# In this notebook

Many college courses conclude by giving students the opportunity to evaluate the course and the instructor anonymously. In the article "Beauty in the Classroom: Professors' Pulchritude and Putative Pedagogical Productivity" (PDF), authors Daniel Hamermesh and Amy M. Parker suggest (based on a data set of teaching evaluation scores collected at UT Austin) that student evaluation scores can partially be predicted by features unrelated to teaching, such as the physical attractiveness of the instructor.

In this lab, we will use this data to try and predict the average instructor rating with a multiple linear regression.

### **Attribution**

Parts of this lab are based on a lab assignment from the OpenIntro textbook "Introductory Statistics with Randomization and Simulation" that is released under a Creative Commons Attribution-ShareAlike 3.0 Unported license. The book website is at <a href="https://www.openintro.org/book/isrs/">https://www.openintro.org/book/isrs/</a>. You can read a PDF copy of the book for free and watch video lectures associated with the book at that URL. You can also see the lab assignment that this notebook is based on.

#### Data

The data were gathered from end of semester student evaluations for a large sample of professors from the University of Texas at Austin. In addition, six students looked at a photograph of each professor in the sample, and rated the professors' physical appearance. More specifically:

Each of the professors' pictures was rated by each of six undergraduate students: Three women and three men, with one of each gender being a lower-division, two upper-division students (to accord with the distribution of classes across the two levels). The raters were told to use a 10 (highest) to 1 rating scale, to concentrate on the physiognomy of the professor in the picture, to make their ratings independent of age, and to keep 5 in mind as an average.

We are using a slightly modified version of the original data set from the published paper. The dataset was released along with the textbook "Data Analysis Using Regression and Multilevel/Hierarchical Models" (Gelman and Hill, 2007).)

#### Setup

We will start by importing relevant libraries, setting up our notebook, reading in the data, and checking that it was loaded correctly.

```
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import numpy as np
from sklearn import metrics
from sklearn import model_selection
from sklearn.linear_model import LinearRegression

from IPython.core.interactiveshell import InteractiveShell
InteractiveShell.ast_node_interactivity = "all"
%matplotlib inline
```

```
url = 'https://www.openintro.org/stat/data/evals.csv'
df = pd.read_csv(url)
df.head()
```

```
df.columns
df.shape
```

```
score
                 rank
                          ethnicity gender language
                                                     age
                                                          cls_perc_eval \
0
    4.7 tenure track
                           minority female
                                            english
                                                      36
                                                               55.81395
1
    4.1 tenure track
                           minority female
                                             english
                                                      36
                                                               68.80000
                                                               60.80000
     3.9 tenure track
                           minority female
                                             english
                                                      36
3
                                                      36
                                                               62.60163
    4.8 tenure track
                           minority female
                                            english
4
    4.6
              tenured not minority
                                       male
                                            english
                                                      59
                                                               85.00000
   cls_did_eval cls_students cls_level ...
                                            cls_credits bty_f1lower \
0
            24
                                            multi credit
                          43
                                 upper ...
                                        ... multi credit
1
            86
                         125
                                 upper
2
                                       ... multi credit
                                                                   5
            76
                         125
                                 upper
3
            77
                         123
                                                                   5
                                 upper ... multi credit
4
                          20
                                                                   4
            17
                                 upper ... multi credit
  bty flupper bty flupper bty mllower bty mlupper bty mlupper bty avg \
0
            7
                         6
                                      2
                                                   4
                                                               6
                                                                      5.0
            7
                         6
                                      2
                                                               6
                                                                      5.0
1
2
            7
                         6
                                      2
                                                               6
                                                                      5.0
                                                  4
3
            7
                         6
                                      2
                                                  4
                                                               6
                                                                      5.0
                                      2
                                                   3
4
            4
                         2
                                                               3
                                                                      3.0
  pic_outfit pic_color
0 not formal
                 color
1 not formal
                 color
2 not formal
                 color
3 not formal
                 color
4 not formal
                 color
[5 rows x 21 columns]
```

```
(463, 21)
```

Each row in the data frame represents a different course, and columns represent variables about the courses and professors. The data dictionary is reproduced here from the OpenIntro lab:

variable	description
score	average professor evaluation score: (1) very unsatisfactory - (5) excellent.
rank	rank of professor: teaching, tenure track, tenured.
ethnicity	ethnicity of professor: not minority, minority.
gender	gender of professor: female, male.
language	language of school where professor received education: english or non-english.
age	age of professor.

