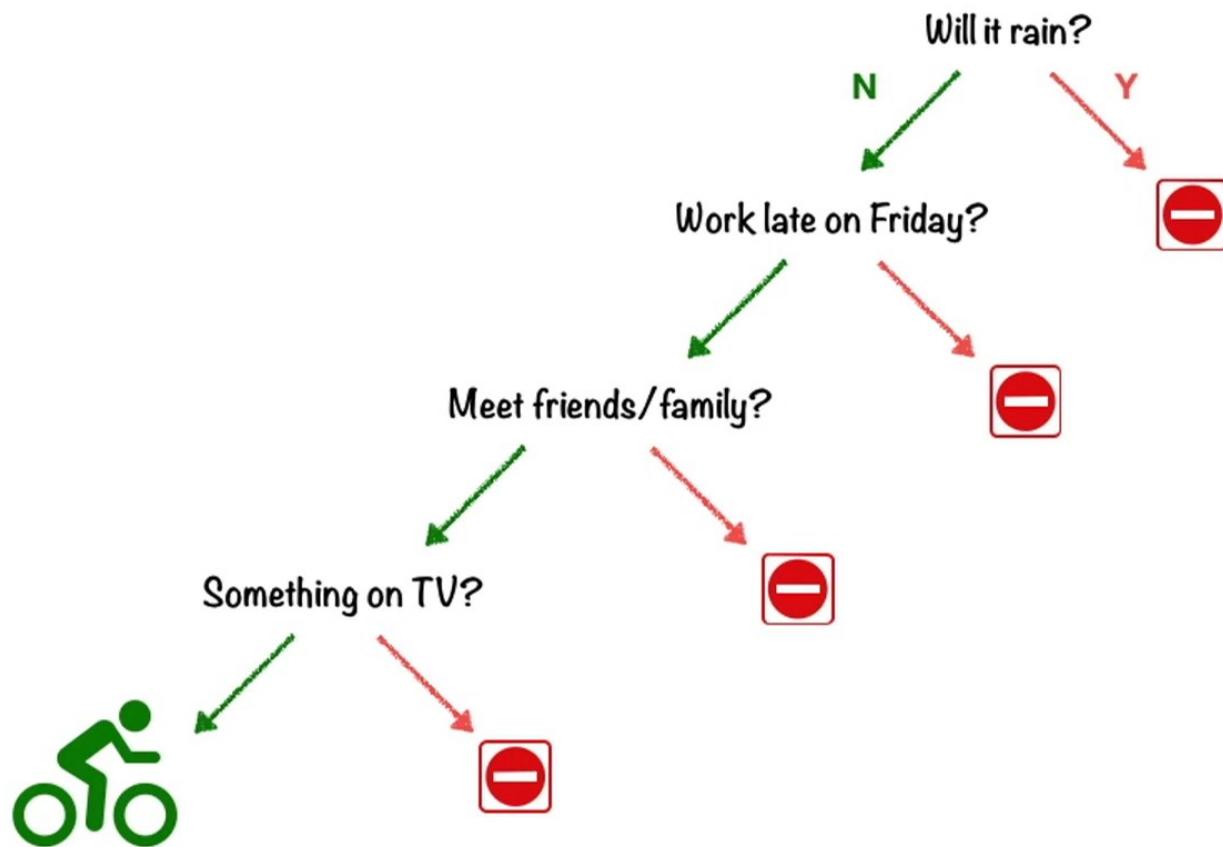


# Decision Trees

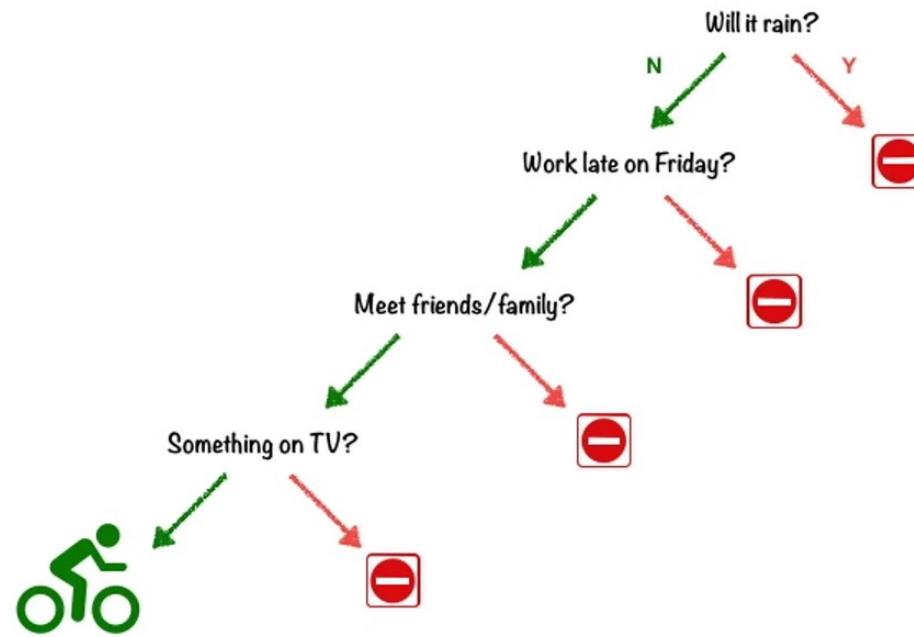
# Should I go biking on Saturday morning?

- Will it rain?
- Will I work late on Friday?
- Do I need to meet friends/family?
- Is there something on TV?

# Should I go biking on Saturday morning?



## Decision Tree



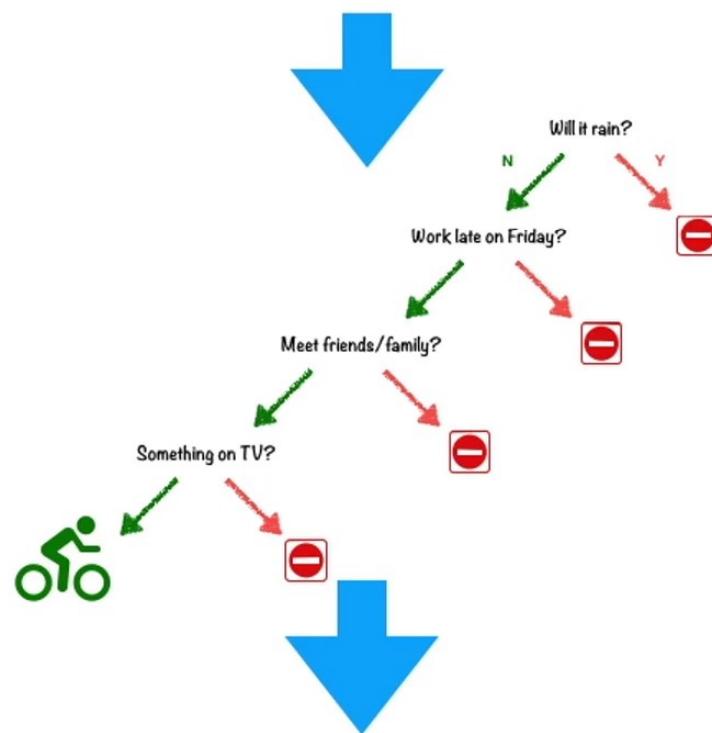
This is exactly what a decision tree looks like

