

## Week-10:-

(as magnetic field).

\*  $B \rightarrow$  magnetic flux density.

(no. of lines per unit area).

(Tesla, T) depends on core-material.

(not in circuits...)

mag. field intensity.

\*  $H \rightarrow$  magnetic strength / magnetic field strength

doesn't depend on type of core material

(but depends on coil. in circuits).

$$(B = \mu H)$$

permeability.

$$AS \propto H \uparrow, B \propto H$$

$$\mu = \frac{\mu_0 \cdot H_r}{J}$$

may not be constant for a material.

Function of

magnetic field. intensity.

(hysteresis)

field intensity/strength.

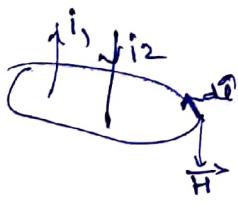
\*  $H$  depends on setup ( $n, j$ ) but not on material.

$B$  depends on material.

$\hookrightarrow$  mag. flux density.

depends on material.

\* Ampere's law :-



$$\oint \vec{H} \cdot d\vec{l} = i_1 - i_2$$

field intensity / currents

\* Hence



$$H \cdot 2\pi r = i$$

$$H = \frac{i}{2\pi r}$$

$$\therefore B_o = \frac{\mu_0 i}{2\pi r}$$

\*  $(B = \mu_0 H_r H)$  Weber/m<sup>2</sup> or Tesla.

medium variable

units of  $\Phi$ .

$(4\pi \cdot 10^{-7})$  Henry m.

units of inductance.

## contents:-

- Ampere's law E

- relation between

$B, H, i$

- Magnetic circuits

- Hysteresis curve & coreloss.

- Transformer

- Transformer equivalent circuit.

- No-load test, short circuit test

- Voltage regulation of transformer.

- Efficiency of transformer.

- Three phase transformer. (basic introduction)

## → magnetic equivalent circuit

### magnetic field intensity H

$$H \cdot 2\pi r = Ni$$

$$H = \frac{Ni}{2\pi r}$$

$$B = \mu_0 \left( \frac{Ni}{2\pi r} \right)$$

$$H = \frac{Ni}{2\pi r}$$

now;  $H = \frac{Ni}{2\pi r}$

all grown up...

for more info go to page 10

more info

more info

\*  $H \cdot l = Ni$   $\rightarrow$   $H = \frac{Ni}{l}$

$$H = \frac{N \cdot i}{l} \text{ At/m}$$

$$B = \frac{\mu_0 Ni}{l}$$

$$B \cdot l = \mu_0 \cdot (Ni)$$

$$\gamma = Ni = \int H \cdot dl$$

$$H \cdot 2\pi r = Ni$$

(Ni) is called magnetomotive force (mmf).

like  $\int E \cdot dl = emf$ .

$$\int H \cdot dl = mmf$$

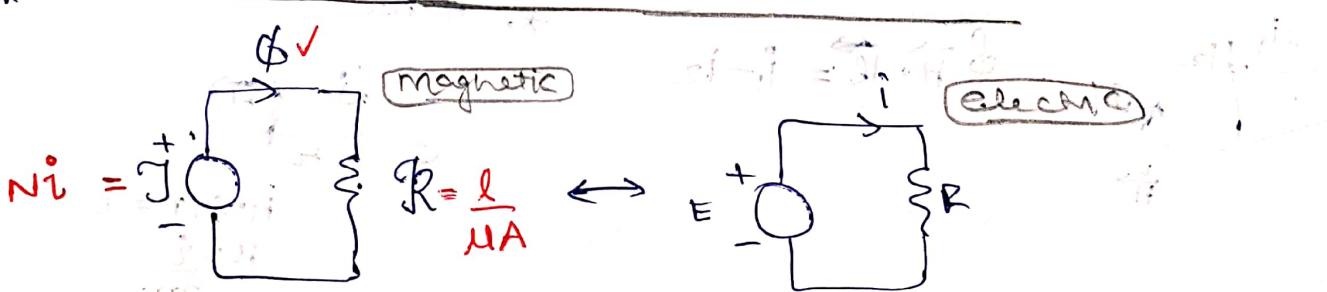
units: Amperes-turns

At

$$= AB$$

$$= \frac{\mu_0 Ni \cdot A}{l}$$

$$\phi = \frac{Ni}{(l/ma)} = \frac{mmf}{(l/ma)}$$



$$\phi = \frac{Ni}{l/ma}$$

$$= \frac{i}{R} \text{ mmf}$$

reluctance of magnetic path.

if  $A$  is more;  $H$  same  $\phi \uparrow \Rightarrow R \downarrow$

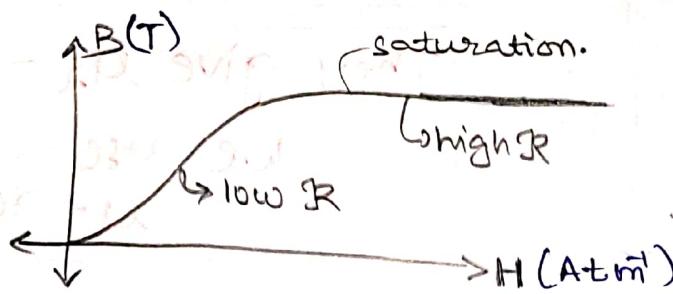
if  $l$  is more;  $H$  less  $\phi$  same  $\Rightarrow R \uparrow$

$$i = \frac{E}{R} - \text{emf}$$

APPLY INDUCTIVE LAW

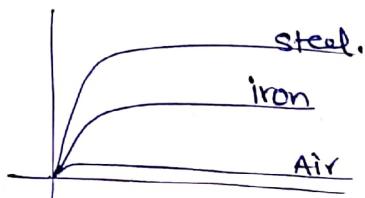
resistances

\* B-H curve :- ( $B$  varies with  $H$ ).  
not constant!



No hysteresis

$H \rightarrow$  free charges



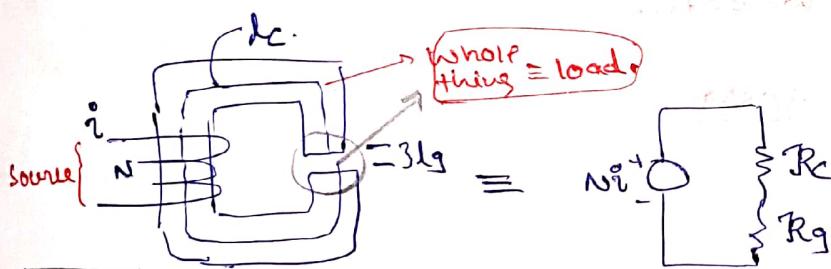
$B \rightarrow$  Bound + free charge?...

(or) only bound.

Saturating means ... bounded!

### \* Composite magnetic circuits:-

\* When the path of flux encounters more than one medium, then series resistors:-



$$B = Ni$$

$$\text{Reluctance}_{\text{core}} = \frac{l_c}{\mu_c \cdot A_c}$$

$$R_g = \frac{l_g}{\mu_0 \cdot A_g}$$

! vacuum  $\approx$  air.

air gap also a resistor.  
very high  
resistance!  
(as low  $\mu_r$ )  
 $\mu_r = 1$ ...

