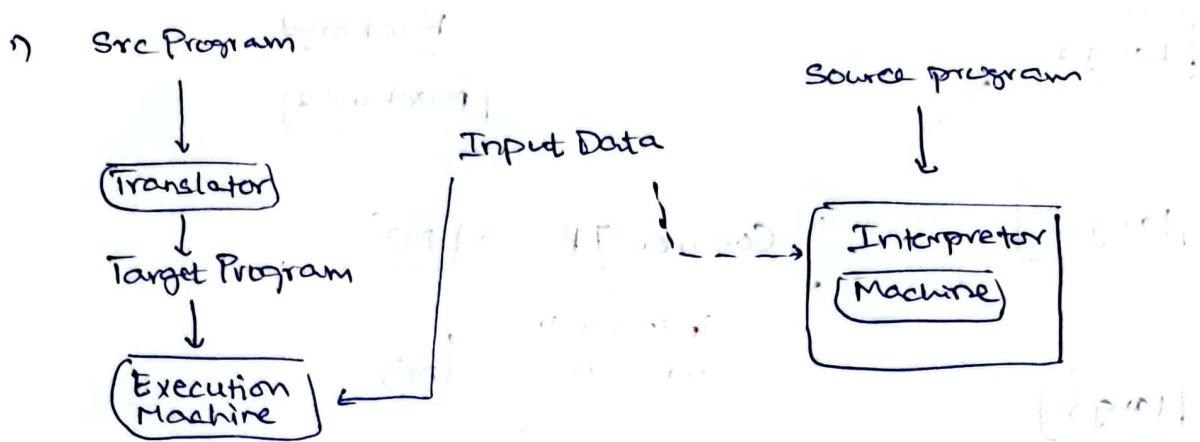
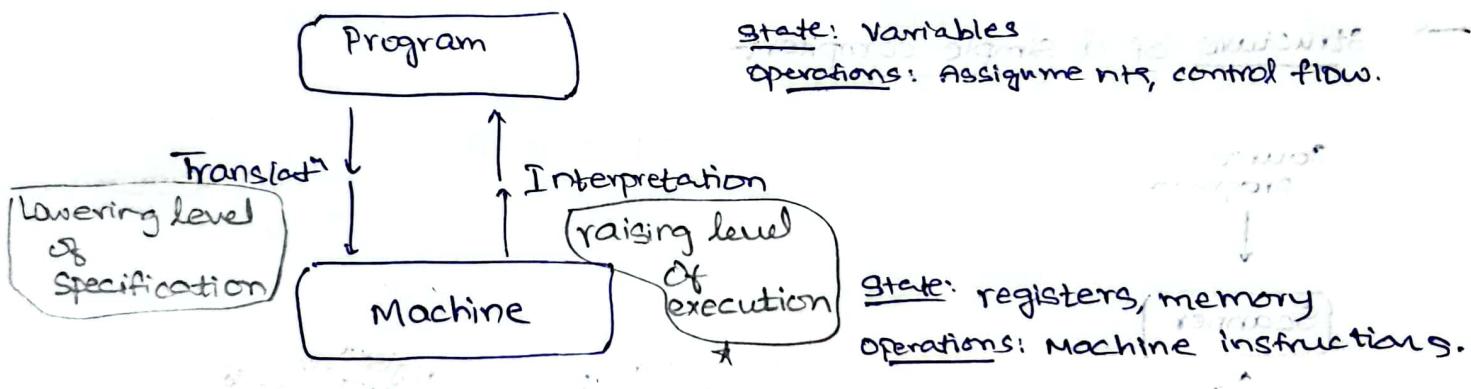


Overview to compilers:-

* compilation vs interpretation:



2) A gap exists b/w the program specification and execution.



* Why both compilers AND interpreters?

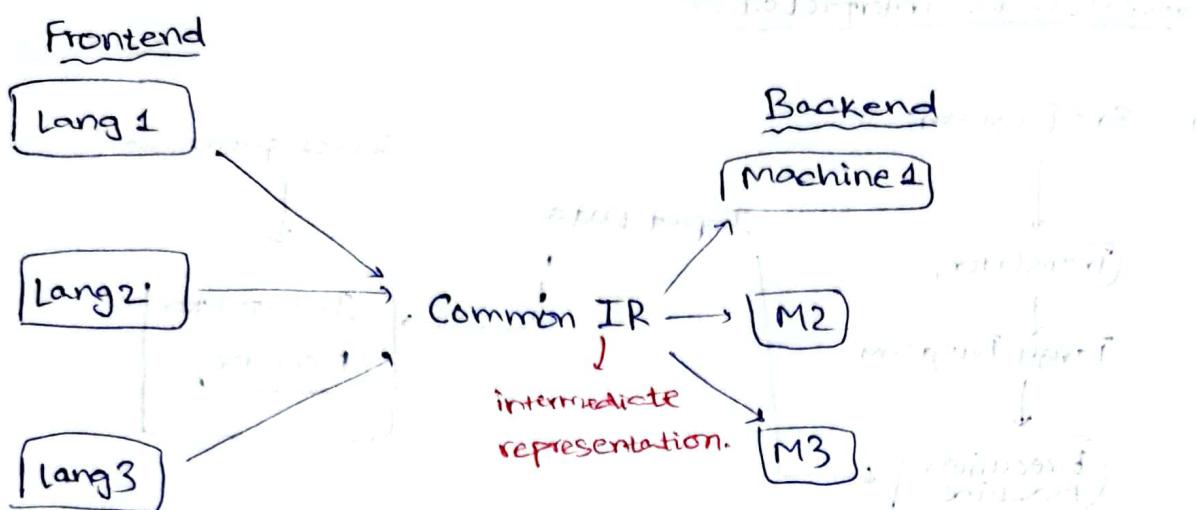
$$t_{\text{compiler}} = t_{\text{Analyze}} + t_{\text{optimize}} + t_{\text{overhead}} + t_{\text{Synthesis}} + t_{\text{execute}} \times j$$

$$t_{\text{interpreter}} = (t_{\text{analyze}} + t_{\text{overhead}} + t_{\text{exec}}) \times j$$

interpreter overhead.

Eg: for a browser, 'j' is large; so use compilers over interpreters.

