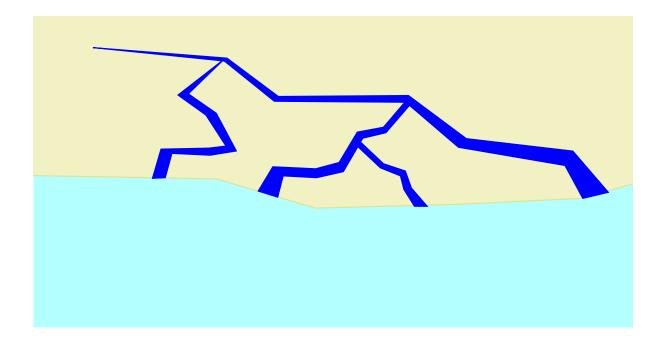
# TREES CREATE BY - ATUL KUMAR (LINKEDIN)

- trees
- binary trees
- traversals of trees
- template method pattern
- data structures for trees

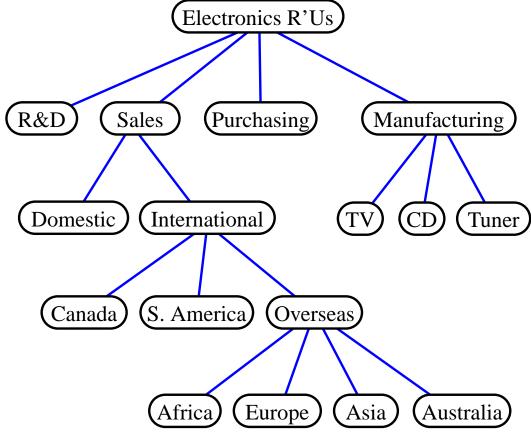


**INSTAGRAM - @atulkumarx** 

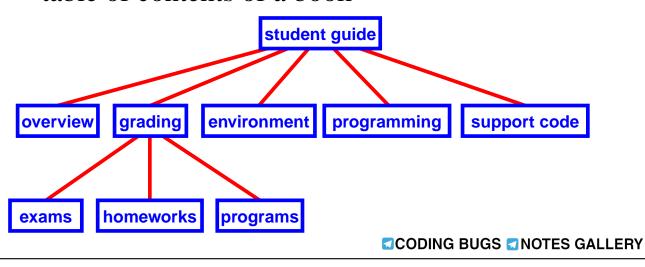
**SCODING BUGS SONOTES GALLERY** 

#### **Trees**

- a tree represents a hierarchy
  - organization structure of a corporation

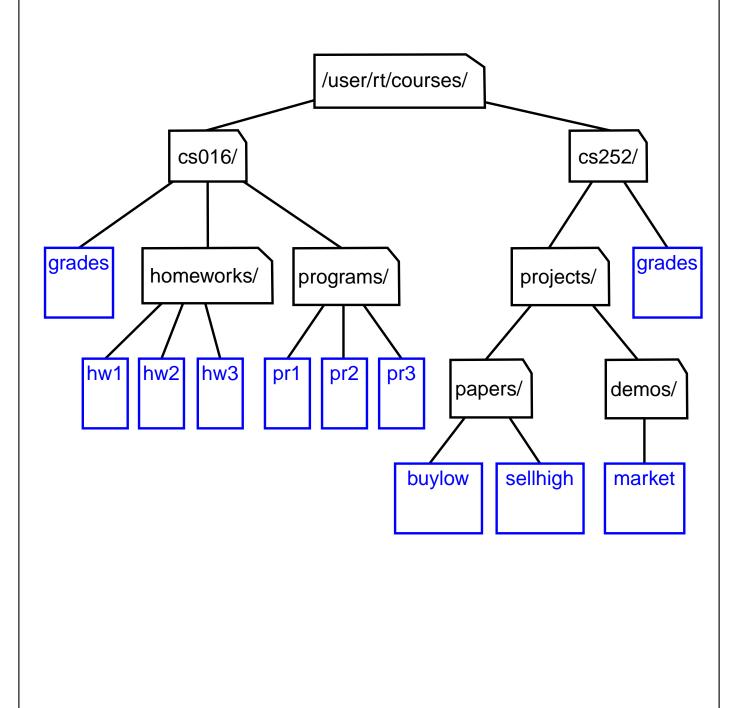


- table of contents of a book



## **Another Example**

• Unix or DOS/Windows file system



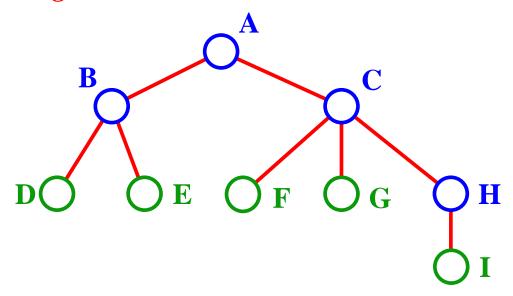
Trees 3

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## **Terminology**

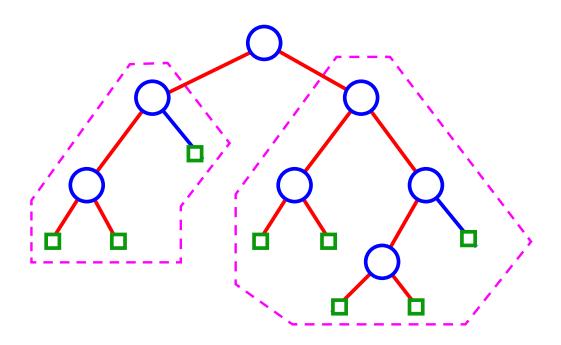
- A is the **root** node.
- **B** is the **parent** of D and E.
- C is the sibling of B
- **D** and **E** are the **children** of B.
- D, E, F, G, I are external nodes, or leaves.