But y?: proof:

$$B_c = H_c \cdot \mu_c$$

$$= \frac{\phi_c}{A_c} = \frac{\phi}{A_c}$$

$$B_g = \frac{\phi_g}{A_g} \approx \frac{\phi_c}{A_c} = \frac{\phi}{A_c}$$

$\phi_c \approx \phi_g$  as  $\phi_{\text{net}}$  should be conserved... {Kirchoff 1st law...}

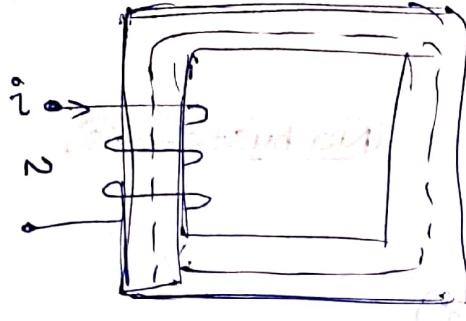
E since  $B = \frac{\phi}{A}$ ;  $B_c = B_g \Rightarrow H_c \neq H_g$ . this is what sir meant; when he said  $H$  depends on  $N$ ;  $B$  doesn't!

$$H_c = \frac{\phi}{A_c \cdot \mu_c}; H_g = \frac{\phi}{A_g \cdot \mu_0}$$

& Amper's law! (Kirchoff's 2nd law)

$$Ni = \frac{\phi}{A_c \cdot \mu_c} \cdot l_c + \frac{\phi}{A_g \cdot \mu_0} \cdot l_g$$

Eg:



(+) flux density ( $\mu$ ) - upwards

They give  $\mu_r = 200$

We use

$$\mu = 200 \times 4\pi \times 10^{-7}$$

$$mmf = Ni$$

$$R = \frac{l}{\mu A}, \text{ (as } \mu \uparrow, \phi \uparrow \text{) } \therefore R \downarrow$$

$$\text{where } \phi = \frac{Ni \cdot \mu A}{l} \quad \text{Amperes law... } H \cdot l_c = Ni$$

$$= \frac{4000 \times 1.5 \times 2000 \times 10 \times 5 \times 10^{-4}}{(120 \times 10^{-2})} \text{ m}^2$$

$$\frac{\phi}{A} \cdot l_c = Ni$$

$$\phi = 6.28 \times 10^{-3} \text{ Wb weber...}$$

$$B = \frac{\phi}{A} = 1.25 \text{ T tesla}$$

Inductance in the core

\* Ans.

Now; flux linkage

$$= N \cdot \phi$$

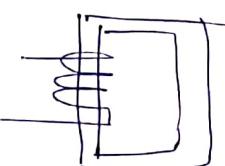
net turns.



total 'N' turns.

$$\therefore \text{Inductance} = \frac{\text{flux linkage}}{i} = \frac{N \cdot N}{l/\mu A k} = \frac{N^2}{R}$$

will be similar for



case.

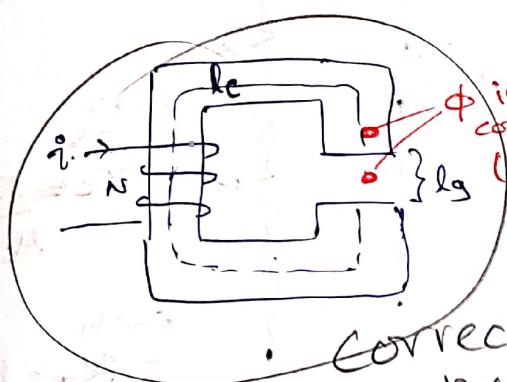
Q: What is the value of  $R$ ?

Ans:  $R = \mu A / l$

$\mu = \mu_0 \cdot \mu_r$  (relative permeability)

## Assignment:-

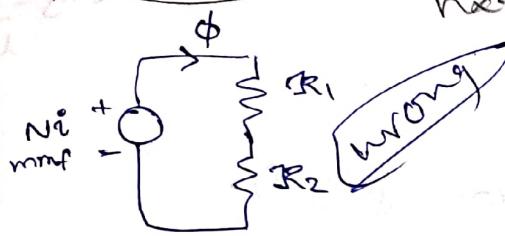
a) ✓ relay → did the job of bridging, electric & electronic circuits.  
 (they were used before transistors).



(need a metal rod...)

- $\phi$  is conserved.
- (Kirchoff's 1st law).
- $B$  is same.
- $H$  is different.

so, sir said "H is dependent on material of core".



Corrected net pg.

$$N = 500$$

$$l_c = 360 \text{ mm}$$

$$l_g = 1.5 \text{ mm}$$

$B = 0.8 T$  to actuate the relay.

$$R_1 = \frac{l_c}{\mu_0 \cdot A_c}$$

$$R_2 = \frac{l_g}{\mu_0 \cdot A_c}$$

satisfy all equations  
"cause a machine to work."

$$\therefore R_{\text{net}} = \dots$$

$$\phi = \frac{Ni}{R_{\text{net}}} = B \cdot A_c$$

$$\Rightarrow B \cdot A_c = \frac{Ni}{R_{\text{net}}} \cdot A_c = \frac{Ni}{\frac{l_c + l_g}{\mu_0}} = \frac{Ni \mu_0}{l_c + l_g}$$

need 1 more variable...

- q

(or)

$\mu$

$$M_{\text{cast}} = \frac{B}{\mu} = \frac{0.8}{450}$$

$$\therefore 0.8 = \frac{500 \cdot i}{\frac{360 + 1.5}{450}}$$

$$\therefore i = \frac{0.8}{500} \times \left( \frac{360 \cdot 450 + 1.5 \cdot 10^7}{0.8} \right) \cdot 10^{-3} \text{ Amperes.}$$

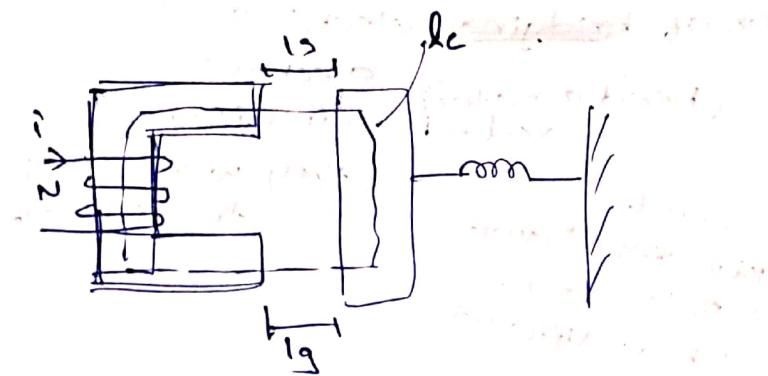
$$= \frac{0.8}{500} (202500 + 1172 \cdot 10^3) \cdot 10^{-3}$$

$$i = 19.017 \text{ A}$$

$$19.017 \text{ A} = 19.017 \cdot \frac{500}{450} \text{ Amperes}$$

(Q1)

### relay.



$$N = 500 \text{ turns}$$

$$l_c = 360 \text{ mm}$$

$$l_g = 1.5 \text{ mm}$$

$$B = 0.8 \text{ T}$$

$$(Mc)r = 1150 \text{ (from google).}$$



$$RC = \frac{l_c}{\mu_0 \cdot Ac}$$

$$Rg = \frac{l_g}{\mu_0 \cdot Ac}$$

$$\begin{aligned} R_{net} &= \left( \frac{360}{1150 \cdot Ac} + 2 \cdot \frac{1.5}{Ac} \right) \cdot \frac{10^{-3}}{\mu_0} \\ &= \left( \frac{36}{115} + 3 \right) \cdot \frac{10^{-3}}{\mu_0 \cdot Ac}. \end{aligned}$$

$$\frac{3.313 \times 10^{-3}}{\mu_0 \cdot Ac}$$

$$\therefore N_i = \frac{B \cdot Ac}{Rg} \times \frac{3.313 \times 10^{-3}}{\mu_0 \cdot Ac}$$

$$\Rightarrow i = \frac{0.8 \times 3.313 \times 10^{-3}}{4\pi \times 10^{-7} \times 500}$$

a)  $i = 4.022 \text{ A}$

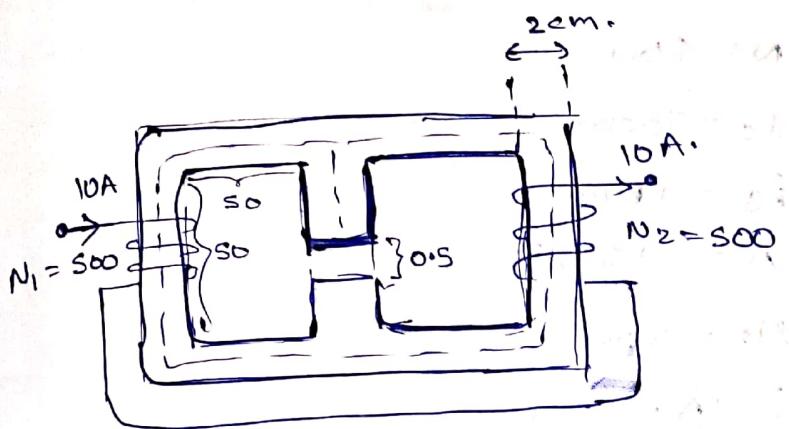
b)  $Mc = 1.45 \times 10^{-3} \text{ SI units.}$

$Ncr = 1150 \text{ (from google).}$

c) now;  $R_{net} = \frac{0.313 \times 10^{-3}}{\mu_0 \cdot Ac}$

$\therefore i_{now} = \frac{0.313}{3.918} \times 4.022 = 0.398 \text{ A.}$

Q2)



$$M_r = 1200$$

ferro magnetic.

neglect leakage.