## Decision Tree

- Helps predict an outcome given a set of inputs
- In business, it represents visually how a decision is taken with inputs and consequences of each decision

# Decision Tree

Input Variables/Predictors



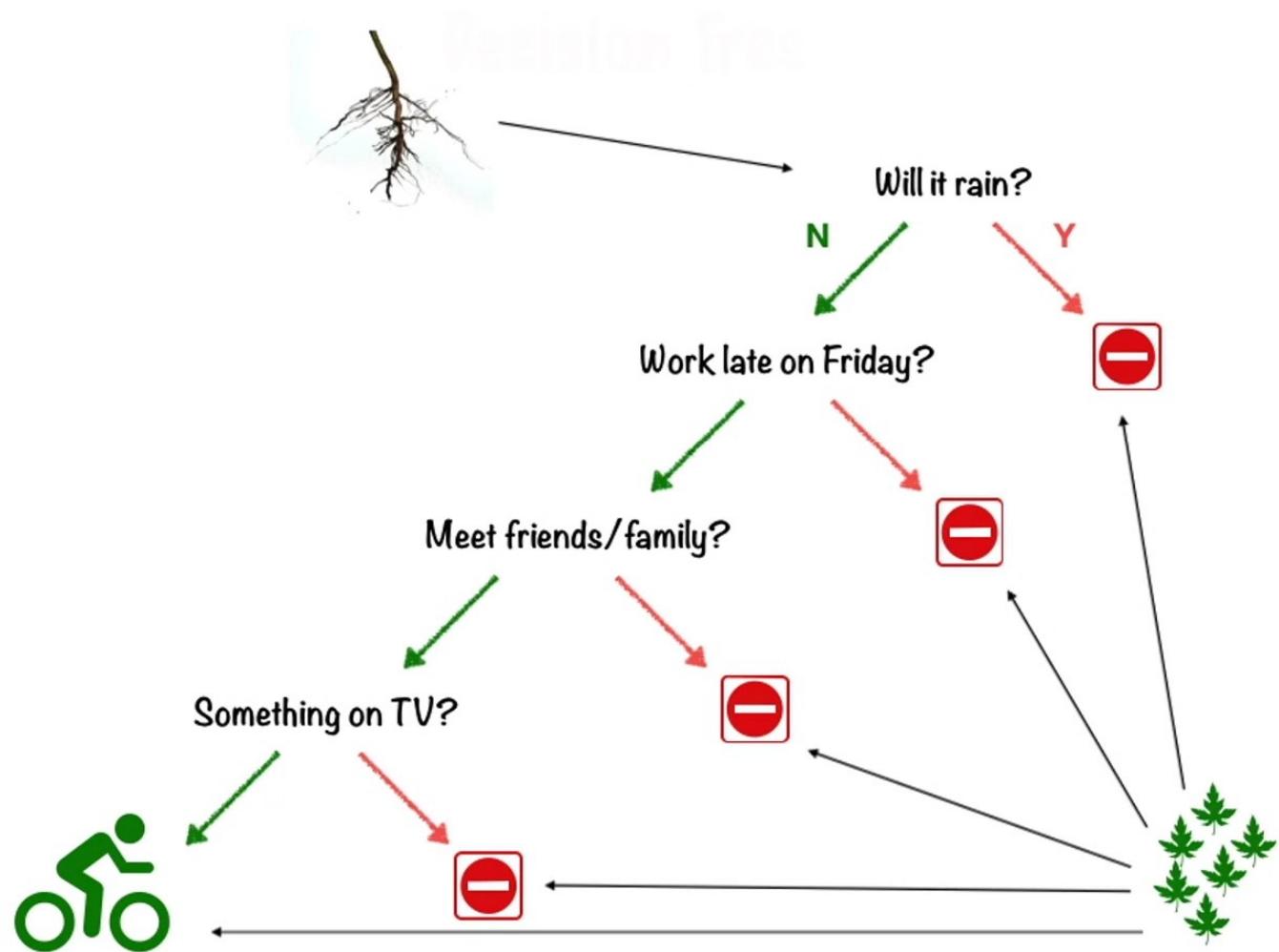
Outcome/Output Variables

## Decision Tree

- Can be used for classification, just like SVM
- With SVM, can't understand relationship between input variables and outcome
- Decision Trees are not a blackbox