- A, B, C, H are internal nodes.
- The depth (level) of E is 2
- The *height* of the tree is 3.
- The *degree* of node B is 2.



**Property:** (# edges) = (# nodes) - 1

### **Binary Trees**

- Ordered tree: the children of each node are ordered.
- *Binary tree*: ordered tree with all internal nodes of *degree* 2.
- Recursive definition of binary tree:
- A *binary tree* is either
  - an external node (leaf), or
  - an internal node (the *root*) and two binary trees (*left subtree* and *right subtree*)

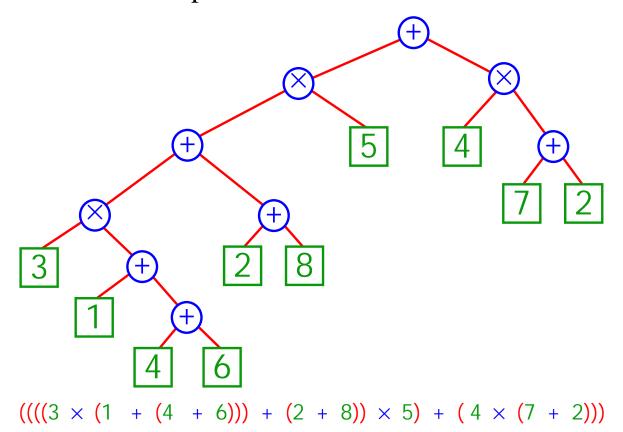


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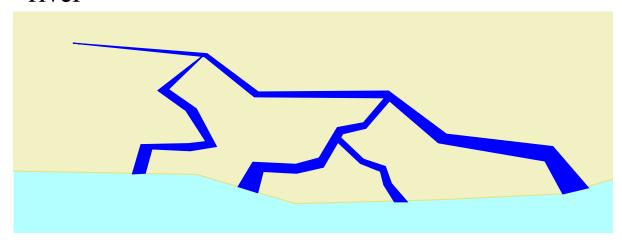
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## **Examples of Binary Trees**

• arithmetic expression



• river



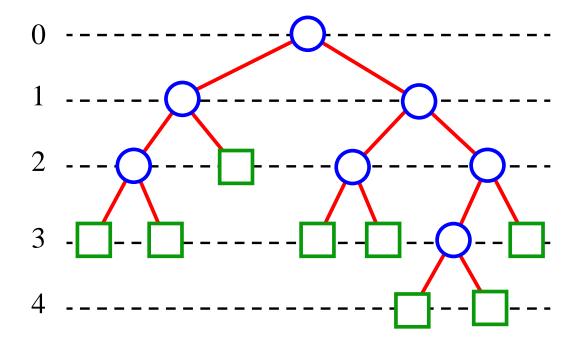
Trees 6

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### **Properties of Binary Trees**