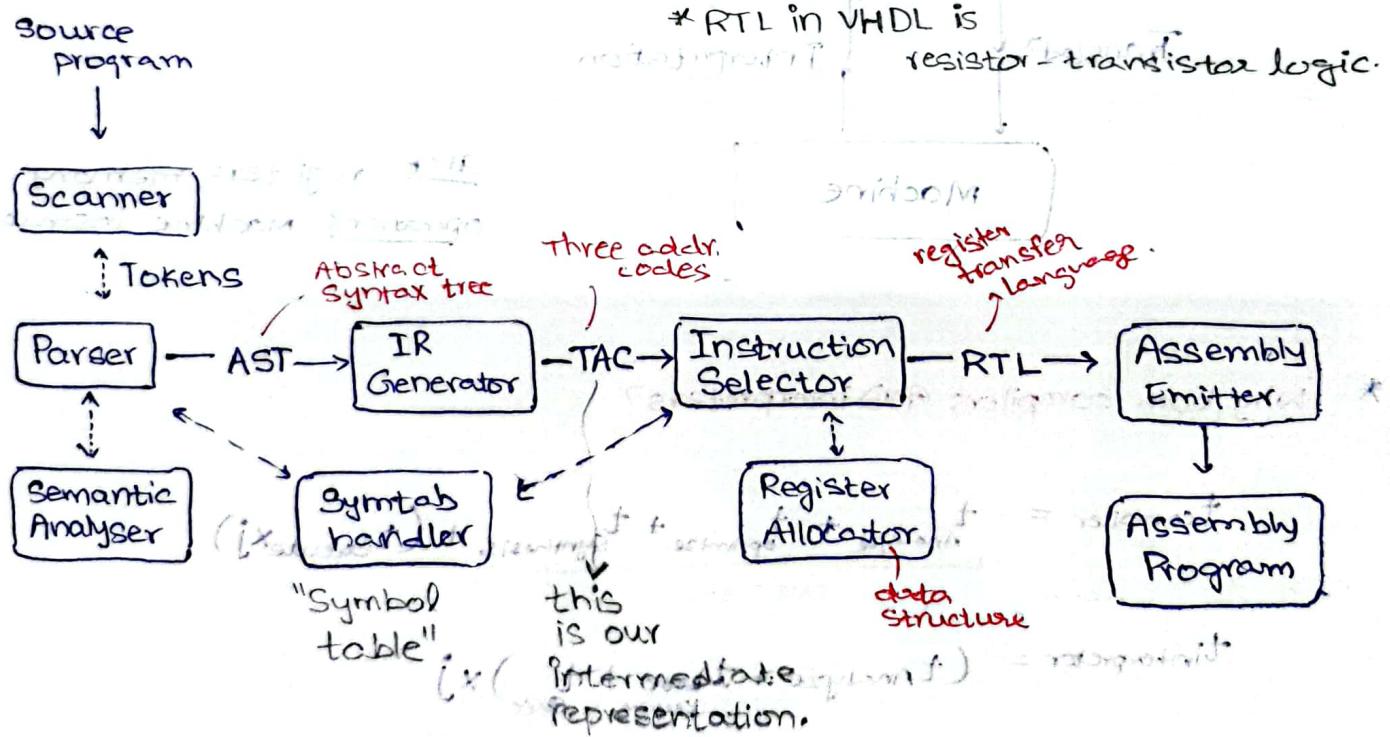
→ Reusability of lang processor modules.



$m \times n$ compilers from $m+n$ modules.

"Retargetable"

→ Structure of a simple compiler:



<slide 55/210 - 101>

Demo of all intermediate states.

Parse tree → AST → TAC → RTL → SPIM instructions.

S.no	State	Matching String.	Buffer	Next char	Last Final State.	marked Position	Action.
------	-------	------------------	--------	-----------	-------------------	-----------------	---------

Symbol: Notation :-

Single terminal a,b,c

Single non-terminal ABC

String grammar
Symbol
Atom (NUT)

String of terminals xyz

String of grammar symbols α,β,γ

null ε

shift < SLR(1) < LALR(1) < CLR(1)

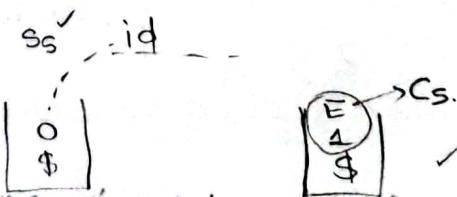
Shift reduce parsing

Step	Stack	rem. input	Action
1	\$	id*(id+id)\$	shift id.

parse tree, Derivation tree
points to right

State transition

	(*)	id	+	*	C)	\$	E	T	F	Q ₀ to
0		S ₅		S ₄				C ₁	C ₂	C ₃	
1			S ₆			acc		C ₅	C ₄		
2											
3											
4											



most leftmost derivation of the string is called as normal form

viable prefix:

prefix of a right sentential form that does not extend beyond handle.

valid item:

is a grammar production with (\cdot) .

$E \rightarrow \cdot A$ (Kernel)

$A \rightarrow \cdot B$

$B \rightarrow \cdot x$ (closure items)

} set of
Pitems
form a state
in DFA

LR(K)

↙ left to right input read
 right sentential in reverse
 K Lookahead in items

shift?
SLR(0) : LR(0) items & no lookahead in input

SLR(1) : LR(0) items & 1 lookahead in input.

CLR(1) : LR(1) items & 1 lookahead in input
 canonical

↑ terminals only
FIRST() & FOLLOW sets

* if β derives ϵ ; $\epsilon \in \text{First}(\beta)$

contains terminals, that may begin a string derivable from

$A \rightarrow x_1 x_2 \dots x_k$

least fixed point soln of

then $\text{first}(A) \supseteq x_i$

following constraints.

provided $x_j \neq i$, $\epsilon \in \text{First}(x_j)$

(\cdot)

follow: → what follows symbol A in a right sentential form.