## Decision Tree

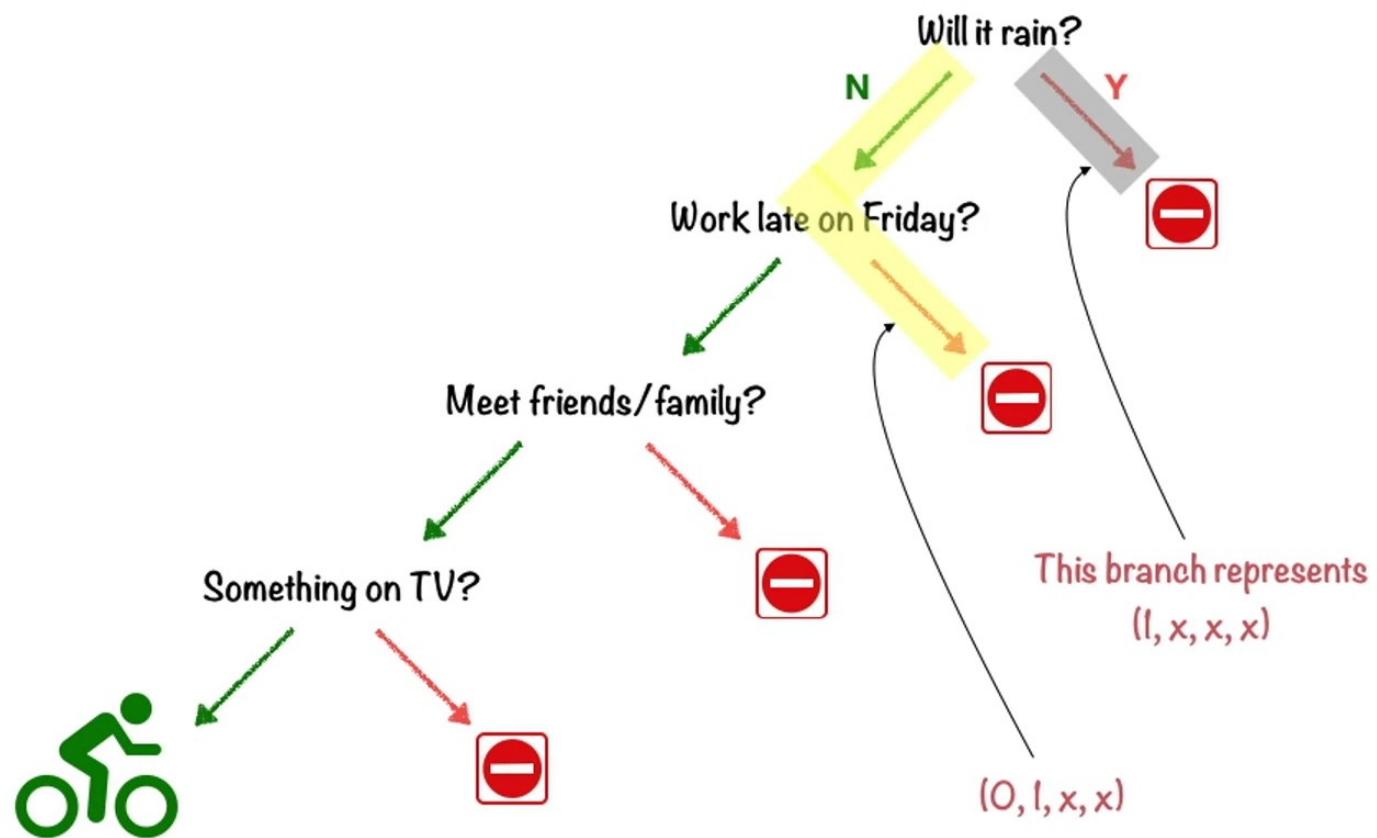
- Inputs can be categorical or continuous
- Outputs can also be categorical or continuous
  - Called regression tree when outcome is continuous



# Decision Tree

- The leaves of a tree are the outcomes
- In a classification problem, these are class labels
- The tree gives the most likely outcome given the values of the variables
- The branches are combinations of predictor values leading to an outcome

# Decision Tree



## Decision Tree Learning

- The process of creating/learning a decision tree from training data
- Start with training data in the form of feature vector, label/outcome
  - (1,0,1,1), No biking
  - (0,0,0,0), I bike!
- Obtain a decision tree used to classify/predict a new instance
- A supervised learning approach

# Decision Tree Learning

- Recursive partitioning is the most common strategy for decision tree learning
- Decision tree learning algorithms
  - CART
  - ID3
  - C4.5
  - CHAID

Be

Int

Ad

## Key takeaways from this chapter

What is Decision Tree?

A decision tree is a graphical representation of all the possible solutions to a decision based on certain conditions. It's called a decision tree because it starts with a single box (or root), which then branches off into a number of solutions, just like a tree.

We will start with the training data in the form of feature vector, label/outcome.

Types of Decision Tree Algorithms

CART

ID3

C4.5

CHAID

## Decision Tree Learning

- Algorithm needs to tell us the order in which the predictors are evaluated
- If the predictor is continuous, the tree needs to split the variable into ranges