- (# external nodes) = (# internal nodes) + 1
- (# nodes at level i)  $\leq 2^{i}$
- (# external nodes)  $\leq 2^{\text{(height)}}$
- (height)  $\geq \log_2$  (# external nodes)
- (height)  $\geq \log_2 (\# \text{ nodes}) 1$
- (height)  $\leq$  (# internal nodes) = ((# nodes) 1)/2

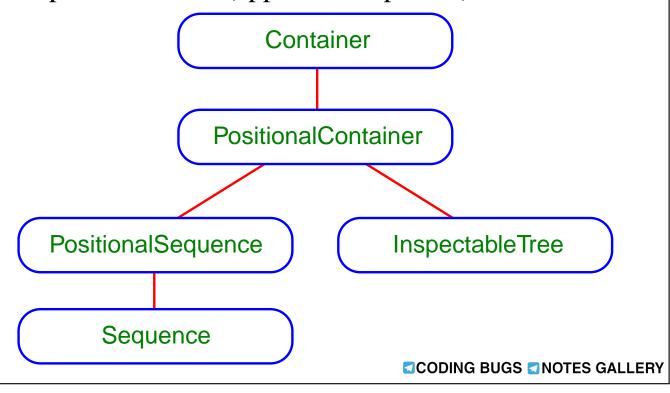
#### Level



CODING BUGS NOTES GALLERY

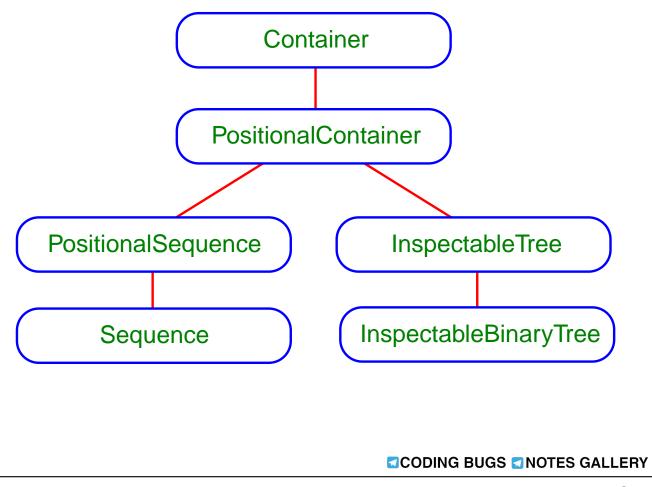
#### The Tree ADT

- the nodes of a tree are viewed as positions
- generic container methods
  - size(), isEmpty(), elements(), newContainer()
- positional container methods
  - positions(), replace(p,e), swap(p,q)
- query methods
  - isRoot(p), isInternal(p), isExternal(p)
- accessor methods
  - root(), parent(p), children(p), siblings(p)
- update methods (application specific)



### The Binary Tree ADT

- extends the tree ADT
- accessor methods
  - leftChild(p), rightChild(p), sibling(p)
- update methods
  - expandExternal(p), removeAboveExternal(p)
  - other application specific methods
- interface hierarchy of positional containers



## **Traversing Trees**

• preorder traversal

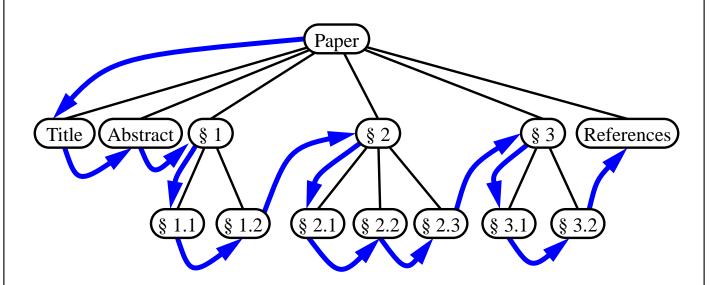
Algorithm preOrder(v)

"visit" node v

for each child w of v do

recursively perform preOrder(w)