$A \rightarrow \alpha B \beta$

1) if A is start symbol
 $\text{Follow}(A) \supseteq \{\$ \}$ end symbol

2) $\text{Follow}(B) \supseteq \text{First}(\beta) - \{ \epsilon \}$

3) if $\epsilon \in \text{First}(\beta)$ or $\beta \equiv \epsilon$

$\text{Follow}(B) \supseteq \text{Follow}(A)$

- * SLR(1) parsing needs ~~no~~ ~~reduces~~, follow sets for symbols; to determine when to reduce...

$$\begin{array}{l} E' \rightarrow E \\ E \rightarrow E+E \\ E \rightarrow E \cdot * E \\ E \rightarrow id \end{array}$$

$$\text{Follow}(E') \supseteq \{\$\}$$

$$\text{Follow}(E) \supseteq \text{Follow}(E')$$

$$\text{Follow}(E) \supseteq \{+, *\}$$

$$\text{Follow}(E) = \{+, *\}$$

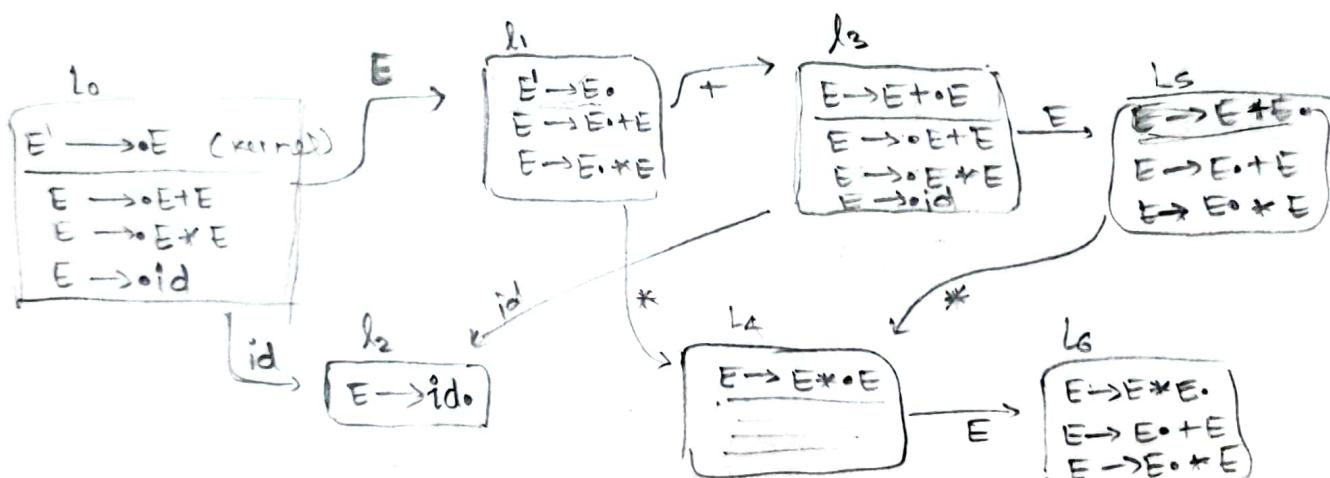
or
reject.

E' —

$$E \rightarrow S_1 X_2 \dots X_K$$

$$S_i \rightarrow S_i^1 S_i^2 \dots$$

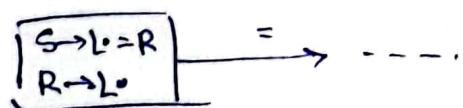
$$\begin{array}{l} E' \\ \vdash \\ id + id \end{array}$$



reduce;
when

- complete item
- no transition
- next input is in follow set of LHS.

	id	+	*	\$	E
1	S1	S2			C1
2			T3	T3	
3	S2				CS
4	S2				CG
5	S3/r1	S4/r1		r1	
6	S3/r2	S4/r2		r2	



$$\therefore \text{Follow}(R) \supseteq \{=\}$$

then, shift-reduce conflict!

LR(0):

items are

$$A \rightarrow \alpha \cdot \beta, a$$

lookahead

* if S is start symbol, then do has $S^* \rightarrow \cdot S, \$$

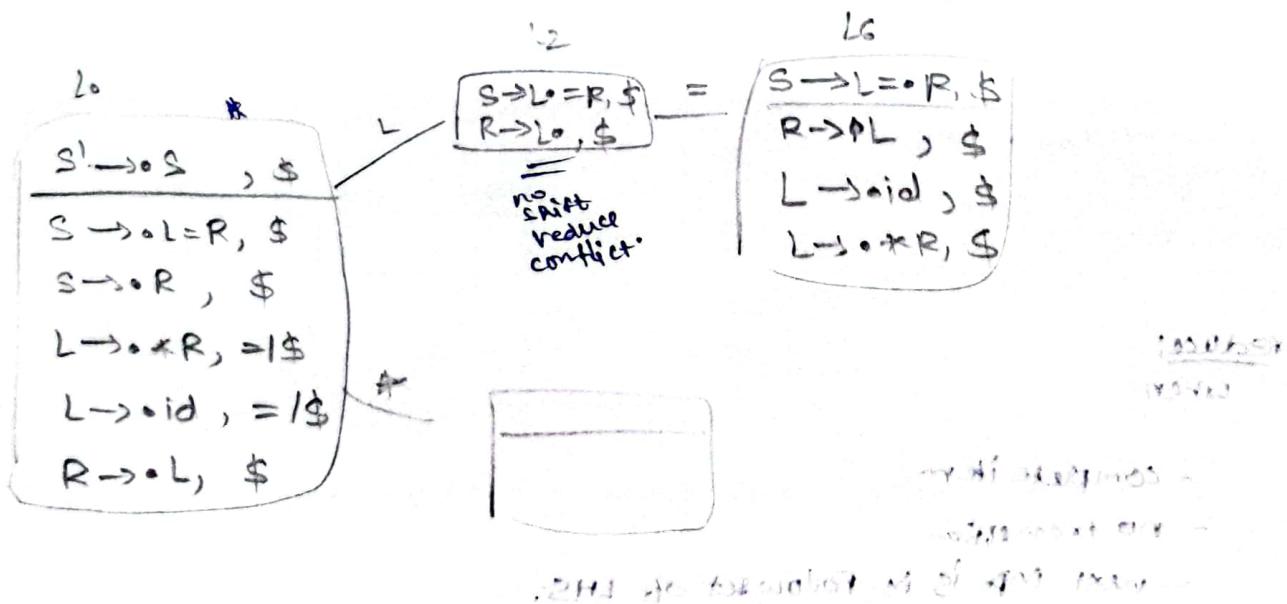
* lookahead don't change on shift.

lookahead only change on closure.

