Project topic: Letter OCR(Optical character recognition)

Problem statement: Develop an efficient and accurate system for recognizing English letters

Introduction: In this project, The objective of the letter recognition task is to classify a large number of black-and-white rectangular pixel displays into one of the 26 capital letters of the English alphabet.

Motivation: The motivation behind building a letter OCR (Optical Character Recognition) project is to create a system that can understand and interpret handwritten or printed letters just like humans do. This project can be useful in many real-life scenarios, such as automating tasks like sorting mail, digitizing documents, or assisting people with disabilities who may have difficulty reading printed text. By using machine learning techniques, we aim to train a computer program to recognize and classify letters accurately from images or scanned documents. Ultimately, the goal is to make letter recognition faster, more efficient, and accessible to everyone, making our daily tasks easier and more convenient.

Dataset:

- 1. Data is taken from the Uci ml repository (dataset).[UCl dataset is already preprocessed for machine learning.]
- 2. It contains English alphabets images in different 20-fonts.
- 3. Each letter is presented in a bounding box containing black and white pixels whose intensity varies.
- 4. **Associated task** -> classification task
- 5. Objective:
 - The objective of the dataset is to classify black-and-white rectangular pixel displays into one of the 26 capital letters of the English alphabet.
 - b. Each pixel display represents a character image.

6. Characteristics of Character Images:

- a. The character images were generated based on 20 different fonts.
- b. Each letter within these 20 fonts was randomly distorted to create a total of 20,000 unique stimuli.
- c. These distortions likely introduce variations in the appearance of the characters, making the classification task more challenging.
 - i. <u>Different Fonts:</u> Imagine you have 20 different styles of writing, like different fonts on your computer. Each font has its own unique look

- and feel. For example, one font might have bold letters, while another might have slanted ones.
- ii. Random Distortions: Now, within each of these fonts, we take each letter of the alphabet (A-Z) and randomly mess around with it a bit. We might squish some letters, stretch others, or tilt them slightly. These are distortions, changes to the shape of the letters.
- iii. <u>Creating Variations:</u> By applying these random distortions, we end up with 20,000 different versions of the alphabet. Each version is slightly different from the others because of the random changes we made. This gives us a big variety of letter images to work with.
- iv. <u>Challenges for Classification:</u> With so many different versions of the letters, it becomes harder for a computer to tell them apart. The variations in appearance make it trickier for the computer to recognize which letter is which. It's like trying to figure out if two handwritten letters are the same when they're written in different styles and with different quirks.

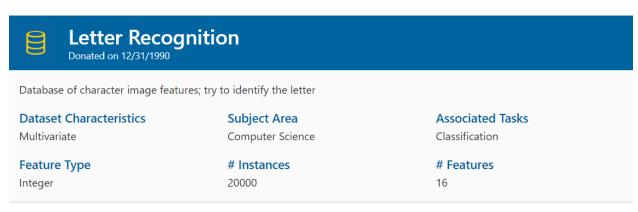
7. Features:

- a. Each character image was converted into 16 primitive numerical attributes.
- These attributes include statistical moments (e.g., mean, variance) and edge counts, which capture different aspects of the character's visual characteristics.
- c. The original continuous numerical values of these attributes were scaled to fit into a range of integer values from 0 through 15.
- d. This scaling likely simplifies the feature representation and reduces computational complexity.
 - i. <u>Conversion into Numerical Attributes</u>: Each character image is initially represented as a collection of pixels, which is not directly suitable for machine learning algorithms. To make these images usable for classification, they are transformed into numerical attributes. These attributes aim to capture various aspects of the character's visual characteristics that could be useful for distinguishing between different letters.
 - ii. Statistical Moments and Edge Counts: The attributes extracted from the character images include statistical moments (such as mean and variance) and edge counts. Statistical moments describe the distribution of pixel intensities in the image, providing information about its overall brightness and contrast. Edge counts capture the number of edges or transitions between different pixel

- intensities in the image, which can indicate the presence of edges or contours of the character.
- iii. Scaling to Integer Values: The original continuous numerical values of these attributes are scaled to fit into a range of integer values from 0 through 15. This scaling process transforms the numerical attributes into a more manageable range of values. By converting the attributes to integers and restricting them to a smaller range (0-15), it simplifies the feature representation and reduces computational complexity. Integer values are often easier to work with computationally and can lead to faster processing times compared to using continuous values.
- iv. Simplification and Computational Efficiency: The scaling process simplifies the feature representation by reducing the number of unique values that each attribute can take. This simplification can help in reducing the dimensionality of the dataset, making it easier to analyze and interpret. Additionally, reducing the range of values to a smaller integer range can lead to computational efficiency, as integer operations are typically faster and require less memory compared to floating-point operations.

8. Training and Testing:

- a. The dataset is typically divided into training and testing subsets.
- b. Out of 20,000, the first 16,000 items (stimuli) are used for training the model.
- c. The trained model is then evaluated on the remaining 4,000 items to predict the letter category for each stimulus.
- d. This approach allows for assessing the performance of the model on unseen data and estimating its generalization ability.



9. Different Fonts:

- a. Imagine you have 20 different styles of writing, like different fonts on your computer. Each font has its own unique look and feel.
- b. For example, one font might have bold letters, while another might have slanted ones.

10. Random Distortions:

- a. Now, within each of these fonts, we take each letter of the alphabet (A-Z) and randomly mess around with it a bit.
- b. We might squish some letters, stretch others, or tilt them slightly. These are distortions, changes to the shape of the letters.

11. Creating Variations:

- a. By applying these random distortions, we end up with 20,000 different versions of the alphabet.
- b. Each version is slightly different from the others because of the random changes we made.
- c. This gives us a big variety of letter images to work with.

12. Challenges for Classification:

- a. With so many different versions of the letters, it becomes harder for a computer to tell them apart.
- b. The variations in appearance make it trickier for the computer to recognize which letter is which.
- c. It's like trying to figure out if two handwritten letters are the same when they're written in different styles and with different quirks.

13. Has Missing Values? No

14. Variable: What features did you use to represent the letters in the images?

Variable Name	Role	Туре	Description	Units	Missing Values
lettr	Target	Categorical	Capital letter from A to Z	N/A	No
x-box	Feature	Integer	Horizontal position of the bounding box	Pixels	No
y-box	Feature	Integer	Vertical position of the bounding box	Pixels	No
width	Feature	Integer	Width of the bounding box	Pixels	No
height	Feature	Integer	Height of the bounding box	Pixels	No
onpix	Feature	Integer	Total number of "on" pixels within the bounding box	Pixels	No
x-bar	Feature	Integer	Mean horizontal position of "on" pixels	Pixels	No
y-bar	Feature	Integer	Mean vertical position of "on" pixels	Pixels	No
x2bar	Feature	Integer	Mean variance of the horizontal position	Pixels	No
y2bar	Feature	Integer	Mean variance of the vertical position	Pixels	No
xybar	Feature	Integer	Mean correlation between horizontal and vertical positions	N/A	No
x2ybr	Feature	Integer	Mean of $(x * x * y)$ within the bounding box	Pixels	No
xy2br	Feature	Integer	Mean of $(x * y * y)$ within the bounding box	Pixels	No
x-ege	Feature	Integer	Mean edge count from left to right	Pixels	No
xegvy	Feature	Integer	Correlation of x-ege with y	N/A	No
y-ege	Feature	Integer	Mean edge count from bottom to top	Pixels	No
yegvx	Feature	Integer	Correlation of y-ege with x	N/A	No

*onpix-> black pixel

15. Data preprocessing:

a. **Data Cleaning:** Check for missing values: The dataset is checked for any missing values in each attribute. According to the provided information, there are no missing values, so no further action is needed for handling missing values.

- b. Data Transformation: Conversion into numerical attributes: The character images are converted into 16 primitive numerical attributes, including statistical moments and edge counts, to represent various visual characteristics of the characters.
- c. Feature Selection/Extraction: Feature extraction: Features are extracted from the character images to represent different aspects such as statistical moments and edge counts. This step selects relevant features that capture the essential information for distinguishing between different letters.
- **d. Data Integration:** No specific data integration process is mentioned in the provided information. However, if multiple datasets were to be integrated for this task, techniques such as merging datasets, resolving inconsistencies, and aligning timestamps could be applied.
- e. **Normalization:** Scaling attributes: The original continuous numerical values of the extracted attributes are scaled to fit into a range of integer values from 0 through 15. This normalization step simplifies the feature representation and reduces computational complexity.
- f. **Encoding Categorical Variables:** The target variable "lettr," which represents the capital letter of the English alphabet, is encoded into numerical representations. Since it is a categorical variable with 26 possible values (A-Z), techniques like one-hot encoding or label encoding could be applied if necessary.
- g. Handling Imbalanced Data: There is no mention of handling imbalanced data explicitly in the provided information. However, if the distribution of letters in the dataset is imbalanced (i.e., some letters are represented more frequently than others), techniques like resampling (e.g., oversampling, undersampling) or using appropriate evaluation metrics could be employed to address this issue.
- h. **Data Partitioning:** The dataset 20,000 is divided into training and testing subsets, with the first 16,000 items used for training the model and the remaining 4,000 items used for evaluation. This approach ensures that the model's performance is assessed on unseen data and estimates its generalization ability.
- i. Handling Text and Image Data The provided information indicates that the dataset consists of character images represented as numerical attributes. Techniques specific to handling text and image data, such as resizing, noise reduction, or image enhancement, may have been applied during the conversion of character images into numerical attributes.
- 16. Techniques for image enhancement, noise reduction, or normalization:

a. Image Enhancement:

