

Hypothesis Testing Assignment Questions

Answer = 1

To test whether the new customer feedback process has improved satisfaction, we can perform a **one-sample t-test**

STEP = 1

Null Hypothesis (H_0): 72

Alternative Hypothesis (H_1): Mean score > 72 (This is a one-tailed test.)

Given Data

- Population means before(μ): = 72
- Sample mean after{x} = 78
- Sample standard deviation: (std)= 10
- Sample size: (n) = 30
- Significance level: (α) = 0.05

STEP = 2

STANDAR ERROR:

$$\text{SE} = \text{Sigma}/\text{Sqrt}(n)$$

Sigma (std) =10

Sample size(n) = 30 sqrt (5.477)

$$10/5.477 = \textbf{1.82}$$

STEP = 3

We use the t-statistic formula:

$$T \text{ CAL } (X\text{BAR} - \text{MU}) / \text{SE}$$

$$X\text{bar} = 78$$

$$\text{MU} = 72$$

$$\text{SE} = 1.82$$

$$(78 - 72) / 1.82 = 3.29$$

STEP = 4

Critical Value

Sample size (n)

$$\text{Degrees of freedom: } df = 30 - 1 = 29$$

From the t-distribution table, the critical value for a one-tailed test at $\alpha = 0.05$ and $df = 29$ is approximately 1.699.

Decision

- Calculated t-value: 3.29
- Critical t-value: 1.699

Since $3.29 > 1.699$, we reject the null hypothesis.

Conclusion

There is **statistically significant evidence** at the 5% level to conclude that the new customer feedback process has **improved customer satisfaction.**

Answer = 2

To verify the school's claim, we'll perform a one-sample t-test to see if the sample mean is significantly greater than the national average.

STEP = 1

Null Hypothesis (H_0): 75

Alternative Hypothesis (H_1): $\mu > 75$ (This is a one-tailed test.)

Given Data

- **National average: (μ)= 75**
- **Sample means: $\{\bar{x}\} = 77$**
- **Sample standard deviation: (std) = 8**
- **Sample size: (n) = 50**
- **Significance level: (α) = 0.01**

STEP = 2

STANDARD ERROR:

$$\text{SE} = \text{Sigma}/\text{Sqrt}(n)$$

Sigma (std) = 8

Sample size(n) = 50 sqrt (7.071)

$$8/7.071 = \text{1.13}$$

STEP = 3

We use the t-statistic formula:

$$T_{CAL} = (XBAR - MU) / SE$$

$$Xbar = 77$$

$$MU = 75$$

$$SE = 1.13$$

$$(77-75)/1.13 = 1.77$$

STEP = 4

Critical Value

Sample size (n)

Degrees of freedom: $df = 50 - 1 = 49$

From the t-distribution table, the critical value for a **one-tailed test** at $\alpha = 0.01$ and $df = 49$ is approximately **2.405**.

Decision

- Calculated t-value: **1.77**
- Critical t-value: **2.405**

Since $1.77 < 2.405$, we **fail to reject the null hypothesis**.

Conclusion

At the 0.01 significance level, there is **not enough statistical evidence** to support the school's claim that their students' average math score is higher than the national average.

Answer = 3

To determine whether the new sales strategy significantly increased average daily sales, we'll perform a **one-sample t-test**.

STEP = 1

Null Hypothesis (H_0): 10,000

Alternative Hypothesis (H_1): $\mu > 10,000$ (This is a one-tailed test.)

Given Data

- **Population means: (μ) = 10,000**
- **Sample mean: $\{\bar{x}\} = 11,200$**
- **Sample standard deviation: (σ) = 1,500**
- **Sample size: (n) = 15**
- **Significance level: (α) = 0.05**

STEP = 2

STANDARD ERROR:

$$\text{SE} = \text{Sigma} / \text{Sqrt}(n)$$

Sigma (σ) = 1,500

Sample size(n) = 15 sqrt (3.873)

$$1500 / 3.873 = \text{387.29}$$

STEP = 3

We use the t-statistic formula:

$$\mathbf{T\ CAL\ (XBAR - MU)/SE}$$

$$\mathbf{Xbar = 11,200}$$

$$\mathbf{MU = 10,000}$$

$$\mathbf{SE = 387.29}$$

$$\mathbf{(11,200 - 10,000) / 387.29 = 3.10}$$

STEP = 4

Critical Value

Sample size (n)

Degrees of freedom: $df = 15 - 1 = 14$

From the t-distribution table, the critical value for a **one-tailed test** at $\alpha = 0.05$ and $df = 14$ is approximately **1.761**.

