B \rightarrow D \quad 3NF$

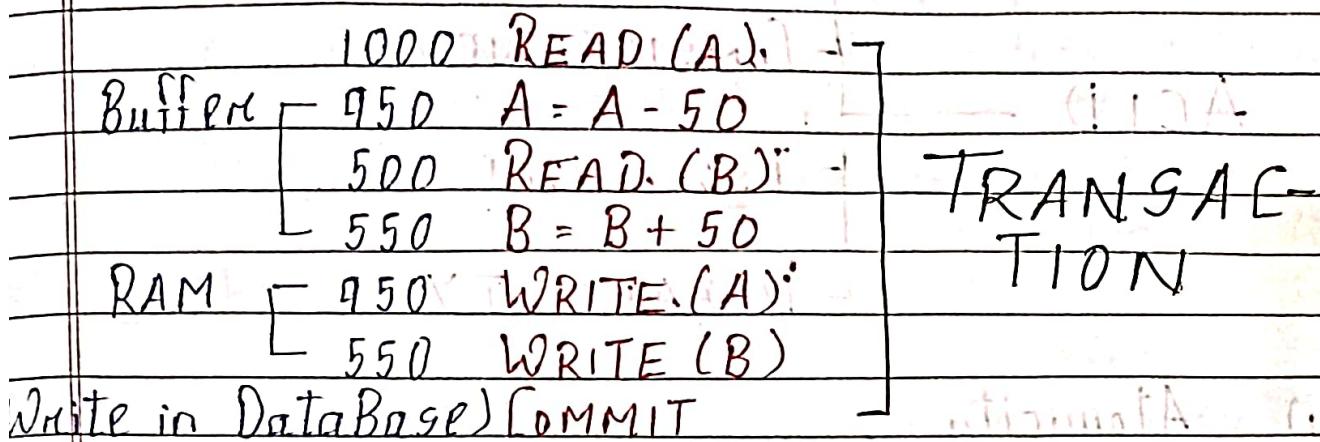
$BC \rightarrow A \quad BCNF$

$\therefore$  The relation  $R_2$  is 3NF.

# TRANSACTION AND CONCURRENCY CONTROL

Transactions ( $T_x$ ) is a set of operations used to perform a logical unit of work.

Money transfer from A to B.



READ : It is used to read the value of the X from the database & store it in a buffer in the main memory for further actions.

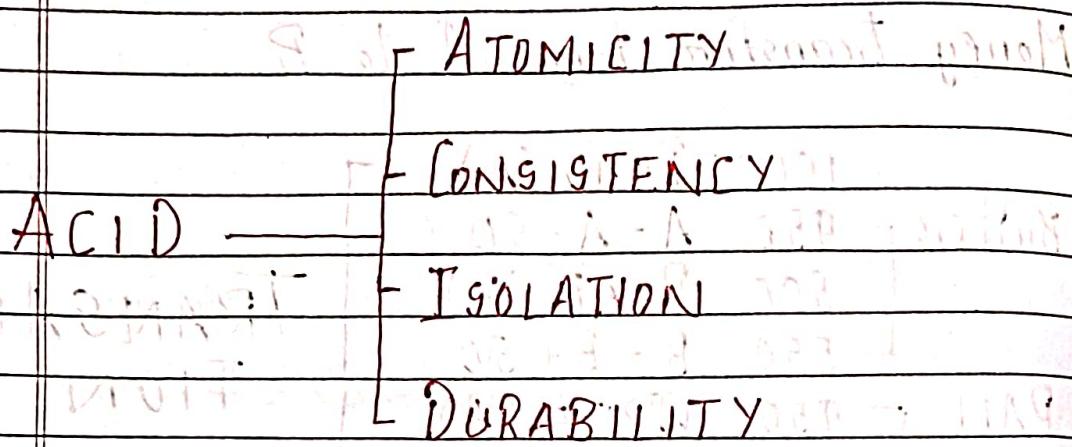
WRITE : It is used to write the value to the database from the buffer in the main memory. For a write operation to be performed, first a read operation is performed to bring its value in buffer.