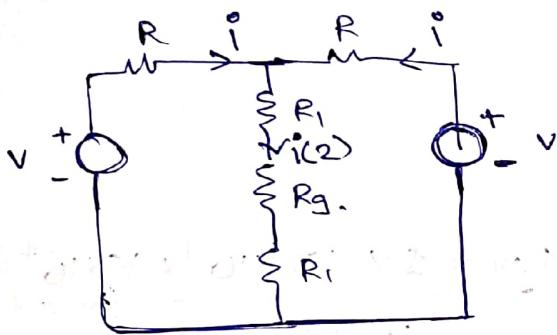
(apply Kirchhoff's law)

(cm):

cross-section = square.

III

taking all SI units.



$$R = \frac{(S_1 + S_2 + S_3) \text{ cm}}{\mu_0 \cdot A}$$

$$R_1 = \frac{\left(\frac{51.5}{2}\right)}{\mu_0 \cdot A}$$

$$R_g = \frac{0.5}{\mu_0 \cdot A}$$

$$V = N_i = 10 \times 500$$

$$= 5 \times 10^3$$

$$A_c = 2 \times 2 \times 10^{-4}$$

$$= 4 \times 10^{-4} \text{ m}^2$$

Sq m)

$$\therefore \phi = 2.06 \times 10^{-4} \text{ Wb}$$

$$B_g = \frac{\phi_g}{A_c} = \frac{4.12 \times 10^{-4}}{4 \times 10^{-4}} = 1.03 \text{ T}$$

$$H_g = \frac{B_g}{\mu} = 821865 \text{ Atm}$$

+ final (i) :

loop law in left loop:-

$$+V - iR - 2i(2R_1 + R_g) = 0$$

$$\Rightarrow i = \frac{V}{R + 4R_1 + 2R_g}$$

$$= \frac{5 \times 10^3 \times 4\pi \times 10^{-7} \times 4 \times 10^{-4}}{10^{-2} \left( \frac{156}{1200} + 4 \times \frac{51.5}{2} + 2 \cdot 0.5 \right)}$$

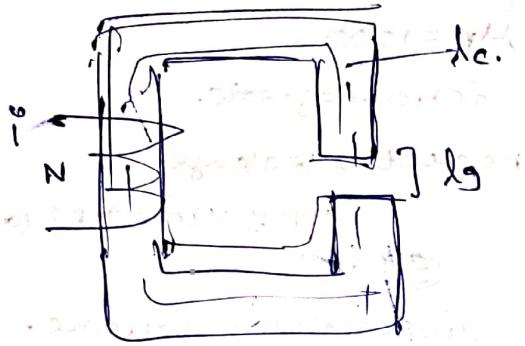
$$= \frac{2 \cdot 52 \times 10^{-4}}{1.22}$$

$$i = 2.06 \times 10^{-4} \text{ A}$$

$$\therefore \phi = 2.06 \times 10^{-4} \text{ Wb}$$

$$\therefore \phi_g = 2\phi = 4.12 \times 10^{-4} \text{ Wb}$$

(Q3)



$$N = 400$$

$$l_c = 50 \text{ cm}$$

$$l_g = 1 \text{ mm}$$

$$A_c = 15 \text{ cm}^2$$

$$\mu_r = 3000$$

$$i = 1 \text{ A}$$

(Sol)

a) Ni

$$R_c = \frac{l_c}{3000 \mu_0 A_c}$$

$$R_g = \frac{l_g}{\mu_0 A_c}$$

$$\phi = \frac{Ni (\mu_0 A_c)}{\frac{0.5}{3000} + 0.001} = \frac{400 \times 1 \times 4\pi \times 10^{-7} \times 15 \times 10^{-4}}{0.00117}$$

$$\phi = 6.4 \times 10^{-4} \text{ weber.}$$

transformer ratio  $B_g = \frac{\phi_g}{A_c} = 0.4309 \text{ T.}$

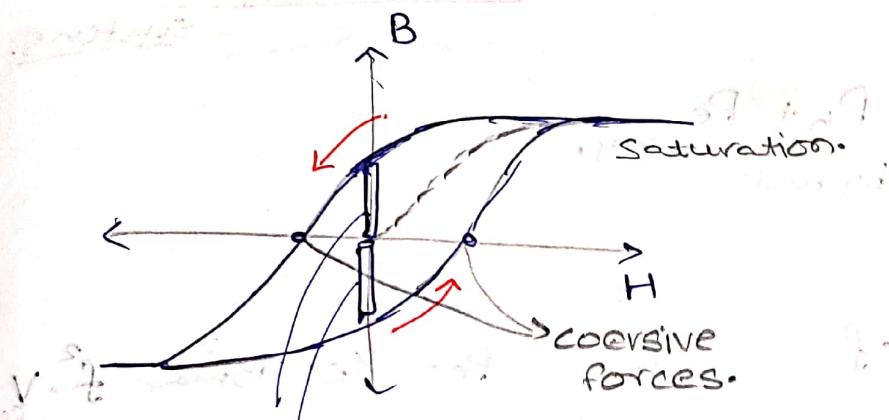
b)  $L = \frac{\text{flux linked}}{\text{current}} = \frac{N \cdot \phi}{i} = \frac{400 \times 6.4 \times 10^{-4}}{1 \text{ A}} = 0.258 \text{ H.}$

total flux  $\phi = 6.4 \times 10^{-4} \text{ weber}$

max flux density  $= 6.4 \times 10^{-4} \text{ weber}$

→ B-H curve again!:-

Diagram shows for hysteresis loss in core



(residual magnetism)  $\downarrow \downarrow$  cool w.

Hysteresis loss:-

- when core is subjected to alternating excitation;

✓ (loss coming)

area of BH loop

$$= K \cdot B_{\max}$$

Because we always  
need to negate the

residual  
magnetism;  
in both direct's.

Q.

Hysteresis loss on Heat frequency

$$P_h = K_h \cdot B_{\max}^n \cdot f$$

empirical formulae.

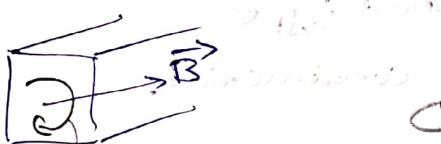
loss won't come;



now;  
while going  
+  $\rightarrow$  - we  
do work;  
when  
 $\rightarrow$   $\leftarrow$ ;  
it is doing  
work  
for us.

Eddy current loss:-

- where  $\vec{B}$ ; there are eddy currents wrong!



where  $\frac{d\vec{B}}{dt}$  there eddy currents!  
down!

$$P_e = K_e \cdot B_{\max}^2 \cdot f^2 \cdot V_{core} \cdot \text{Volume}$$

$$\& K_e = \frac{\pi^2 t^2}{6P}$$

where  $t$  = lamination  
thickness

$P$  = resistivity  
of lamination

this is electrical  
loss.

above loss is  
magnetic loss

with resistance

make laminations; less  $f$  to avoid this.

not  
core

use high  $P$  to avoid this.

