

COMPUTER SECURITY ASSIGNMENT

ADITYA
1605004

12. Using the Euclidean algorithm, find the gcd of:

(a) 88 and 220

| <u>q</u> | <u>r_1</u> | <u>r_2</u> | <u>r</u> |
|----------|-------------------------|-------------------------|-----------------------|
| 0 | 88 | 220 | 88 |
| 2 | 220 | 88 | 44 |
| 2 | 88 | 44 | 0 |

$\text{GCD}(88, 220) = 44$

(b) 300 and 42

| <u>q</u> | <u>r_1</u> | <u>r_2</u> | <u>r</u> |
|----------|-------------------------|-------------------------|-----------------------|
| 7 | 300 | 42 | 6 |
| 7 | 42 | 6 | 0 |
| | (6) | 0 | |

$\text{GCD}(300, 42) = 6$

(c) 24 and 320

| <u>q</u> | <u>r_1</u> | <u>r_2</u> | <u>r</u> |
|----------|-------------------------|-------------------------|-----------------------|
| 0 | 24 | 320 | 24 |
| 13 | 320 | 24 | 8 |
| 3 | 24 | 8 | 0 |
| | (8) | 0 | |

$\text{GCD}(24, 320) = 8$

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(d) 401 and 700

| <u>q</u> | <u>r₁</u> | <u>r₂</u> | <u>r</u> |
|----------|----------------------|----------------------|----------|
| 0 | 401 | 700 | 401 |
| 1 | 700 | 401 | 299 |
| 1 | 401 | 299 | 102 |
| 2 | 299 | 102 | 95 |
| 1 | 102 | 95 | 7 |
| | | | 4 |
| 13 | 95 | 7 | |
| 1 | 7 | 4 | 3 |
| 1 | 4 | 3 | 1 |
| 3 | 3 | 1 | 0 |
| | (1) | 0 | |

$$\text{GCD}(401, 700) = 1$$

16. Using the ext. Euclidean algo., find gcd:

(a) 4 and 7

| q | r ₁ | r ₂ | r | s ₁ | s ₂ | s | t ₁ | t ₂ | t |
|---|----------------|----------------|---|----------------|----------------|----|----------------|----------------|----|
| 0 | 4 | 7 | 4 | 1 | 0 | 1 | 0 | 1 | 0 |
| 1 | 7 | 4 | 3 | 0 | 1 | -1 | 1 | 0 | 1 |
| 1 | 4 | 3 | 1 | 1 | -1 | 2 | 0 | 1 | -1 |
| 3 | 3 | 1 | 0 | -1 | 2 | -7 | 1 | -1 | 4 |
| | 1 | 0 | | 2 | -7 | | -1 | 4 | |
| | | | | | | | | | |
| | | | | | | | | | |

$$\text{GCD}(4, 7) = 1$$

$$s = 2$$

$$t = -1$$

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(b) 291 and 42

| q | r_1 | r_2 | r | s_1 | s_2 | s | t_1 | t_2 | t |
|----|-------|-------|-----|-------|-------|-----|-------|-------|-----|
| 6 | 291 | 42 | 39 | 1 | 0 | 1 | 0 | 1 | -6 |
| 1 | 42 | 39 | 3 | 0 | 1 | -1 | 1 | -6 | 7 |
| 13 | 39 | 3 | 0 | 1 | -1 | 14 | -6 | 7 | -97 |
| | 3 | 0 | | -1 | 14 | | 7 | -97 | |

$$\text{GCD}(291, 42) = 3$$

$$s = -1$$

$$t = 7$$

(c) 84 and 320

| q | r_1 | r_2 | r | s_1 | s_2 | s | t_1 | t_2 | t |
|---|-------|-------|-----|-------|-------|-----|-------|-------|-----|
| 0 | 84 | 320 | 84 | 1 | 0 | 1 | 0 | 1 | 0 |
| 3 | 320 | 84 | 68 | 0 | 1 | -3 | 1 | 0 | 1 |
| 1 | 84 | 68 | 16 | 1 | -3 | 4 | 0 | 1 | -1 |
| 4 | 68 | 16 | 4 | -3 | 4 | -19 | 1 | -1 | 5 |
| 4 | 16 | 4 | 0 | 4 | -19 | 80 | -1 | 5 | -21 |
| | 4 | 0 | | -19 | 80 | | 5 | -21 | |

$$\text{GCD}(84, 320) = 4$$

$$s = -19$$

$$t = 5$$

(d) 400 and 60

| q | r_1 | r_2 | r | s_1 | s_2 | s | t_1 | t_2 | t |
|----|-------|-------|-----|-------|-------|-----|-------|-------|-----|
| 6 | 400 | 60 | 4 | 1 | 0 | 1 | 0 | 1 | -6 |
| 15 | 60 | 4 | 0 | 0 | 0 | 1 | -15 | -6 | 91 |
| | | | | 1 | -15 | | -6 | 91 | |
| | 4 | | | | | | | | |

$$\text{GCD}(400, 60) = 4$$

$$s = 1$$

$$t = -6$$

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21. Encrypt the message "this is an exercise" using one of the following ciphers. Decipher while ignoring the text:

~~tag: additve cipher (key=20)~~

<text> = "this is an exercise"

Ans.

cipher

plaintext

ciphertext

Additive
cipher
(key = 20)

<text>

NBCMCMUHT RYLWCHY

Multiplicative
cipher (key = 15)

<text>

ZBQKQKANHIVEQKI

Affine, (key = 15, 20)

<text>

TVKEKEU HCBCPYKEC

22. Encrypt <text> = "the house is being sold tonight."

cipher

plaintext

ciphertext

Vigenere (key = "dollars")

<text>

LVPSBOLKHWDME
ZFJGZWDRGQWRST

Autokey (key = 7)

<text>

AALLVIMWMATPMVTG
ZOWHBRONA

25. Use a Hill cipher "We live in an insecure world".

Use:

$$\text{key} = \begin{bmatrix} 03 & 02 \\ 05 & 07 \end{bmatrix}$$

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$$\begin{bmatrix} 8 & 20 \\ 21 & 0 \\ 5 & 18 \\ 11 & 3 \\ 13 & 13 \\ 11 & 3 \\ 22 & 12 \\ 2 & 14 \\ 19 & 10 \\ 6 & 12 \\ 2 & 07 \\ 4 & 25 \end{bmatrix} \times \begin{bmatrix} 22 & 4 \\ 11 & 8 \\ 21 & 4 \\ 08 & 13 \\ 00 & 13 \\ 08 & 13 \\ 18 & 4 \\ 02 & 20 \\ 17 & 4 \\ 22 & 14 \\ 17 & 11 \\ 03 & 25 \end{bmatrix} \times \begin{bmatrix} 3 & 2 \\ 5 & 7 \end{bmatrix}$$

$\begin{matrix} C & & P & & K \end{matrix}$

IUVAFSLDNNZDWMCOTKGMCH²

|
bogus.

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