variable	description
cls_perc_eval	percent of students in class who completed evaluation.
cls_did_eval	number of students in class who completed evaluation.
cls_students	total number of students in class.
cls_level	class level: lower, upper.
cls_profs	number of professors teaching sections in course in sample: single, multiple.
cls_credits	number of credits of class: one credit (lab, PE, etc.), multi credit.
bty_f1lower	beauty rating of professor from lower level female: (1) lowest - (10) highest.
bty_f1upper	beauty rating of professor from upper level female: (1) lowest - (10) highest.
bty_f2upper	beauty rating of professor from second upper level female: (1) lowest - (10)
	highest.
bty_m1lower	beauty rating of professor from lower level male: (1) lowest - (10) highest.
bty_m1upper	beauty rating of professor from upper level male: (1) lowest - (10) highest.
bty_m2upper	beauty rating of professor from second upper level male: (1) lowest - (10) highest.
bty_avg	average beauty rating of professor.
pic_outfit	outfit of professor in picture: not formal, formal.
pic_color	color of professor's picture: color, black & white.

# Explore data

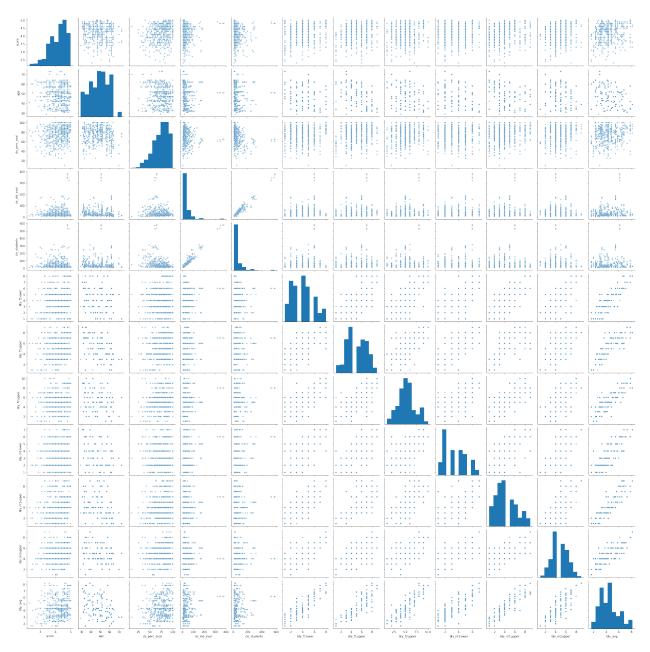
As always, start by exploring the data:

df.describe()

	score	age	cls_perc_eval	cls_did_eval	cls_students	\
count	463.000000	463.000000	463.000000	463.000000	463.000000	
mean	4.174730	48.365011	74.427788	36.624190	55.177106	
std	0.543865	9.802742	16.756311	45.018481	75.072800	
min	2.300000	29.000000	10.416670	5.000000	8.000000	
25%	3.800000	42.000000	62.696165	15.000000	19.000000	
50%	4.300000	48.000000	76.923080	23.000000	29.000000	
75%	4.600000	57.000000	87.249170	40.000000	60.000000	
max	5.000000	73.000000	100.000000	380.000000	581.000000	
	bty_f1lower	bty_f1upper	bty_f2upper	bty_m1lower	<pre>bty_m1upper \</pre>	
count	463.000000	463.000000	463.000000	463.000000	463.000000	
mean	3.963283	5.019438	5.213823	3.412527	4.146868	
std	1.873936	1.934437	2.018224	1.637102	2.110586	
min	1.000000	1.000000	1.000000	1.000000	1.000000	
25%	2.000000	4.000000	4.000000	2.000000	3.000000	
50%	4.000000	5.000000	5.000000	3.000000	4.000000	
75%	5.000000	7.000000	6.000000	5.000000	5.000000	
max	8.000000	9.000000	10.000000	7.000000	9.000000	
	bty_m2upper	bty_avg				
count	463.000000	463.000000				
mean	4.751620	4.417844				
std	1.575266	1.527380				
min	1.000000	1.667000				
25%	4.000000	3.167000				
50%	5.000000	4.333000				
75%	6.000000	5.500000				
max	9.000000	8.167000				