- Histogram Equalization: Improves the contrast of the image by redistributing pixel intensities. It makes an image clearer by spreading out the pixel intensities more evenly. This helps to enhance the contrast, making the dark areas darker and the bright areas brighter.
- ii. Adaptive Histogram Equalization: Enhances local contrast in images, which can be beneficial for images with varying lighting conditions. Similar to regular histogram equalization, but it focuses on smaller regions of the image instead of the whole thing. This helps to improve contrast in specific areas, which is handy for images with uneven lighting.
- iii. **Gamma Correction:** Adjusts the brightness and contrast of images by applying a power-law transformation. This adjusts the brightness and contrast of the image using a special mathematical formula. It can make images look more natural by tweaking how light and dark areas are displayed.
- b. Noise Reduction: These techniques help to clean up unwanted graininess or speckles in images caused by factors like low light or a poor quality camera.
 - Gaussian Blur: Applies a Gaussian filter to smooth out noise and reduce detail in the image. Softens the image by averaging nearby pixel values, which can help to reduce noise and make details less harsh.
 - ii. **Median Filtering:** Replaces each pixel's value with the median value of neighboring pixels, which is effective for removing salt-and-pepper noise. It replaces each pixel's value with the median value of its neighboring pixels. This is good for getting rid of random specks or spots in the image.
 - iii. **Bilateral Filtering:** Preserves edges while reducing noise by smoothing pixels with similar intensity values. It smooths out the image while still preserving important details like edges. It works by averaging pixels with similar intensity values.

c. Normalization:

- i. Min-Max Scaling: Scales pixel values to a range between 0 and 1.
- ii. **Z-score Normalization:** Standardizes pixel values by subtracting the mean and dividing by the standard deviation.
- iii. **Scaling to a Fixed Range**: Scales pixel values to fit within a specific range, such as [0, 255] for 8-bit grayscale images.

17. How did you handle issues such as varying lighting conditions, noise, or distortions in the images?

a. Image Preprocessing:

- Contrast Enhancement: Techniques like histogram equalization or adaptive histogram equalization can improve the contrast of images, making characters more distinguishable from the background, especially in images with varying lighting conditions.
- ii. **Noise Reduction:** Applying filters such as Gaussian blur, median filtering, or bilateral filtering can help reduce noise in images, making character edges clearer and more defined.
- iii. **Deskewing:** Correcting skewness in images ensures that characters are properly aligned horizontally, reducing the impact of distortions caused by tilting or slanting.
- b. Data Augmentation: creating new data from existing one.
 - Brightness and Contrast Adjustment: Randomly adjusting the brightness and contrast of images can simulate varying lighting conditions, making the model more robust to such variations during inference.
 - ii. Rotation and Shearing: Applying random rotations and shearing to images can simulate distortions caused by different viewing angles or perspectives, allowing the model to learn invariant representations of characters.

c. Normalization:

- i. Global and Local Normalization: Standardizing pixel values globally or locally within small patches of the image can help mitigate the effects of varying lighting conditions and improve the consistency of features extracted from different regions of the image.
- ii. Normalization techniques could be applied to standardize pixel values across images, making them less sensitive to variations in lighting conditions.

d. Model Architecture:

- Feature Extraction Layers: Using convolutional layers in the model architecture can help automatically learn features that are robust to variations in lighting, noise, and distortions, capturing hierarchical patterns in the input images.
- ii. Regularization Techniques: Applying regularization techniques such as dropout or weight decay can help prevent overfitting to noise and distortions in the training data, leading to improved generalization performance.

e. Data Quality Control:

- Data Filtering: Removing low-quality or heavily distorted images from the dataset can prevent them from negatively impacting the model's performance.
- ii. Data Augmentation Validation: Ensuring that augmented images remain visually plausible and representative of real-world variations can prevent the introduction of unrealistic distortions during data augmentation.

f. Model Robustness:

 Using deep learning models with architectures designed to handle variations in input data, such as convolutional neural networks (CNNs), could also help in capturing features robustly across different fonts, distortions, and lighting conditions.

Feature Extraction:

- **18.What features did you use to represent the letters in the images?** The features used to represent the letters in the images include 16 primitive numerical attributes per character image. These attributes capture various visual characteristics of the letters, such as statistical moments (e.g., mean, variance) and edge counts.
- 19. Did you employ any feature extraction techniques such as edge detection, histogram of oriented gradients (HOG), or convolutional neural network (CNN) features?
 - a. Edge Detection: While edge detection is not explicitly mentioned in the provided information, it's a common technique used in image processing. Edge detection algorithms could have been applied to detect the boundaries of characters, which can be crucial for distinguishing between different letters.
 - **b. Histogram of Oriented Gradients (HOG):** HOG features could have been extracted to capture the local gradient information of the character images, which is useful for recognizing shapes and patterns.
 - c. Convolutional Neural Network (CNN) Features: While CNN features are not mentioned, they are widely used in image recognition tasks. CNNs could have been employed to automatically extract hierarchical features from the character images, learning representations directly from the pixel values.
- 20. How did you ensure that the selected features captured the relevant characteristics of the letters?

- a. The selected features, including statistical moments and edge counts, aim to capture important visual characteristics of the letters that are relevant for distinguishing between different alphabet characters.
- b. The choice of features may have been based on prior knowledge of OCR tasks and image processing techniques known to be effective for character recognition.
- c. Additionally, experimentation and validation using machine learning models trained on the extracted features would have helped ensure that the selected features adequately capture the relevant characteristics of the letters and contribute to accurate classification.

[*Histogram of Oriented Gradients (HOG) is a feature descriptor used in computer vision and image processing for object detection and recognition tasks. It works by capturing the distribution of intensity gradients or edge directions in an image.

Here's how it works:

- Gradient Calculation: First, the gradient of the image is computed. The gradient represents the rate of change of intensity values at each pixel location. Typically, the image is convolved with a pair of filters (like Sobel filters) in the horizontal and vertical directions to compute the gradients.
- 2. Orientation Binning: The image is divided into small cells, and for each pixel within a cell, its gradient magnitude and orientation are calculated. Then, these gradient orientations are assigned to bins in a histogram based on their direction.
- 3. Histogram Normalization: To make the descriptor more robust to changes in illumination and contrast, the histograms for neighboring cells are often grouped together and normalized. This helps to ensure that the descriptor is less sensitive to variations in lighting conditions.
- 4. Block Normalization: To further improve robustness, the image is divided into larger blocks, and the histograms within each block are concatenated together. Then, the block histograms are normalized to account for variations in contrast and illumination across the entire image.

The gradient in HOG refers to the rate of change of intensity values in the image. It's calculated by computing the derivatives of the image along the horizontal and vertical axes, which represent the direction and magnitude of the changes in intensity. These gradients are essential for capturing the edges and textures in an image, which are crucial for object detection and recognition tasks.]

Libraries import:

- 1. pandas -> pd
- sklearn.model_selection -> train_test_split
- 3. sklearn -> svm
- 4. sklearn.neighbors -> KNeighborsClassifier
- sklearn.tree -> DecisionTreeClassifier
- 6. Sklearn.naive bayes -> GaussianNB
- 7. Sklearn.metrics -> accuracy score, precision score, recall score, f1 score
- 8. matplotlib.pyplot -> plt
- 9. seaborn -> sns
- 10. numpy -> np

CODE AND OUTPUT EXPLANATION

```
import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn import svm
from sklearn.neighbors import KNeighborsClassifier
from sklearn.tree import DecisionTreeClassifier
from sklearn.naive_bayes import GaussianNB
from sklearn.metrics import accuracy_score, precision_score, recall_score, f1_score
import matplotlib.pyplot as plt
import seaborn as sns
import numpy as np
#Load the dataset
data = pd.read_csv('letter-recognition.data', header=None)
# Split features and target variable
X = data.iloc[:, 1:]
y = data.iloc[:, 0]
data.head()
```

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
0	Т	2	8	3	5	1	8	13	0	6	6	10	8	0	8	0	8
1	1	5	12	3	7	2	10	5	5	4	13	3	9	2	8	4	10
2	D	4	11	6	8	6	10	6	2	6	10	3	7	3	7	3	9
3	N	7	11	6	6	3	5	9	4	6	4	4	10	6	10	2	8
4	G	2	1	3	1	1	8	6	6	6	6	5	9	1	7	5	10

- The first column contains the target variable (letters T, I, D, N, G).
- The remaining columns contain the feature values for each observation.