Decision

- Calculated t-value: **3.10**
- Critical t-value: **1.761**

Since $3.10 > 1.761$, we **reject the null hypothesis**.

Conclusion

At the 5% significance level, there is **strong statistical evidence** that the new sales strategy has **increased average daily sales**.

Answer = 4

To test if the advertised lifespan of 1200 hours is accurate, we'll perform a **one-sample t-test** since the population standard deviation is unknown and the sample size is relatively small ($n = 40$).

STEP = 1

Null Hypothesis (H_0): 1200 hour

Alternative Hypothesis (H_1): $\neq 1200$ hour (This is a two-tailed test.)

Given Data

- **Population means: (μ) = 1200 hour**
- **Sample mean $\{\bar{x}\} = 1180$ hours**
- **Sample standard deviation (std) = 50 hours**
- **Sample size (n) = 40**
- **Significance level (α) = 0.05**

STEP = 2

STANDARD ERROR:

$$\text{SE} = \text{Sigma} / \text{Sqrt}(n)$$

Sigma (std) = 50

Sample size(n) = 40 sqrt (6.32)

$$50/6.32 = \textbf{7.91}$$

STEP = 3

We use the t-statistic formula:

$$\mathbf{T\ CAL\ (XBAR - MU)/SE}$$

$$\mathbf{XBar = 1180}$$

$$\mathbf{MU = 1200}$$

$$\mathbf{SE = 7.91}$$

$$\mathbf{(1800 - 1200)/7.91 = -2.53}$$

STEP = 4

Critical Value

Sample size (n)

$$\mathbf{Degrees\ of\ freedom\ (df) = 40 - 1 = 39}$$

From the t-distribution table, **the critical t-value for a two-tailed test at $\alpha = 0.05$ and $df = 39$ is approximately: t_{critical} 2.022**

Decision

- Calculated t-value: **-2.53**
- Critical t-value: **2.022**

Since $2.53 > 2.022$, we reject the null hypothesis.

Conclusion

At the 0.05 significance level, there is **sufficient evidence to conclude** that the actual mean lifespan of the bulbs **differs from the advertised 1200 hours**

Answer = 5

To test whether the average height of adult males in the city differs from the national average of 5.8 feet, we'll perform a **two-tailed one-sample t-test**.

STEP = 1

Null Hypothesis (H_0): 5.8

Alternative Hypothesis (H_1): $\neq 5.8$ (This is a two-tailed test.)

Given Data

- Population mean: $(\mu) = 5.8\text{feet}$
- Sample mean $\{\bar{x}\} = 5.7\text{feet}$
- Sample standard deviation (std) = 0.3feet
- Sample size (n) = 25
- Significance level (α) = 0.01

STEP = 2

STANDARD ERROR:

- **$SE = \text{Sigma}/\text{Sqrt}(n)$**
 - Sigma (std) = 0.3
 - Sample size(n) = 25 sqrt (5)
- $0.3/5 = \mathbf{0.06}$

STEP = 3

We use the t-statistic formula:

$$\mathbf{T\ CAL\ (XBAR - MU)/SE}$$

$$\mathbf{Xbar = 5.7}$$

$$\mathbf{MU = 5.8}$$

$$\mathbf{SE = 0.06}$$

$$\mathbf{(5.7 - 5.8)/0.06 = 1.67}$$

STEP = 4

Critical Value

Sample size (n)

$$\mathbf{Degrees\ of\ freedom\ (df) = 25 - 1 = 24}$$

From the t-distribution table, the critical t-value for a two-tailed test at $\alpha = 0.01$ and $df = 24$ $t_{\{critical\}} 2.797$

Decision

- Calculated t-value: **-1.67**
- Critical t-value: **2.797**

Since $1.67 < 2.797$, we fail to reject the null hypothesis.

Conclusion

At the 1% significance level, there is not enough evidence to conclude that the average height of adult males in the city differs from the national average of 5.8 feet.