# Greedy Algorithm for Learning a Decision Tree

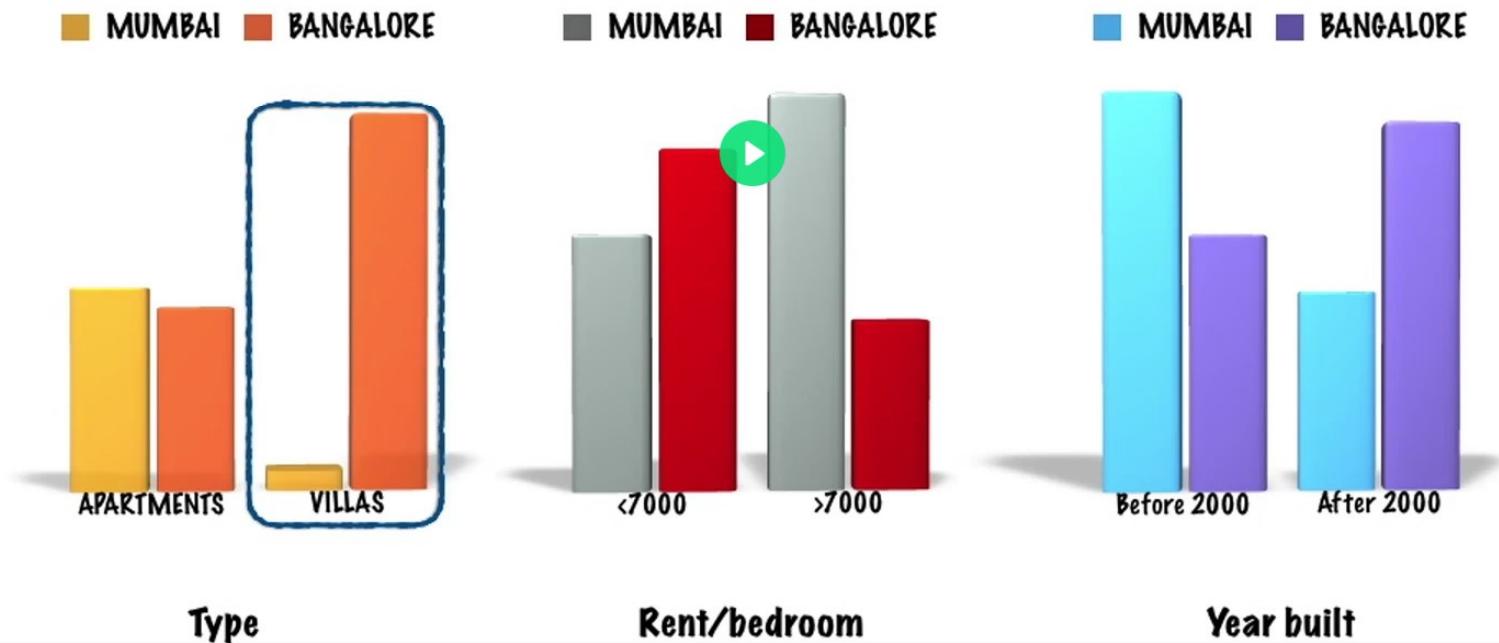
GIVEN THE  
TYPE OF HOUSING,  
RENT/BEDROOM AND  
THE YEAR IT WAS BUILT

PREDICT THE CITY TO  
WHICH A RESIDENCE  
BELONGS

MUMBAI (OR)  
BANGALORE

# Greedy Algorithm for Learning a Decision Tree

DRAW A HISTOGRAM FOR EACH ATTRIBUTE, FOR RESIDENCES IN EACH CITY





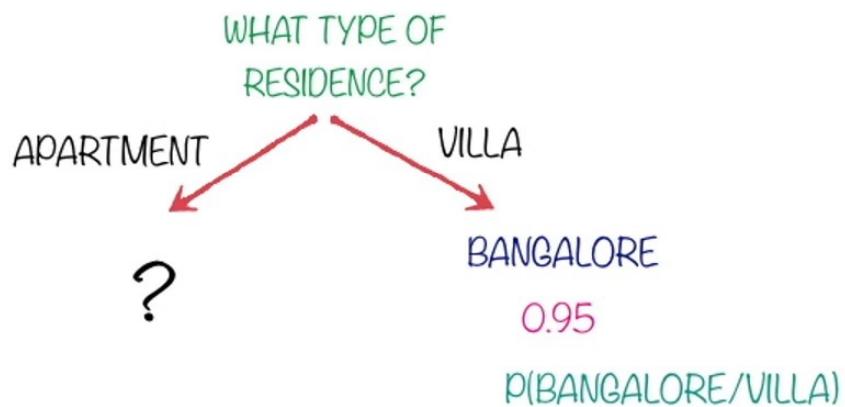
THE TYPE OF HOUSING SEEMS TO BE  
THE CLEAREST INDICATOR OF  
WHETHER A RESIDENCE BELONGS TO  
MUMBAI OR BANGALORE

IF IT IS A VILLA, THEN IT MOST LIKELY  
BELONGS TO BANGALORE

IF IT IS AN APARTMENT, WE ARE STILL  
NOT SURE WHICH CITY IT BELONGS TO

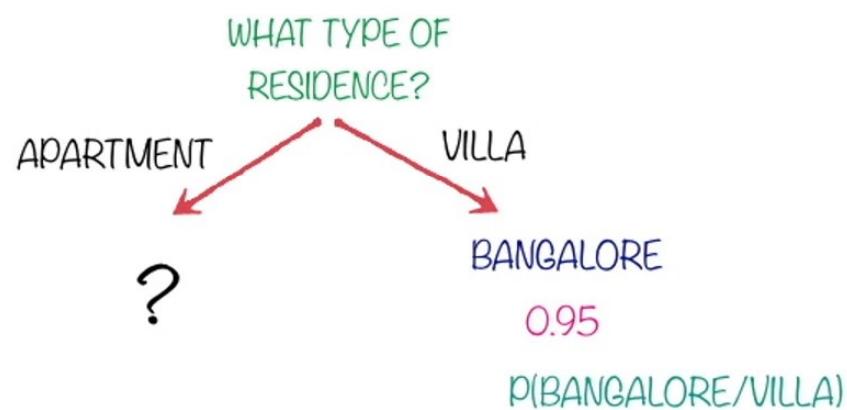


WE NOW HAVE THE FIRST  
NODE OF OUR DECISION TREE



WE'VE DIVIDED OUR DATA INTO  
2 SUBSETS - APARTMENTS  
AND VILLAS

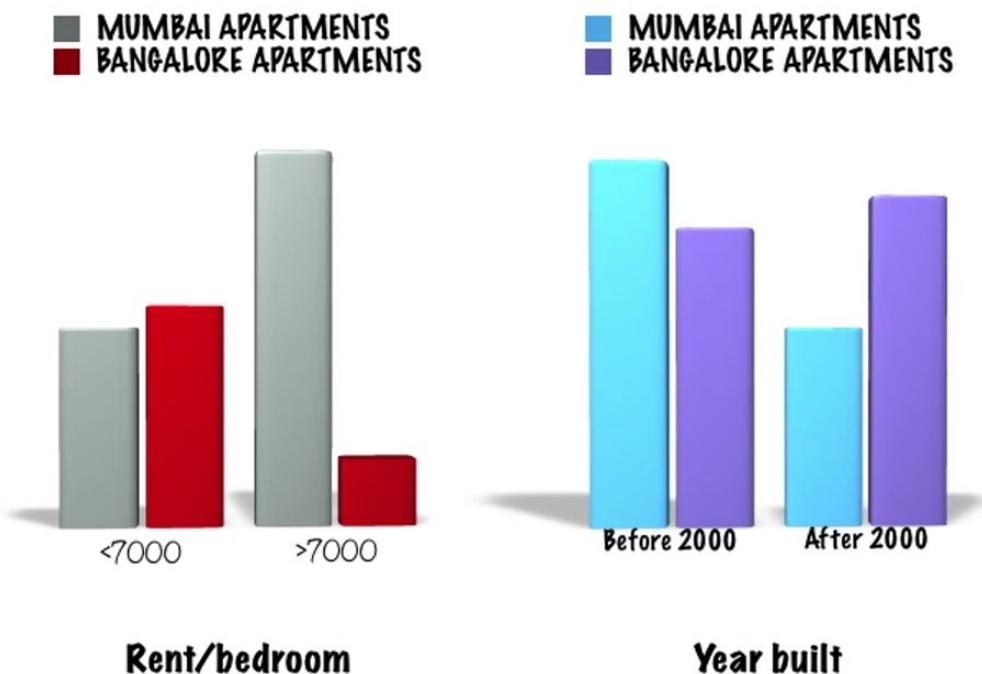
WE NOW HAVE THE FIRST  
NODE OF OUR DECISION TREE