## \* core loss:-

losses in core material of electro magnetic systems.

$$P_{\text{core}} = P_h + P_e$$

eddies,  
hysteresis

that was easy...

$$P_h = K_h \cdot B_{\text{max}} \cdot f \quad ?$$

$$P_h = \left( \frac{\text{Area of BH}}{\text{BH}} \right) \times V_{\text{core}} \times f$$

*K<sub>h</sub> depends on V<sub>core</sub> & material*

$$P_e = K_e \cdot B_{\text{max}}^2 \cdot f^2 \cdot V_{\text{core}}$$

$$P_e = \left( \frac{\pi^2 t^2}{6f} \cdot B_{\text{max}}^2 \right) \cdot V_{\text{core}} \cdot f^2$$

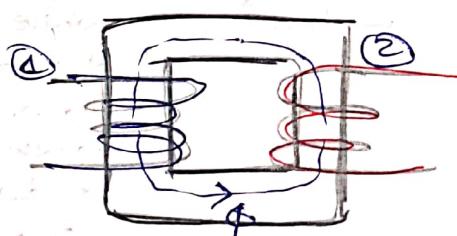
*t, P of lamination material.*

*Not core.*

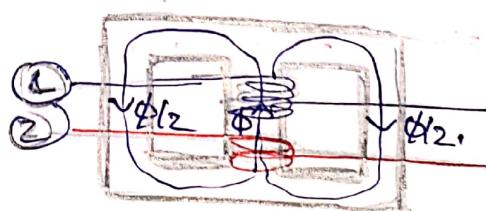
## Transformer construction:-

\* first; core's construction.

**Only AC**



**core-type construction.**



**Shell type construction.**

Here

windings surround  
core.

∴ hence core is  
surrounded by  
windings.

∴ small leakage flux  
existing

Here core surrounds

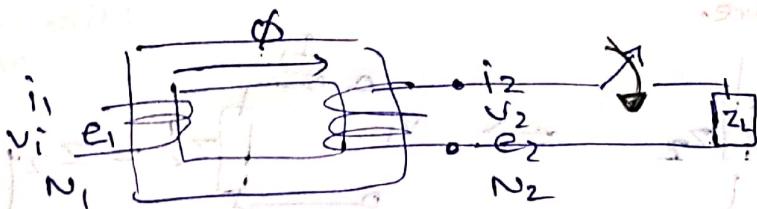
windings "shell".

∴ hence shell

core acts as shell

& even  
smaller flux exists.

## → transformer equations:-



$$V_1 = E_1 = N_1 \frac{d\phi}{dt} \quad \text{Faraday's induction law}$$

$$\therefore V_2 = N_2 \frac{d\phi}{dt}$$

$$\therefore \frac{V_1}{V_2} = \frac{N_1}{N_2} = \alpha$$

$V_2$  is secondary winding terminal voltage

terminal voltage

ideally; we take  $R_c = 0$

these

are absolute

not RMS.

$$\alpha = \frac{N_1}{N_2}$$

$$\frac{i_1}{i_2} = \frac{N_2}{N_1}$$

## \* ideal transformer:-

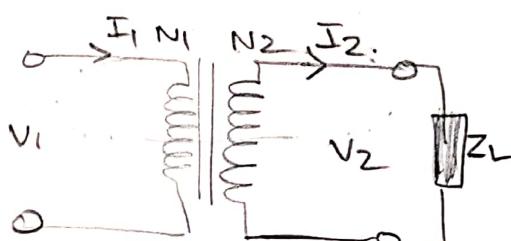
1) all core & winding losses neglected.

2) assumed  $R_{core} = 0$

$$\therefore R_{core} = 0$$

$$\text{net mmf} = 0.$$

3) no leakage flux.



$$Z_1 = \text{input impedance} = \frac{V_1}{I_1}$$

$$Z_2 = \text{secondary side impedance} = Z_L$$

to reduce the circuit diagram

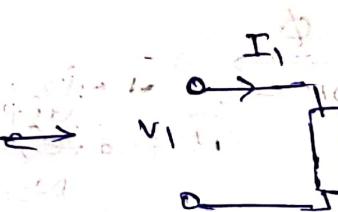
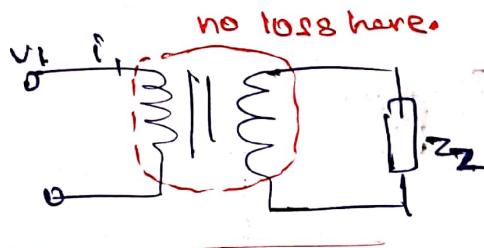
$Z'_1$ : primary side impedance seen from secondary side

$$Z'_1 = Z_2 \cdot \left(\frac{N_1}{N_2}\right)^2$$

$$\left(\frac{N_1}{N_2}\right)^2$$

one reduction of circuits  
technique.

## \* Impedance ( $Z_2'$ ) transfer



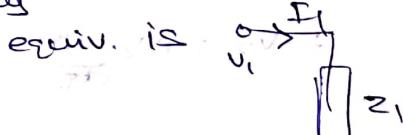
(like thevenin  
Norton...)

$$Z_2' = Z_2 \cdot \left( \frac{N_1}{N_2} \right)^2$$

this whole is one circuit.

Should be able to reduce it!

if say



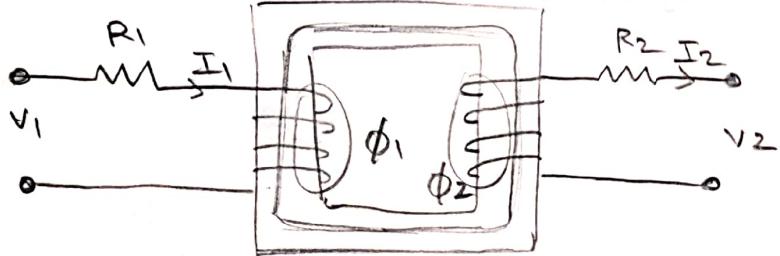
$$\begin{aligned} a &= \frac{V_2}{V_1} = \frac{I_2 \cdot Z_2}{I_1 \cdot Z_1} \\ &= \frac{N_1}{N_2} \cdot \frac{Z_2}{Z_1} \end{aligned}$$

$$a = \left( \frac{N_1}{N_2} \right)^2 \cdot \frac{Z_2}{Z_1} \quad \text{tadaaa!}$$