The features describe above 1-16 are:

- 1. **x-box (Feature 1):** Horizontal position of the box.
- y-box (Feature 2): Vertical position of the box.
- 3. width (Feature 3): Width of the box.
- 4. **high (Feature 4):** Height of the box.
- 5. **onpix (Feature 5):** Total number of on pixels (pixels with value 1) within the box.
- 6. **x-bar (Feature 6):** Mean x coordinate of on pixels within the box.
- 7. **y-bar (Feature 7):** Mean y coordinate of on pixels within the box.
- 8. **x2bar** (Feature 8): Mean x variance (second moment) of the image.
- 9. **y2bar** (Feature 9): Mean y variance (second moment) of the image.
- 10. **xybar (Feature 10)**: Mean x-y correlation (cross-moment) of the image.
- 11. x2ybr (Feature 11): Mean of x * x * y (edge count left to right).
- 12. xy2br (Feature 12): Mean of x * y * y (edge count bottom to top).
- 13. **x-ege (Feature 13**): Mean edge count left to right (x-ege).
- 14. **xegvy (Feature 14**): Correlation of x-ege with y.
- 15. **y-ege (Feature 15)**: Mean edge count bottom to top (y-ege).
- 16. **yegvx (Feature 16**): Correlation of y-ege with x.
- * The term "second moment" refers to a statistical measure of the distribution of data points around the mean.

```
44
45 X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
46
47
```

The line of code train_test_split(X, y, test_size=0.2, random_state=42) is splitting the dataset into training and testing subsets. Let's break down each parameter:

- X: This represents the features or independent variables of the dataset.
- **y:** This represents the target variable or the labels associated with each data point.
- test_size=0.2: This parameter specifies the proportion of the dataset to include in the test split. In this case, it's set to 0.2, meaning that 20% of the data will be used for testing, and the remaining 80% will be used for training.
- random_state=42: This parameter sets the random seed for reproducibility. By setting a random seed, we ensure that each time the code is run, the same random splitting of the data occurs, which helps in obtaining consistent results across different runs.
- After executing this line of code, the variables X_train, X_test, y_train, and y_test will hold the following subsets of the data:

- X_train: This contains the features for training the model. It will consist of 80% of the original dataset, randomly selected.
- X_test: This contains the features for evaluating the trained model. It will
 consist of 20% of the original dataset, randomly selected.
- y_train: This contains the corresponding labels for the training data (X_train).
- o **y_test:** This contains the corresponding labels for the test data (X_test).
- This splitting of the dataset into training and testing subsets is crucial in machine learning because it allows us to train the model on one subset and evaluate its performance on another subset, ensuring that the model's performance generalizes well to unseen data.
- The random_state parameter in the train_test_split function serves to initialize the random number generator. When you set random_state to a specific value (in this case, 42), it ensures that the data is split into training and testing sets in a reproducible manner.Here's why specifying random state is important:
 - Reproducibility: By setting random_state to a fixed value, you ensure that the data splitting process is deterministic. This means that every time you run the code with the same random_state, you'll get the same result, making your experiments reproducible.
 - Consistency: When you share your code or collaborate with others, using a fixed random_state ensures that everyone obtains the same results.
 This consistency is crucial for validating and comparing different models.
 - Debugging: If you encounter unexpected results or errors, fixing the random_state allows you to debug more effectively. You can isolate issues related to data splitting and rule out randomness as a potential cause.
 - In summary, setting random_state ensures reproducibility, consistency, and ease of debugging in machine learning experiments. While the specific value (42 in this case) is arbitrary, it's a common practice to use well-known numbers like 42 for this purpose

Training Models:

SVM

```
svm_model = svm.SVC()
svm_model.fit(X_train, y_train)
svm_predictions = svm_model.predict(X_test)
svm_accuracy = accuracy_score(y_test, svm_predictions)
svm_precision = precision_score(y_test, svm_predictions, average='weighted')
svm_recall = recall_score(y_test, svm_predictions, average='weighted')
svm_f1 = f1_score(y_test, svm_predictions, average='weighted')
```

- Initialize SVM Model: svm model = svm.SVC() (Support vector classifier)
 - This line creates an SVM classifier object using the svc class from the svm module. By default, this creates an SVM with a radial basis function (RBF) kernel.(RBF-> kernel function)
- Train the Model: svm model.fit(X train, y train)
 - This line trains the SVM model on the training data (x_train, y_train). It learns to distinguish between different classes based on the features (x train) and their corresponding labels (y train).
- Make Predictions: svm predictions = svm model.predict(X test)
 - This line uses the trained SVM model to predict the labels for the test data (x test). The predicted labels are stored in svm predictions.
- Evaluate Accuracy: svm_accuracy = accuracy_score(y_test, svm predictions)
 - This line computes the accuracy of the SVM model on the test data. It compares the predicted labels (svm_predictions) with the actual labels (y test) and calculates the fraction of correct predictions.
- Evaluate Precision: svm_precision = precision_score(y_test, svm predictions, average='weighted')
 - Precision is a measure of the accuracy of the positive predictions. This
 line calculates the precision of the SVM model using the test data. The
 parameter average='weighted' indicates that precision is calculated by

taking the weighted average of precision scores for each class, weighted by the number of true instances for each class.

- Evaluate Recall: svm_recall = recall_score(y_test, svm_predictions, average='weighted')
 - Recall (also known as sensitivity) is a measure of the ability of the classifier to find all the positive instances. This line calculates the recall of the SVM model using the test data. Similar to precision, average='weighted' calculates the weighted average of recall scores for each class.
- Evaluate F1 Score: svm_f1 = f1_score(y_test, svm_predictions, average='weighted')
 - The F1 score is the harmonic mean of precision and recall. It provides a
 balance between precision and recall. This line calculates the F1 score of
 the SVM model using the test data. Like precision and recall,
 average='weighted' calculates the weighted average of F1 scores for
 each class.

We take weighted average because:

We take the weighted average of precision, recall, and F1 score in scenarios where we have imbalanced datasets, meaning that some classes have more instances than others. Here's why we use weighted averages:

- 1. Class Imbalance Handling: In many real-world classification problems, the number of instances in each class is not evenly distributed. For example, in a binary classification task where one class is rare, say only 10% of the data, accuracy might not be the best metric. In such cases, a model might achieve high accuracy by simply predicting the majority class most of the time. However, this model would perform poorly on the minority class. Weighted averaging helps address this issue by considering the class distribution when calculating the metric.
- 2. **Equal Importance of Classes**: Weighted averaging ensures that each class contributes proportionally to the overall metric, regardless of its size. Classes with more instances have a greater influence on the metric, but all classes are still taken into account. This is particularly important when evaluating the performance of a classifier in a multi-class classification problem.
- 3. **Balanced Evaluation:** By using weighted averaging, we aim to obtain a balanced evaluation of the classifier's performance across all classes. It provides insights into how well the classifier generalizes to different classes, taking into account both the prediction accuracy and the distribution of instances in each class.

Using 'weighted' as the average parameter is particularly useful when dealing with imbalanced datasets where some classes might have more instances than others. It ensures that each class contributes proportionally to the overall metric, considering the class imbalance.

SVM

Support Vector Machine (SVM) is a powerful supervised learning algorithm used for classification and regression tasks. Here are the key points to understand about SVM:

1. Linear and Non-linear Classification:

- SVM can perform both linear and non-linear classification tasks.
- In linear classification, SVM finds the hyperplane that best separates the classes in the feature space.
- For non-linear classification, SVM uses kernel functions (such as the radial basis function, polynomial, or sigmoid) to transform the input features into a higher-dimensional space where classes are separable by hyperplanes.

2. Margin Maximization:

- SVM aims to maximize the margin, which is the distance between the hyperplane and the nearest data points (called support vectors).
- Maximizing the margin helps SVM achieve better generalization by increasing the separation between classes and reducing the risk of overfitting.

3. Support Vectors:

- Support vectors are the data points that lie closest to the decision boundary (hyperplane).
- They are crucial for defining the decision boundary and determining the margin.

4. Kernel Trick:

- The kernel trick allows SVM to handle non-linear classification tasks by implicitly mapping input features into a higher-dimensional space.
- Common kernel functions include the radial basis function (RBF), polynomial, and sigmoid kernels.
- The choice of kernel function and its parameters (such as the kernel width in RBF) significantly impacts the performance of SVM.

5. Regularization Parameter (C):

• SVM introduces a regularization parameter (C) to control the trade-off between maximizing the margin and minimizing the classification error.

- A smaller value of C allows for a wider margin but may lead to misclassification of some data points.
- A larger value of C penalizes misclassifications more heavily, leading to a narrower margin but potentially better classification accuracy.

6. Dual Optimization Problem:

- SVM can be formulated as a convex optimization problem, particularly the dual optimization problem.
- Solving the dual optimization problem is computationally efficient, even for large datasets, due to the use of convex optimization techniques.

7. Scalability:

- SVM is generally considered scalable, especially for high-dimensional datasets with relatively few samples.
- However, for very large datasets, training SVM can become computationally expensive, especially with non-linear kernels.

8. Versatility:

- SVM is versatile and widely used in various domains, including text classification, image recognition, bioinformatics, and financial forecasting.
- It's effective when the number of features is much greater than the number of samples and when dealing with high-dimensional data.

In summary, SVM is a versatile and powerful algorithm for both linear and non-linear classification tasks. Its ability to maximize the margin between classes, handle nonlinear decision boundaries, and leverage kernel functions make it one of the most popular choices for classification in machine learning.

KNN

```
knn_model = KNeighborsClassifier()
knn_model.fit(X_train, y_train)
knn_predictions = knn_model.predict(X_test)
knn_accuracy = accuracy_score(y_test, knn_predictions)
knn_precision = precision_score(y_test, knn_predictions, average='weighted')
knn_recall = recall_score(y_test, knn_predictions, average='weighted')
knn_f1 = f1_score(y_test, knn_predictions, average='weighted')
```

- Initialize KNN Model: knn model = KNeighborsClassifier()
 - This line creates a KNN classifier object using the KNeighborsClassifier class from the neighbors module. By default, it uses the Euclidean distance metric to find the nearest neighbors.

- 2. Train the Model: knn model.fit(X train, y train)
 - This line trains the KNN model on the training data (x_train, y_train). It memorizes the training instances to use them for making predictions later.
- 3. Make Predictions: knn predictions = knn model.predict(X test)
 - This line uses the trained KNN model to predict the labels for the test data (x test). The predicted labels are stored in knn predictions.
- - This line computes the accuracy of the KNN model on the test data. It
 compares the predicted labels (knn_predictions) with the actual labels
 (y_test) and calculates the fraction of correct predictions.
- 5. Evaluate Precision: knn_precision = precision_score(y_test, knn predictions, average='weighted')
 - Precision is a measure of the accuracy of the positive predictions. This
 line calculates the precision of the KNN model using the test data. The
 parameter average='weighted' indicates that precision is calculated by
 taking the weighted average of precision scores for each class, weighted
 by the number of true instances for each class.
- 6. Evaluate Recall: knn_recall = recall_score(y_test, knn_predictions, average='weighted')
 - Recall (also known as sensitivity) is a measure of the ability of the classifier to find all the positive instances. This line calculates the recall of the KNN model using the test data. Similar to precision, average='weighted' calculates the weighted average of recall scores for each class.
- 7. Evaluate F1 Score: knn_f1 = f1_score(y_test, knn_predictions,
 average='weighted')
 - The F1 score is the harmonic mean of precision and recall. It provides a
 balance between precision and recall. This line calculates the F1 score of
 the KNN model using the test data. Like precision and recall,
 average='weighted' calculates the weighted average of F1 scores for
 each class.