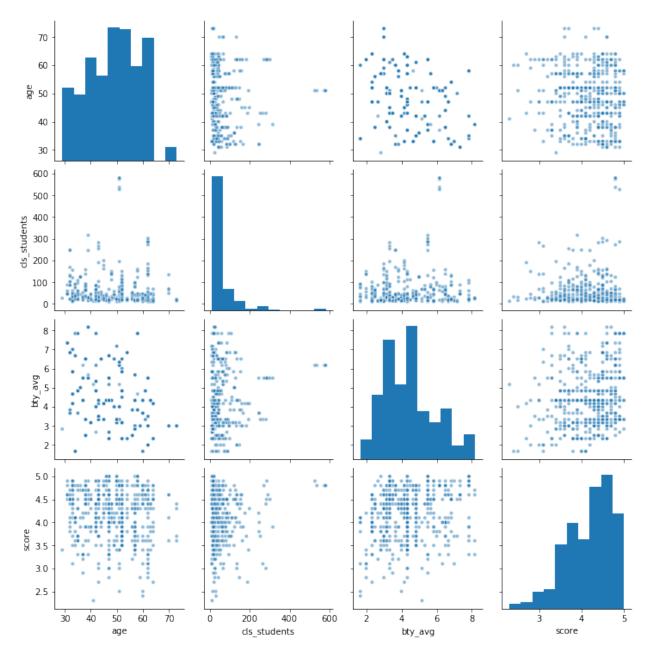
```
sns.pairplot(df, plot_kws={'alpha':0.5, 'size': 0.1})
```

## <seaborn.axisgrid.PairGrid at 0x7fe2c0c2a5e0>



With so many numeric variables, the pair plot is hard to read. We can create a pairplot excluding some variables that we don't expect to be useful for visualization: cls\_perc\_eval, cls\_did\_eval. We will also exclude the individual attractiveness ratings bty\_f1lower, bty\_f1upper, bty\_f2upper, bty\_m1lower, bty\_m1upper, bty\_m2upper, since the overall attractiveness rating is still represented by bty\_avg.

<seaborn.axisgrid.PairGrid at 0x7fe2a1d47ee0>



As part of our exploration of the data, we can also examine the effect of non-numeric variables related to the instructor and the class: rank, ethnicity, gender, language, cls\_level, cls\_profs, cls\_credits.

```
for feature in ['rank', 'ethnicity', 'gender', 'language', 'cls_level', 'cls_profs',
    'cls_credits']:
    df.groupby([feature])['score'].describe()
```

	count	mean	std	min	25%	50%	75%	max
rank								
teaching	102.0	4.284314	0.498263	3.3	3.9	4.40	4.7	5.0
tenure track	108.0	4.154630	0.561104	2.3	3.7	4.35	4.6	4.9
tenured	253.0	4.139130	0.550262	2.4	3.8	4.20	4.6	5.0

```
ethnicity
             64.0 4.071875 0.581588 2.7 3.675 4.05 4.525 5.0
minority
not minority 399.0 4.191228 0.536505 2.3 3.850 4.30 4.600 5.0
       count
                               min
                                    25% 50%
                                             75%
                 mean
gender
female 195.0 4.092821
                      0.563814
                               2.3
                                    3.7 4.1
                                             4.5
       268.0 4.234328 0.521896
                               2.4
male
                                    3.9
                                         4.3
                                             4.6
                                std min 25%
                                              50%
                                                   75% max
            count
                     mean
language
           435.0 4.189655 0.547183 2.3 3.9 4.30 4.6 5.0
english
non-english
            28.0 3.942857 0.434979 3.4 3.6 3.75
          count
                    mean
                              std min 25%
                                            50%
                                                75%
cls_level
lower
          157.0 4.238217 0.592532 2.5 3.8 4.4 4.7
          306.0 4.142157 0.515104 2.3 3.8 4.2
upper
          count
                                       25%
                                            50%
                                                75%
                              std min
                                                     \max
                    mean
cls_profs
multiple
         306.0 4.184641 0.551177 2.4 3.8 4.3 4.6 5.0
single
          157.0 4.155414 0.530529 2.3
                                      3.8 4.3
            count
                                          25%
                                              50%
                      mean
                                 std min
                                                   75%
cls credits
multi credit 436.0 4.147018 0.542464 2.3 3.8 4.2 4.6
one credit
             27.0 4.622222 0.334357 3.5 4.5 4.7 4.9 5.0
```

**Question 1** Describe the relationship between score and the overall attractiveness rating bty\_avg. Is there an apparent correlation? If so, is it a positive or a negative correlation? What about age and cls\_students, do they appear to be correlated with score?

Also describe the relationship between score and the categorical variables you explored above that are related to characteristics of the *instructor*: rank, ethnicity, gender, language. Which of these variables have an apparent correlation with score? Is it a positive or a negative correlation?