WE'VE DIVIDED OUR DATA INTO  
2 SUBSETS - APARTMENTS  
AND VILLAS

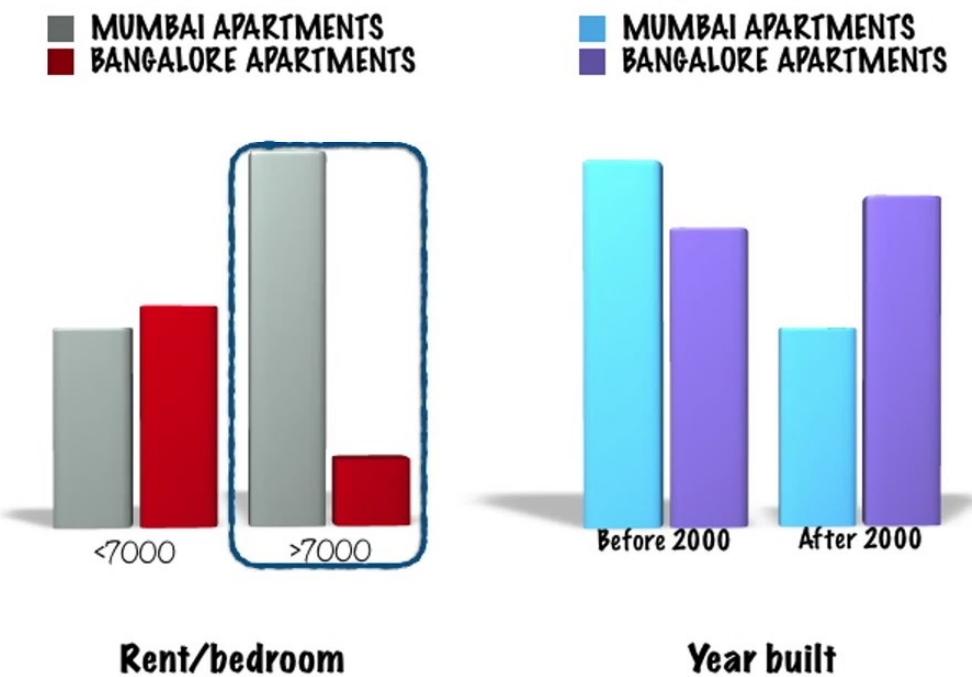
REPEAT THIS PROCESS RECURSIVELY,  
FOR EACH SUBSET

DRAW A HISTOGRAM FOR  
EACH OF THE REMAINING  
ATTRIBUTES FOR ONLY  
THE APARTMENTS IN EACH  
CITY

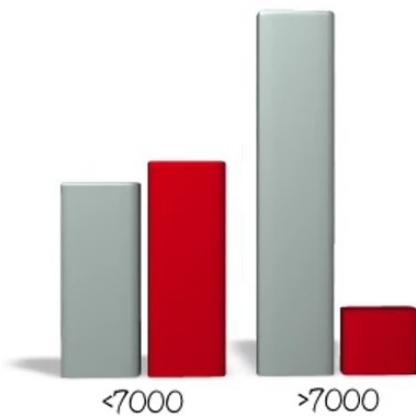


REPEAT THIS PROCESS RECURSIVELY,  
FOR EACH SUBSET

DRAW A HISTOGRAM FOR  
EACH OF THE REMAINING  
ATTRIBUTES FOR ONLY  
THE APARTMENTS IN EACH  
CITY



■ MUMBAI APARTMENTS  
■ BANGALORE APARTMENTS

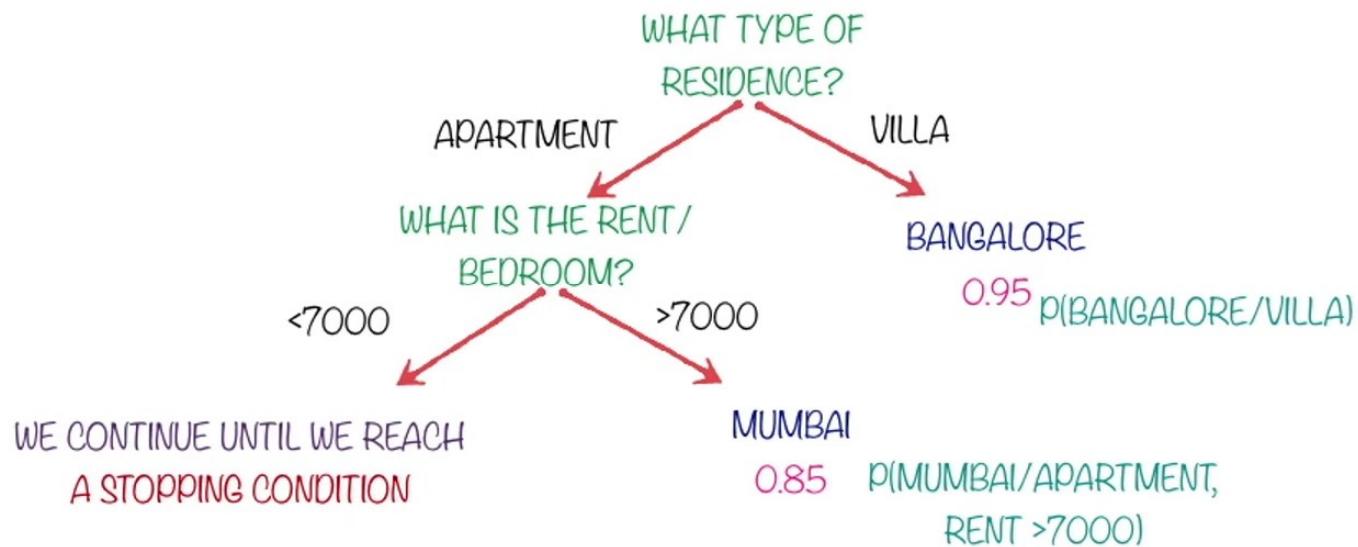