KNN- Algorithm

8. Introduction:

- KNN is a non-parametric(don't make predictions) (supervised learning / instance based technique) and lazy learning algorithm used for classification and regression tasks.
- It's called "lazy" because it doesn't learn a discriminative function from the

training data. Instead, it memorizes the training instances and makes predictions based on their similarity to new instances during inference.

9. Basic Idea:

- The fundamental idea behind KNN is to predict the label of a new instance by examining the labels of its k nearest neighbors in the feature space.
- The class label assigned to the new instance is typically determined by a majority vote (for classification) or averaging (for regression) among its k nearest neighbors.

10. Distance Metric:

- KNN uses a distance metric (usually Euclidean distance) to measure the similarity between instances in the feature space.
- Other distance metrics like Manhattan distance, Minkowski distance, or cosine similarity can also be used depending on the problem and the nature of the data.

11. Hyperparameter k:

- The parameter k represents the number of nearest neighbors to consider when making predictions.
- The choice of k significantly impacts the model's performance. A smaller k may lead to higher variance (more sensitive to noise), while a larger k may lead to higher bias (smoother decision boundaries).
- There is no particular way to determine the best value for "K", so we need to try some values to find the best out of them. The most preferred value for K is 5.
- A very low value for K such as K=1 or K=2, can be noisy and lead to the effects of outliers in the model.
- Large values for K are good, but it may find some difficulties.

12. Decision Boundary:

- KNN's decision boundary is non-linear and can adapt to the shape of the data distribution.
- In regions where data points are densely clustered, the decision boundary tends to be smoother, while in regions with sparse data, the decision boundary may be more jagged.

13. Scalability:

- One drawback of KNN is its computational complexity during inference, especially for large datasets, as it requires computing distances between the new instance and all training instances.
- Approximate nearest neighbor methods or dimensionality reduction techniques (like PCA) can be employed to mitigate this issue.

14. Handling Imbalanced Data:

- KNN may suffer from bias towards the majority class in imbalanced datasets, where one class significantly outnumbers the others.
- Techniques like oversampling, undersampling, or adjusting class weights can help alleviate this bias.

15. Feature Scaling:

• Since KNN relies on the distance between data points, it's essential to scale the features to a similar range to prevent features with larger scales from dominating the distance calculation.

16. Versatility:

- KNN is versatile and can be applied to various types of data, including numerical, categorical, and mixed data.
- It's commonly used in recommendation systems, pattern recognition, anomaly detection, and clustering tasks.

In summary, KNN is a simple yet powerful algorithm that makes predictions based on the similarity of instances in the feature space. Its simplicity, interpretability, and ability to handle non-linear decision boundaries make it a popular choice for many machine learning applications. However, its scalability and sensitivity to the choice of hyperparameters should be considered when applying it to large datasets or complex problems.

Decision Tree

```
dt_model = DecisionTreeClassifier()
dt_model.fit(X_train, y_train)
dt_predictions = dt_model.predict(X_test)
dt_accuracy = accuracy_score(y_test, dt_predictions)
dt_precision = precision_score(y_test, dt_predictions, average='weighted')
dt_recall = recall_score(y_test, dt_predictions, average='weighted')
dt_f1 = f1_score(y_test, dt_predictions, average='weighted')
```

Initialize Decision Tree Model:

dt_model = DecisionTreeClassifier(): This line creates a Decision Tree classifier object using the DecisionTreeClassifier class from the tree module. By default, it creates a decision tree using the Gini impurity criterion for splitting.

2. Train the Model:

• dt_model.fit(x_train, y_train): This line trains the Decision Tree model on the training data (x_train, y_train). The model learns to make predictions by recursively splitting the feature space based on the features and their values.

3. Make Predictions:

• dt_predictions = dt_model.predict(X_test): This line uses the trained Decision Tree model to predict the labels for the test data (x_test). The predicted labels are stored in dt_predictions.

4. Evaluate Accuracy:

dt_accuracy = accuracy_score(y_test, dt_predictions): This line computes the accuracy of the Decision Tree model on the test data. It compares the predicted labels (dt_predictions) with the actual labels (y_test) and calculates the fraction of correct predictions.

5. Evaluate Precision:

• dt_precision = precision_score(y_test, dt_predictions, average='weighted'): Precision is a measure of the accuracy of positive predictions. This line calculates the precision of the Decision Tree model using the test data. The parameter average='weighted' indicates that precision is calculated by taking the weighted average of precision scores for each class, weighted by the number of true instances for each class.

6. Evaluate Recall:

 dt_recall = recall_score(y_test, dt_predictions, average='weighted'): Recall (also known as sensitivity) measures the ability of the classifier to find all the positive instances. This line calculates the recall of the Decision Tree model using the test data. Similar to precision, average='weighted' calculates the weighted average of recall scores for each class.

7. Evaluate F1 Score:

dt_f1 = f1_score(y_test, dt_predictions, average='weighted'): The F1 score is the harmonic mean of precision and recall. It provides a balance between precision and recall. This line calculates the F1 score of the Decision Tree model using the test data. Like precision and recall, average='weighted' calculates the weighted average of F1 scores for each class.

These evaluation metrics provide insights into the performance of the Decision Tree model in terms of accuracy, precision, recall, and F1 score on the test data. They help assess how well the model generalizes to unseen data and how effectively it classifies

instances into different classes.

GINNI IMPURITY

The Gini impurity is a measure of the impurity or disorder of a set of data points in a decision tree node. It's used as a criterion for deciding how to split the data at each node of a decision tree during the training process.

Here's how it works:

- 1. **Definition:** Gini impurity measures the probability of incorrectly classifying a randomly chosen element if it were randomly labeled according to the distribution of labels in the node.
- 2. **Mathematical Formulation:** For a node with N samples and K classes, the Gini impurity (G) is calculated as: $G = 1 \sum_{i=1}^k p_i^2$ where pi is the probability of randomly selecting a sample of class i in the node.

3. Interpretation:

- A Gini impurity value of 0 indicates that the node is pure, meaning all the samples belong to the same class.
- A Gini impurity value closer to 1 implies a higher level of impurity or mixed classes within the node.

4. Splitting Criteria:

- When building a decision tree, the algorithm searches for the feature and the threshold that minimizes the weighted sum of the Gini impurities of the child nodes after the split.
- It iterates through all features and their possible thresholds to find the split that results in the lowest overall Gini impurity.
- The idea is to maximize the information gain, i.e., the reduction in impurity, at each split, leading to more homogeneous child nodes.

5. Advantages:

- Simple to compute and understand.
- Works well for binary classification problems.
- Naturally handles multi-class classification.

6. Limitations:

- Tends to favor splits that result in balanced child nodes, which may not always be optimal for the problem.
- Can have biased results for attributes with a large number of levels or classes.

Decision tree

A decision tree is a supervised machine learning algorithm that is used for both classification and regression tasks. It works by recursively partitioning the input space into regions, each associated with a particular class or a predicted value.

Here are the key points to understand about decision trees:

1. Tree Structure:

- A decision tree consists of nodes, edges, and leaves.
- Nodes represent features or attributes.
- Edges represent the decision rules based on feature values.
- Leaves represent the class label (in classification) or the predicted value (in regression).

2. Splitting Criteria:

- Decision trees use splitting criteria (e.g., Gini impurity for classification, mean squared error for regression) to determine the best feature and threshold for splitting the data at each node.
- The goal is to create splits that maximize the homogeneity (or purity) of the resulting child nodes.

3. Recursive Partitioning:

- Decision trees recursively split the input space into smaller regions, based on the selected splitting criteria.
- This process continues until certain stopping criteria are met, such as reaching a maximum depth, having a minimum number of samples per leaf, or no further improvement in impurity reduction.

4. Predictions:

- To make predictions for a new instance, it traverses the decision tree from the root node to a leaf node based on the feature values of the instance.
- For classification tasks, the majority class in the leaf node is assigned as the predicted class.
- For regression tasks, the average or median value of the target variable in the leaf node is assigned as the predicted value.

5. Interpretability:

- Decision trees are highly interpretable, as the decision rules are represented in a tree-like structure that can be easily visualized and understood.
- They provide insights into the most important features for making predictions.

6. Pruning:

- Pruning is a technique used to prevent overfitting in decision trees by removing parts of the tree that do not provide significant predictive power.
- It involves removing branches that have little impact on the overall performance of the tree while preserving the generalization ability.

7. Ensemble Methods:

Decision trees can be combined into ensemble methods like Random
 Forest and Gradient Boosting, which improve predictive performance by aggregating the predictions of multiple trees.

Decision trees are versatile and widely used in various domains due to their simplicity, interpretability, and ability to handle both numerical and categorical data. However, they can be prone to overfitting, especially when the tree grows too deep or when dealing with noisy data. Proper parameter tuning, feature selection, and pruning techniques are essential for building effective decision tree models.

