

## **CS 669: Pattern Recognition**

## Assignment 1 – Bayes Classifier Odd Semester 2017

# Submitted by – Group 2 Deepesh Goel, B15312 Aayush Mishra, B15101

Akash Agrawal, B15303

## <u>Dataset 1 (2 Dimensional artificial data of 3 classes)</u>

#### a) Linearly Separable dataset

#### Mean Vector for each case -

```
• Class 1 - [19.783 -5.867]^T
```

- Class 2 [8.932 9.968]<sup>T</sup>
- Class 3 [-2.887 -4.941]<sup>T</sup>

#### Case 1: $\Sigma = \sigma^2 I$ (same for all classes)

Classification Accuracy (Class 1) – 1.0

Classification Accuracy (Class 2) – 1.0

Classification Accuracy (Class 3) – 1.0

Mean Classification Accuracy - 1.0

Precision (Class 1) -1.0

Precision (Class 2) -1.0

Precision (Class 3) – 1.0

Mean Precision -1.0

Recall (Class 1) -1.0

Recall (Class 2) – 1.0

Recall (Class 3) – 1.0

Mean Recall – 1.0

F-Measure (Class 1) -1.0

F-Measure (Class 2) -1.0

F-Measure (Class 3) – 1.0

Mean F-Measure – 1.0

#### **Mean Covariance Matrix -**

5.640	0
0	5.640

#### **Confusion Matrices -**

#### • Class 1, 2 and 3 (same for all the classes in this case)

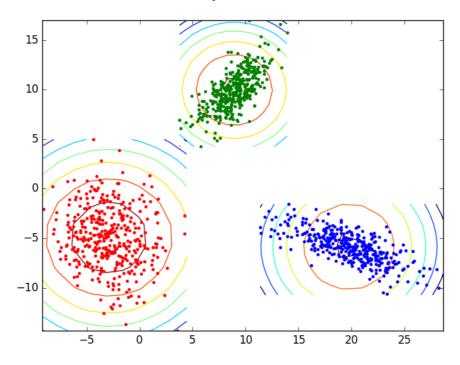
125	0
0	250

## • All classes together

125	0	0
0	125	0
0	0	125

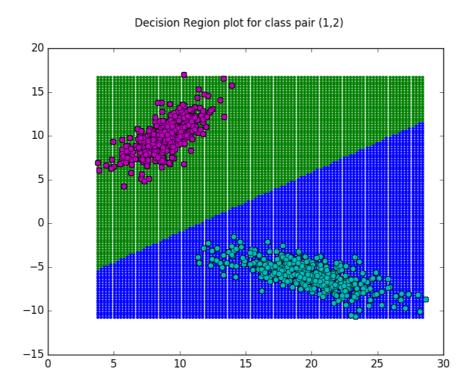
## Constant density contour plot for all the classes -

#### Constant Density Contours for all classes

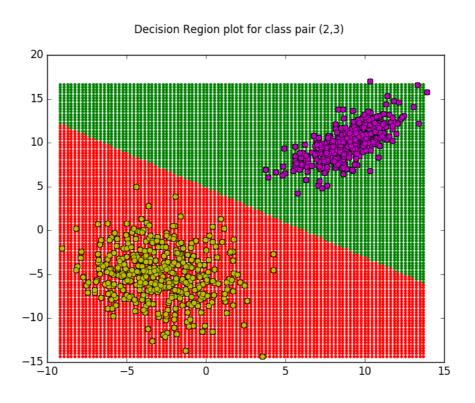


## Pairwise Decision region plots -

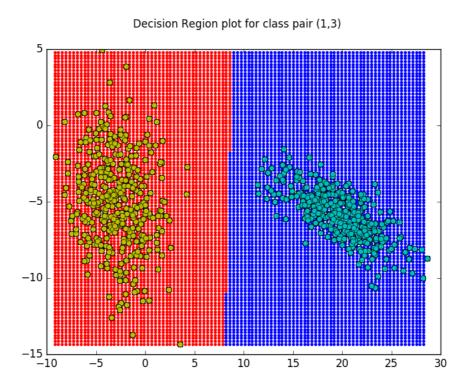
## • <u>Class 1 and 2</u>



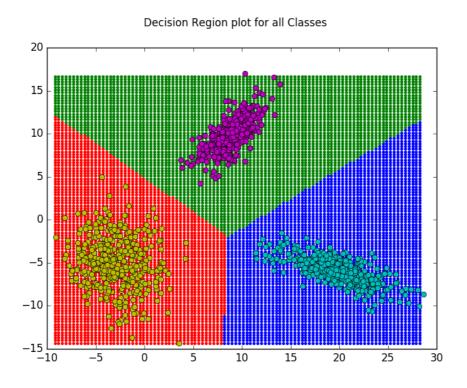
## • <u>Class 2 and 3</u>



## • <u>Class 1 and 3</u>



## <u>Decision region plot for all the classes -</u>



#### Case 2: Full covariace matrix( $\Sigma$ ) is same for all the classes

Classification Accuracy (Class 1) – 1.0

Classification Accuracy (Class 2) -1.0

Classification Accuracy (Class 3) – 1.0

Mean Classification Accuracy -1.0

Precision (Class 1) -1.0

Precision (Class 2) -1.0

Precision (Class 3) – 1.0

Mean Precision -1.0

Recall (Class 1) -1.0

Recall (Class 2) -1.0

Recall (Class 3) – 1.0

Mean Recall -1.0

F-Measure (Class 1) -1.0

F-Measure (Class 2) -1.0

F-Measure (Class 3) – 1.0

Mean F-Measure -1.0

#### **Mean Covariance Matrix -**

6.179	-0.784
-0.784	5.102

#### **Confusion Matrices -**

#### • Class 1, 2 and 3 (same for all the classes in this case)

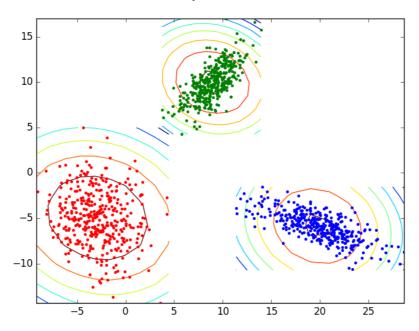
125	0
0	250

#### • All classes together

125	0	0
0	125	0
0	0	125

#### Constant density contour plot for all the classes -

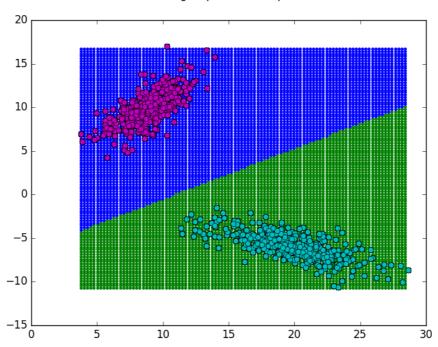
Constant Density Contours for all classes