* closure of $A \rightarrow \alpha \cdot B \beta, a$ contains

$$B \rightarrow \cdot \gamma, \text{First}(B, a)$$

full follow	
$S \rightarrow L = R$	$S^* \quad \{=, \beta\}$
$S \rightarrow R$	$S \quad \{\$, \beta\}$
$L \rightarrow \cdot *R$	
$L \rightarrow \cdot id$	$R \quad \{\$, =\}$
$R \rightarrow L$	$L = \{\$, =\}$

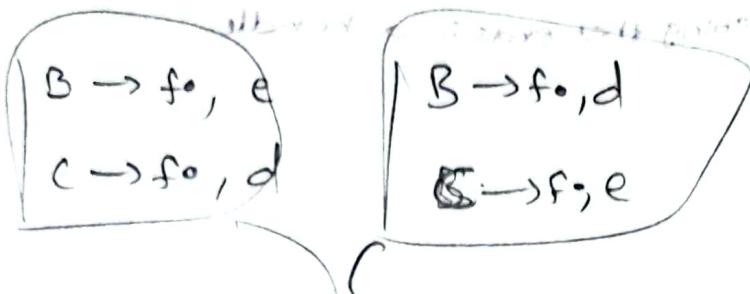


LR(0) is the subset of LR(1).

LR(0) is not necessarily prefix-free.

LALR(1) ~~conflict with reduce before reduce~~ before reduce + conflicts after
merge state

Shared with parser produces reduce-reduce parser.



reduce-reduce conflict

4 arrays representation

transition table:

State	0	1	2	3
0	0	1	2	3
1	1	1	0	3
2	1	1	3	3
3	0	1	2	

→ input symbol

Index	next	check
0	0	3
1	1	3
2	2	3
3	3	0
4	1	2
5	0	1
6	3	2
7	NONE	NONE

State	Default	Base
0	3	0
1	2	3
2	0	4
3	'NONE'	0

write none!!

this will hint at
empty transition...

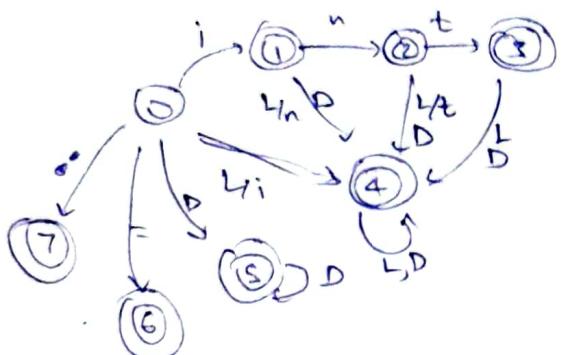
Step 3: identifying handles in right sentential forms:-

viable prefixes:-

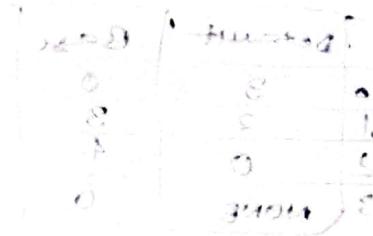
Prefix of a RSF, that does not extend beyond the handle

- it's either a string with no handle
- a string that ends in a handle.

scanning example:-



Sno	S	MS	Bufr	NC	LFS	MP	Act.
1	o	-	int32=S; i	-	-	-	
2	i	o	int32=S; en	1	1	-	
3	in	"	" + 2	2	-		
4	int	32=S; o	Li 3	3	found INT		
5	o	-	uint32=S; w	-	-	Decd	
6	o	-	int32=S; o	-	-		
7	i	o	int32=S; o	7	b, l		



standardized to 100% of the

maximum value in each

sample (Table 1).

The first step in the analysis was to determine which variables were significantly correlated with the total number of species per sample. This was done by calculating the correlation coefficient between the total number of species per sample and each of the environmental variables.

Variables that were significantly correlated with the total number of species per sample were then included in a multiple regression model.

2.2. Data analysis

Relationships between

species richness

and environmental variables

were tested using

multiple regression analysis

(Legendre & Legendre 1998)

using SPSS 11.5

(SPSS Inc., Chicago, IL,

USA) and R 2.1.1

(R Development Core Team

2005). Species richness

was used as the dependent variable

and environmental variables

as independent variables

in the regression

models. The

multiple regression

models were

standardized to 100%

of the maximum value

in each sample

(Table 1). The

multiple regression

models were

standardized to 100%

of the maximum value

in each sample

(Table 1). The

Semantic Analysis:-

compiletime errors

linktime errors

Runtime errors

- undefined behaviour : unchecked prohibited warnings these also error
- unspecified behaviour : implementation defined (well-defined by compiler)
- Exceptions: prohibited checked errors

→ SDDs :-

for generating IRs:-

$S \rightarrow id = E$

$C_1 = gen(id.place, =, E.place)$

$S.code = E.code || C_1$

$E \rightarrow E_2 op E_3$

$t_1 = getNewTemp();$

$C_1 = E_2.code; C_2 = E_3.code$

$C_3 = gen(t_1, =, expr(E_2.place, OP, E_3.place))$

$E.code = C_1 || C_2 || C_3$

$E.place = t_1$

$E_1 \rightarrow (E_2)$

$E_1.code = E_2.code$

$E_1.place = E_2.place$

$E \rightarrow id$

$E_1.code = NULL$

$E_1.place = id.name$

$E_1 \rightarrow E_2?E_3:E_4$

$t_1 = getNewTemp(); t_2 = getNewTemp()$

$L_1 = getNewLabel(); L_2 = _____();$

$C_1 = E_2.code || gen(t_1 = E_2.place) || gen(if t_1 goto L_1)$

$C_2 = E_3.code || gen(t_2 = E_3.place) || gen(goto L_2)$

$C_3 = gen(L_1: || E_4.code || gen(t_2 = E_4.place))$

$C_4 = gen(L_2:)$

$E_1.code = C_1 || C_2 || C_3 || C_4$

$E_1.place = t_1$

field access: Approach 1

F.name : name of struct var.