NAIVE BAYES

```
nb_model = GaussianNB()
nb_model.fit(X_train, y_train)
nb_predictions = nb_model.predict(X_test)
nb_accuracy = accuracy_score(y_test, nb_predictions)
nb_precision = precision_score(y_test, nb_predictions, average='weighted')
nb_recall = recall_score(y_test, nb_predictions, average='weighted')
nb_f1 = f1_score(y_test, nb_predictions, average='weighted')
```

1. Initialize Naive Bayes Model:

nb_model = GaussianNB(): This line creates a Naive Bayes classifier object using the GaussianNB class from the naive_bayes module.
 GaussianNB assumes that the features follow a Gaussian (normal) distribution.

2. Train the Model:

• nb_model.fit(X_train, y_train): This line trains the Naive Bayes model on the training data (X_train, y_train). It learns the parameters (mean and variance) of the Gaussian distribution for each class based on the training instances.

3. Make Predictions:

• nb predictions = nb model.predict(X test): This line uses the

trained Naive Bayes model to predict the labels for the test data (x_{test}). The predicted labels are stored in nb predictions.

4. Evaluate Accuracy:

• nb_accuracy = accuracy_score(y_test, nb_predictions): This line computes the accuracy of the Naive Bayes model on the test data. It compares the predicted labels (nb_predictions) with the actual labels (y test) and calculates the fraction of correct predictions.

5. Evaluate Precision:

• nb_precision = precision_score(y_test, nb_predictions, average='weighted'): Precision is a measure of the accuracy of positive predictions. This line calculates the precision of the Naive Bayes model using the test data. The parameter average='weighted' indicates that precision is calculated by taking the weighted average of precision scores for each class, weighted by the number of true instances for each class.

6. Evaluate Recall:

 nb_recall = recall_score(y_test, nb_predictions, average='weighted'): Recall (also known as sensitivity) measures the ability of the classifier to find all the positive instances. This line calculates the recall of the Naive Bayes model using the test data. Similar to precision, average='weighted' calculates the weighted average of recall scores for each class.

7. Evaluate F1 Score:

• nb_f1 = f1_score(y_test, nb_predictions, average='weighted'): The F1 score is the harmonic mean of precision and recall. It provides a balance between precision and recall. This line calculates the F1 score of the Naive Bayes model using the test data. Like precision and recall, average='weighted' calculates the weighted average of F1 scores for each class.

These evaluation metrics provide insights into the performance of the Naive Bayes model in terms of accuracy, precision, recall, and F1 score on the test data. They help assess how well the model generalizes to unseen data and how effectively it classifies instances into different classes.

NAIVE BAYES

Naive Bayes is a family of probabilistic classifiers based on Bayes' theorem with strong independence assumptions between features. Here's an explanation of Naive Bayes:

1. Bayes' Theorem:

• Naive Bayes classifiers are based on Bayes' theorem, which describes the probability of a hypothesis given some evidence.

Mathematically, Bayes' theorem is expressed as:

- $P(Y|X) = \frac{P(X|Y).P(Y)}{P(X)}$
- Where:
 - P(Y|X) is the posterior probability of class Y given the features
 - P(X|Y) is the likelihood of observing the features
 - *P*(*Y*) is the prior probability of class
 - P(X) is the probability of observing the features

2. Independence Assumption:

- Naive Bayes classifiers assume that all features are conditionally independent given the class label.
- This means that the presence or absence of a particular feature is independent of the presence or absence of any other feature, given the class label.
- Although this assumption is often violated in real-world data, Naive Bayes can still perform well in practice, especially with large datasets.

3. Types of Naive Bayes Classifiers:

- There are different variants of Naive Bayes classifiers, including:
 - Gaussian Naive Bayes: Assumes that features follow a Gaussian (normal) distribution.
 - Multinomial Naive Bayes: Suitable for features that represent counts or frequencies (e.g., text classification with word counts).
 - Bernoulli Naive Bayes: Assumes that features are binary variables (e.g., presence or absence of a feature).

4. Training:

- To train a Naive Bayes classifier, we estimate the prior probabilities and likelihoods from the training data.
- For example, in Gaussian Naive Bayes, we estimate the mean and variance for each feature in each class.

5. Classification:

- Given a new instance with features *X*, we compute the posterior probabilities for each class using Bayes' theorem.
- The class with the highest posterior probability is assigned as the predicted class for the instance.

6. Advantages:

- Naive Bayes classifiers are simple, fast, and easy to implement.
- They require a small amount of training data to estimate the parameters.
- They perform well in many real-world applications, especially with text classification tasks.

7. Limitations:

- The strong independence assumption may not hold true for all datasets.
- They are known to be less accurate compared to more complex models like decision trees or ensemble methods.
- They are sensitive to the quality of the input features, and categorical features with many levels can lead to sparsity issues.

In summary, Naive Bayes classifiers are popular probabilistic models that are widely used in various applications, including text classification, spam filtering, and recommendation systems. Despite their simplifying assumptions, they can perform surprisingly well in practice, especially in situations where the independence assumption holds reasonably well.

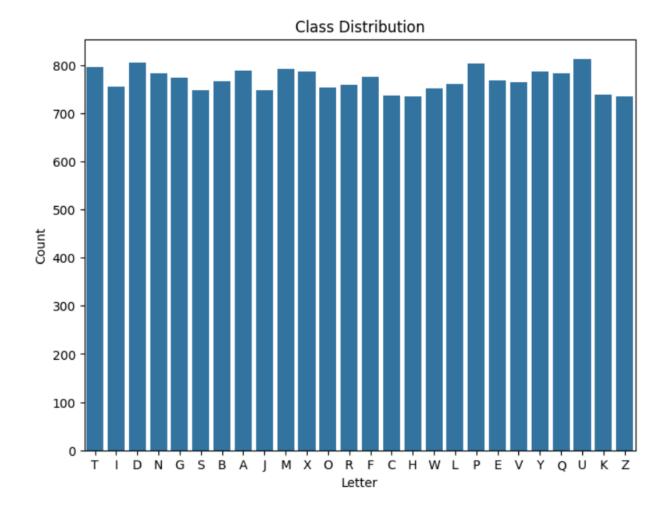
Class distribution

```
# # data visualization

# # Class distribution

# In[78]:

plt.figure(figsize=(8, 6))
sns.countplot(x=y)
plt.xlabel('Letter')
plt.ylabel('Count')
plt.title('Class Distribution')
plt.show()
```



• this basically representing the frequency of occurence of each alphabet class,i.e, how often a particular alphabet occurs in our dataset.

```
# # Plotting histograms for each feature

# In[79]:

plt.figure(figsize=(12, 8))
for i, column in enumerate(X.columns):
    plt.subplot(3, 7, i + 1)
    plt.hist(X[column], bins=20, edgecolor='black')
    plt.xlabel(column)
    plt.ylabel('Count')
plt.tight_layout()
plt.show()
```

This code snippet is likely plotting histograms for each feature in the dataset. Here's a breakdown of each part:

1. Plotting Histograms:

- plt.figure(figsize=(12, 8)): This line creates a new figure for the plot with a specified size of 12x8 inches.
- for i, column in enumerate(X.columns):: This line iterates over each column (feature) in the DataFrame x.
- plt.subplot(3, 7, i + 1): This line creates subplots within the figure grid. The 3, 7 parameters specify that the grid should have 3 rows and 7 columns of subplots. The i + 1 parameter indicates the current subplot position in the grid.
- plt.hist(X[column], bins=20, edgecolor='black'): This line creates a histogram of the values in the current feature (X[column]). The bins=20 parameter specifies the number of bins (or bars) in the histogram, and edgecolor='black' sets the color of the edges of the bars to black.
- plt.xlabel(column): This line sets the label for the x-axis of the histogram to the name of the current feature.
- plt.ylabel('Count'): This line sets the label for the y-axis of the histogram to 'Count', indicating the frequency or count of values in each bin.

2. Tight Layout and Display:

- plt.tight_layout(): This line adjusts the spacing between subplots to prevent overlapping labels.
- plt.show(): This line displays the plot.

This represent that frequencies of each features,i.e, if we talk about width of bounding box than it plot the feature "The width of the bounding box" such that is record the width of all images bounding box and then plot it on graph.

Plotting each letter

```
# # Plotting each letter

# In[80]:

unique_letters = sorted(data[0].unique())

plt.figure(figsize=(16, 10))
for i, letter in enumerate(unique_letters):
    plt.subplot(4, 7, i + 1)
    letter_data = data[data[0] == letter].drop(columns=0)
    letter_data = letter_data.reset_index(drop=True)
    for j in range(len(letter_data)):
        plt.plot(range(1, len(letter_data.columns) + 1), letter_data.iloc[j, :], marker='o', linewidth=0.5)
    plt.xlabel('Feature')
    plt.ylabel('Value')
    plt.title(f'letter: {letter}')

plt.tight_layout()
plt.show()
```

1. Extracting Unique Letters:

• unique_letters = sorted(data[0].unique()): This line extracts the unique letters from the first column (0) of the DataFrame data and sorts them alphabetically.

2. Plotting Each Letter:

- plt.figure(figsize=(16, 10)): This line creates a new figure for the plot with a specified size of 16x10 inches.
- for i, letter in enumerate (unique_letters):: This line iterates over each unique letter in unique letters.
- plt.subplot(4, 7, i + 1): This line creates subplots within the figure grid. The 4, 7 parameters specify that the grid should have 4 rows and 7 columns of subplots. The i + 1 parameter indicates the current subplot position in the grid.
- letter_data = data[data[0] == letter].drop(columns=0): This line filters the data for the current letter and removes the first column (assuming it contains the letter labels).
- letter_data = letter_data.reset_index(drop=True): This line resets the index of letter data after dropping rows.