#### Pairwise Decision region plots -

#### • <u>Class 1 and 2</u>

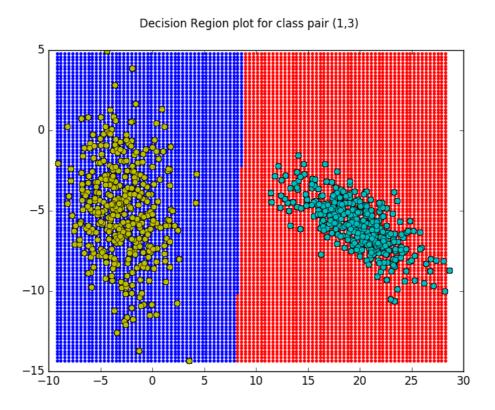
Decision Region plot for class pair (1,2)



## • <u>Class 2 and 3</u>

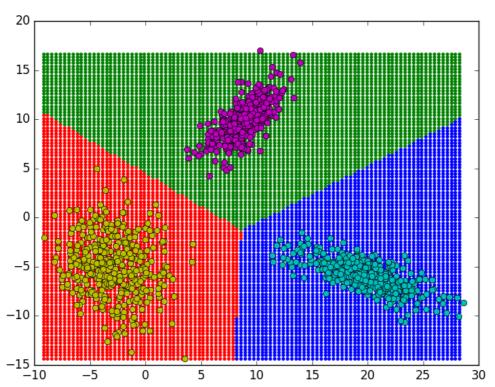


## • <u>Class 1 and 3</u>



## <u>Decision region plot for all the classes -</u>





#### Case 3: Diagonal Covariance matrix (different for all classes)

Classification Accuracy (Class 1) – 1.0

Classification Accuracy (Class 2) – 1.0

Classification Accuracy (Class 3) – 1.0

Mean Classification Accuracy -1.0

Precision (Class 1) -1.0

Precision (Class 2) -1.0

Precision (Class 3) – 1.0

Mean Precision -1.0

Recall (Class 1) -1.0

Recall (Class 2) – 1.0

Recall (Class 3) – 1.0

Mean Recall – 1.0

F-Measure (Class 1) -1.0

F-Measure (Class 2) -1.0

F-Measure (Class 3) – 1.0

Mean F-Measure -1.0

#### **Covariance Matrix for each class -**

#### • Class 1

9.898	0
0	2.409

#### • <u>Class 2</u>

2.800	0
0	3.818

#### • <u>Class 3</u>

5.838	0
0	9.078

#### **Confusion Matrices -**

#### • Class 1, 2 and 3 (same for all the classes in this case)

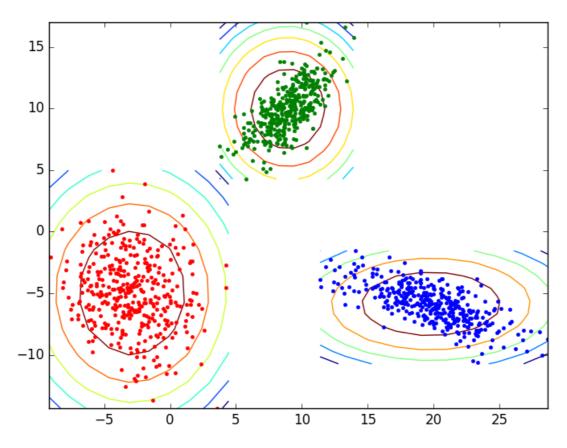
125	0
0	250

#### • All classes together

125	0	0
0	125	0
0	0	125

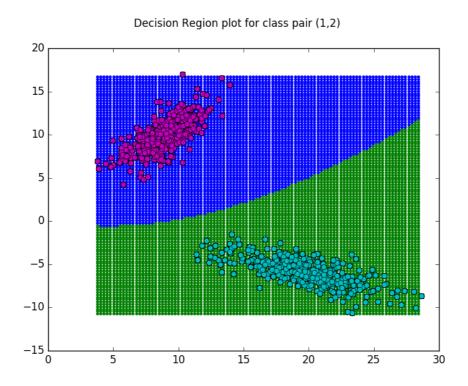
#### **Constant density contour plot for all the classes -**