## → Practical transformers

$$K = \frac{M}{\sqrt{L_1 L_2}} \cdot \text{practical } K = 0.99$$

Flux leakage problem

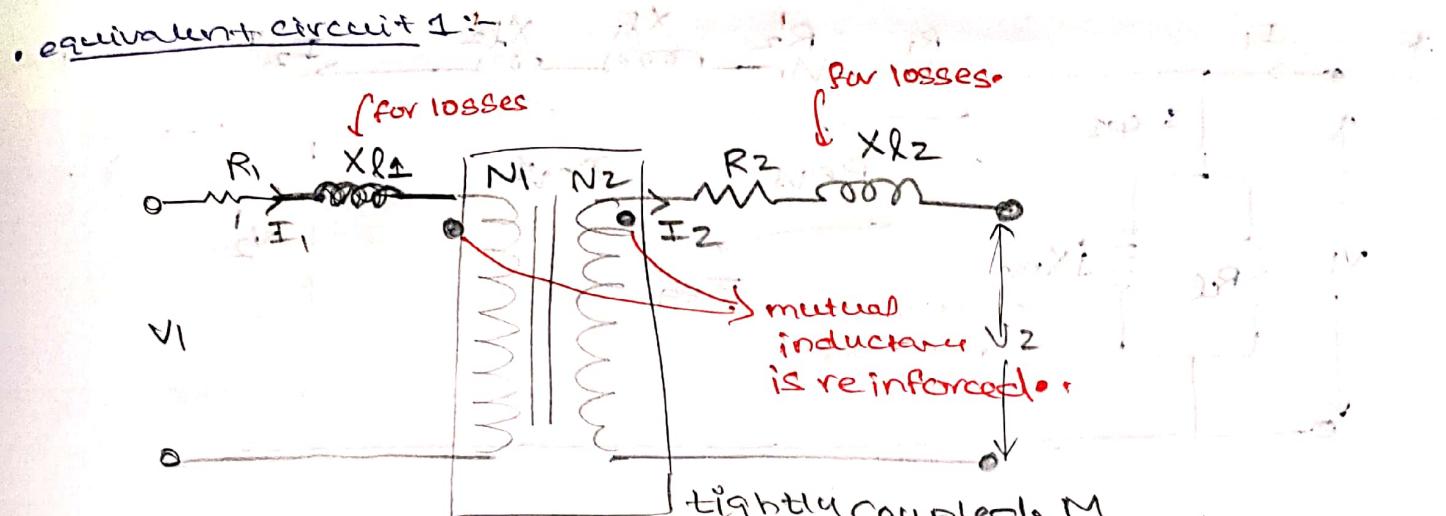


$$\frac{R_2}{R_1} = \text{motional reactance}$$

of primary w.r.t. secondary

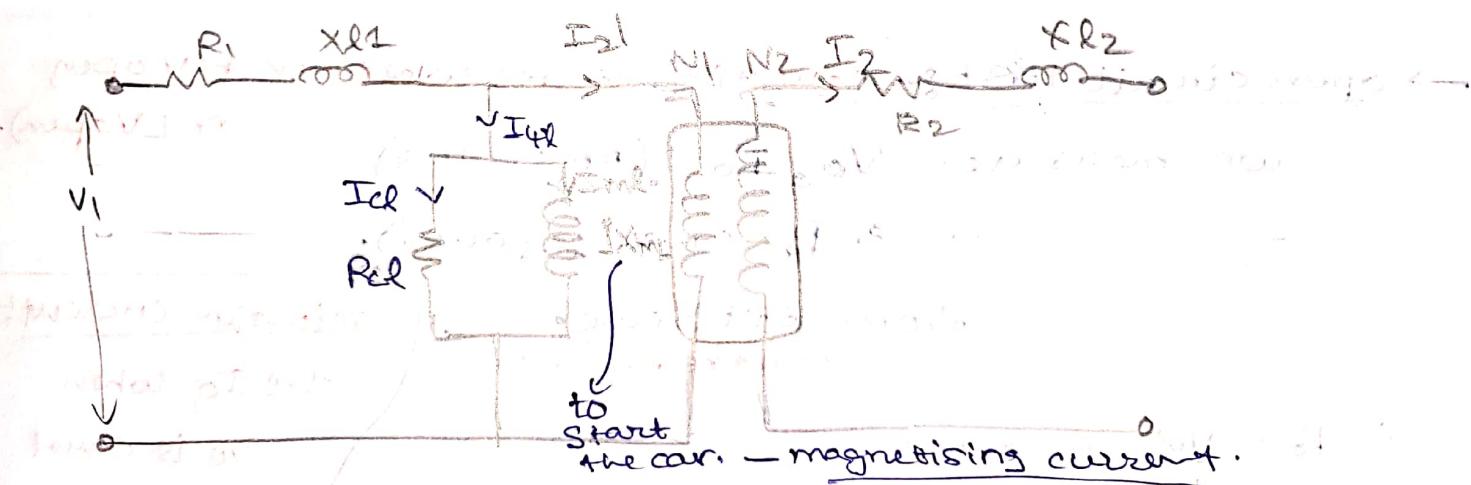
secondary w.r.t. primary

total reactance of both



$X_{L1}, X_{L2}$  leakage reactance.

### \* equ. circuit 2:-



$$* \underline{I_{cl}^2 R_{cl}} = P_{core} = P_h + P_e.$$

net core losses.

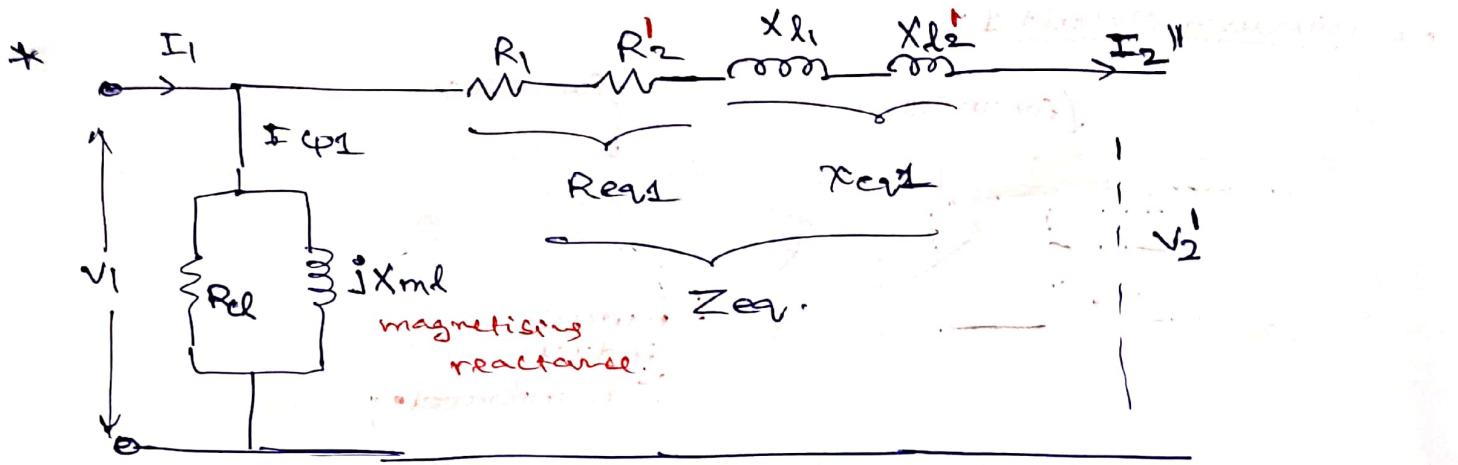
(mmf) re lye.

Since  $\delta \neq \infty$   
 $R \neq 0$

\* magnetising reactance is  $jX_{ml}$ .

$I_{ml}$  = magnetising current.

(PTO: equivalent circuit)



now; we need to find these parameters

~~• open circuit test of transformer~~

not!

~~• short circuit test~~

1) Open circuit test. to get  $R_{eq}$ ,  $X_{m1}$ .

2) Short circuit test.

→ open circuit test: (question states whether HV open, or LV open).  
we measure.  $V_o$ ,  $I_o$  (RMS value), &  $P_o$  (copper power).

from left side.  
could be HV or LV

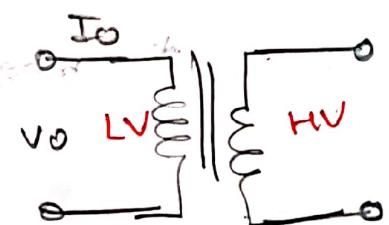
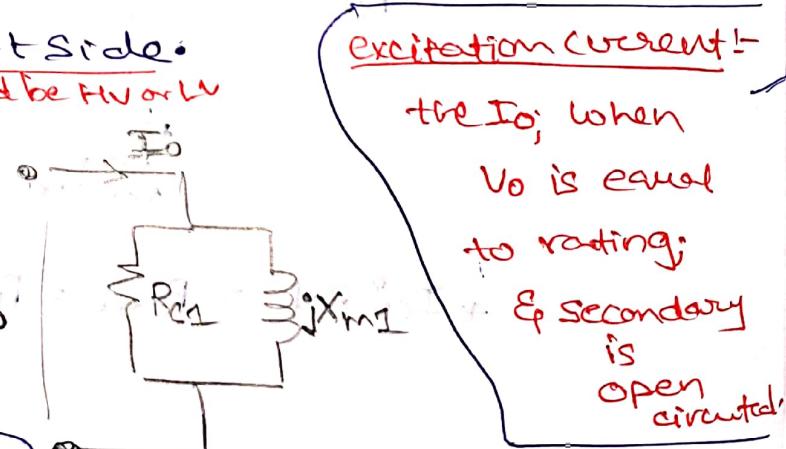
$$\therefore P_o = \frac{V_o^2}{R_{eq}} \quad o \rightarrow \text{open.}$$