COMMIT : It is used to save all changes made during the transaction permanently to the database.

# CHAPTER NINETEEN

ROLLBACK : It is used to undo all changes made during the transaction.

## \* ACID Properties of Transaction



### 1) Atomicity

- Do all operations & COMMIT
- Else ROLLBACK
- FAIL transactions cannot be resumed
- Just RESTART
- A transaction is an indivisible unit

### 2) Consistency

- Before The start & after the Transaction completed, sum of amount will be saved.

- Consistency maintained by software in DBMS or application developer.

### 3) Isolation

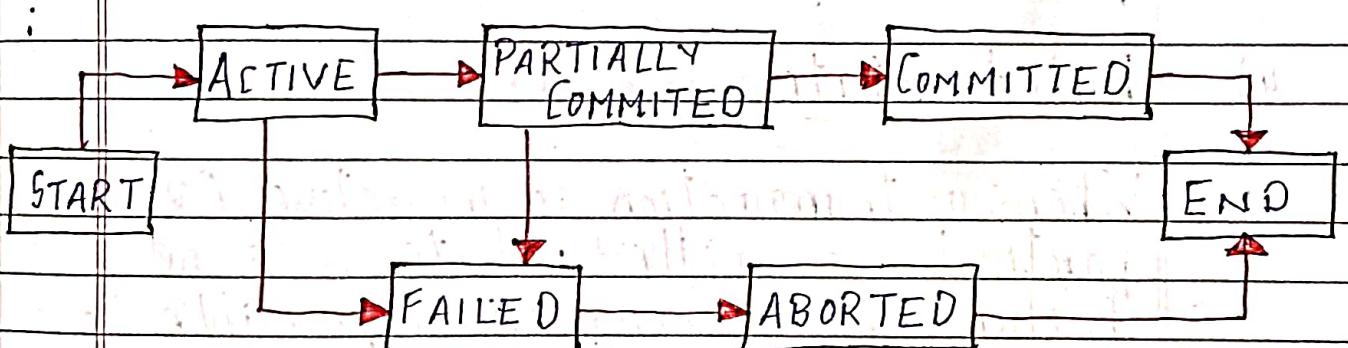
- It is the responsibility of the concurrency control subsystem to ensure isolation where each Tr can execute independently so that partial effect of each Tr should not be visible to other Tr.

### 4) Durability

- It is the responsibility of the recovery manager to record permanently the effect of successfully completed Tr & must not be lost due to subsequent failure.

05/12/2<sup>nd</sup>

### Transaction Life Cycle



### 1) Active State

⇒ 1st state of transaction life cycle.

⇒ A transaction is called in an active state as long as the transactions are getting executed.

⇒ All changes are stored in buffer.

### 2) Partially Committed State

⇒ After the execution of instructions when it is stored in intermediate buffer then it is in partially committed state.

### 3) Committed State

⇒ All changes are stored in database permanently from the buffer.

### 4) Failed State

⇒ When a transaction is in active OR partially committed state & some failure may occur & impossible to continue the execution.

## 5) Aborted State

- ⇒ After the transaction is in failed state all changes are made by transaction to be undone. OR Rollback.
- ⇒ After rollback completely transactions enter into aborted state.

## 6) Terminated State

- ⇒ Last state of transaction life cycle.
- ⇒ After committed or aborted, transaction will be end of lifecycle OR terminated state.

## Concurrency Problem

When multiple transactions execute concurrently in an uncontrolled OR unrestricted manner. Then there might be several problems :-

- i) Dirty Read
- ii) Unrepeatable Read
- iii) Lost Update
- iv) Phantom Read

### i) Dirty Read

	<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>
	Statement and assignment and	From line expanded. Then
	→ R(A)	Transact must be end of
ROLL BACK	Statement and assignment and	A = A - 50 950
		W(A) 950
		Commit
	— T <sub>1</sub> FAIL	state. batman

⇒ There is always a chance that uncommitted transaction might ROLLBACK.