#### Constant Density Contours for all classes

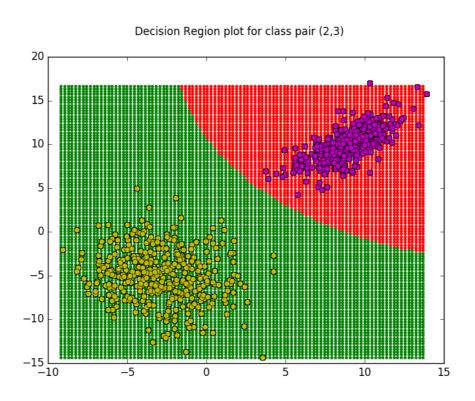


## Pairwise Decision region plots -

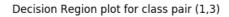
## • <u>Class 1 and 2</u>

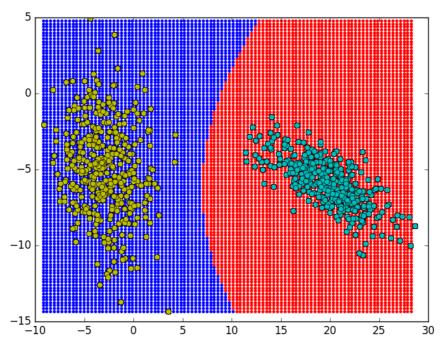


#### • <u>Class 2 and 3</u>



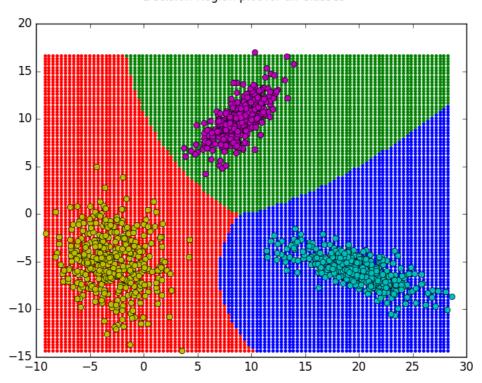
## • <u>Class 1 and 3</u>





## <u>Decision region plot for all the classes -</u>

#### Decision Region plot for all Classes



#### Case 4: Different full covariance matrix for each class

Classification Accuracy (Class 1) – 1.0

Classification Accuracy (Class 2) -1.0

Classification Accuracy (Class 3) – 1.0

Mean Classification Accuracy – 1.0

Precision (Class 1) -1.0

Precision (Class 2) -1.0

Precision (Class 3) – 1.0

Mean Precision -1.0

Recall (Class 1) -1.0

Recall (Class 2) – 1.0

Recall (Class 3) – 1.0

Mean Recall – 1.0

F-Measure (Class 1) -1.0

F-Measure (Class 2) -1.0

F-Measure (Class 3) – 1.0

Mean F-Measure -1.0

#### **Covariance Matrix for each class -**

#### • <u>Class 1</u>

9.898	-3.443
-3.443	2.409

#### • <u>Class 2</u>

2.800	2.234
2.234	3.818

#### • <u>Class 3</u>

5.838	-1.143
-1.143	9.078

#### **Confusion Matrices -**

#### • Class 1, 2 and 3 (same for all the classes in this case)

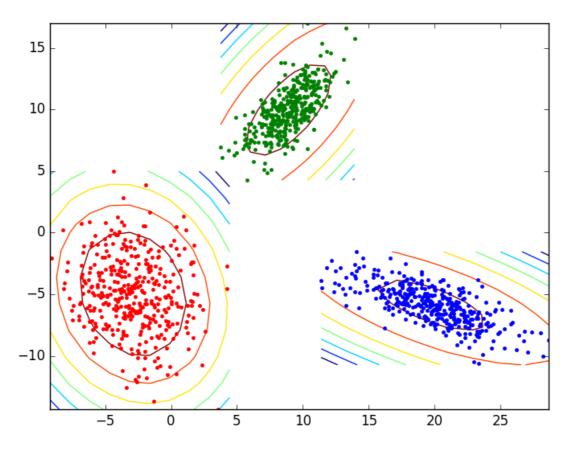
125	0
0	250

#### • All classes together

125	0	0
0	125	0
0	0	125

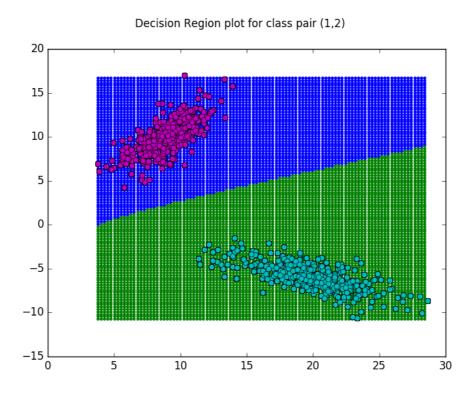
#### **Constant density contour plot for all the classes -**

#### Constant Density Contours for all classes

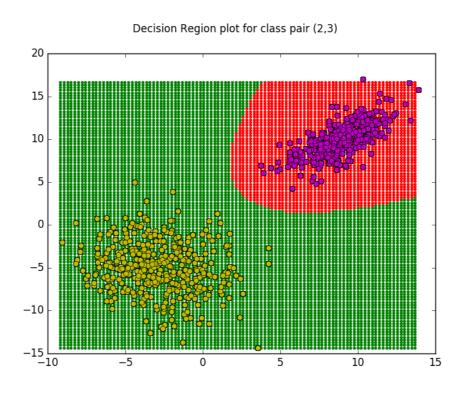


## Pairwise Decision region plots -

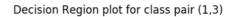
#### • <u>Class 1 and 2</u>

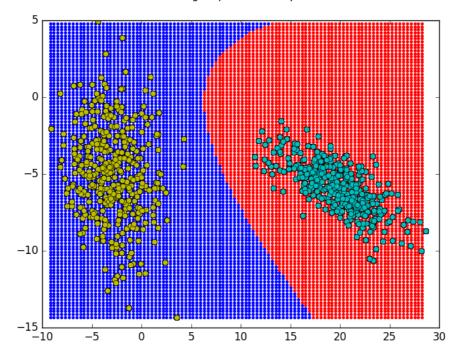


#### • <u>Class 2 and 3</u>



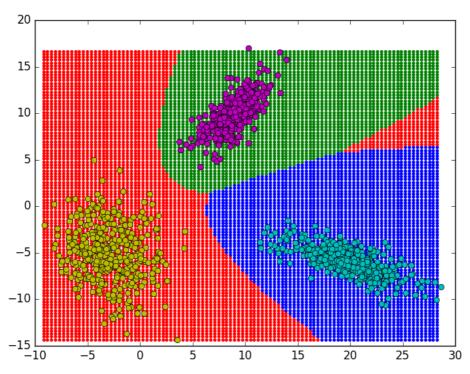
## • <u>Class 1 and 3</u>





## <u>Decision region plot for all the classes -</u>

#### Decision Region plot for all Classes



#### b) Non-Linearly Separable dataset

#### Mean Vector for each case -

• Class 1 -  $[1.551 0.712]^T$ 

• Class 2 -  $[-0.448 -0.848]^T$ 

• Class 3 -  $[3.052 -0.848]^T$ 

## Case 1: $\Sigma = \sigma^2 I$ (same for all classes)

Classification Accuracy (Class 1) -0.797

Classification Accuracy (Class 2) – 0.920

Classification Accuracy (Class 3) – 0.877

Mean Classification Accuracy – 0.865

Precision (Class 1) -0.713

Precision (Class 2) -0.868

Precision (Class 3) -0.802

Mean Precision -0.794

Recall (Class 1) -0.656

Recall (Class 2) – 0.896

Recall (Class 3) – 0.840

Mean Recall – 0.797

F-Measure (Class 1) -0.683

F-Measure (Class 2) -0.882

F-Measure (Class 3) – 0.820

Mean F-Measure – 0.795

#### **Covariance Matrix for each class -**

#### • For All Classes

0.648	0
0	0.648

## **Confusion Matrices -**

#### • <u>Class 1</u>

82	33
43	217

## • <u>Class 2</u>

112	17
13	233

#### • <u>Class 3</u>

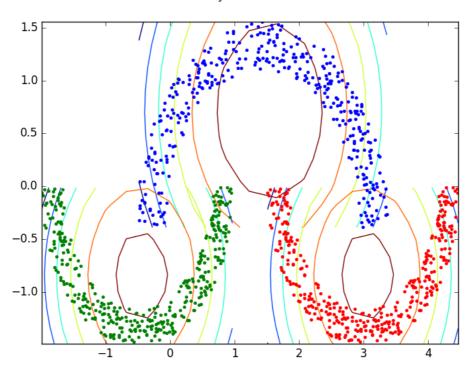
105	26
20	224

## • All classes together

82	13	20
17	112	0
26	0	105

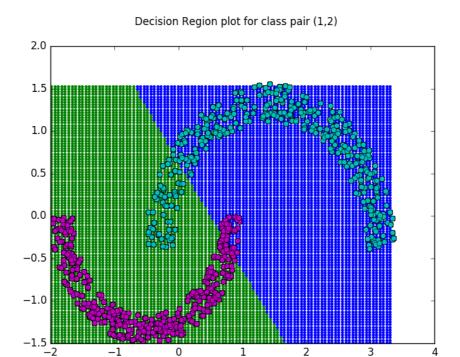
## **Constant density contour plot for all the classes -**