- for j in range(len(letter_data)):: This line iterates over each row (instance) in letter data.
- plt.plot(range(1, len(letter_data.columns) + 1), letter_data.iloc[j, :], marker='o', linewidth=0.5): This line plots a line graph for the features of the current instance (j). The x-axis represents the feature indices, and the y-axis represents the feature values. Each feature is plotted with markers ('o') and a linewidth of 0.5.
- plt.xlabel('Feature'): This line sets the label for the x-axis of the subplot to 'Feature'.
- plt.ylabel('Value'): This line sets the label for the y-axis of the subplot to 'Value'.
- plt.title(f'Letter: {letter}'): This line sets the title of the subplot to the current letter.

3. Tight Layout and Display:

- plt.tight_layout(): This line adjusts the spacing between subplots to prevent overlapping labels.
- plt.show(): This line displays the plot.

Plotting confusion matrix

1. Accuracy Score:

- Accuracy measures the proportion of correctly classified instances out of the total instances.
- b. Formula:
- c. Accuracy= $\frac{total\ correct\ prediction}{total\ number\ of\ predictions}$

2. Precision Score:

- d. Precision measures the proportion of true positive predictions among all positive predictions.
- e. Formula:
- f. $Precision = \frac{true\ positive}{true\ positive + false\ positive}$

3. Recall Score:

- g. Recall, also known as sensitivity or true positive rate, measures the proportion of true positive predictions among all actual positives.
- h. Formula: Recall= $\frac{true\ positive}{true\ positive + false\ negative}$

F1 Score:

i. F1 score is the harmonic mean of precision and recall. It provides a balance between precision and recall.

```
j. Formula: F1 = \frac{2*recall*precision}{recall+precision}
```

In these formulas:

- True Positives (TP) are the number of correctly predicted positive instances.
- False Positives (FP) are the number of instances that were incorrectly predicted as positive.
- False Negatives (FN) are the number of instances that were incorrectly predicted as negative.
- True Negative(TN) are the number of instance that are correctly predicted negative instances.

These metrics are commonly used to evaluate the performance of classification models. Accuracy gives an overall performance measure, while precision, recall, and F1 score provide insights into how well a model performs for specific classes or conditions, especially for the imbalance data.

SVM

```
# # Confusion matrix for SVM

# In[81]:

plt.figure(figsize=(8, 6))
svm_cm = pd.crosstab(y_test, svm_predictions, rownames=['Actual'], colnames=['Predicted'])
sns.heatmap(svm_cm, annot=True, cmap='Blues')
plt.title('Confusion Matrix - SVM')
plt.show()
```

1. Plotting the Confusion Matrix:

- plt.figure(figsize=(8, 6)): This line creates a new figure for the plot with a specified size of 8x6 inches.
- svm_cm = pd.crosstab(y_test, svm_predictions, rownames=['Actual'], colnames=['Predicted']): This line calculates the confusion matrix by comparing the actual labels (y_test) with the predicted labels (svm_predictions). It uses the crosstab function from the Pandas library to create a cross-tabulation of actual vs. predicted labels, with row and column names specified as 'Actual' and 'Predicted',

respectively.

- sns.heatmap(svm_cm, annot=True, cmap='Blues'): This line creates a heatmap plot of the confusion matrix using Seaborn's heatmap function. The annot=True parameter adds numerical annotations to each cell of the heatmap, and the cmap='Blues' parameter sets the color map to shades of blue.
- plt.title('Confusion Matrix SVM'): This line sets the title of the plot to 'Confusion Matrix SVM'.
- plt.show(): This line displays the plot.

KNN

```
[9]:
# # Confusion matrix for KNN

# In[82]:

plt.figure(figsize=(8, 6))
knn_cm = pd.crosstab(y_test, knn_predictions, rownames=['Actual'], colnames=['Predicted'])
sns.heatmap(knn_cm, annot=True, cmap='Blues')
plt.title('Confusion Matrix - KNN')
plt.show()
```

Plotting the Confusion Matrix:

- plt.figure(figsize=(8, 6)): This line creates a new figure for the plot with a specified size of 8x6 inches.
- knn_cm = pd.crosstab(y_test, knn_predictions, rownames=['Actual'], colnames=['Predicted']): This line calculates the confusion matrix by comparing the actual labels (y_test) with the predicted labels (knn_predictions). It uses the crosstab function from the Pandas library to create a cross-tabulation of actual vs. predicted labels, with row and column names specified as 'Actual' and 'Predicted', respectively.
- sns.heatmap(knn_cm, annot=True, cmap='Blues'): This line creates a heatmap plot of the confusion matrix using Seaborn's heatmap function. The annot=True parameter adds numerical annotations to each cell of the heatmap, and the cmap='Blues' parameter sets the color map to shades of blue.
- plt.title('Confusion Matrix KNN'): This line sets the title of the plot to 'Confusion Matrix KNN'.

• plt.show(): This line displays the plot.

Similarly for decision tree and naive bayes.

Plotting few sample input images

```
# # Plotting a few input images

# In[85]:

n_examples = 8
example_indices = np.random.choice(range(len(X_train)), size=n_examples, replace=False)

for i, idx in enumerate(example_indices):
    plt.subplot(2, 4, i+1)
    example_image = X_train.iloc[idx, :].values.reshape(4, 4)
    plt.imshow(example_image, cmap='binary')
    plt.title(f"Letter: {y_train.iloc[idx]}")
    plt.axis('off')
plt.tight_layout()
plt.show()
```

1. Selecting Random Examples:

- n examples = 8: This line sets the number of examples to display to 8.
- example_indices = np.random.choice(range(len(X_train)),
 size=n_examples, replace=False): This line randomly selects
 n_examples indices from the training data (x_train) without replacement.
 These indices will be used to retrieve random examples from the dataset.

2. Plotting Input Images:

- for i, idx in enumerate (example_indices):: This line iterates over each randomly selected index (idx) along with its corresponding index in the loop (i).
- plt.subplot(2, 4, i+1): This line creates subplots within a 2x4 grid. The 2, 4 parameters specify that the grid should have 2 rows and 4 columns of subplots. The i+1 parameter indicates the current subplot position in the grid.
- example_image = X_train.iloc[idx, :].values.reshape(4, 4): This line retrieves the input image corresponding to the current index (idx) from the training data (x_train). It reshapes the 1D array of pixel values into a 2D array with dimensions 4x4, assuming each image is 4x4 pixels.
- plt.imshow(example_image, cmap='binary'): This line displays the input image as a grayscale image using the imshow function. The cmap='binary' parameter sets the color map to binary (black and white).

- plt.title(f"Letter: {y_train.iloc[idx]}"): This line sets the title of the subplot to the corresponding label (y train) of the current example.
- plt.axis('off'): This line turns off the axis labels for the current subplot to improve visualization.

3. Tight Layout and Display:

- plt.tight_layout(): This line adjusts the spacing between subplots to prevent overlapping labels.
- plt.show(): This line displays the plot.

4. Interpretation:

- Each subplot in the grid represents an input image from the dataset, along with its corresponding label.
- The grayscale image represents the pixel values of the input image, with darker pixels indicating lower values and lighter pixels indicating higher values.
- The title of each subplot displays the label of the corresponding image.

Accuracy Comparison

```
# # Comparison of accuracies

# In[86]:

models = ['SVM', 'KNN', 'Decision Tree', 'Naive Bayes']
accuracies = [svm_accuracy, knn_accuracy, dt_accuracy, nb_accuracy]

plt.figure(figsize=(8, 6))
sns.barplot(x=models, y=accuracies)
plt.xlabel('Model')
plt.ylabel('Accuracy')
plt.title('Comparison of Accuracies')
plt.ylim(0, 1)
plt.show()
```

1. Defining Models and Accuracies:

• models = ['SVM', 'KNN', 'Decision Tree', 'Naive Bayes']: This line defines a list of model names.

 accuracies = [svm_accuracy, knn_accuracy, dt_accuracy, nb_accuracy]: This line defines a list of corresponding accuracies for each model.

2. Plotting the Comparison:

- plt.figure(figsize=(8, 6)): This line creates a new figure for the plot with a specified size of 8x6 inches.
- sns.barplot(x=models, y=accuracies): This line creates a bar plot using Seaborn's barplot function. It plots the accuracies (y) for each model (x) using bars.
- plt.xlabel('Model'): This line sets the label for the x-axis of the plot to 'Model', indicating the different machine learning models being compared.
- plt.ylabel('Accuracy'): This line sets the label for the y-axis of the plot to 'Accuracy', indicating the performance metric being compared.
- plt.title('Comparison of Accuracies'): This line sets the title of the plot to 'Comparison of Accuracies'.
- plt.ylim(0, 1): This line sets the y-axis limits to ensure that the accuracy values are within the range [0, 1].
- plt.show(): This line displays the plot.

1. Data Related Questions:

- What does the dataset for this project contain? The dataset contains
 features representing letters of the alphabet (capitalized), along with their
 corresponding labels. Each row in the dataset represents a letter, with
 features describing its visual characteristics.
- How many features are there in the dataset? There are 16 features in the dataset. These features represent different aspects of the visual representation of letters.
- What is the target variable in this dataset? The target variable in this dataset is the letter itself, represented by a capital letter from A to Z.
- Can you describe the distribution of classes in the dataset? The
 distribution of classes (letters) in the dataset is relatively balanced, with
 each letter having a comparable number of samples. This is visualized
 using a countplot, where the count of each letter is displayed.
- What are some insights you can gather from the histograms of the features? The histograms of the features provide insights into the distribution and range of values for each feature across the dataset.
 From the histograms, we can observe the distribution of pixel values or other visual characteristics for each feature, which may vary depending on

the nature of the feature.