⇒ Uncommitted transaction might make another transaction read a value that doesn't even exist.

⇒ Lead inconsistency in DBMS.

### ii) Unrepeatable Read

	<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>
	1000 R(X)	Initial state
	900 A = A - 100	R(X) = 1000
	900 W(A)	Initial state
		R(X) - 900

This problem occurs when a transaction read diff. value even it is not updated

### iii) Lost Update

<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>
1000 R(A)	R(A) 950
950 A = A - 50	A = A - 100 850
950 W(A)	W(A) 850
Commit	Commit

In concurrent transaction multiple transaction executed concurrently & updates from one or more transactions getting lost.

### iv) Phantom Read

<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>
R(A)	R(A)
delete	A = A - 50

The problem occurs when a transaction reads some variable from the buffer & the same variables are updated from other T<sub>2</sub>s which doesn't exist.

06/12/24

Page No. / /

Date: / /

## Schedule

Serial

Non-Serial

Serializable

Non-Serializable

Conflict

View

Recoverable

Non-Recoverable

Cascading Cascadless Strict

## Schedule

A sequence of operations by a set of concurrent transactions that preserves the order of operations in each of the individual ~~open~~ transactions.

It is of 2 types :-

i) Serial

ii) Non-serial

### i) Serial Schedule

A schedule where the operations of each transaction are executed concurrently without any interleaved operations from other transactions.

Advantages

Consistent

Recoverable

Disadvantages

Waiting Time More.

Efficiency Less.

ii) Non-Serial Schedule

A non-serial schedule perform the operations concurrently in an interleaved manner.

Disadvantages

i) Not always consistent

ii) &amp; recoverable

Advantages

i) Efficiency more

ii) Waiting Time less

It is further divided into 2 types :-

a) Serializable

b) Non-Serializable

a) Serializable

The objective of serializability is to find non-serial schedule that allows transaction to execute concurrently

without interfering one another & thereby produce a database state that could be produced by a serial execution.

That means a non-serial schedule is serializable & correct if it produces same result as a serial execution.

It is of 2 types :

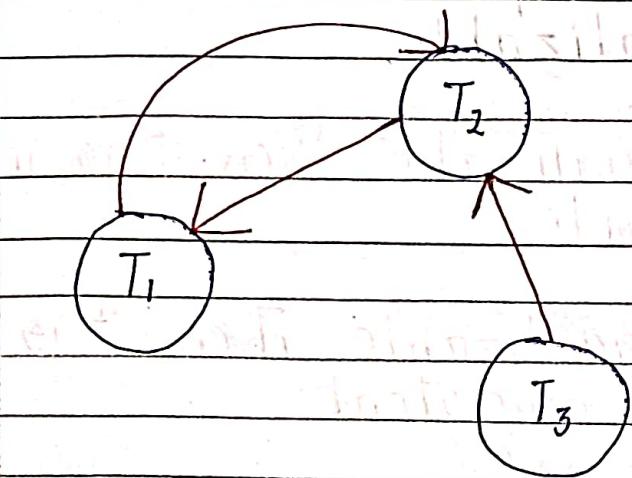
- i) Conflict free
- ii) View
- iii) Conflict

If a given non-serial schedule can be converted into a serial schedule by swapping its non-conflicting operations then it is called conflict serializable schedule.

Both the operations belong to different transactions & both are on the same data.