$$R_{eq} = \frac{V_o^2}{P_o}$$

$$X_{m1} = \frac{V_o^2}{Q_o} = \frac{V_o^2}{(V_o I_o)^2 - P_o^2}$$

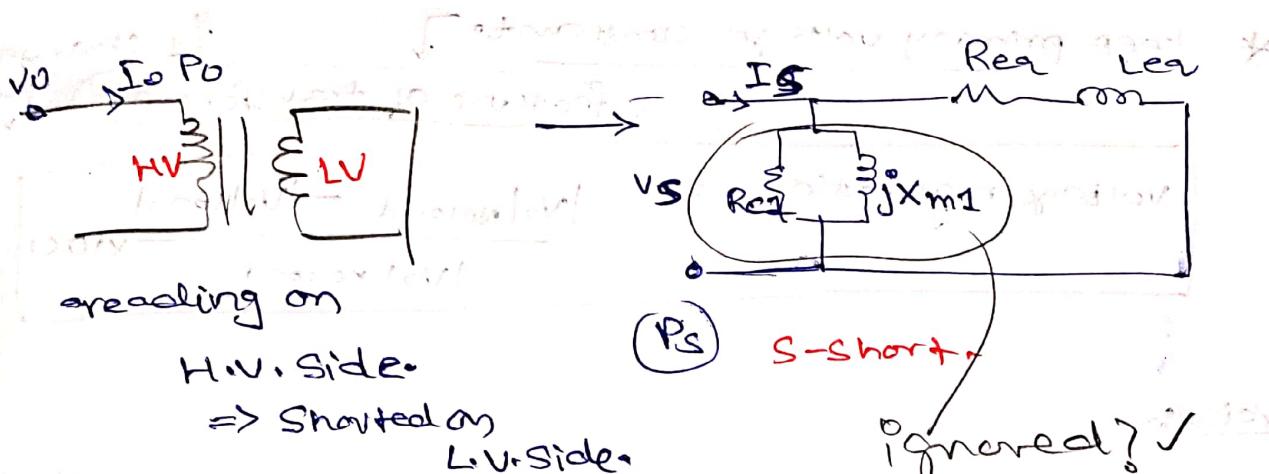
reactive power!

parameters of the transformer ✓✓



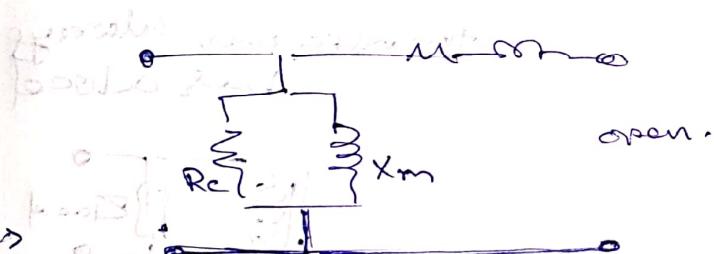
$I, V, P \rightarrow$  reading on  
secondary  
Low voltage  
side.

→ short circuit test:- (Question states, whether HV closed or LV closed)



$$R_{eq} = \frac{P_s}{I_s^2}$$

unadjusted test:  $Z_{eq} = \sqrt{Z_{eq}^2 - R_{eq}^2}$ ;  $Z_{eq} = \frac{V_s}{I_s}$



$$Z_{net} = \frac{R_{o1} + jX_{o1}}{R_{o2} + jX_{o2}}$$

$$i_o = \frac{V_{rated}}{Z_{net}}$$

$$i_{rated} = \frac{Prated}{V_{rated}}$$

$$\therefore \% = \frac{(V_{rated})^2}{Z_{net} \cdot Prated}$$

will come same; if we reduce the circuit

to HV referred;  
or  
LV referred.

HV, LV means;

HV      LV

1φ, 10KVA, 2200/220 V,  
Prated

unity  
power factor

GOH  
f.

$N_p = 1300$  secondary.

→ Voltage regulation of transformer: (at 20% load)

\* keep primary voltage constant  $\Rightarrow$  feature of transformer  $I_1$  changes as per needs.

$$\text{Voltage regulation} = \frac{|V_2|_{\text{No load}} - |V_2|_{\text{load}}}{|V_2|_{\text{No load}}} \times 100$$

### Exercise:

(a)  $P = 500 \text{ W}$  (load condition:  $P_p = P_s$ ) Under load condition.

$$10:1 \Rightarrow a = 10$$

$$V_p = 240 \text{ V(rms)}$$

calculate percentage regulation; when  $1:1$   $\Omega$  load impedance is present.

SOL)



ii)  $L \rightarrow \infty$  (open / no load).

$$\text{then } V_s = \frac{1}{a} V_p = 24 \text{ V.}$$

iii)

$$P_s = \frac{(V_s)^2}{Z}$$

$$\Rightarrow V_s = \sqrt{500 \times 1.0} = 22.36 \text{ V}$$

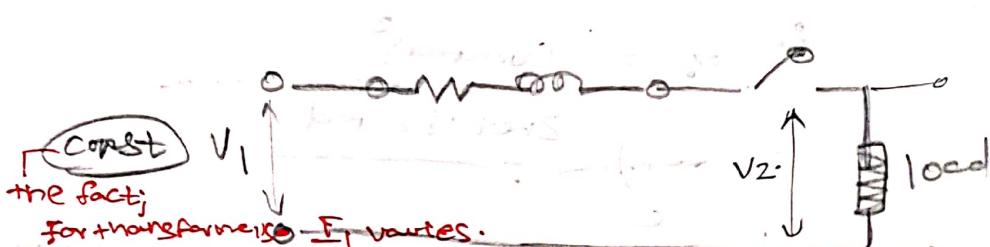
$$\therefore \% \text{ Reg} = 2.29\%$$

transformer always has a load



wow.... couldn't have done better? → No! can't do better:-

the power rating corresponds to the situation when transformer has load.



\* if  $V_s$  rated is given;  $E_p$ ,  $a$  given;

We find  $V_{\text{rated}}$  using  $E$  then we get this! the  $V_{\text{load}} = \frac{V_{\text{rated}}}{a}$

## → Efficiency of transformer:

Ideally; Power<sub>primary</sub> = Power<sub>secondary</sub>.

but;

$$\eta_{\text{efficiency}} = \frac{\text{P}_{\text{secondary}}}{\text{P}_{\text{primary}}} \times 100\%$$

No moving parts in transformer.

but

just written.

only copper losses & iron losses.

winding losses  
( $I^2R$ )

core loss  
 $(I^2R) + 8.745 \cdot 3$

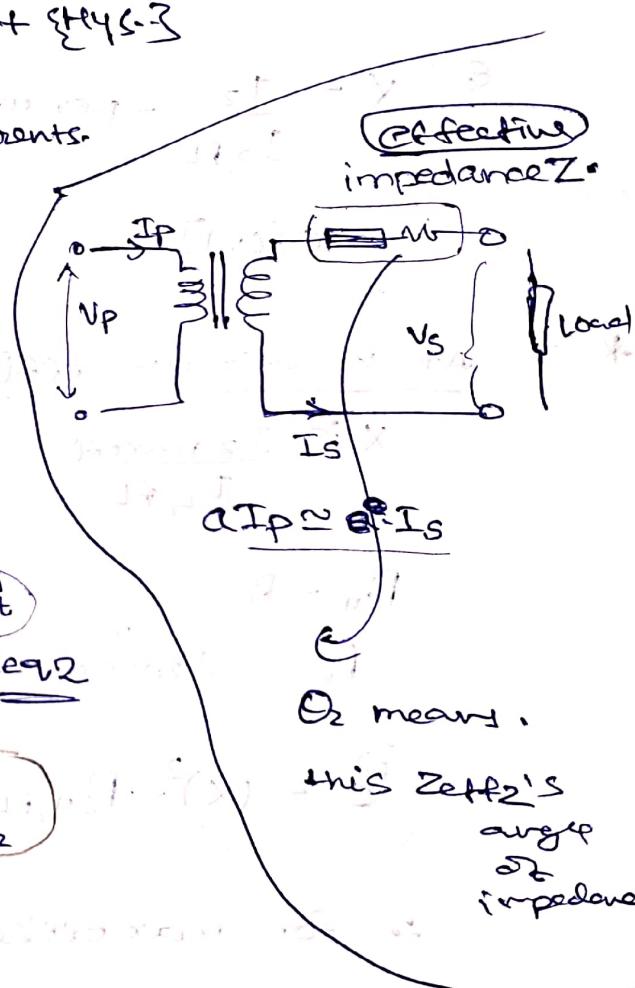
eddy currents.

effective impedance  $Z_e$

$$* \eta = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{P_{\text{out}}}{P_{\text{out}} + P_{\text{core}} + P_{\text{cu}}}$$

$$P_{\text{out}} = V_2 I_2 \cos \theta_2$$

$$P_{\text{cu}} = I_1^2 \cdot R_{\text{net}} \approx I_2^2 \cdot R_{\text{net}}$$



$$\frac{d\eta}{dI_2} = 0$$

maximum efficiency!

$$\text{Power loss} = \text{P}_{\text{Cu}} \text{ loss}$$

$$\Rightarrow I_2^2 R_{\text{req2}} = P_{\text{Cu}}$$

↳ independent of  $I_1, I_2$ .  
depends on material.