Are any of the apparent relationships you observed unexpected to you? Explain.

## **Encoding categorical variables**

For one hot encoding of categorical variables, we can use the <code>get\_dummies</code> function in <code>pandas</code>. Create a copy of the dataframe with all categorical variables transformed into indicator ("dummy") variables, and save it in a new data frame called <code>df\_enc</code>. Compare the columns of the <code>df</code> data frame versus the <code>df\_enc</code> data frame.

```
df_enc = pd.get_dummies(df)
df_enc.columns
```

## Split data

Next, we split the encoded data into a training set (70%) and test set (30%). We will be especially interested in evaluating the model performance on the test set. Since it was not used to train the model parameters (intercept and coefficients), the performance on this data gives us a better idea of how the model may perform on new data.

We'll use the train\_test\_split method in sklearn's model\_selection module. Since it randomly splits the data, we'll pass a random "state" into the function that makes the split repeatable (same split every time we run this notebook) and ensures that everyone in the class will have exactly the same split.

```
train, test = model_selection.train_test_split(df_enc, test_size=0.3, random_state=9)
# why 9? see https://dilbert.com/strip/2001-10-25
train.shape
test.shape
```

```
(324, 31)
```

```
(139, 31)
```

#### Simple linear regression

Now we are finally ready to train a regression model.

Since the article is nominally abou the attractiveness of the instructor, we will train the simple linear regression on the bty\_avg feature.

In the cell that follows, write code to

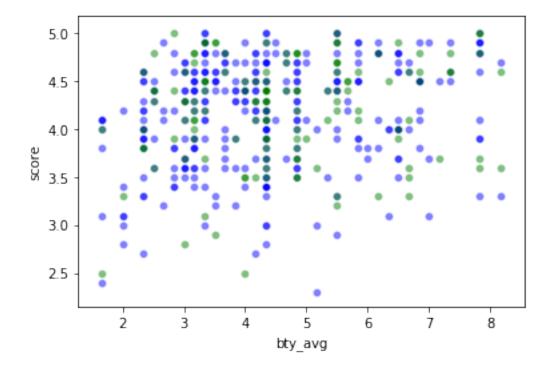
- use sklearn to fit a simple linear regression model on the training set, using bty\_avg as the feature on which to train. Save your fitted model in a variable reg\_simple.
- print the intercept and coefficient of the model.
- use predict on the fitted model to estimate the evaluation score on the training set, and save this array in y\_pred\_train.
- use predict on the fitted model to estimate the evaluation score on the test set, and save this array in y\_pred\_test.

Then run the cell after that one, which will show you the training data, the test data, and your regression line.

```
# TODO 1
# reg_simple = ...
```

```
# y_pred_train = ...
# y_pred_test = ...
```

```
sns.scatterplot(data=train, x="bty_avg", y="score", color='blue', alpha=0.5);
sns.scatterplot(data=test, x="bty_avg", y="score", color='green', alpha=0.5);
sns.lineplot(data=train, x="bty_avg", y=y_pred_train, color='red');
```



#### **Evaluate simple linear regression performance**

Now we will evaluate our model performance.

In the following cell, write a function to compute key performance metrics for your model:

- · compute the R2 score on your training data, and print it
- compute the RSS per sample on your training data, and print it
- compute the RSS per sample, divided by the sample variance of score, on your training data, and print it. Recall that this metric tells us the ratio of average error of your model to average error of prediction by mean.
- · and compute the same three metrics for your test set

```
# TODO 2 fill in the function -
```

```
def print_regression_performance(y_true_train, y_pred_train, y_true_test, y_pred_test):
    # ...
```

```
File "<ipython-input-11-8ec32a16a89a>", line 4
# ...

SyntaxError: unexpected EOF while parsing
```

Call your function to print the performance of the simple linear regression. Is a simple linear regression on bty\_avg better than a "dumb" model that predicts the mean value of score for all samples?

```
print_regression_performance(train['score'], y_pred_train, test['score'], y_pred_test)
```

```
NameError Traceback (most recent call last)
<ipython-input-12-cbaae82fc60b> in <module>
----> 1 print_regression_performance(train['score'], y_pred_train, test['score'], y_pred_test)

NameError: name 'print_regression_performance' is not defined
```

## **Multiple linear regression**

Next, we'll see if we can improve model performance using multiple linear regression, with more features included.

To start, we need to decide which features to use as input to our model. One possible approach is to use every feature in the dataset excluding the target variable, score.