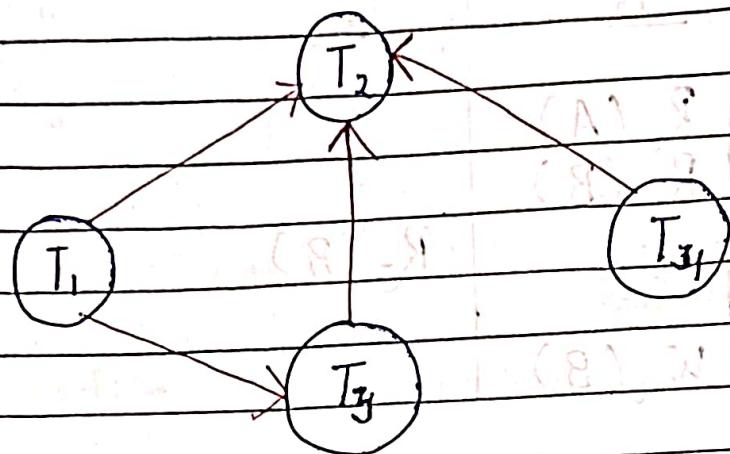
$S \rightarrow R_1(A) \quad R_2(A) \quad R_1(B) \quad R_2(B)$   
 $R_3(B) \quad W_1(A) \quad W_2(B)$

<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>	<u>T<sub>3</sub></u>
R <sub>1</sub> (A)	R <sub>2</sub> (A)	
R <sub>1</sub> (B)	R <sub>2</sub> (B)	
W <sub>1</sub> (A)		R <sub>3</sub> (B)
	W <sub>2</sub> (B)	



There is a cycle is present. So schedule is not conflict serializable.

<u>09/12/24</u>	<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>	<u>T<sub>3</sub></u>	<u>T<sub>4</sub></u>
	R(A)			R(A)
		R(A)		
	W(B)			R(A)
		W(A)		
			R(B)	
			W(B)	



There is no cycle present. So, it is conflict serializable.

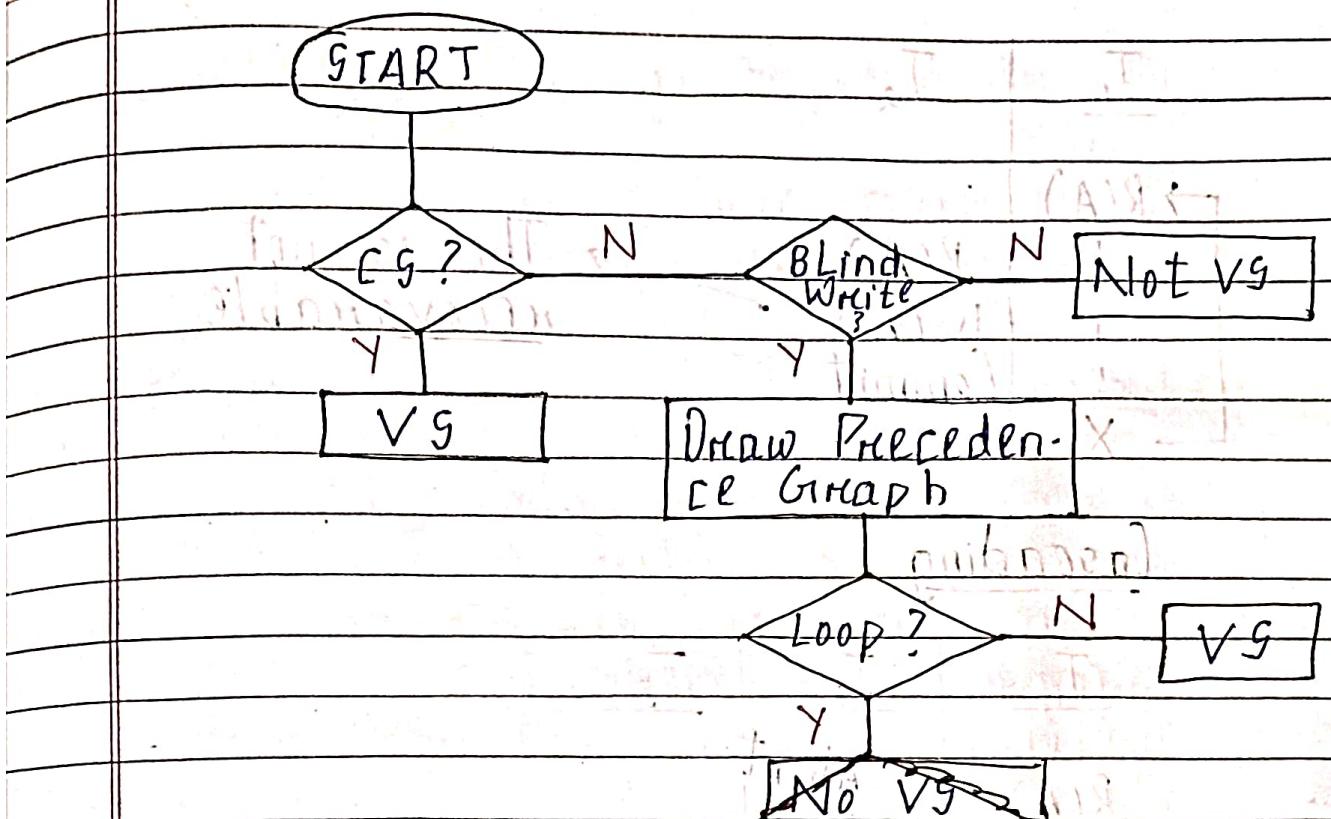
Note If conflict serializable Then it is view Serializable.