NO F-code

at compile time calc.

F.Offset : offset for the field

F.type : type of struct var.

offset(T, f) : offset of type f in struct T.

@type(T, f) : type of f in struct T.

E → F : $t_1 = \underline{\quad}$ $t_2 = \underline{\quad}$ $t_3 = \underline{\quad}$

C₁ = gen(t₁, =, &F.name)

C₂ = gen(t₂, =, t₁ + F.Offset)

C₃ = gen(t₃, =, F.type)

E.code = C₁ || C₂ || C₃; E.place = t₃

F → id1.id2 F.name = id1.name

F.type = type(id1.type, id2.name)

F.offset = offset(id1.type, id2.name)

F → f.id F.name = f.name
F.type = type(F.type, id.name)
F.offset = F.offset + offset(F.type, id.name)

Approach 2: runtime computation

{
F.code is true.
F.address is true...
F.type is true
}

E → F $t_1 = \underline{\quad}$; E.place = t₁

E.code = F.code || gen(t₁, =, &F.address)

F → id1.id2

$t_1 = \underline{\quad}$
 $t_2 = \underline{\quad}$

F.type = type(id1.type, id2.name)

C₁ = gen(t₁, =, &id2.name)

F.code = C₁ || gen(t₂, =, t₁ + offset(id1.type, id2.name))

(id1.type, id2.name) = t₂

so F.type = t₁ + offset(id1.type, id2.name)

$F_1 \rightarrow F_2.id$ $t_1 = ___ \cup$

$F_1.type = type(F_2.type, id.name)$

$T_1 = gen(t_1, =, F_2.address + offset(F_2.type, id.name))$

$F_1.code = F_2.code || C_1$

$F_1.address = t_1$

$F \rightarrow id_1 \rightarrow id_2$

let T be $id.type$ pointer(T)

$t_1 = ___ \cup$

$F.type = type(T, id_2.name)$

$F.code = gen(t_1, =, id_2.name + offset(T, id_2.name))$

$F.address = t_1$

$F \rightarrow F_2 \rightarrow id_1$

let T be such ~~that~~ $F_2.type = pointer(T)$

$t_1 = ___ \cup, t_2 = ___ \cup$

$F_1.type = type(T, id_1.name)$

$C_1 = gen(t_1, =, *F_2.address)$

$F_1.code = F_2.code || call gen(t_2, =, t_1 + offset$

$(T, id_1.name))$

$F_1.address = t_2 \cup$

Syntax directed translation scheme :-

~~synthesized
attribute
(normal)~~

~~inherited
attribute
(from top to left)~~

~~if type is inherited to varlist.~~

~~* An SOD is S-attributed if all are synthesized.~~

~~is L-attributed if uses inherited attribute that
(function, variable) depend on some symbol on left.~~

$X \rightarrow Y_1 Y_2 Y_3 Y_4$

~~can
depend on X~~

SDTS:

$\text{Decl} \rightarrow \text{Type} \{ \underbrace{\text{Varlist.type} = \text{Type.name}}_{\text{actions.}} \} \text{ Varlist.}$

~~declaration
processing.~~

Type analysis:-

- type expression
 - type equivalence
 - type checking inference

1) type expression

- basic types as bool, int, float
 - user defined type name.
 - type constructor applied to

array (k, j)

pointer (T)

Structure $(f_1, T_1) (f_2, T_2) \dots$ \vdash $\neg f_1 \neg T_1 \neg f_2 \neg T_2 \dots$

$\Gamma_1 \rightarrow \Gamma_2$ penation. (b) Homotopy class of

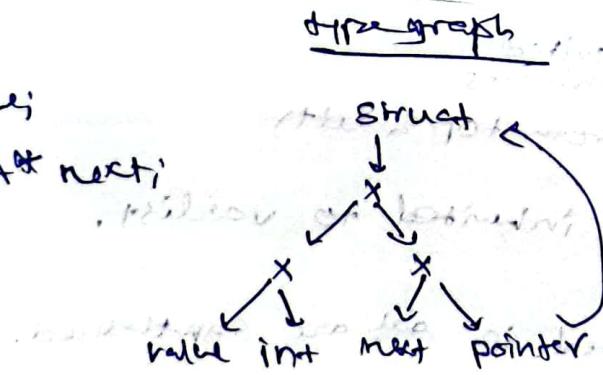
$T_1 \times T_2 \times T_3$: product of three sets
1. list.

STRUCT AG

int value;

enact A⁴ next;

3



$A = \text{struct} ((\text{val}, \text{int}), (\text{next}, \text{pointer}(A)))$

• ticket. Passengers returning to ~~NYC~~ to see

Name & Scope analysis

> Stack of symbol tables.

static scoping ✓

dynamic scoping: ↗

- names declared in procedures enclosing X;
- in a call chain reaching X.

no
only
vars.

* Scope analysis - SDTS

transient rules.

Program → {push-new-syntab();} DL SL

$DL \rightarrow DL \cup D \mid \epsilon$ DL: list of declarations.

$D \rightarrow T \ id \{add var to syntab
(id.name, T.type); \}$ T: type

$D \rightarrow T \ id \ \{add_ \} \{push-new-syntab
(PL) \ \& \ DL \ SL\} \{pop syntab\}$ PL: list of formal parameters.

$T \rightarrow int \mid void \mid \dots$ SL: list of statements.