Constant Density Contours for all classes



#### Pairwise Decision region plots -

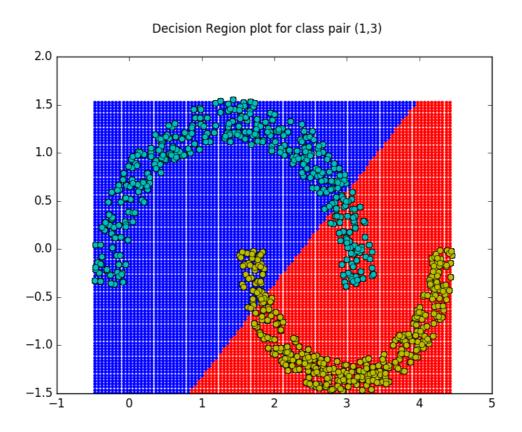
#### • <u>Class 1 and 2</u>



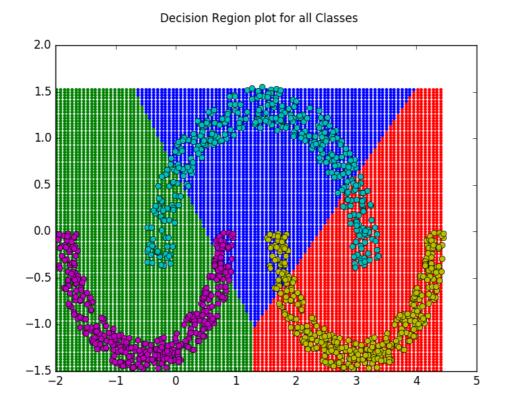
## • <u>Class 2 and 3</u>



## • <u>Class 1 and 3</u>



#### **Decision region plot for all the classes -**



#### Case 2: Full covariace matrix( $\Sigma$ ) is same for all the classes

Classification Accuracy (Class 1) – 0.915

Classification Accuracy (Class 2) – 0.973

Classification Accuracy (Class 3) – 0.941

Mean Classification Accuracy – 0.943

Precision (Class 1) -0.891

Precision (Class 2) -0.946

Precision (Class 3) – 0.906

Mean Precision – 0.914

Recall (Class 1) – 0.848

Recall (Class 2) -0.976

Recall (Class 3) – 0.920

Mean Recall – 0.915

F-Measure (Class 1) -0.869

F-Measure (Class 2) – 0.961

F-Measure (Class 3) – 0.913

Mean F-Measure – 0.914

#### **Average Covariance Matrix for each class -**

1.079	-0.002
-0.002	0.216

#### **Confusion Matrices -**

#### • <u>Class 1</u>

106	13
19	237

#### • <u>Class 2</u>

122	7
3	243

#### • <u>Class 3</u>

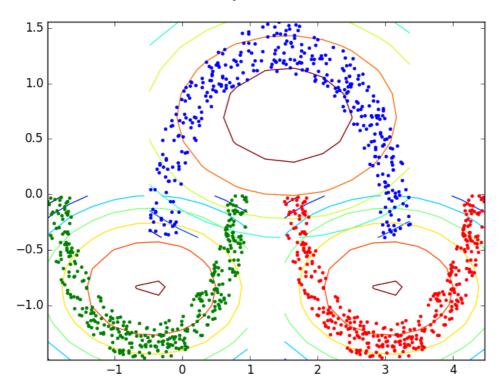
115	12
10	238

#### • All classes together

106	3	10
7	122	0
12	0	115

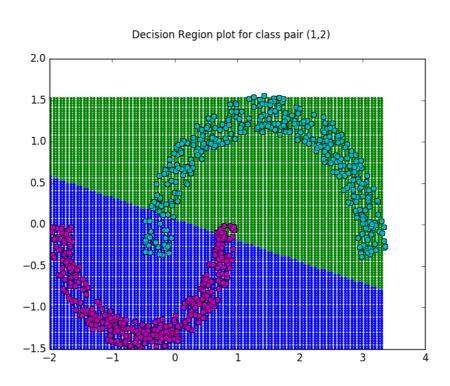
## **Constant density contour plot for all the classes -**