• reading a document from beginning to end



#### **Traversing Trees**

• postorder traversal

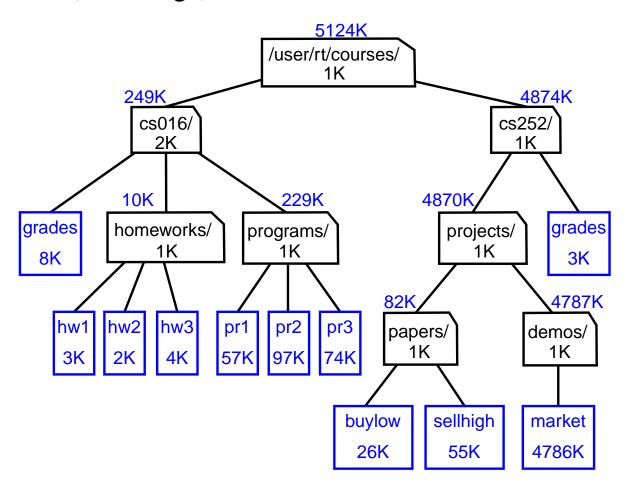
```
Algorithm postOrder(v)

for each child w of v do

recursively perform postOrder(w)

"visit" node v
```

• du (disk usage) command in Unix



# **Evaluating Arithmetic Expressions**

• specialization of a postorder traversal

```
Algorithm evaluateExpression(v)
  if v is an external node
  return the variable stored at v
```

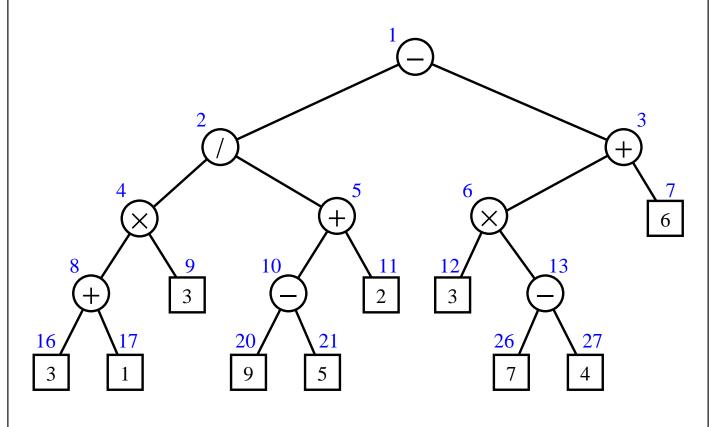
else

let o be the operator stored at v

 $x \leftarrow evaluateExpression(leftChild(v))$ 

 $y \leftarrow evaluateExpression(rightChild(v))$ 

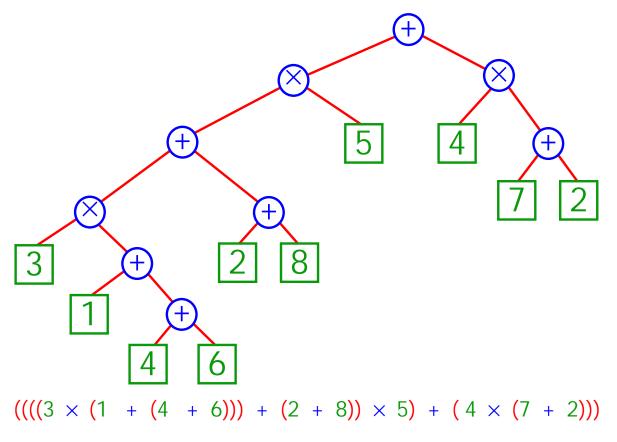
return x o y



#### **Traversing Trees**

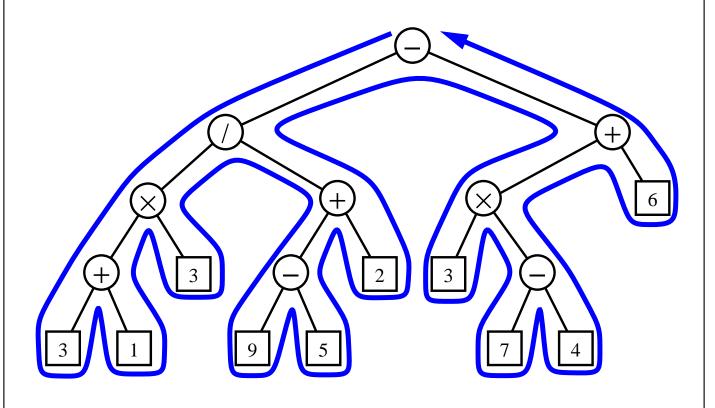
inorder traversal of a binary tree
 Algorithm inOrder(v)
 recursively perform inOrder(leftChild(v))
 "visit" node v
 recursively perform inOrder(rightChild(v))