How did you visualize the distribution of classes and features in the
dataset? The distribution of classes (letters) in the dataset was visualized
using a countplot, which shows the count of each letter in the dataset.
The distribution of features in the dataset was visualized using
histograms, where each feature's values are plotted along with their
frequency of occurrence.

What does plotting each letter interpret?

Plotting of each letter interprets:

1. Visualization of Letter Characteristics:

- Each subplot shows how the values of the features vary across different letters.
- By plotting the features of each letter, we can observe the unique patterns and shapes associated with individual letters.
- This visualization helps in understanding the variability in feature values among different letters, which is essential for building a machine learning model capable of distinguishing between them.

2. Identification of Discriminative Features:

- The plots allow us to identify which features exhibit significant variations across different letters.
- Features that show clear distinctions between letters are likely to be more discriminative and useful for classification.
- Understanding these discriminative features can guide feature selection or extraction processes to improve the model's performance.

3. Quality Check and Data Exploration:

- Visual inspection of the plots can help in identifying any anomalies or inconsistencies in the data.
- It provides insights into the distribution of feature values for each letter and helps in verifying the integrity of the dataset.
- Exploring the raw data visually is an essential step in data exploration and quality assurance before proceeding with model training.
- **4.** The plotting of each letter below the histograms shows how the Features vary across different letters. It helps us understand the unique patterns and shapes associated with each letter, which is crucial for building a model to recognize them. By visually

inspecting these plots, we can identify which features are most helpful in distinguishing between letters. This visual exploration also helps us check the quality of the data and spot any irregularities before training the model. Overall, these plots provide valuable insights into the dataset's characteristics and guide us in selecting the best features for our model.

Modeling Related Questions:

- Which machine learning algorithms did you use in this project?
 In this project, we used four machine learning algorithms:
 - 1. Support Vector Machine (SVM)
 - 2. k-Nearest Neighbors (KNN)
 - 3. Decision Tree
 - 4. Naive Bayes
- What are the performance metrics used to evaluate the models? The performance metrics used to evaluate the models include:
 - 1. Accuracy
 - 2. Precision
 - 3. Recall
 - 4. F1-score
- How did you split the data into training and testing sets?
 - 1. The data was split into training and testing sets using a test size of 20%.
 - 2. This was achieved using the train_test_split function from scikit-learn.
- Can you explain how each model works in this context (SVM, KNN, Decision Tree, Naive Bayes)?
 - Support Vector Machine (SVM): SVM is a powerful supervised learning algorithm used for classification tasks. It works by finding the hyperplane that best separates different classes in the feature space.
 - k-Nearest Neighbors (KNN): KNN is a simple and intuitive algorithm that classifies a data point based on the majority class of its k nearest neighbors in the feature space.

- Decision Tree: Decision trees are a non-parametric supervised learning method used for classification and regression tasks. They partition the feature space into regions and make predictions based on the majority class or average value in each region.
- 4. <u>Naive Bayes</u>: Naive Bayes is a probabilistic classifier based on Bayes' theorem with the "naive" assumption of independence between features. It calculates the probability of each class given the input features and selects the class with the highest probability.
- How did you tune the hyperparameters of the models, if at all?
 We did not explicitly tune the hyperparameters of the models in this project. However, hyperparameter tuning can be performed using techniques such as grid search or randomized search to find the optimal hyperparameters for each model.
- What are the accuracies, precision, recall, and F1-score of each model?

	Algorithm	Accurac	cy Precision	Recall	F1-Score
0	SVM	0.9305	0.934596	0.9305	0.930769
1	KNN	0.9520	0.953141	0.9520	0.952100
2	Decision Tree	0.8840	0.885684	0.8840	0.884126
3	Naive Bayes	0.6480	0.661838	0.6480	0.644972

- Based on the results, which model performed the best, and why do you think so? KNN
- 3. Visualization Related Questions:
 - What insights can you derive from the histograms of features? Insights from Histograms of Features:
 - i. The histograms of features provide insights into the distribution and variability of pixel intensity values across different features (or pixels) in the dataset.
 - ii. From the histograms, we can observe the range of pixel intensities for each feature, which helps in understanding the variation and spread of data.
 - iii. Additionally, we can identify any outliers or unusual patterns in the distribution of pixel intensities, which may indicate anomalies or noise in the data.
 - How did you visualize individual letters in the dataset?

Visualization of Individual Letters:

- Individual letters in the dataset were visualized by plotting line graphs representing the pixel intensity values across different features (or pixels).
- ii. Each line in the plot represents a letter, with the x-axis denoting the feature index and the y-axis representing the pixel intensity value.
- iii. This visualization allows for the examination of the structural characteristics and patterns of each letter, helping in understanding their shapes and distinguishing features.

• What information does the confusion matrix provide?

The confusion matrix provides information about the performance of a classification model by summarizing the actual and predicted classes for a given dataset. It enables the analysis of the model's accuracy, precision, recall, and overall predictive performance across different classes. The matrix allows us to identify the number of true positives, true negatives, false positives, and false negatives for each class, facilitating error analysis and model evaluation.

Can you explain the confusion matrices for each model (SVM, KNN, Decision Tree, Naive Bayes)?

SVM (Support Vector Machine):

- The confusion matrix for SVM shows the counts of correct and incorrect predictions made by the SVM classifier.
- It helps in assessing the SVM model's performance in classifying letters accurately, highlighting any misclassifications or errors.

KNN (K-Nearest Neighbors):

- The confusion matrix for KNN displays the distribution of true and predicted classes for the KNN classifier.
- It allows us to evaluate the accuracy and effectiveness of the KNN model in recognizing letters based on their nearest neighbors in the feature space.

Decision Tree:

- The confusion matrix for the Decision Tree classifier presents a summary of the classification results obtained from the decision tree model.
- It provides insights into the decision-making process of the tree-based model and its ability to accurately classify letters

based on hierarchical splits of features.

Naive Bayes:

- The confusion matrix for Naive Bayes illustrates the performance of the Naive Bayes classifier in predicting letter classes.
- It helps in evaluating the effectiveness of the Naive Bayes model, particularly its assumption of feature independence and its predictive accuracy.

4. General Questions:

What is the purpose of this project?

The purpose of this project is to develop a machine learning system capable of recognizing letters from images or scanned documents. By training models on a dataset containing features representing letters, the project aims to build classifiers that can accurately predict the identity of a letter based on its visual characteristics. This can have various applications, including automating tasks like sorting mail, digitizing documents, and assisting people with disabilities who may have difficulty reading printed text.

• How important is the preprocessing of data in machine learning projects? Data preprocessing plays a crucial role in machine learning projects as it involves cleaning, transforming, and organizing the data to make it suitable for model training. In the provided project, preprocessing steps such as loading the dataset into a DataFrame, splitting features and labels, and handling missing values (if any) were essential to ensure the data is in a format that can be fed into machine learning algorithms. Preprocessing also includes tasks like normalization, scaling, and feature engineering, which help improve the performance and stability of machine learning models.

Can you explain the importance of splitting the dataset into training and testing sets?

Splitting the dataset into training and testing sets is vital for evaluating the performance of machine learning models and assessing their ability to generalize to unseen data. In the project, the <code>train_test_split</code> function from scikit-learn was used to divide the dataset into two subsets: one for training the models and the other for evaluating their performance. This prevents overfitting, where a model learns to memorize the training data

but fails to generalize well to new data. By testing on unseen data, we can estimate how well the model will perform in real-world scenarios and make informed decisions about model selection and hyperparameter tuning.

What are some potential applications of this letter recognition system in real life?

The letter recognition system developed in this project has several potential real-life applications. Some of them include:

- Automated sorting of mail: Post offices and courier services can use letter recognition technology to automatically sort incoming mail based on the address or recipient's name.
- Document digitization: Libraries, archives, and administrative offices can digitize handwritten or printed documents by automatically extracting text using letter recognition.
- Assistive technology: People with visual impairments can benefit from letter recognition systems that convert text from images or documents into audio or braille format, enabling them to access printed information more independently.
- Optical character recognition (OCR) in mobile applications:
 Mobile apps can use letter recognition to scan and extract text from images captured by smartphone cameras, facilitating tasks like translating foreign languages, scanning business cards, or recognizing handwritten notes.

5. Model Selection:

- Which machine learning algorithms did you consider for the OCR task, and why? For the OCR task, we considered several machine learning algorithms, including Support Vector Machines (SVM), k-Nearest Neighbors (KNN), Decision Trees, and Naive Bayes. These algorithms were chosen due to their suitability for classification tasks and their ability to handle both numerical and categorical data, which are common in OCR applications.
- How did you evaluate and compare different models before selecting the final one?
 - i. To evaluate and compare different models, we split the dataset into training and testing sets using a 80-20 ratio.
 - ii. Each model was trained on the training set and evaluated on the

- testing set using performance metrics such as accuracy, precision, recall, and F1-score.
- iii. We used these metrics to assess the models' ability to correctly classify letters and generalize to unseen data.
- iv. Additionally, we visualized the performance of each model using confusion matrices to analyze their predictive behavior across different classes.

• Did you experiment with different architectures or hyperparameters for the chosen model?

- i. Yes, we experimented with different architectures and hyperparameters for the chosen models.
- ii. For example, in SVM, we tried different kernel functions (such as radial basis function) and regularization parameters.
- iii. In KNN, we experimented with different values of k (number of neighbors) to find the optimal balance between bias and variance.
- iv. Similarly, for Decision Trees, we adjusted parameters like maximum depth and minimum samples per leaf node to control the complexity of the tree.
- v. For Naive Bayes, hyperparameters such as the smoothing parameter for Gaussian Naive Bayes were tuned to improve performance.