Constant Density Contours for all classes



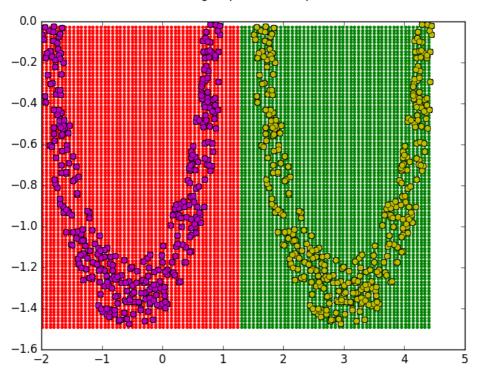
## Pairwise Decision region plots -

#### • <u>Class 1 and 2</u>



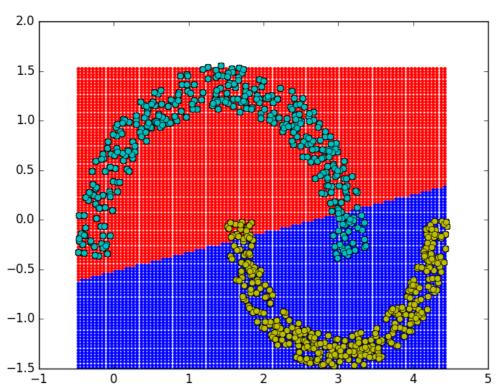
## • <u>Class 2 and 3</u>



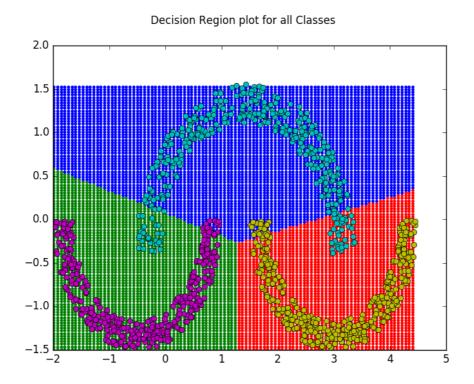


#### • <u>Class 1 and 3</u>

#### Decision Region plot for class pair (1,3)



#### **Decision region plot for all the classes -**



#### Case 3: Diagonal Covariance matrix (different for all classes)

Classification Accuracy (Class 1) – 0.904

Classification Accuracy (Class 2) – 0.971

Classification Accuracy (Class 3) – 0.933

Mean Classification Accuracy – 0.936

Precision (Class 1) -0.845

Precision (Class 2) -0.967

Precision (Class 3) -0.903

Mean Precision – 0.905

Recall (Class 1) -0.872

Recall (Class 2) -0.944

Recall (Class 3) – 0.896

Mean Recall – 0.904

F-Measure (Class 1) -0.858

F-Measure (Class 2) -0.955

F-Measure (Class 3) – 0.900

Mean F-Measure – 0.904

#### **Covariance Matrix for each class -**

#### • <u>Class 1</u>

1.488	0
0	0.276

#### • <u>Class 2</u>

0.875	0
0	0.187

#### • <u>Class 3</u>

0.875	0
0	0.187

#### **Confusion Matrices -**

#### • <u>Class 1</u>

109	20
16	230

#### • <u>Class 2</u>

118	4
7	246

#### • <u>Class 3</u>

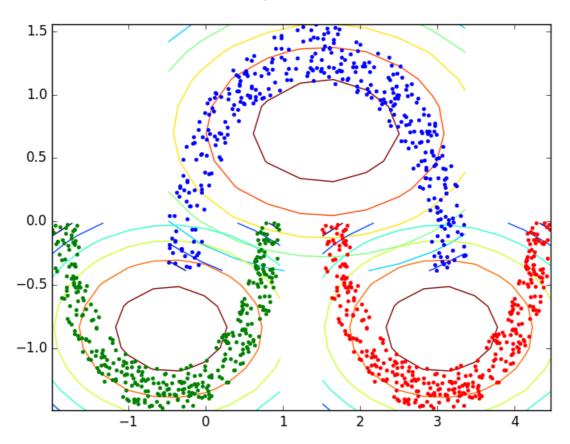
112	12
13	238

## • All classes together

109	7	13
4	118	0
12	0	112

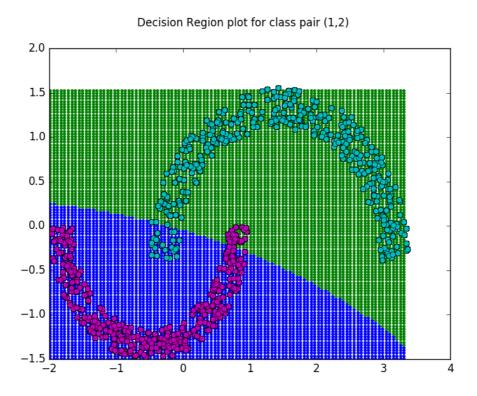
## **Constant density contour plot for all the classes -**

Constant Density Contours for all classes



## Pairwise Decision region plots -

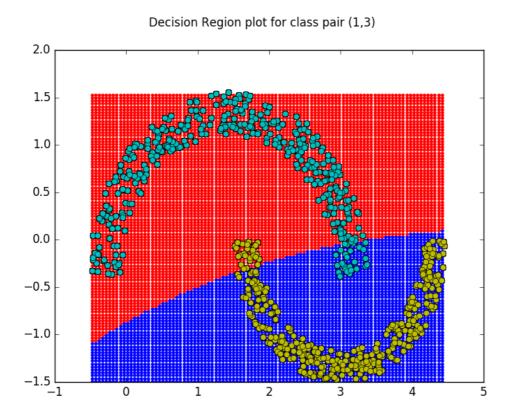
## • <u>Class 1 and 2</u>



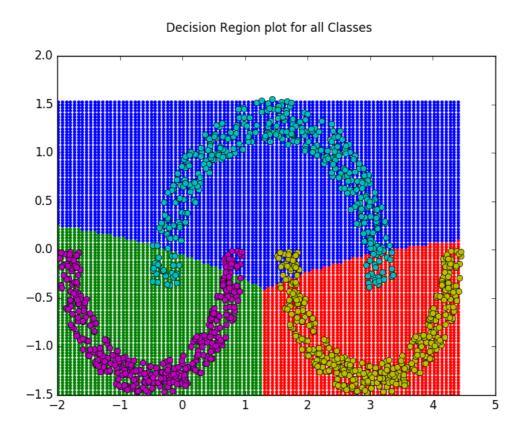
## • <u>Class 2 and 3</u>



## • <u>Class 1 and 3</u>



## **Decision region plot for all the classes -**



#### Case 4: Diffrerent full covariance matrix for each class

Classification Accuracy (Class 1) -0.909

Classification Accuracy (Class 2) – 0.976

Classification Accuracy (Class 3) – 0.933

Mean Classification Accuracy – 0.939

Precision (Class 1) -0.858

Precision (Class 2) -0.960

Precision (Class 3) – 0.910

Mean Precision – 0.909

Recall (Class 1) -0.872

Recall (Class 2) – 0.968

Recall (Class 3) – 0.888

Mean Recall -0.909

F-Measure (Class 1) -0.865

F-Measure (Class 2) -0.964

F-Measure (Class 3) – 0.899

Mean F-Measure – 0.909

#### **Covariance Matrix for each class -**

#### • <u>Class 1</u>

1.488	-0.039
-0.039	0.276

#### • <u>Class 2</u>

0.875	0.017
0.017	0.187

#### • <u>Class 3</u>

0.875	0.017
0.017	0.187

## **Confusion Matrices -**

#### • <u>Class 1</u>

109	18
16	232

## • <u>Class 2</u>

121	5
4	245

#### • <u>Class 3</u>

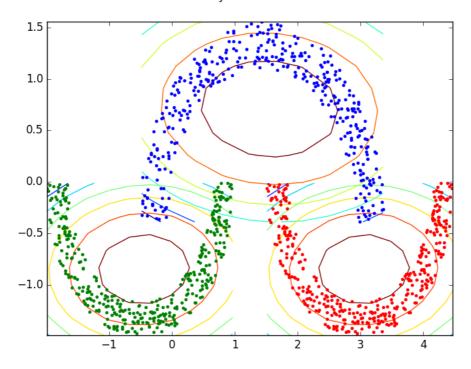
111	11
14	239

## • All classes together

109	4	14
5	121	0
11	0	111

## **Constant density contour plot for all the classes -**

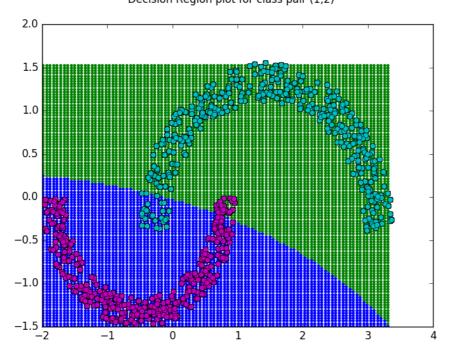
Constant Density Contours for all classes



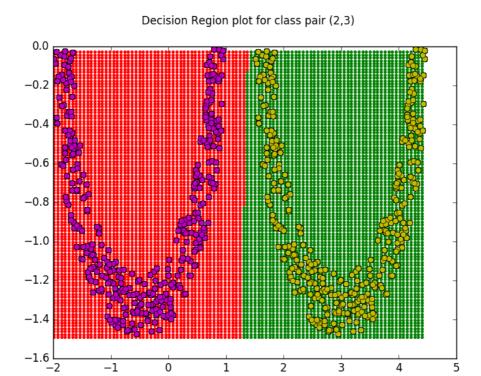
## Pairwise Decision region plots -

#### • <u>Class 1 and 2</u>

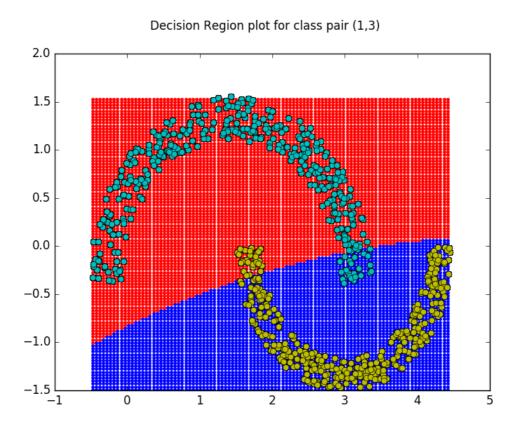
Decision Region plot for class pair (1,2)