$PL \rightarrow PL, P \mid P$ AL: actual parameters

$P \rightarrow T \ id \ \{add param to syntab(id.name, T.name)\}$ in reg action

$SL \rightarrow SL \cup call \mid \epsilon$

$call \rightarrow id \ \{lookup(id.name)\} \ (AL);$

$AL \rightarrow AL, id \ \{lookup(id.name)\} \mid id \ \{lookup(id.name)\}$

function

param

call

Declaration Processing :-

int a[20][10];

C array size calculation:-

x.bt base type

x.dt derived type

x.v value

x.s size

x.nm name

x.w width

D → T { I.bt = T.bt; I.w = T.w } I; { Enter in symbols (I.nm, I.dt, I.s)}

T → int { T.bt = int; T.w = 4 }

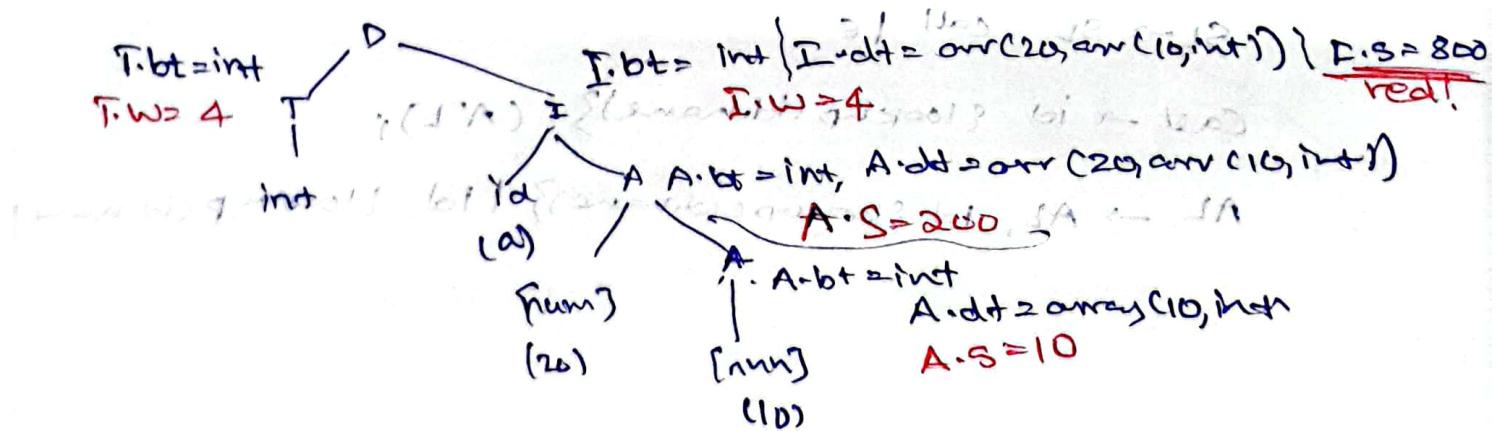
T → double { T.bt = double; T.w = 8 }

I → id { I.dt = I.bt; I.nm = id.nm; I.s = I.w }

I → id { A.bt = I.bt } A { I.dt = A.dt, I.nm = id.nm, I.s = A.s * I.w }

A → [num] { A.dt = array(num.v, A.bt); A.s = num.v }

A1 → [num] { A2.dt = A1.bt } A2 { A1.dt = array(num.v, A2.dt); A1.s = A2.s * num.v }



For pointers:

only additional rules.

Item1 \rightarrow *{item2.bt = Item1.bt} Item2 { }

Ii.dt = pointer (Ij.dt);
- I1.s = 4



Stack grows downwards

1000 I1 = 4 \rightarrow

1004 I2 = 8 \rightarrow

(1012) 7 \rightarrow

1012 7 \rightarrow 11

1016 11 \rightarrow 12

1020 12 \rightarrow 13

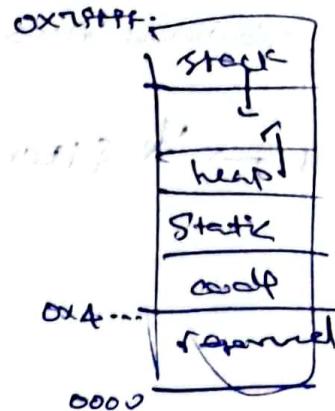
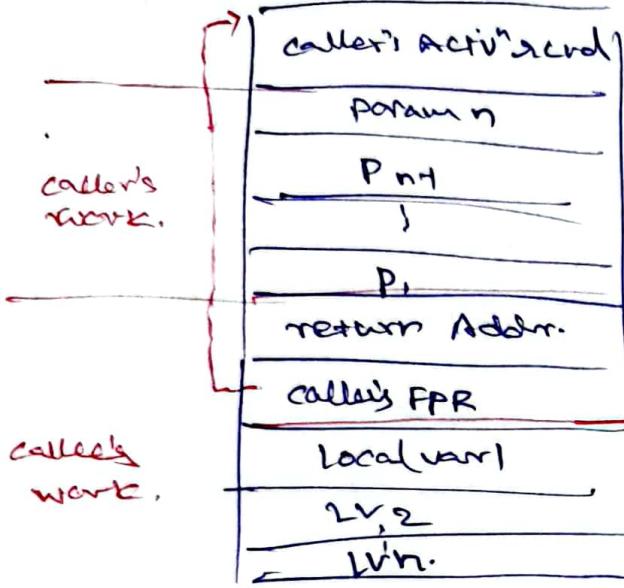
Runtime support :-

→ procedure calls:

Activation Records:-

Function returns stack P

P = L+P



variable	Address	size.
Param1	$\mathbf{S}(\$R_P)$	P_1
P2	$(S+P)(\$R_P)$	P_2
P3	$(S+P+P_2)(\$R_P)$	P_3
L1	$-R_1(\underline{\$FP})$	L_1
L2	$(-L_1-L_2)(\$FP)$	L_2
L3	$(-L_1-L_2-L_3)(\$FP)$	L_3

Example: function prologue, epilogue, call

```
int f (int a, int b)
{
    int c;
    c = a+b;
    return c;
}

int main()
{
    int x,y,z;
    z = f(x,y);
    printf("%d", z);
    return 0;
}
```

main function:

• **f -:**
prologue
sw \$ra, 0(\$sp) # save the return add.
su \$fp, -4(\$sp) # save the frame ptr.
sub \$fp, \$sp, 4 # under frame ptr.
sub \$sp, \$sp, 12 # make space for locals;
prologue ends
epilogue starts
add \$sp, \$sp, 12 # remove space of
locals \$ra, \$sp
lw \$fp, -4(\$sp) # set \$fp to \$sp-4
lw \$ra, 0(\$sp) # save ra.
jr \$ra # jump to caller.
epilogue ends

Access-link:
How to access variables in scoping rules.