You can build and view this list of features by running:

```
features = df_enc.columns.drop(['score'])
features
```

In the following cell, write code to

- use sklearn to fit a linear regression model on the training set, using the features array as the list of features to train on. Save your fitted model in a variable reg\_multi.
- print a table of the features used in the regression and the coefficient assigned to each. If you have saved your fitted regression in a variable named reg\_multi, you can create and print this table with:

```
'coefficient': reg_multi.coef_})
df_coef

# TODO 3
# reg_multi = ...
```

**Question 2** Look at the list of features and coefficients, especially those related to the attractiveness ratings.

Are these results surprising, based on the results of the simple linear regression? Explain your answer.

# **Effect of collinearity**

Note especially the coefficients associated with each of the individual attractiveness rankings, and the coefficient associated with the average attractiveness ranking. Each of these features separately seems to have a large effect; however, because they are strongly *collinear*, they cancel one another out.

(You should be able to see the collinearity clearly in the pairplot you created.)

In the following cell, write code to

- create a new features array, that drops the *individual* attractiveness rankings in addition to the score variable (but do *not* drop the average attractiveness ranking)
- use sklearn to fit a linear regression model on the training set, using the new features array as the list of features to train on. Save your fitted model in a variable reg\_avgbty.
- print a table of the features used in the regression and the coefficient assigned to each.

```
# TODO 4
# features = ...
# reg_avgbty = ...
```

**Question 3** Given the model parameters you have found, rank the following features from "strongest effect" to "weakest effect" in terms of their effect (on average) on the evaluation score:

- Instructor ethnicity
- · Instructor gender

(Note that in general, we cannot use the coefficient to compare the effect of features that have a different range. Both ethnicity and gender are represented by binary one hot-encoded variables.)

# Evaluate multiple regression model performance

Evaluate the performance of your reg\_avgbty model. In the next cell, write code to:

- use the predict function on your fitted regression to find  $\hat{y}$  for all samples in the *training* set, and save this in an array called y\_pred\_train
- use the predict function on your fitted regression to find  $\hat{y}$  for all samples in the test set, and save this in an array called y\_pred\_test
- call the print\_regression\_performance function you wrote in a previous cell, and print the performance metrics on the training and test set.

```
# TODO 5
# y_pred_train = ...
# y_pred_test = ...
```

**Question 4** Based on the analysis above, what portion of the variation in instructor teaching evaluation can be explained by the factors unrelated to teaching performance, such as the physical characteristics of the instructor?

**Question 5** Based on the analysis above, is your model better at predicting instructor teaching scores than a "dumb" model that just assigns the mean teaching score to every instructor? Explain.

**Question 6** Suppose you are hired by the ECE department to develop a classifer that will identify high-performing faculty, who will then be awarded prizes for their efforts.

Based on the analysis above, do you think it would be fair to use scores on teaching evaluations as an input to your classifier? Explain your answer.

## **Exploring unexpected correlation**

There are some features that we do not expect to be correlated with the instructor's score.

For example, consider the "features" related to the photograph used by the students who rated the instructor's attractiveness.

There is no reason that characteristics of an instructor's photograph - whether it was in black and white or color, how the instructor was dressed in the photograph - should influence the ratings of students in the instructor's class. These students most likely did not even see the photograph.

In the next cell, write code to

- create a new features array that drops the score variable, all of the individual attractiveness rankings, and the variables related to the photograph used for attractiveness rankings.
- use it to fit a model (saved in reg\_nopic).
- use reg\_nopic to predict the evaluation scores on both the training and test set
- compute the same set of metrics as above.

```
# TODO 6
# features = ...
# reg_nopic = ...
```

**Question 7** Is your model less predictive when features related to the instructor photograph are excluded? Explain.

Finally, we will observe the effect of excluding class-related variables (whether it is an upper-division or lower-division class, number of credits, etc.)

In the next cell, write code to:

- create a new features array that drops the score variable, all of the individual attractiveness rankings, the variables related to the photograph used for attractiveness rankings, and all of the variables that begin with the cls prefix.
- use it to fit a model (saved in reg\_nocls).
- use reg nocls to predict the evaluation scores on both the training and test set
- · compute the same set of metrics as above.

```
# TODO 7
# features = ...
# reg_nocls = ...
```

When a machine learning model seems to use a feature that is not expected to be correlated with the target variable (such as the characteristics of the instructor's photograph...), this can sometimes be a signal that information is "leaking" between the training and test set.