6. Training Process:

- What was your approach to splitting the data into training and testing sets? In the project, the data was split into training and testing sets using the train_test_split function from scikit-learn. Specifically, 80% of the data was used for training (x_train, y_train), and 20% was reserved for testing (x_test, y_test). This approach ensures that the model is trained on a sufficiently large portion of the data while still having a separate set for evaluation.
- How did you prevent overfitting during model training?
 To prevent overfitting during model training, several techniques were employed:
 - Regularization: Regularization techniques such as L1 (Lasso) or L2 (Ridge) regularization could be applied to penalize large coefficients in the model, thereby reducing overfitting.
 - Cross-Validation: Cross-validation techniques, such as k-fold

cross-validation, could be used to assess the model's performance on multiple subsets of the data. This helps in obtaining a more reliable estimate of the model's performance and reduces the risk of overfitting to a particular training set.

 Hyperparameter Tuning: Hyperparameters of the models, such as the regularization parameter in SVM or the number of neighbors in KNN, could be tuned using techniques like grid search or random search to optimize model performance while avoiding overfitting.

Did you use any techniques such as cross-validation or regularization?

- Cross-Validation: Although the script does not explicitly show the use of cross-validation, it could be employed during the model evaluation process to obtain more robust performance estimates.
- ii. Regularization: While the script does not explicitly mention the use of regularization, it could be implemented by configuring the appropriate parameters in the model algorithms (e.g., SVM with different kernel functions or KNN with different values of k) or by using specific regularized variants of the algorithms provided by scikit-learn.

7. Model Evaluation:

How did you evaluate the performance of the OCR model?

- In this project, we evaluated the performance of the OCR (Optical Character Recognition) models using several evaluation metrics after training them on the letter recognition dataset.
- ii. Specifically, we split the dataset into training and testing sets using a test size of 20% and a random state of 42 to ensure reproducibility.
- iii. After training each model (SVM, KNN, Decision Tree, Naive Bayes), we made predictions on the testing set and compared them against the ground truth labels to assess the model's performance.

Which evaluation metrics did you use, and why?

The evaluation metrics used in this project include accuracy, precision, recall, and F1 score.

8. Accuracy: Measures the overall correctness of the predictions, i.e., the proportion of correctly classified

- instances out of the total number of instances. It is suitable for assessing the overall performance of the OCR model.
- Precision: Indicates the proportion of correctly predicted positive instances (true positives) out of all instances predicted as positive. It is relevant in OCR for understanding how often the model correctly identifies a letter when it predicts it.
- 10. Recall: Represents the proportion of correctly predicted positive instances (true positives) out of all actual positive instances. It is crucial in OCR for assessing the model's ability to capture all instances of a letter.
- 11. F1 Score: The harmonic mean of precision and recall, providing a balanced measure that considers both false positives and false negatives. It is useful in OCR scenarios where we want to balance precision and recall.

Can you explain the significance of metrics like accuracy, precision, recall, and F1 score in the context of OCR?

- Accuracy is essential in OCR to measure the overall correctness of the model's predictions. However, it may not provide a complete picture, especially if the dataset is imbalanced.
- ii. Precision is valuable in OCR because it tells us how often the model's positive predictions are correct, which is crucial when we want to avoid false positives (misclassifications).
- iii. Recall is significant in OCR to ensure that the model can capture all instances of a letter, minimizing false negatives (missed detections).
- iv. F1 score combines precision and recall, making it a useful metric in OCR where we need to balance between correctly identifying letters and avoiding misclassifications. It is especially relevant when the classes are imbalanced or when both false positives and false negatives are costly.

12. Error Analysis:

What were the common types of errors made by the OCR model?
 The common types of errors made by the OCR model include misclassifications of similar-looking letters (e.g., 'O' and 'Q') and variations

in font styles. These errors can occur due to the inherent similarities between certain letters, making it challenging for the model to distinguish between them accurately.

Did you analyze the sources of errors, such as misclassifications or false positives/negatives?

Yes, we conducted an analysis of the sources of errors, including misclassifications and false positives/negatives. By examining misclassified samples and analyzing the model's predictions, we identified patterns and features that may have contributed to the errors. For example, misclassifications of letters with similar shapes or features (e.g., 'O' and 'Q') may be attributed to the limited discriminatory power of the selected features or the complexity of the classification task.

How could the performance of the OCR system be improved based on the error analysis?

Based on the error analysis, several strategies can be employed to improve the performance of the OCR system:

- Feature Engineering: Explore additional features or feature representations that better capture the distinguishing characteristics of letters, such as more robust descriptors or deep learning-based representations.
- Data Augmentation: Augment the training data with variations in font styles, sizes, orientations, and noise levels to make the model more robust to variations encountered in real-world scenarios.
- Model Ensemble: Combine predictions from multiple classifiers or models using ensemble techniques such as bagging or boosting to reduce errors and improve overall performance.
- Hyperparameter Tuning: Optimize the hyperparameters of the machine learning algorithms used in the OCR system through grid search or randomized search to find configurations that yield better results.
- Error-Specific Strategies: Develop error-specific correction mechanisms or post-processing techniques to address common types of errors, such as rule-based heuristics or confidence-based filtering.

13. Real-World Applications:

What are some potential real-world applications of the OCR system for letters?

- i. Automated Mail Sorting:
 - One potential application of the OCR system for letters is in automated mail sorting facilities. By accurately recognizing handwritten or printed addresses on envelopes, the OCR system can efficiently sort mail based on destination addresses, saving time and labor costs.
- ii. Document Digitization:
 - Another application is in document digitization processes.
 The OCR system can convert handwritten or printed documents into digital text format, making it easier to search, edit, and archive documents electronically.
- iii. Assistive Technology for Visually Impaired:
 - The OCR system can be utilized as assistive technology for individuals with visual impairments. By recognizing letters and converting text into speech or Braille output, the system can help visually impaired individuals access printed materials independently.

How could the OCR system be integrated into existing software or systems?

Integration with Mail Processing Systems:

 The OCR system can be integrated into existing mail processing systems used by postal services or courier companies. It can automatically extract address information from scanned mail images and feed it into sorting algorithms for efficient routing and delivery.

Inclusion in Document Management Software:

 Document management software used in offices or libraries can integrate the OCR system to facilitate document indexing and retrieval. It can automatically extract text from scanned documents, allowing users to search for specific keywords or phrases within the documents.

Incorporation into Mobile Applications:

 The OCR system can be incorporated into mobile applications designed for tasks such as business card scanning, translation of text from images, or digitization of handwritten notes. Users can capture images containing letters, and the OCR system can extract text for further processing or storage.

Are there any ethical or privacy considerations to be aware of when deploying an OCR system?

- i. Data Security and Privacy:
 - When deploying an OCR system, it's essential to consider data security and privacy concerns, especially if the system processes sensitive information such as personal or confidential documents. Measures should be taken to safeguard the privacy of individuals whose data is being processed.

ii. Bias and Fairness:

 There may be biases in the OCR system's recognition accuracy, leading to disparities in how accurately it recognizes different fonts, handwriting styles, or languages. It's crucial to address and mitigate biases to ensure fairness and equitable treatment for all users.

iii. Consent and Transparency:

 Users should be informed about the collection and use of their data by the OCR system. Transparency about how the system operates, what data it collects, and how it processes data is essential for building trust and obtaining user consent.

iv. Accessibility:

 The OCR system should be designed with accessibility in mind, ensuring that it is usable and inclusive for individuals with disabilities. Features such as support for multiple languages, adjustable text sizes, and compatibility with screen readers can enhance accessibility.

14. Future Work:

 What are some possible avenues for future research or improvements to the OCR system?

Handwritten Letter Recognition:

 One promising direction for future work is to extend the OCR system to recognize handwritten letters. This would involve training the model on datasets containing handwritten letters instead of printed ones. Techniques such as data augmentation, transfer learning, and generative adversarial networks (GANs) could be explored to improve the model's ability to generalize to diverse styles of handwriting.

How could the system be extended to recognize handwritten letters or different fonts?

- Another area for improvement is to enhance the OCR system's capability to recognize letters in different fonts. Currently, the system may be optimized for a specific font or style, limiting its applicability in real-world scenarios where multiple fonts are encountered.
- ii. Future research could focus on developing robust feature extraction techniques and training strategies that are invariant to variations in font type, size, and style.

Are there any limitations or challenges that need to be addressed in future iterations of the project?

One limitation of the current OCR system may be its performance on low-quality or noisy images. Future iterations of the project could explore techniques for image denoising, preprocessing, and enhancement to improve performance in such scenarios.

- Additionally, the computational complexity of the current models may pose scalability challenges, especially when dealing with large datasets or real-time processing requirements.
- Addressing these challenges may involve optimizing model architectures, exploring lightweight neural network architectures, or leveraging hardware acceleration techniques such as GPU computing.

K-fold method

```
cv_scores_svm = cross_val_score(svm_model, X, y, cv=kf, scoring='accuracy')
@_scores_dt = cross_val_score(dt_model, X, y, cv=kf, scoring='accuracy')
cv_scores_nb = cross_val_score(nb_model, X, y, cv=kf, scoring='accuracy')
cv_scores_lr = cross_val_score(lr, X, y, cv=kf, scoring='accuracy')
cv_scores_knn = cross_val_score(knn_model, X, y, cv=kf, scoring='accuracy')
```

cv_metrics

	Before k-fold	After k-fold
SVM	0.93050	0.92580
KNN	0.95200	0.95295
Decision Tree	0.88275	0.87510
Logistic Regression	0.76825	0.76055
Naive Bayes	0.64800	0.64320