

## Explain various types of Kernels with respect to the formula

Kernels are essential for SVMs because they enable the algorithm to efficiently work in high-dimensional feature spaces without explicitly computing the coordinates of the data points.

### 1. Linear Kernel:

- Formula:  $K(x, y) = x^T \cdot y$
- The linear kernel represents a linear relationship between the input data points. It is the simplest kernel and is used when the data is linearly separable.

### 2. Polynomial Kernel:

- Formula:  $K(x, y) = (x^T \cdot y + c)^d$
- The polynomial kernel calculates the dot product of the input vectors in a higher-dimensional space using a polynomial function. The hyperparameters  $c$  and  $d$  control the degree of the polynomial and the bias, respectively.

### 3. Radial Basis Function (RBF) :

- Formula:  $K(x, y) = \exp(-\gamma \cdot \|x - y\|^2)$
- The RBF kernel maps the input vectors into an infinite-dimensional space by applying a Gaussian function. It measures the similarity between data points based on the Euclidean distance between them. The hyperparameter  $\gamma$  controls the width of the Gaussian distribution.

### 4. Sigmoid Kernel:

- Formula:  $K(x, y) = \tanh(\alpha \cdot x^T \cdot y + c)$
- The sigmoid kernel computes the hyperbolic tangent of the dot product between input vectors, rescaled by the parameters  $c$  and  $\alpha$ . It maps the input vectors into a higher-dimensional space and is suitable for non-linearly separable data.

### 5. Custom Kernels:

users can define custom kernels based on domain knowledge or specific requirements.