(Bcoz; even though

H depends on  $I_1, I_2$

$B_{\text{max}}$  doesn't)

\* Full load:-

$$P_{cu, FL} = I_{2, FL}^2 \cdot R_{eq2}$$

full load  $\rightarrow$  current rating!

at some other load; less than full load:-

$$P_{cu} = I_2^2 R_{eq2}$$

$$\frac{P_{cu}}{P_{cu, FL}} = \left( \frac{I_2}{I_{2, FL}} \right)^2$$

$$= X^2$$

$$X = \frac{I_2}{I_{2, FL}} = \text{per unit loading}$$

\* At maximum efficiency: (which need not be full load)

$$X \text{ is } I_{2, maxeff}$$

$$I_{2, FL}$$

$$P_{cu} = P_c$$

$$P_c = I_{2, maxeff}^2 \cdot R_{eq2}$$

$$P_c = (X)^2 \cdot P_{cu, FL}$$

$\therefore$  for max efficiency;

$$X = \left( \frac{P_c}{P_{cu, FL}} \right)^{1/2}$$

Eg: max. eff = 98% at  $\frac{3}{4}$  th of weighted full load.

$$\cos\phi_2 = 1.$$

meaning;  $I_2 \text{ now} = \frac{3}{4} I_2 \text{ rated.}$

$$P_{\text{core}} = 314 \text{ Watts.}$$

compute

VA. (primary output).

Efficiency; at 50% & 100% load.

$$P_{\text{secondary now}} = \frac{3}{4} (P_{\text{max}})$$

NO  $\frac{3}{4}$  or  $\frac{3}{5}$  of Rated. ...

Sol) Let rated power = S.

$$\text{E now; } P_{\text{sec.}} = \frac{3}{4} S.$$

$$\text{E now; } P_{\text{loss}} = P_{\text{core}} = 314 \text{ Watts.}$$

$$\frac{98}{100} = \frac{3}{4} S \quad ] \text{Psecondary}$$

$$\frac{3}{4} S + 2(314) \quad ] \text{Primary = losses + Psecondary.}$$

$$\Rightarrow S = 41029.3 \text{ VA.}$$

Sol. load:-

$$P_{\text{sec.}} = 20,514.6 \text{ W.}$$

$$P_{\text{core}} = 314 \text{ W (same)}$$

$$P_{\text{cu}} = ? \propto I_2^2 \cdot R_{\text{eq.}}$$

$$P_{\text{cu}, 50\%} = \left(\frac{0.5S}{0.75}\right)^2 \cdot P_{\text{cu}} 75\%.$$

$$\therefore P_{\text{cu}, 50\%} = 139.6 \text{ W.}$$

$$\therefore \text{eff.} = \frac{20514}{20514 + 314 + 139.6} \approx 97.83\%.$$

100% load:-

$$P_{\text{secondary}} = 41029 \text{ W.}$$

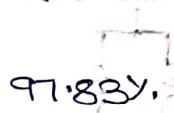
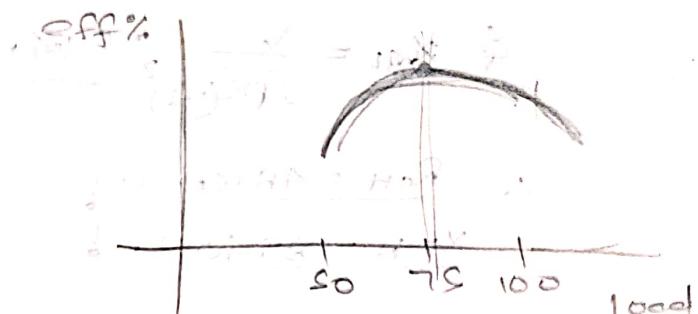
$$P_{\text{cu}} = \left(\frac{1}{0.5}\right)^2 \cdot 139.6 \text{ W.}$$

$$P_c = 314 \text{ W.}$$

$$\therefore \approx 99\%$$

Assumption:

Output voltage of transformer is constant;  $E_i = \text{rated value.}$  irrespective of what fraction load.



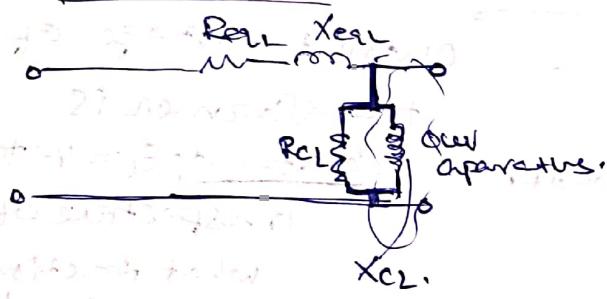
### Assignment Q6:

Tests on a 1φ, 10kVA, 2200/220V, 60Hz transformer & the following results came:-

	open (on H.v.)	closed (on L.v.)
Voltage	220V	150V
current	2.5A	4.55A
power	100W	215W

a) Find circuit parameters :-

sol) open-circuit test:-



$\therefore$  no load;

$$\text{Power} = \frac{V^2}{R_{CL}}$$

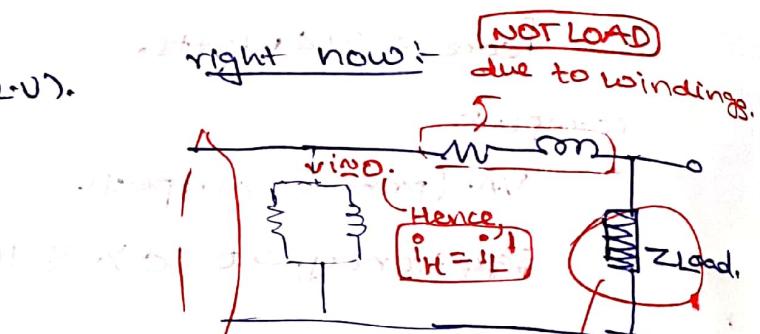
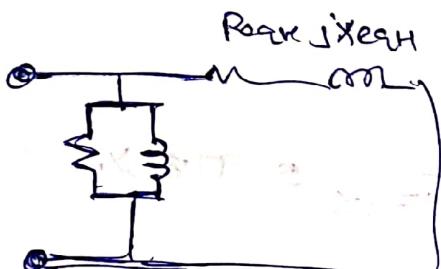
$$\therefore R_{CL} = 484.5\Omega$$

$$\& X_{CL} = \frac{V}{\sqrt{P^2/(VI)}} = 89.4\Omega$$

$$\therefore R_H = 48400\Omega$$

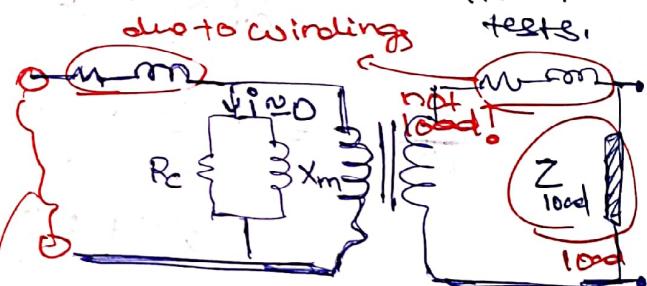
$$X_{MH} = 8940\Omega$$

Closed circuit:- (on Low)



1φ Power factor--

We remove this for open circuit, closed circuit tests.