- printing an arithmetic expression
  - specialization of an inorder traversal
  - print "(" before traversing the left subtree
  - print ")" after traversing the right subtree



#### **Euler Tour Traversal**

- generic traversal of a binary tree
- the preorder, inorder, and postorder traversals are special cases of the Euler tour traversal
- "walk around" the tree and visit each node three times:
  - on the left
  - from below
  - on the right



#### Template Method Pattern

- generic computation mechanism that can be specialized by redefining certain steps
- implemented by means of an abstract Java class with methods that can be redefined by it subclasses

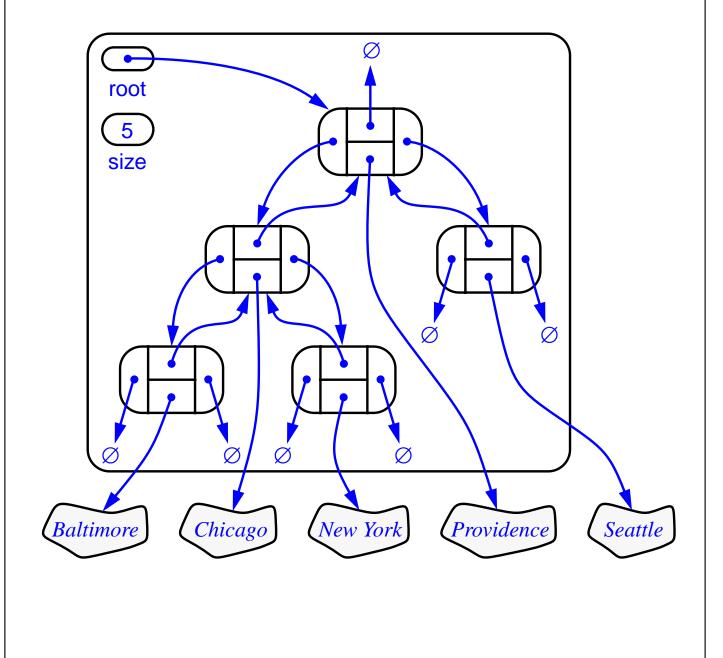
```
public abstract class BinaryTreeTraversal {
protected BinaryTree tree;
protected Object traverseNode(Position p) {
  TraversalResult r = initResult();
  if (tree.isExternal(p)) {
    external(p, r);
  } else {
    left(p, r);
    r.leftResult = traverseNode(tree.leftChild(p));
    below(p, r);
    r.rightResult = traverseNode(tree.rightChild(p));
    right(p, r);
  return result(r);
```

#### Specializing the Generic Binary Tree Traversal

• printing an arithmetic expression

```
public class PrintExpressionTraversal
   extends BinaryTreeTraversal {
 protected void external(Position p, TraversalResult r) {
  System.out.print(p.element());
 protected void left(Position p, TraversalResult r) {
  System.out.print("(");
 protected void below(Position p, TraversalResult r) {
  System.out.print(p.element());
 protected void right(Position p, TraversalResult r) {
  System.out.print(")");
```

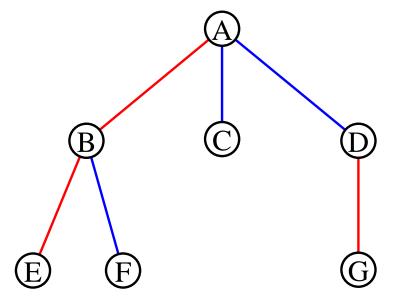
# Linked Data Structure for Binary Trees



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## **Representing General Trees**

• tree T



• binary tree T' representing T