WHEN YOU LOOK ONLY AT  
APARTMENTS, THE RENT/  
BEDROOM SEEMS TO BE A  
GOOD PREDICTOR OF THE CITY

NOW, WE'LL DIVIDE THE  
APARTMENTS INTO TWO  
SUBSETS, RENT >7000,  
RENT <7000

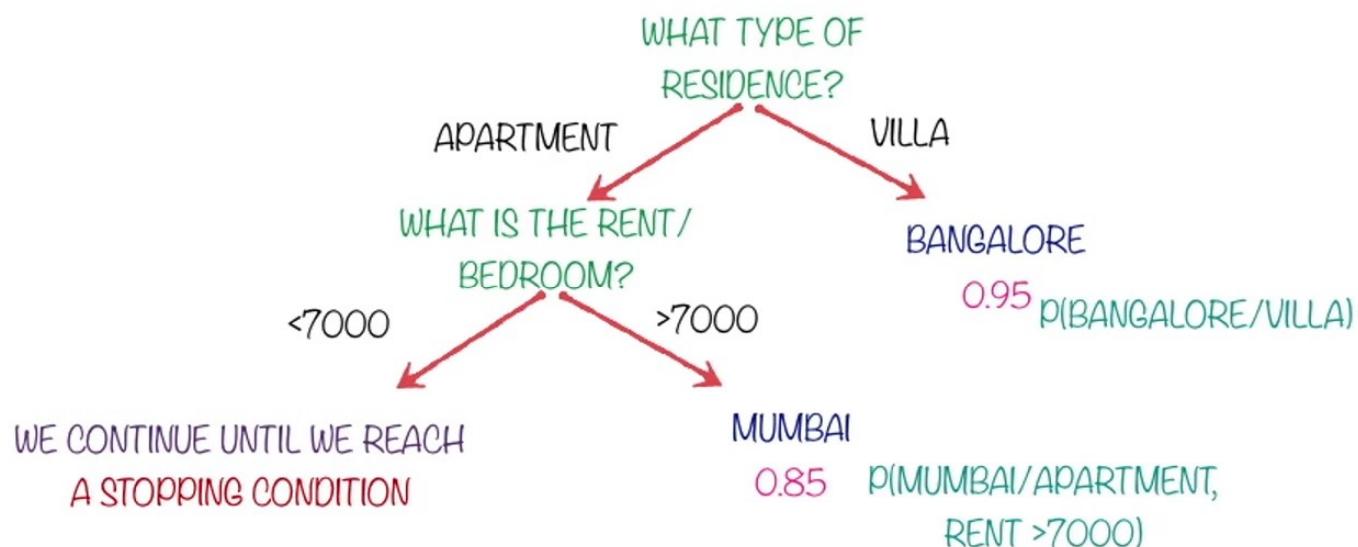


## Our Decision Tree so far



This is Recursive Partitioning

## Our Decision Tree so far

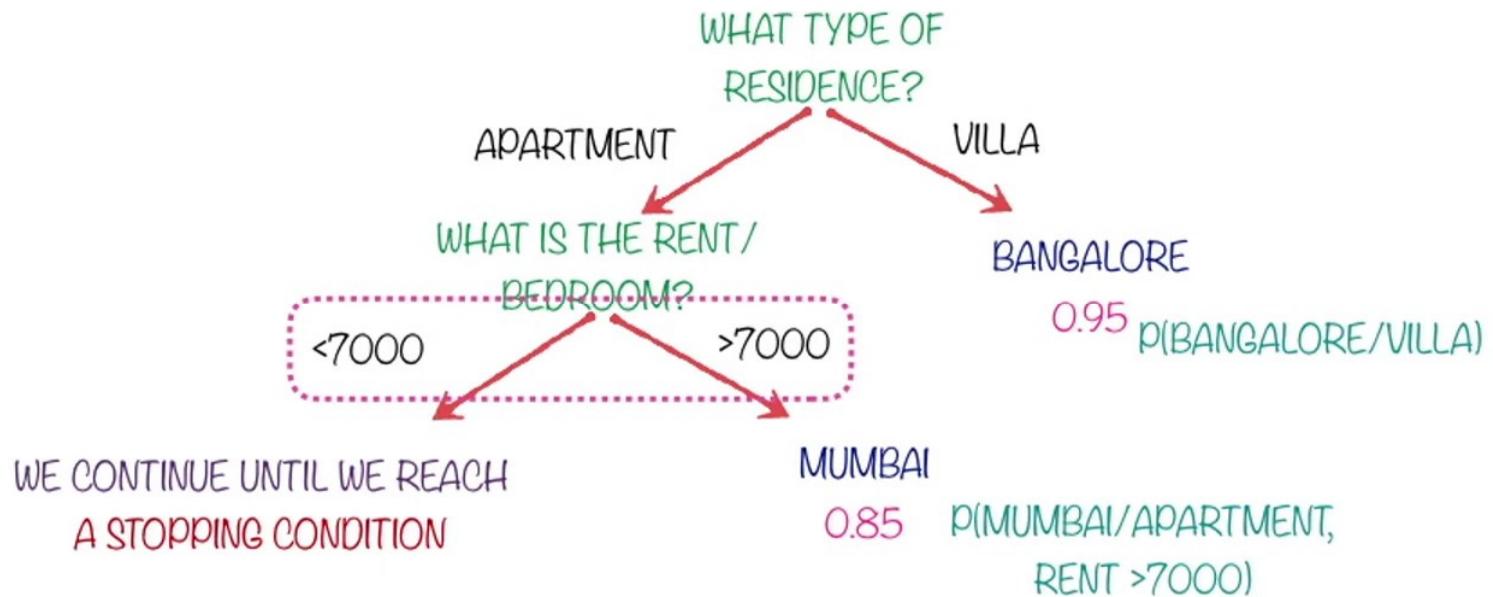


# This is Recursive Partitioning

## The Stopping Condition could be

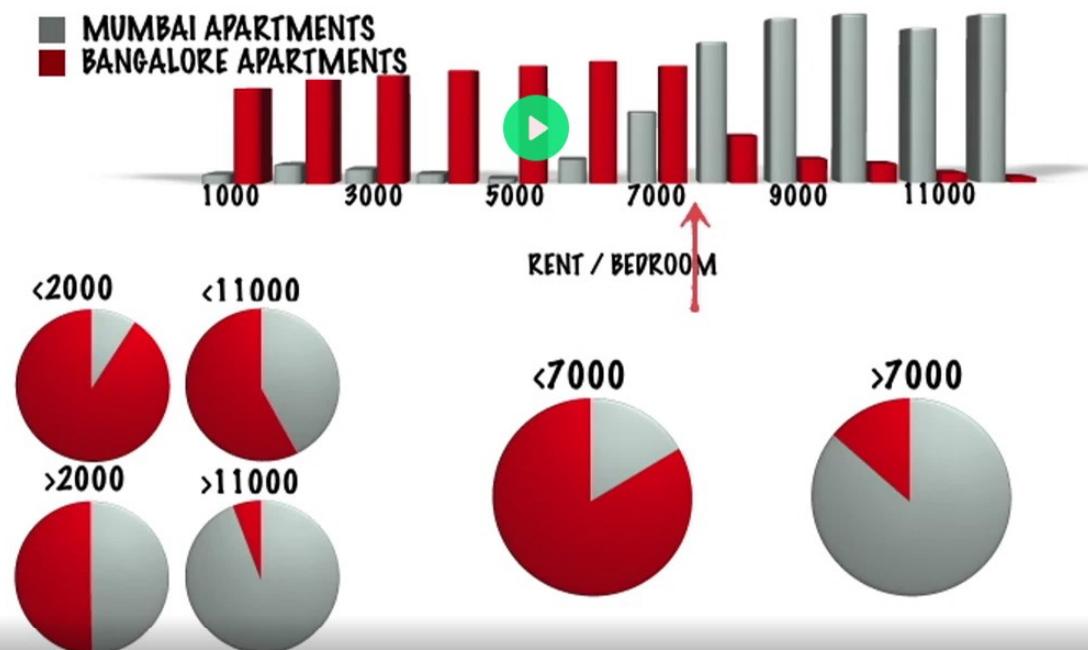
- All our subsets are mostly homogeneous
- We have run out of attributes
- The tree is too large