P.f. of transistor means:

Power

Vin - I\_{in}

Magnitude

$$i_L^1 = \frac{i_L}{a} \approx i_H$$

Current I = 2.5A

$$R_{eq} = \frac{P}{I^2} = 10.4\Omega$$

$$Z_H = \frac{V}{I} = 32.97\Omega$$

$$X_{eq} = 31.3\Omega$$

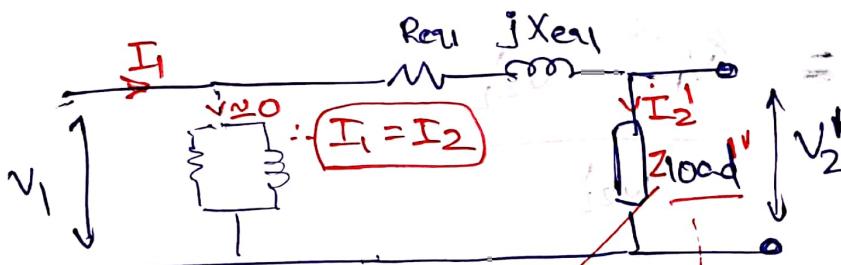
(b) determine voltage regulation for the load conditions:

i) 75% full load & 0.6 p.f. lag.

Both  $I_2$ ,  $P_{\text{out}}$  is 75% of rated values.

ii) 75% full load & 0.6 p.f. lead.

soln



∴ angle of load impedance  $\theta_2$  is this guy's P.f.

P.f. won't change

$$\cos \theta_2 = 0.6.$$

$$\text{like } R_{\text{eq}} = a^2 \cdot R_{\text{eq}}$$

$$\theta_2 = -53^\circ$$

$$Pf_1 = Pf_2 \checkmark$$

i) lag:  $\Rightarrow I_2' = \frac{V_2'}{|Z_{\text{load}}|} \angle -53^\circ$

instead of this;

do  $I_2' = \frac{3}{4} I_2'_{\text{rated}}$

gave this; instead of  $|Z_{\text{load}}|$ .

$$= 0.75 \times \frac{10^4}{2200}$$

$$= 0.75 \times 4.55$$

$$= 3.41 \text{ A.}$$

$$\therefore I_2' = (3.41) \angle -53^\circ = I_1$$

Now;

$$V_1 = V_2 + I_1 \cdot R_{\text{eq}} + I_1 \cdot jX_{\text{eq}}$$

phasediff. =  $-53^\circ$

$$= 2200 \angle 0^\circ + (3.41) \angle -53^\circ + (3.41)(31.3) \angle 90^\circ \times 10.4$$

$$= 2307.20.9^\circ \text{ V}$$

$$\therefore \text{Voltage reg.} = \frac{(V_2)_{NL} - (V_2)_L}{(V_2)_L}$$

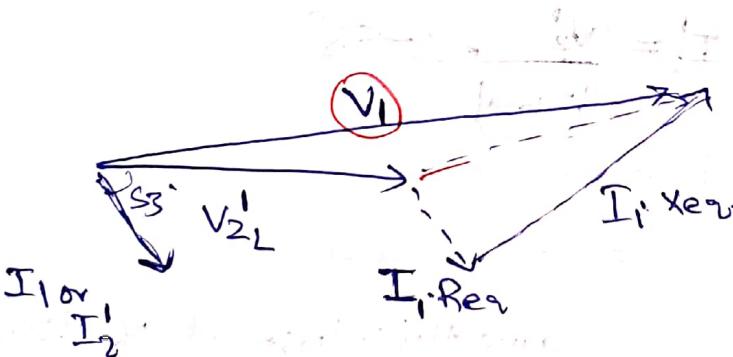
$$= \frac{V_2'_{NL} - V_2'_{L}}{U_2'_{L}} \quad (\because \text{only } \alpha^2 \text{ factor})$$

$$= \frac{V_1 - V_2'_{L}}{U_2'_{L}}$$

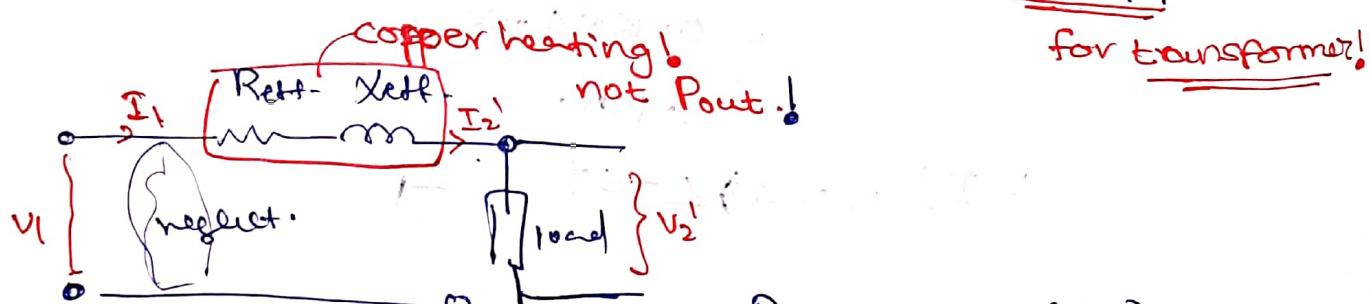
$$= \frac{2307 - 2200}{2200} \times 100 = 4.86\%$$

Phasor:

phew!



c) efficiency at 75% rated output  $\approx 0.6 \text{ PF}$



$$\begin{aligned} P_{out} &= I_1 V_1 \cdot (\text{P.f.}) \\ &= I_2 V_2 \cdot (\text{P.f.}) \end{aligned}$$

this is  
Pout.

$$P_{out} = V_2 \cdot I_2 \cdot (\text{pf})$$

$$= \frac{V_2}{\text{rated}} (I_2' \times 75\%) (0.6)$$

$$= 2200 \times \frac{10^4}{2200} \times \frac{3}{4} \times 0.6,$$

$$= 4500 \text{ W}$$

$$P_c = 100 \text{ W} \text{ given}$$

$P_{\text{copper loss}}$

$$= (I_2')^2 \cdot R_{\text{cu}}$$

$$= (0.75 \times 4.55)^2 \cdot (10^{-4})$$

$$= 121 \text{ W}$$

$$\therefore \eta = \frac{4500}{4500 + 121} = 95.32\%$$

d) max efficiency!

means;

$$P_{\text{copper}} = P_{\text{cu}} = 100 \text{ W}$$

$$\text{P.f.} = ? \text{ let's wait}$$

$$(I_2')^2 \cdot (10 \cdot 4) = 100$$

$$I_2' = 3.1 \text{ A}$$

$$I_2 = 3 \text{ A}$$

$$V_2 = 220 \text{ V}$$

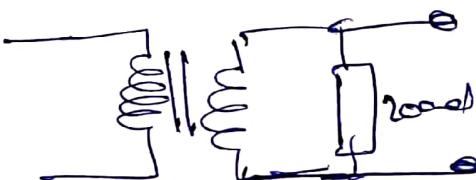
$$\therefore \eta = \frac{(220) \cdot (3) \cos \theta_2}{6820 \cos \theta_2 + 200}$$

$\therefore \cos \theta_2 = 1$  for max... ✓

$$\eta_{\text{max}} = 97.15\%$$

Transformer:-

order:



$$1) V_1$$

$$2) V_2 = \alpha V_1$$

$$3) I_2 = \frac{V_2}{Z_{\text{load}}}$$

$$4) I_1 = \frac{I_2}{\alpha}$$

Sequence  
of  
hoco  
physical  
quantities  
attain  
Harmony.

\* our sources

fixes  $V_1$ .

But can't fix  $I_1$ . Hence,  
voltage trans.  
forms.

$$P_{\text{out}} = P_{\text{in}} - 200$$

$$1 - P_{\text{VA}} = \frac{7020}{7020}$$

$$\Rightarrow \% \text{ load} = \frac{30}{4.55} = 68.2\%$$