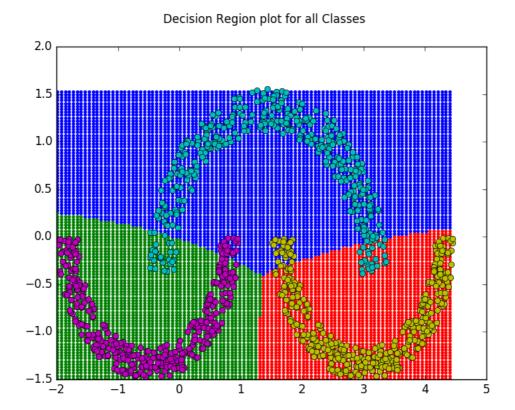
## • <u>Class 2 and 3</u>



## • <u>Class 1 and 3</u>



## <u>Decision region plot for all the classes -</u>



## **Dataset 2 (Real world dataset of 3 classes)**

#### Mean Vector for each case -

- Class 1 [316.284 2274.908]<sup>T</sup>
- Class 2 [369.999 761.888]<sup>T</sup>
- Class 3 [733.737 1121.756]<sup>T</sup>

#### Case 1: $\Sigma = \sigma^2 I$ (same for all classes)

Classification Accuracy (Class 1) -0.996

Classification Accuracy (Class 2) -0.978

Classification Accuracy (Class 3) – 0.977

Mean Classification Accuracy – 0.984

Precision (Class 1) -1.0

Precision (Class 2) -0.953

Precision (Class 3) – 0.975

Mean Precision – 0.976

Recall (Class 1) -0.988

Recall (Class 2) – 0.986

Recall (Class 3) – 0.950

Mean Recall – 0.975

F-Measure (Class 1) – 0.994

F-Measure (Class 2) -0.969

F-Measure (Class 3) – 0.962

Mean F-Measure – 0.975

#### **Covariance Matrix for each class -**

#### For All Classes

5116.934	0
0	5116.934

## **Confusion Matrices -**

#### • <u>Class 1</u>

590	0
7	1163

## • <u>Class 2</u>

613	30
9	1108

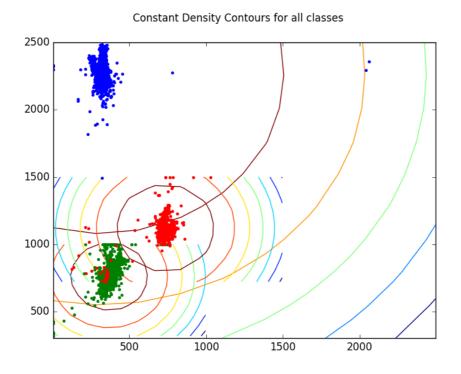
### • <u>Class 3</u>

514	13
27	1206

## • All classes together

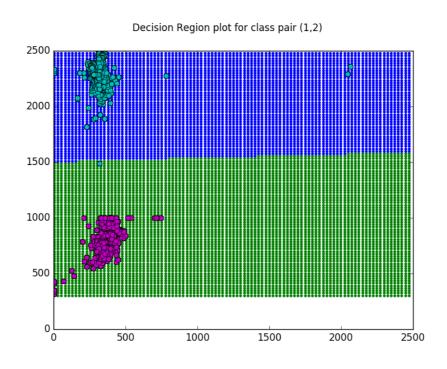
590	0	0
3	613	27
4	9	514

### Constant density contour plot for all the classes -

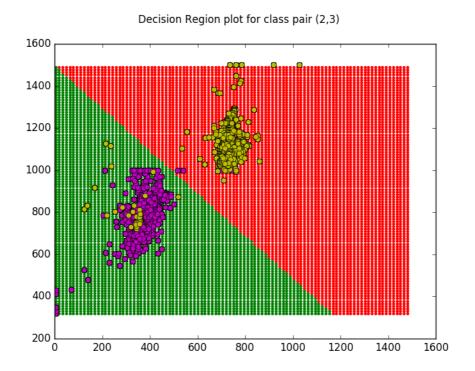


## Pairwise Decision region plots -

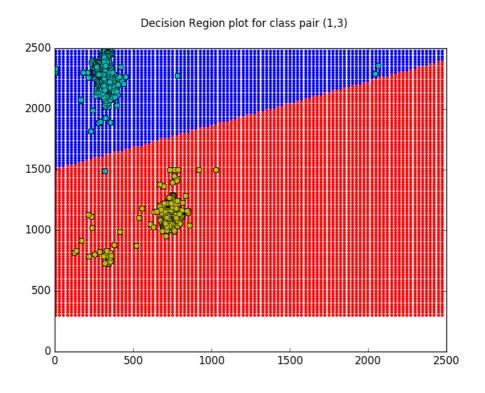
#### • <u>Class 1 and 2</u>



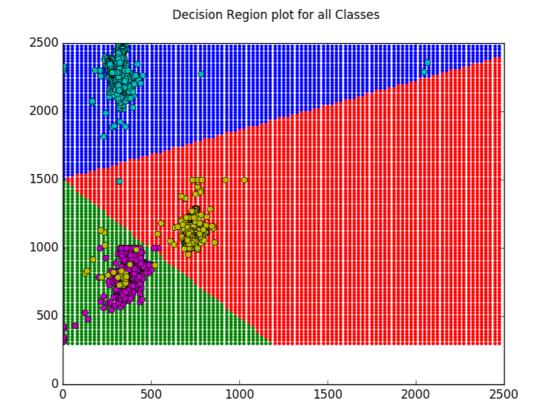
# • <u>Class 2 and 3</u>



#### • <u>Class 1 and 3</u>



#### **Decision region plot for all the classes -**



#### Case 2: Full covariace matrix( $\Sigma$ ) is same for all the classes

Classification Accuracy (Class 1) – 0.990

Classification Accuracy (Class 2) -0.977

Classification Accuracy (Class 3) – 0.970

Mean Classification Accuracy – 0.979

Precision (Class 1) -0.998

Precision (Class 2) -0.952

Precision (Class 3) – 0.957

Mean Precision – 0.969

Recall (Class 1) -0.972

Recall (Class 2) – 0.986

Recall (Class 3) – 0.946

Mean Recall – 0.968