Example: variable bind

Stack	Frame
(0x0000) + 0x1000	0x1000 + 0x1000
(0x0000) + 0x2000	(0x1000) + 0x1000
(0x0000) + 0x3000	(0x2000) + 0x1000

→ parameter passing:

```

int a
int main()
{
    a = 5;
    f(a, a+1);
    cout << a;
    return 0;
}

void f(x, y)
{
    a = a+10;
    a = a+y;
    x = x+y+100;
}
  
```

call by value-result:-

$a = 5$; $a = 5$
 $t_0 = a+1$; $t_0 = 6$
 $x = a \rightarrow x = 5$
 $y = t_0$; $y = 6$
 $a > a+10$; $a = 15$
 $a > a+y$; $a = 21$
 $x = x+y+100$; $x = 111$
 $a = x \rightarrow a = 111$
 $t_0 = y$

call by name :

$x = a$ replace every occurrence..
 $y = a+1$
 $a = a+10$; $a = 15$
 $a = a+y$; $a = 31$
 $\equiv a+a+1$
 $x = x+y+100$
 $a = a+a+100$; $a = 163$

writes to (cati)
 are invisible

call by need:-

$a = 5$
 $x \equiv a$; don't calculate yet
 $y \equiv a+1$; " "
 $a = a+10$; $a = 15$
 $a = a+y$; $y > a+1 = 16$
 $" a = 31$
 $\{ \cancel{x = x+y+100} ; x = a = 31$
as a . $\rightarrow a = 147$

only once
 lazy;
 not always.

" textual substitution of formal
 parameters by actual parameters,
 but evaluation only once".

g()

f(e):

f(e)

call by name:

$use(x) \rightarrow use(e)$
 $def(x) \rightarrow def(*(\&e))$

call by need:

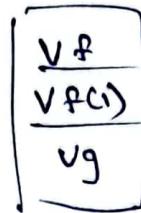
$use(x) \rightarrow \boxed{x = e}$
 $use; > 1(x) \rightarrow use(x)$
 $def(x) \rightarrow def(*(\&x))$

to....

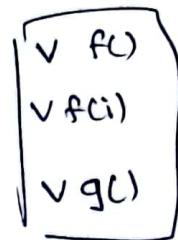
→ virtual functions:

Class A :

virtual f()
virtual f(Same)
virtual g()

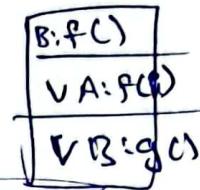
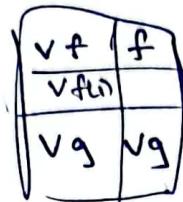


final table



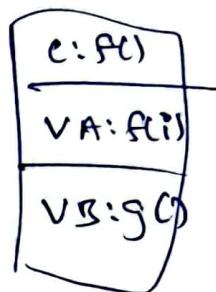
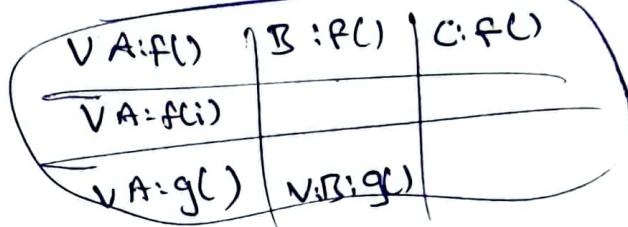
Class B : A

virtual void g()
 void f()



Class C : B

f()



compile time activity:-

- 1) collect all virtual across class hierarchy
- 2) Ignore non-virtual functions
- 3) Analyze the hierarchy; for overriding functions

Run time:

- dereference obj pointer to know the class & access virtual functions table.
- add offset to base of the table to access function IDH
- Dereference funcptr to make call.

200 different species

1114 at 247

total with 100% -

100% of 3

100% of 100%

but it's not clear what's meant by that

and there's no legend

and there's no legend

so all we can say is that

species with 100%

species with 100%

species with 100%

etc

catalogue of

species that have 100% of 3

is very hard to determine

which species are found with 100% of 3 or
more than 100% of 3

species that have

species that have 100% of 3

species that have 100% of 3 or more than 100% of 3

excludes 100% of 3

excludes 100% of 3

Species associated with 100% of 3

Species associated with 100% of 3 or more than 100% of 3

Species associated with 100% of 3 or more than 100% of 3

Species associated with 100% of 3 or more than 100% of 3

Species associated with 100% of 3 or more than 100% of 3

Species associated with 100% of 3 or more than 100% of 3

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Code generation:-

TAC to RTL.

→ Register Allocation:-

Local reg. allocation: Sethi-Ullmann Algorithm.

- using registers to hold intermediate values of expressions

Global reg. Allocation: Chatin-Briggs graph colouring.

- keep the values in registers across statements.

→ Chatin-Briggs register allocator:-

- identify live ranges
- compute interference graphs
- Colour the graph.

Steps

1. Coalescing:

eliminate copy statements $x=y$ or $C=t_1$.

2. Identify live ranges:-

- Seq. of statements from definition/assignment of a variable to its last use of that value.
- Bottom up analysis.

3. Construction of inference graph:-

live ranges l_1, l_2 interfere if definition/assignment of a variable "of a variable V_1 " of l_1 occurs in range of l_2 "of a variable/temp. symbol V_2 ".

4) Simplify the inference graph?

5) Color the nodes.

Eg:-

0. $P(a,b,c,d)$ a b c d

1. $t_0 = b + c$ a b c d e f STEP-1

2. $t_1 = a + t_0$ a b c d

3. ~~$e = t_1$~~ a b c d e f

4. $t_2 = c * a$ a b c d e f

5. $t_3 = t_2 - t_1$ a b c d e f

6. $c = t_3$ a b c d e f

7. $f = t_1 + d$ a b c d e f

8. $a = d + t_1$ a b c d e f

$\underline{\underline{a = d + t_1}}$

K-colouring chatins:-

1) simplify(a)

for n , $D(n) < K$, remove & push onto stack in arbitrary order.

2) Simplify(b)

if graph is not empty; find node with least spill cost, spill it and go back to(a)

3) color

pop from stack; plug it in graph & color.

K-colouring Brigs:-

1) simplify(a): if $n < K$

for n when $D(n) < K$; push onto stack.

(\leftarrow stack)

2) Simplify(b):

if graph not empty; mark the node as Potentially Spillable (PS) & stack them too!