In this dataset, each row represents a single course. However, some instructors teach more than one course, and an instructor might get similar evaluation scores on all of the courses he or she teaches. (According to the paper for which this dataset was collected, 94 faculty members taught the 463 courses represented in the dataset, with some faculty members teaching as many as 13 courses.)

For example, consider the output of the following command, which prints all of the one credit courses in the data:

```
df.loc[df['cls_credits'] == 'one credit']
```

```
language
                   rank
                            ethnicity gender
    score
                                                           age
124
      3.5
               teaching not minority female
                                                  english
                                                            52
179
      4.4 tenure track
                            minority female
                                                  english
                                                            47
185
      4.6 tenure track
                            minority female
                                                  english
                                                            47
245
      4.2
               teaching not minority female
                                                  english
                                                           50
246
      4.7
               teaching not minority female
                                                  english
                                                            50
339
      4.8 tenure track not minority
                                        male
                                                  english
                                                            43
      4.9 tenure track not minority
                                        male
                                                  english
340
                                                            43
343
      4.5 tenure track not minority
                                        male
                                                  english
                                                            43
344
      4.9 tenure track not minority
                                        male
                                                  english
                                                            43
345
      4.4 tenure track not minority
                                        male
                                                  english
                                                            43
347
                                                  english
                                                            50
      4.6
            teaching
                            minority
                                        male
348
      5.0
             teaching
                            minority
                                        male
                                                  english
                                                            50
                                                  english
349
      4.9
              teaching
                            minority
                                        male
                                                           50
350
      4.6
               teaching
                            minority
                                        male
                                                  english
                                                            50
351
      4.8
               teaching
                            minority
                                        male
                                                  english
                                                            50
352
      4.9
               teaching
                            minority
                                        male
                                                  english
                                                            50
353
      4.9
               teaching
                            minority
                                        male
                                                  english
                                                            50
354
      4.9
               teaching
                            minority
                                                  english
                                                           50
                                        male
355
      5.0
               teaching
                            minority
                                        male
                                                  english
                                                           50
356
      4.5
               teaching
                            minority
                                        male
                                                  english
                                                            50
393
      4.8
               teaching not minority
                                        male
                                                  english
                                                            45
394
               teaching not minority
      4.2
                                        male
                                                  english
                                                            45
396
      4.8
               teaching not minority
                                        male
                                                  english
                                                            45
409
      4.7
               teaching not minority female
                                                  english
                                                            47
410
      4.6
               teaching not minority female
                                                  english
                                                            47
411
      4.6
               teaching not minority female
                                                  english
                                                            47
462
      4.1 tenure track
                            minority female non-english
    cls_perc_eval cls_did_eval cls_students cls_level ... cls_credits \
```

124	101	00 47000	477	10		1	
185							
246					lower	one credit	
246 6.666666 14 21 lower one credit 339 53.57143 15 28 lower one credit 340 60.0000 18 30 lower one credit 343 94.44444 17 18 lower one credit 344 84.61539 22 26 lower one credit 345 60.00000 18 30 lower one credit 346 60.00000 18 30 lower one credit 347 70.83334 17 24 lower one credit 348 90.90909 20 22 lower one credit 348 84.00000 21 25 lower one credit 349 84.00000 21 25 lower one credit 350 88.46154 23 26 lower one credit 351 86.36364 19 22 lower one credit 352 76.92308 20 26 lower one credit 353 85.00000 17 20 lower one credit 354 81.81818 18 22 lower one credit 355 95.23810 20 21 lower one credit 356 90.47619 19 21 lower one credit 394 85.00000 17 20 lower one credit 394 73.07692 19 21 lower one credit 394 73.07692 19 26 lower one credit 410 100.00000 10 10 lower one credit 411 94.11765 16 17 lower one credit 410 100.00000 28 35 lower one credit 411 94.11765 16 17 lower one credit 411 94.11765 16 17 lower one credit 412 4 6 6 6 6 3 3 5 10 1 1 lower one credit 413 94.11765 16 17 lower one credit 414 19 4.11765 16 17 lower one credit 415 2 4 4 4 2 2 4 4 4 4 2 2 4 4 4 4 4 2 4 4 4 4 2 4	185	95.23810	20	21	lower	one credit	
339   53.57143   15   28   lower   one credit	245	75.00000	24	32	lower	one credit	
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352       1       5       4       1       4         353       1       5       4       1       4         354       1       5       4       1       4         355       1       5       4       1       4         356       1       5       4       1       4         393       1       4       2       5       4         394       1       4       2       5       4         396       1       4       2       5       4         409       8       6       6       4       9	124 179 185 245 246 339 340 343 344 345 347 348 349	6 2 2 2 2 3 3 3 3 3 1 1 1	6 6 6 3 3 4 4 4 4 4 5 5	f2upper bty_n 4 6 6 5 5 4 4 4 4 4 4 4	11lower bt 2 3 3 2 2 2 2 2 2 1 1 1	y_m1upper \ 4	
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356       1       5       4       1       4         393       1       4       2       5       4         394       1       4       2       5       4         396       1       4       2       5       4         409       8       6       6       4       9	124 179 185 245 246 339 340 343 344 345 347 348 350 351 352	6 2 2 2 2 3 3 3 3 3 1 1 1 1 1	6 6 6 3 3 4 4 4 4 4 5 5 5 5 5 5	f2upper bty_n 4 6 5 5 4 4 4 4 4 4 4 4 4 4	11lower bt 2 3 3 2 2 2 2 2 2 1 1 1 1 1	y_m1upper \ 4	
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	124 179 185 245 246 339 340 343 344 345 347 348 350 351 352 353 354 355 356 393 394 396 409	6 2 2 2 2 3 3 3 3 1 1 1 1 1 1 1 1 1 1 1 1	6 6 6 6 6 6 6 3 3 4 4 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 4 4 4 4 4 4 6	f2upper bty_n 4 6 5 5 4 4 4 4 4 4 4 4 4 4 4 2 2 2 6	11lower bt 2 3 3 2 2 2 2 2 2 1 1 1 1 1 1 1 5 5 5 4	y_m1upper \ 4 5 5 3 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 9	