F-Measure (Class 1) -0.985

F-Measure (Class 2) – 0.968

F-Measure (Class 3) – 0.952

 $Mean \ F-Measure-0.968$ 

### **Average Covariance Matrix for each class -**

3767.705	1524.447
1524.447	6466.162

#### **Confusion Matrices -**

### • <u>Class 1</u>

580	1
17	1162

#### • <u>Class 2</u>

613	31
9	1107

#### • <u>Class 3</u>

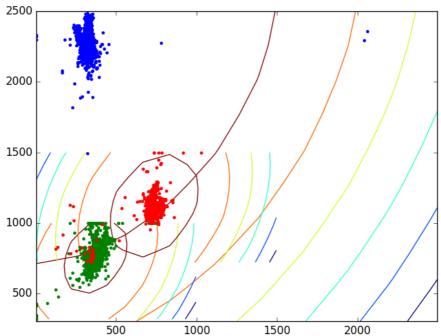
512	23
29	1196

#### • All classes together

580	0	1
3	617	28
14	9	512

# **Constant density contour plot for all the classes -**

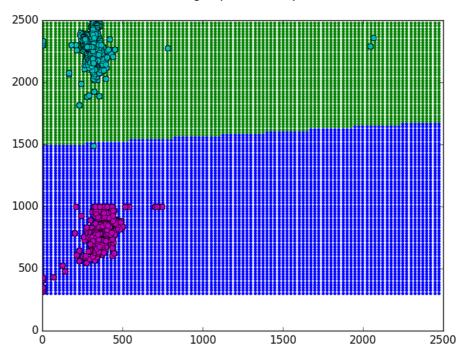
Constant Density Contours for all classes



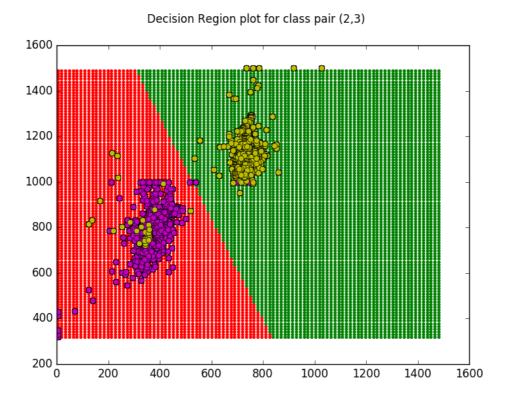
#### Pairwise Decision region plots -

## • <u>Class 1 and 2</u>

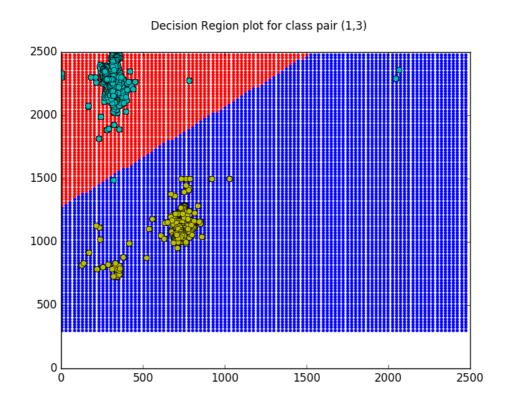
Decision Region plot for class pair (1,2)



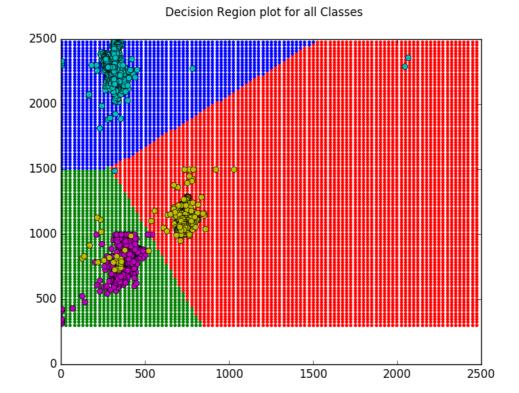
## • <u>Class 2 and 3</u>



#### • <u>Class 1 and 3</u>



#### **Decision region plot for all the classes -**



#### Case 3: Diagonal Covariance matrix (different for all classes)

Classification Accuracy (Class 1) – 0.992

Classification Accuracy (Class 2) – 0.978

Classification Accuracy (Class 3) – 0.973

Mean Classification Accuracy – 0.981

Precision (Class 1) – 0.998

Precision (Class 2) -0.953

Precision (Class 3) – 0.964

Mean Precision – 0.972

Recall (Class 1) -0.978

Recall (Class 2) – 0.986

Recall (Class 3) – 0.948

 $Mean\ Recall-0.971$ 

F-Measure (Class 1) -0.988

F-Measure (Class 2) – 0.969

F-Measure (Class 3) – 0.956

Mean F-Measure – 0.971

### **Covariance Matrix for each class -**

#### • <u>Class 1</u>

4487.057	0
0	7611.523

#### • <u>Class 2</u>

2145.310	0
0	6128.158

#### • <u>Class 3</u>

4670.748	0
0	5858.805

#### **Confusion Matrices -**

#### • <u>Class 1</u>

584	1
13	1162

#### • <u>Class 2</u>

613	30
9	1108

#### • <u>Class 3</u>

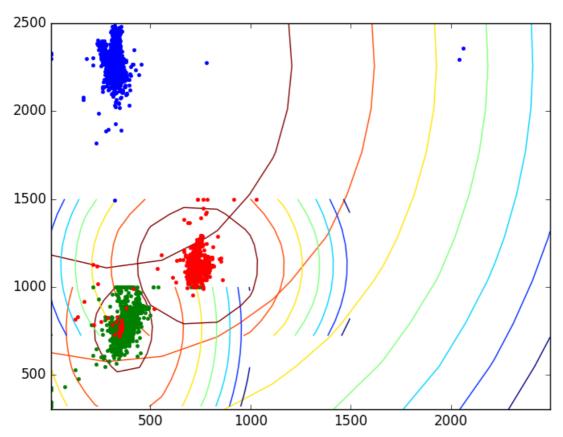
513	19
28	1200

## • All classes together

584	0	1
3	613	27
10	9	513

### **Constant density contour plot for all the classes -**

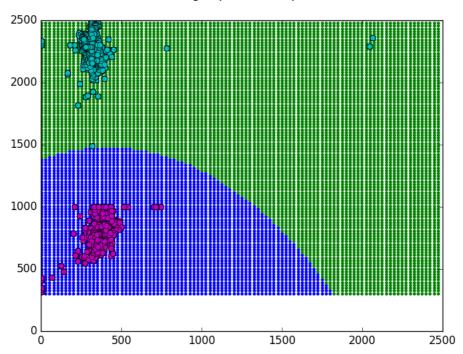
Constant Density Contours for all classes