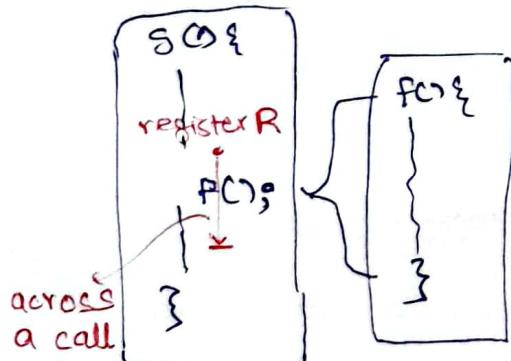
3) color:

in order of increasing degree
pop & color it
if cannot color, spill it, & go back to a.

* Spilling decreases the degree of node;

for a live-range & another round of simplification might give better colouring order.

→ Managing registers across calls



- use a caller-saved register R for values that are not live across a call.
- use a caller-saved register R for values that are live across a call.

* SCLP register usage:

V1

fo { fo, fi } used for function descri.

Registers	Stack	Reg
r	o	
l	d	
s	f	
t	h	

No
t0 - t9 } int
s0 - s7 }

f2 - f30 } float:
(f4, f5) (f30, f31)

→ register allocation in SCLP:-

- * no register is occupied across any assignment in the program.

for LHS variable, result is stored in memory.

not
Temporary? numm...
NO!

- 1) When temporary is assigned a register, mark it occupied.
- 2) When temporary is used in TAC Statement, mark the register free.

TAC order : first opd, result, second opd.
For register allocation

→ Integrated Instruction Selection, & register Allocation:- local. reg. allocation

Sethi-Ullman Algo:-

- Simple machine model
- optimal no. of instructions with min. no of registers & stores
- Linear in size of exp. tree.
- contiguous evaluation!

Aho-Thompson Algo:-

- very general machine model
- linear in exp. tree size
- optimal in terms of cost of execution.

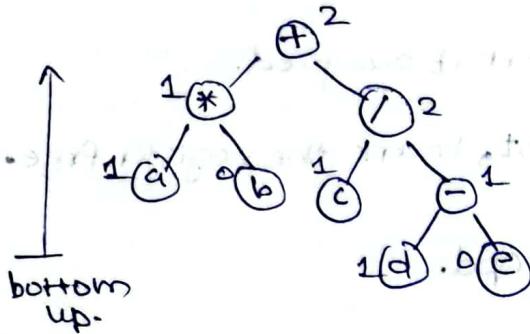
Instructions:-

$r \leftarrow m$, $m \leftarrow r$
 $m \leftarrow r_1 \text{ op. } r_2$
 $r \leftarrow r_1 \text{ op. } m$
 $r \leftarrow m \text{ op. } r_2$

Algorithm:-

1. Traverse tree bottom up & label each node with min. no. of registers needed to evaluate the subexpression.
2. Traverse top-down & generate code.

$\text{label}(n) = \begin{cases} 1, & n \text{ is leaf \& in register (left leaf)} \\ 0, & n \text{ is right leaf} \\ \max(l_1, l_2), & n \text{ has two children with } l_1 \text{ \& } l_2. \\ l_1 + 1, & \text{when } l_1 = l_2. \end{cases}$



Always first generate RIL Post-part with more label.

→ Generating code:

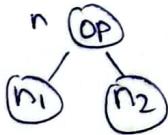
case-1:

name n

gen code(n) is

emit (top(rstack) ← name)

case-3:



$\text{label}(n_1) \geq \text{label}(n_2)$

&

$\text{label}(n_2) < k$

gen code(n):

```

    gen code(n1)
    R = pop(rstack)
    gen code(n2)
    emit (R ← R op top(rstack))
    push (R, rstack)
  
```

case-4:

$\text{label}(n_1) < \text{label}(n_2)$

$\text{label}(n_1) < k$

```

    swap(rstack)
    gen code(n2)
    R = pop(rstack)
    gen code(n1)
    emit (top(rstack) ← top(rstack) op R)
    push (R, rstack)
    swap(rstack)
  
```

case-2:

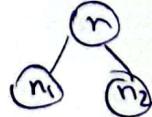


gen code(n):

```

    gen code(n1)
    emit (top(rstack) ←
          top(rstack) op
          name)
  
```

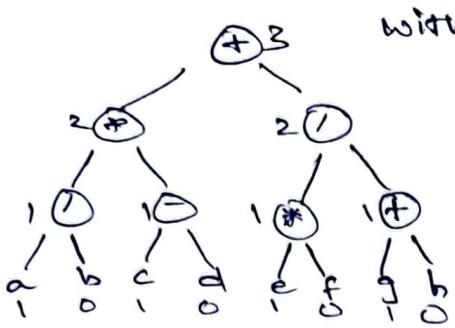
case-5: $\text{label}(n_1) \geq k \text{ \& } \text{label}(n_2) \geq k$



gen code(n2)

```

    T = pop(rstack)
    emit (T ← top(rstack))
    gen code(n1)
    emit (top(rstack) ← top(rstack)
          op T)
    push (T, rstack)
  
```



With 2 registers:-
K=2

$$\begin{aligned}
 & \left. \begin{aligned} r_0 &\leftarrow c \\ r_0 &\leftarrow r_0 * f \\ r_1 &\leftarrow g \\ r_1 &\leftarrow r_1 * h \\ r_0 &\leftarrow r_0 / r_1 \\ t_0 &\leftarrow r_0 \end{aligned} \right\} \text{right subtree.} \\
 & \left. \begin{aligned} r_0 &\leftarrow a \\ r_0 &\leftarrow r_0 / b \\ m &\leftarrow c \\ r_1 &\leftarrow r_1 * d \\ r_0 &\leftarrow r_0 * r_1 \end{aligned} \right\} \text{left subtree.} \\
 & \underline{r_0 \leftarrow r_0 + t_0}
 \end{aligned}$$

→ Dense nodes & major Nodes:

if label(n) ≥ k

if both
children
are dense nodes!

major node
also a
dense node.

- node is dense → parent is dense.
- node is major → parent is need not major.

* if we make a store; then we decrease a dense node & its parent node will no longer be major.

* A store can reduce no. of major nodes by almost one.

E.g.; we call a store for every case-s
major node

E.g.; our no. of stores
is optimal.