411 462	8		6 8	6 7	4 4	9 6	
402	3		ō	1	4	О	
	bty_m2upper	bty_avg	pic_outfit	pic_color			
124	7	4.833	not formal	color			
179	4	4.333	not formal	color			
185	4	4.333	not formal	color			
245	4	3.167	not formal	color			
246	4	3.167	not formal	color			
339	4	3.500	not formal	color			
340	4	3.500	not formal	color			
343	4	3.500	not formal	color			
344	4	3.500	not formal	color			
345	4	3.500	not formal	color			
347	5	3.333	not formal	color			
348	5	3.333	not formal	color			
349	5	3.333	not formal	color			
350	5	3.333	not formal	color			
351	5	3.333	not formal	color			
352	5	3.333	not formal	color			
353	5	3.333	not formal	color			
354	5	3.333	not formal	color			
355	5	3.333	not formal	color			
356	5	3.333	not formal	color			
393	4	3.333	not formal	color			
394	4	3.333	not formal	color			
396	4	3.333	not formal	color			
409	7	6.667	not formal	black&white			
410	7	6.667	not formal	black&white			
411	7	6.667	not formal	black&white			
462	4	5.333	not formal	color			
[27	rows x 21 col	umns]					

We observe that 10 out of 27 one-credit courses are taught by what seems to be the same instructor - an individual who is a teaching-track professor, minority ethnicity, male, English-language trained, 50 years old, average attractiveness 3.333, and whose photograph is in color and not formal.

This provides a clue regarding the apparent importance of the cls\_credits variable and other "unexpected" variables in predicting the teaching score. Certain variables may be used by the model to identify the instructor and then learn a relationship between the individual instructor and his or her typical evaluation score, instead of learning a true relationship between the variable and the evaluation score.

To explore this issue further, we will repeat our analysis using two different ways of splitting the dataset:

- 1. random split
- 2. random split that ensures that each individual *instructor* is represented in the training data or the test data, but not both.

In the latter case, if the regression model is effectively identifying individual instructors, rather than learning true relationships between instructor/course characteristics and teaching ratings, then the model will perform much worse on the test set for this type of split. This is because the instructors it has "learned" are not present in the test set.

First, we will assign an "instructor ID" to each row in our data frame:

```
instructor_id = df[['rank', 'ethnicity', 'gender', 'language',
```

```
'pic_outfit', 'pic_color']].agg('-'.join, axis=1)
instructor_id += '-' + df['age'].astype(str)
instructor_id += '-' + df['bty_avg'].astype(str)

df_enc = df_enc.assign(instructor_id = instructor_id)

df_enc['instructor_id'].head()
```

```
tenure track-minority-female-english-not forma...

instructor_id, dtype: object
```

Now we will perform our splits, train a model, and print performance metrics according to the first scheme, in which an instructor may be present in both the training set and the test set.