## Pairwise Decision region plots -

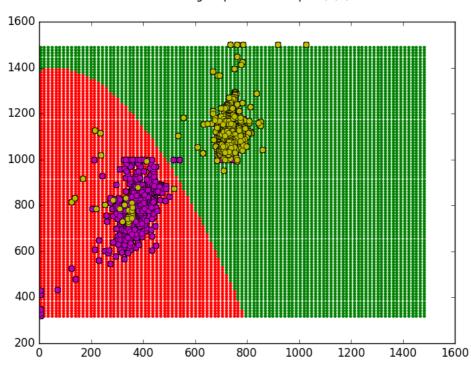
### • <u>Class 1 and 2</u>



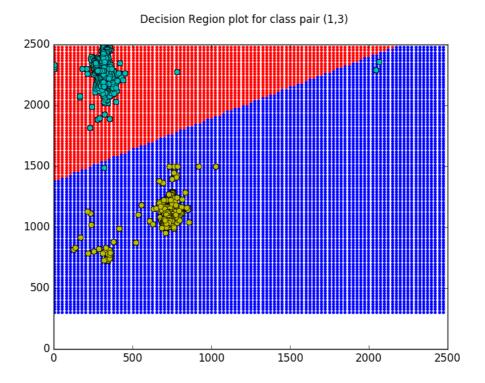


## • <u>Class 2 and 3</u>

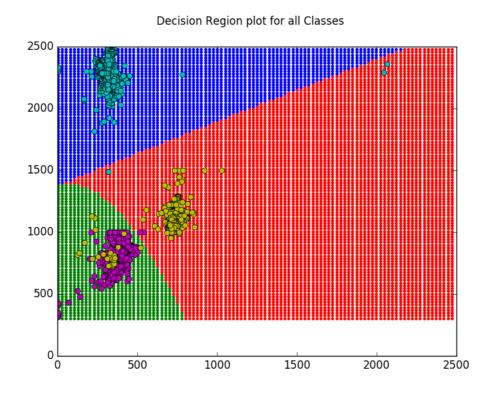
Decision Region plot for class pair (2,3)



## • <u>Class 1 and 3</u>



## **Decision region plot for all the classes -**



#### Case 4: Diffrerent full covariance matrix for each class

Classification Accuracy (Class 1) – 0.991

Classification Accuracy (Class 2) -0.976

Classification Accuracy (Class 3) – 0.970

Mean Classification Accuracy – 0.979

Precision (Class 1) -0.998

Precision (Class 2) -0.952

Precision (Class 3) – 0.957

Mean Precision – 0.969

Recall (Class 1) -0.975

Recall (Class 2) – 0.982

Recall (Class 3) – 0.946

Mean Recall – 0.968

F-Measure (Class 1) -0.986

F-Measure (Class 2) -0.967

F-Measure (Class 3) – 0.952

Mean F-Measure – 0.968

#### **Covariance Matrix for each class -**

#### • <u>Class 1</u>

4487.057	-310.508
-310.508	7611.523

#### • Class 2

2145.310	2194.074
2194.074	6128.158

#### • Class 3

4670.748	2689.776
2689.776	5658.805

## **Confusion Matrices -**

#### • <u>Class 1</u>

582	1
15	1162

## • <u>Class 2</u>

611	31
11	1107

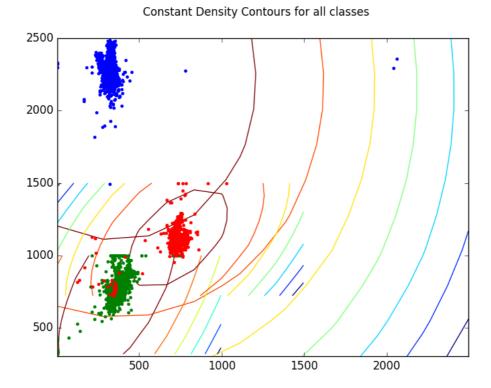
#### • <u>Class 3</u>

512	23
29	1196

## • All classes together

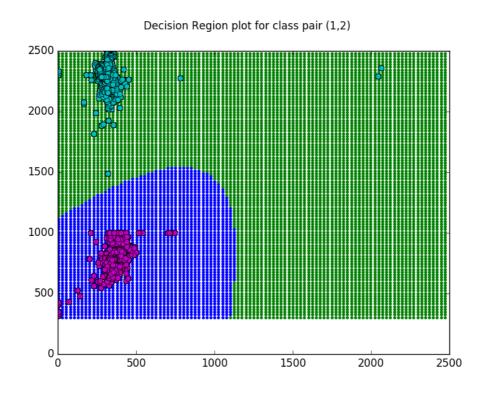
582	0	1
3	611	28
12	11	512

## **Constant density contour plot for all the classes -**

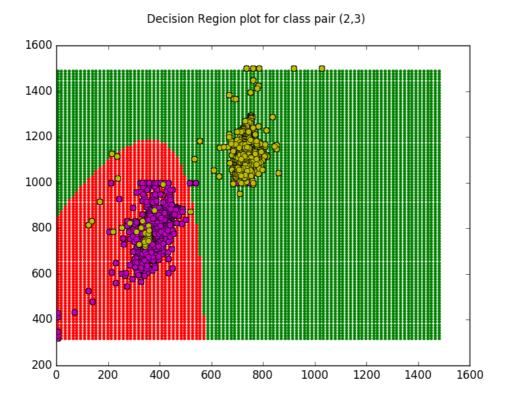


### Pairwise Decision region plots -

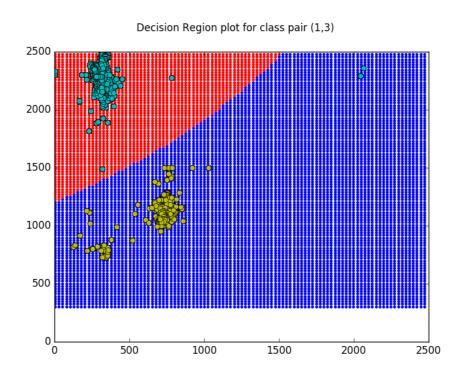
#### • <u>Class 1 and 2</u>



# • <u>Class 2 and 3</u>

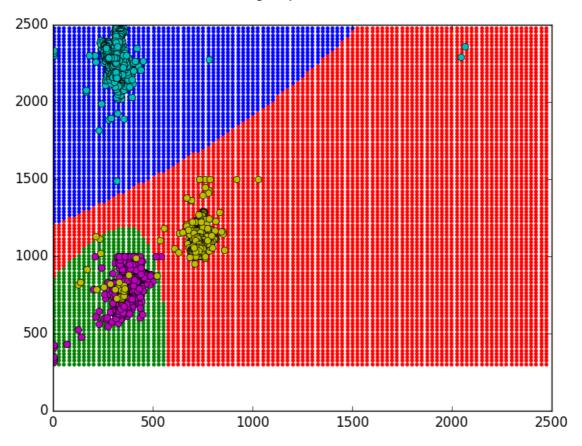


### • <u>Class 1 and 3</u>



# <u>Decision region plot for all the classes -</u>

Decision Region plot for all Classes



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