If conflict serializable Then it is Recoverable & consistent.

iii) View

If a given schedule is found to be view equivalent to some serial schedule Then it is called view serializable.

ALL CONFLICT SERIALIZABLE ARE VIEW SERIALIZABLE BUT ALL VIEW SERIALIZABLE ARE NOT CONFLICT SERIALIZABLE.



A transaction is said to be blind write when the user directly writes the value from buffer without reading a value from database.

T<sub>1</sub>      T<sub>2</sub>

R(A) → R(A) This is recoverable  
 W(A) → W(A) will follow the 1st transaction  
 R(A) → R(A) → action occurs first  
 W(A) → W(A) & committed first.

Commit

Commit

<u>T<sub>1</sub></u>	T <sub>2</sub>	(TRAILER)
R(A)	R(A)	This is not recoverable
W(A)		
Commit		
X		

## Cascading

<u>T<sub>1</sub></u>	<u>T<sub>2</sub></u>	<u>T<sub>3</sub></u>
R(A)	Abort	
W(A)	Abort	
X		
Commit	None	R(A)
	None	W(A)
Commit	None	Commit

If in a schedule, failure of one transaction causes several other dependent transaction to roll back or abort. Then, such a schedule is called cascading schedule. (Ingrading ROLLBACK)

## Cascadeless

If in a schedule, a transaction is not allowed to read a data item until last transaction has written it committed or aborted schedule then it is called cascadeless schedule.

Minimum lock at time marking A

mark Transaction A until certain

sub step A. A read lock will guarantee if

R(A) is issued then no other transaction can write

W(A) is issued until transaction A is committed

Commit

R(A)

(C) W(A) until S of your final

Commit

(R(A)) is issued to

(C) W(A) is issued until

Commit

strict

strict mode is read and write

IF in a schedule a transaction is

neither allowed to read or write a

data item until the last transaction

that has written is committed or

aborted.

It doesn't support blind write.

starting a transaction with a

## Objective of Concurrency Control

1) Serializability

2) Recoverability

### Locking

A procedure used to control concurrent access to data when one transaction is accessing the database. A lock may deny access to other transactions to prevent incorrect results or inconsistent data.

Lock may be 2 types :- (S/W)

a) Shared [S(A)]

b) Exclusive [X(A)]

### Shared

If a transaction has a shared lock on a data, it can read a data but it cannot write or update the data. Only read operation is possible.

### Exclusive

If a transaction has an exclusive lock on a data, it can read & update the data.

<del>T<sub>1</sub></del>	Unlock	Shared	Exclusive	
Unlock	✓	✓	✓	R R ✓
Shared	✓	✓	✗	W R X
Exclusive	✓	✗	✗	W W X

### Advantages of Locking

Data consistency : Lock can help to ensure it by preventing multiple users from modifying the same data simultaneously.