In the following cell, add code as indicated:

```
ss = model_selection.ShuffleSplit(n_splits=10, test_size=0.3, random_state=9)
for train_idx, test_idx in ss.split(df_enc):
   train = df_enc.iloc[train_idx]
   test = df_enc.iloc[test_idx]
   features = df_enc.columns.drop(['score', 'instructor_id'])
   print('----')
    # TODO 8: add code to train a multiple linear regression using
    # the train dataset and the list of features created above
    # save the fitted model in req_rndsplit
    # then use the model to create y_pred_train and y_pred_test,
    # the model predictions on the training set and test set.
    # Finally, use print_regression_performance to see the
    # model performance
    \# reg\_rndsplit = \dots
    # y pred train = ...
    # y_pred_test = ...
   print_regression_performance(train['score'], y_pred_train, test['score'], y_pred_test)
```

```
NameError Traceback (most recent call last)
<ipython-input-21-6f1aae6d8ea4> in <module>
        21
        22
---> 23        print_regression_performance(train['score'], y_pred_train, test['score'], y_pred_test)
```

```
NameError: name 'print_regression_performance' is not defined
```

Then, we will perform our splits, train a model, and print performance metrics according to the second scheme, in which an instructor may be present in either the training set or the test set, but not both.

In the following cell, add code as indicated:

```
gss = model_selection.GroupShuffleSplit(n_splits=10, test_size=0.3, random_state=9)
for train_idx, test_idx in gss.split(df_enc, groups=instructor_id):
    train = df_enc.iloc[train_idx]
    test = df_enc.iloc[test_idx]
   features = df_enc.columns.drop(['score', 'instructor_id'])
    # TODO 9: add code to train a multiple linear regression using
    # the train dataset and the list of features created above
    # save the fitted model in reg_grpsplit
    # then use the model to create y_pred_train and y_pred_test
    # the model predictions on the training set and test set.
    # Finally, use print_regression_performance to see the
    # model performance
    \# reg\_grpsplit = ...
    \# y_pred_train = \dots
    # y_pred_test = ...
   print_regression_performance(train['score'], y_pred_train, test['score'], y_pred_test)
```

**Question 8** Based on your analysis above, do you think your model will be useful to predict the teaching evaluation scores of a new faculty member at UT Austin, based on his or her physical characteristics and the characteristics of the course?

#### Data leakage

In this case study, we saw evidence of data leakage: The identity of the instructor "leaked" into the data set, and then the model learned the instructor ID, not a true relationship between instructor characteristics and teaching evaluation scores.

As a result, the model had overly optimistic error on the test set. The model appeared to generalize to new, unseen, data, but in fact would not generalize to different instructors.

Another example of data leakage:

You have been hired to develop a new spam classifier for NYU Tandon email. To collect a dataset for the spam classification task, you get 5,000 NYU Tandon students, faculty, and staff who agree to manually label every email they receive for the week of March 15-March 21 as "spam" (about 5%) or "not spam" (about 95%). They then share all the emails and labels with you. For example, here are a few of the emails you got from Volunteer 1, who is a member of the ECE department:

Subject	From	То	Label
April Funding Opportunities	Office of Sponsored	All Tandon	Not
	Programs	Faculty	Spam
ML TA meeting next week	Student 23451 (redacted)	Fraida Fund	Not
			Spam
Pass/fail option for students this	Ivan Selesnick	ECE Faculty	Not
semester		•	Spam
A question about quiz1	Student 19245 (redacted)	Fraida Fund	Not
·			Spam
Re: your account is locked	PayPall	Fraida Fund	Spam
Fwd: Gradescope Webinar	Ivan Selesnick	ECE Faculty	Not
·		·	Spam
Memo to Faculty on COVID-19 Protocols	Provost Katherine	All Tandon	Not
	Fleming	Faculty	Spam

You assign the emails from volunteers 1-2,500 to a training set and use it to fit a classifier, then compute the classifier accuracy on the emails from volunteers 2,501-5,000.

Your classifier does really well on the emails from volunteers 2,501-5,000 - in fact, it is 99.9999% accurate! But when you deploy it in production, it misses a lot of spam. Based on the description above, what mistake did you make that caused your performance estimate to be overly optimistic? How would you fix it?

Also potential for data leakage when:

- Learning from adjacent temporal data
- · Learning from data that includes duplicate
- Learning from a feature that is a proxy for target variable

How can we detect data leakage?

- Surprising patterns in data (via exploratory data analysis)
- · Performance is "too good to be true"
- Features that shouldn't be important (based on common sense/domain knowledge) play a role in reducing error
- Early testing in production