# The Best Split for a Continuous Input Variable



# The Best Split for a Continuous Input Variable

The point where the subsets we get are mostly homogeneous



## **Key takeaways from this chapter**

Building the Decision Tree : Decision Tree Learning

Consider the Dataset of Housing Units in a city with Rent, Type of Housing Unit and the city it is in, The year it was built

Recursive partitioning creates a decision tree that strives to correctly classify members of the population by splitting it into sub-populations based on several contrary independent variables.

-All our subsets are mostly homogeneous

-We have run out of attributes

-The tree is too large

The Stopping Condition could be

Choosing the best split for Continuous Input Variable is at the point where the subsets we get are mostly homogeneous.

Take the Housing Rent for Example we got that under and Above Rs.7000 we usually have homogeneous split between the cities.

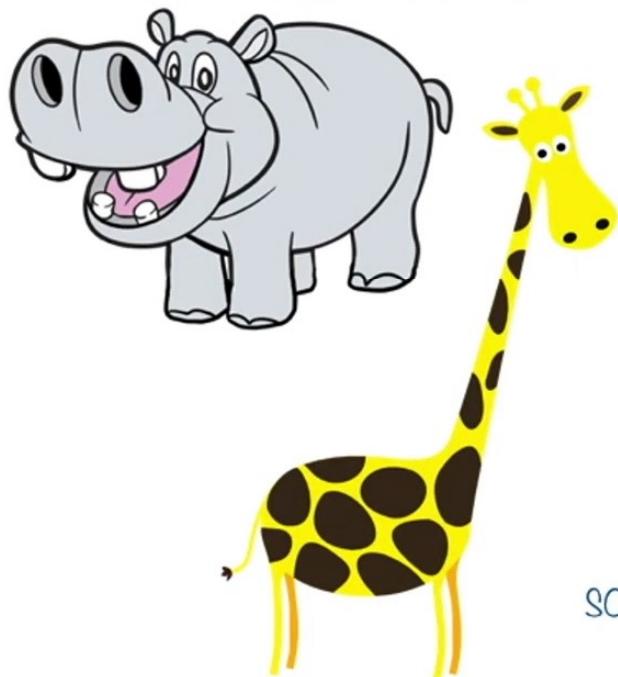
# Information Gain

ANY STATEMENT , NEWS OR MESSAGE  
CONTAINS INFORMATION

SOME HAVE MORE INFORMATION AND  
SOME LESS

THE IDEA OF INFORMATION GAIN IS TO REDUCE  
ENTROPY AND MAXIMIZE INFORMATION

LET'S SAY YOU HAVE TO CLASSIFY AN ANIMAL  
AS A GIRAFFE OR A HIPPO



IF YOU WERE TOLD, THIS ANIMAL HAS 4 LEGS

THIS IS BASICALLY USELESS! BOTH GIRAFFES AND  
HIPPOS HAVE 4 LEGS, SO THIS STATEMENT GIVES US  
NO INFORMATION

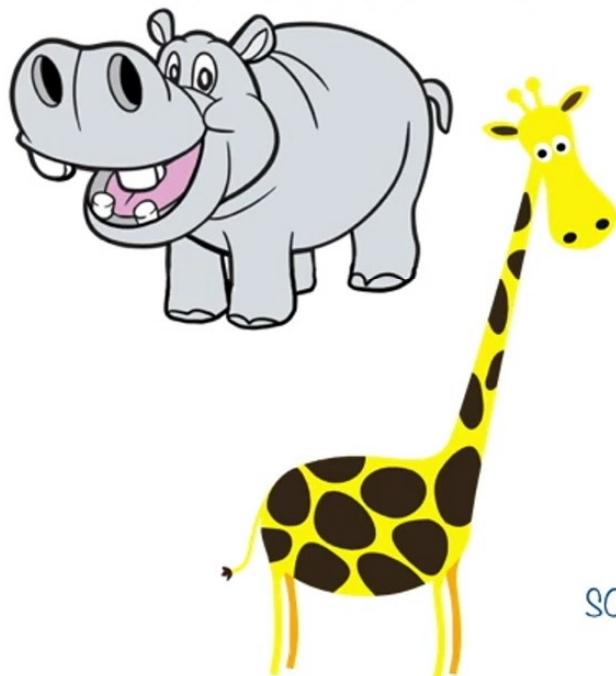
BUT IF YOU WERE TOLD, THIS ANIMAL IS 10 FEET TALL

**THIS IS USEFUL INFORMATION!**

IT TELLS YOU THAT THE ANIMAL IS  
VERY LIKELY A GIRAFFE

SO, CLEARLY - THE VALUES OF SOME ATTRIBUTES GIVE US **MORE**  
INFORMATION THAN OTHERS

LET'S SAY YOU HAVE TO CLASSIFY AN ANIMAL  
AS A GIRAFFE OR A HIPPO



IF YOU WERE TOLD, THIS ANIMAL HAS 4 LEGS

THIS IS BASICALLY USELESS! BOTH GIRAFFES AND  
HIPPOS HAVE 4 LEGS, SO THIS STATEMENT GIVES US  
NO INFORMATION

BUT IF YOU WERE TOLD, THIS ANIMAL IS 10 FEET TALL

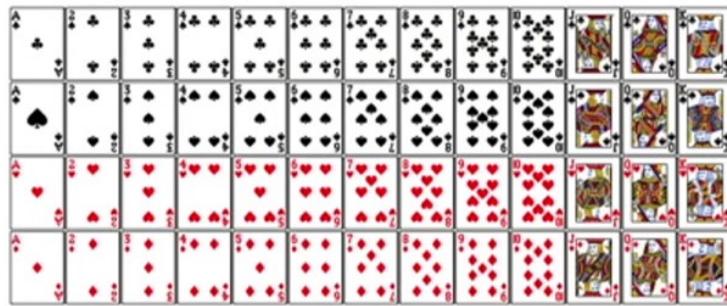
## THIS IS USEFUL INFORMATION!