By controlling access to shared resource locking can help to prevent data conflict.

Isolation : locking can ensure the transaction are executed in isolation from other transaction.

### 2 Phase Locking Protocol

According to this rule, every transaction are divided into 2 phase :

i) Growing Phase : In this phase Tr acquire all the locks needed but cannot release any lock.

~~Shrinking Phase~~: In this phase, it releases all the locks but cannot acquire any new lock.

12/12/24

11

X

X

✓

Demand

Acquisition of glad and pat: maintenance of sufficient excess glucose for maintaining blood glucose homeostasis. It releases insulin which removes all glucose from blood. It increases insulin release by inhibiting glucagon release.

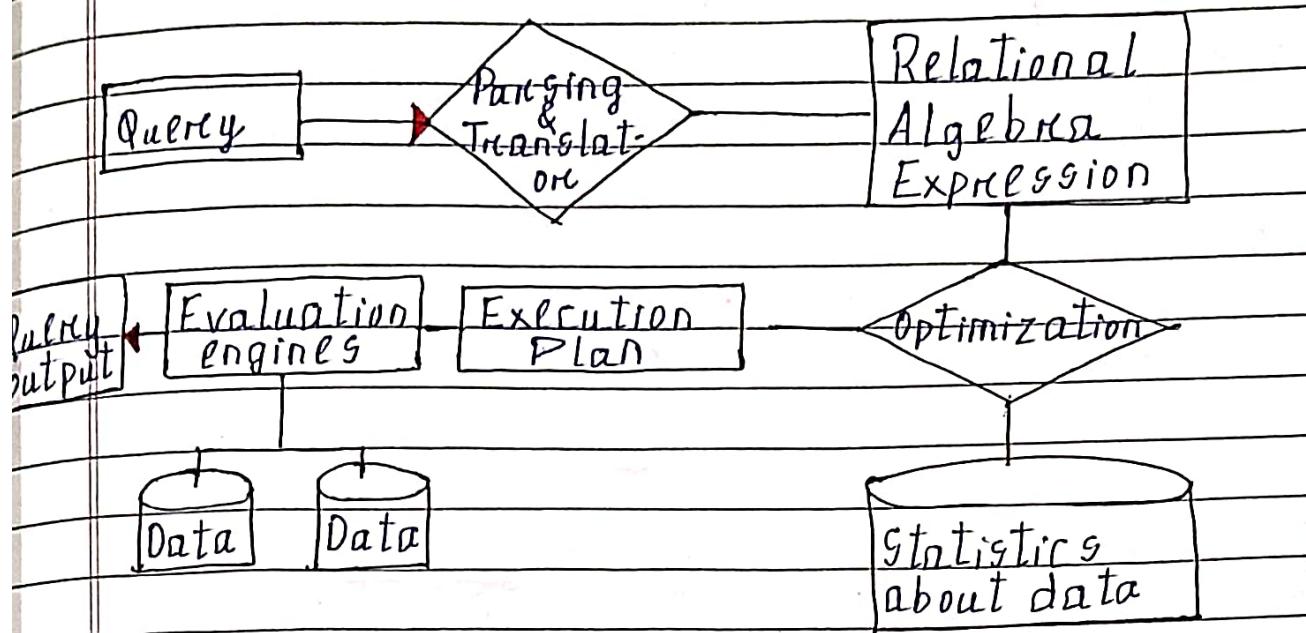
Releasing all glucose and insulin is inhibited by insulin inhibitor hormone. It increases insulin secretion.

Important insulin receptor

activation of insulin receptor cell fat metabolism and glucose ready for future metabolic needs.

Excretion of glucose will affect insulin secretion and glucose levels. And glucose excretion will increase insulin release.

# QUERY PROCESSING AND OPTIMIZATION



select salary from employee  
where salary > 75k

$\pi(\delta(\text{emp}))$   
 $\text{gal}(\text{sal} > 75\text{k})$