IT TELLS YOU THAT THE ANIMAL IS  
VERY LIKELY A GIRAFFE

SO, CLEARLY - THE VALUES OF SOME ATTRIBUTES GIVE US MORE  
INFORMATION THAN OTHERS

AND THERE IS A MATHEMATICAL WAY TO MEASURE  
THIS INFORMATION

INITIALLY,  
THERE ARE  
52 POSSIBLE  
OUTCOMES IN  
ALL



LEFT WITH 4  
POSSIBLE  
OUTCOMES

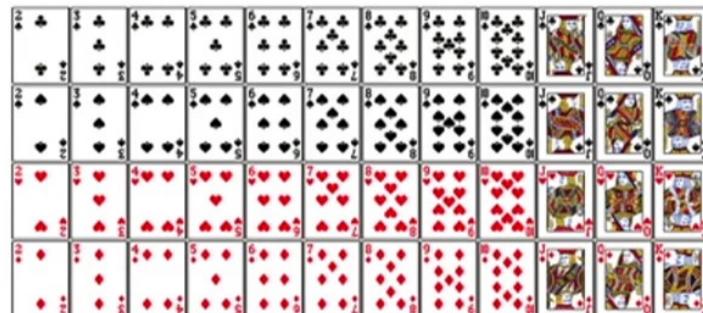


YES                  NO

THE ANSWER "YES"  
GIVES US MORE  
INFORMATION THAN  
THE ANSWER "NO"

YOU ASK  
IS THE CARD AN ACE?

LEFT WITH 48  
POSSIBLE  
OUTCOMES

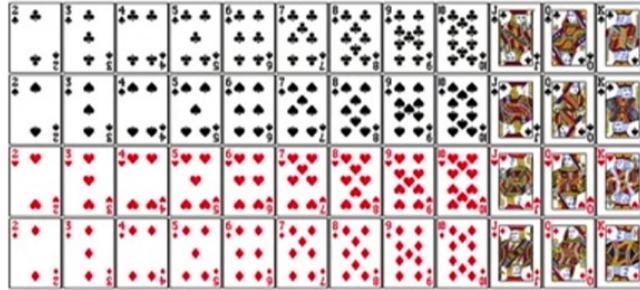


YES



$$P(\text{YES}) = 4/52$$

NO



$$P(\text{NO}) = 48/52$$

IS THE CARD AN ACE?

THE ANSWER "YES" GIVES  
US MORE INFORMATION  
THAN THE ANSWER "NO"

THE ANSWER "YES" HAS A LOWER  
PROBABILITY

IF X IS A RANDOM VARIABLE THAT  
REPRESENTS THE ANSWER TO OUR  
QUESTION

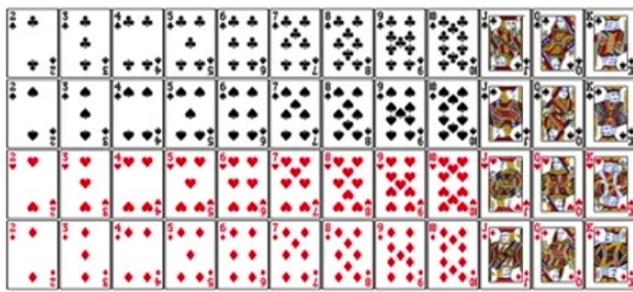
THE LOWER THE PROBABILITY OF  
THE ANSWER, THE MORE  
INFORMATION YOU GET

YES



$$P(\text{YES}) = 4/52$$

NO



$$P(\text{NO}) = 48/52$$

THE ANSWER "YES" HAS A LOWER  
PROBABILITY

IF  $X$  IS A RANDOM VARIABLE THAT  
REPRESENTS THE ANSWER TO OUR  
QUESTION

INFORMATION CONTENT OF  $(X=x)$  =  $-\log(P(X=x))$

IS THE CARD AN ACE?

THE ANSWER "YES" GIVES  
US MORE INFORMATION  
THAN THE ANSWER "NO"

THE LOWER THE PROBABILITY OF  
THE ANSWER, THE MORE  
INFORMATION YOU GET

INFORMATION CONTENT OF  $(X=\text{YES})$  =  $-\log(P(X=\text{YES}))$

INFORMATION CONTENT OF  $(X=\text{NO})$  =  $-\log(P(X=\text{NO}))$

# Information Gain

ANY STATEMENT , NEWS OR MESSAGE  
CONTAINS INFORMATION

SOME HAVE MORE INFORMATION AND  
SOME LESS

THE IDEA OF INFORMATION GAIN IS TO REDUCE  
ENTROPY AND MAXIMIZE INFORMATION

IF X IS A RANDOM VARIABLE THAT  
REPRESENTS THE ANSWER TO OUR  
QUESTION

INFORMATION CONTENT OF  $(X=x) = -\text{LOG}(P(X=x))$

AVERAGE VALUE OF THE INFORMATION  
CONTENT (ALSO CALLED THE EXPECTED  
VALUE)=  
 $\sum P(X=x) (-\text{LOG}(P(X=x)))$

ENTROPY  $H(X)$

ENTROPY IS THE AMOUNT OF  
UNCERTAINTY/UNPREDICTABILITY THERE  
IS IN THE ANSWER

ENTROPY INCREASES WITH  
NUMBER OF POSSIBLE ANSWERS  
2) THE EVENNESS OF THE PROBABILITY DISTRIBUTION

$P(\text{YES}) = 0 \Rightarrow$  THERE IS NO UNCERTAINTY  $\Rightarrow$  ENTROPY = 0

YES AND NO HAVE EQUAL PROBABILITY  $\Rightarrow$  VERY HIGH ENTROPY

IF X IS A RANDOM VARIABLE THAT  
REPRESENTS THE ANSWER TO OUR  
QUESTION

INFORMATION CONTENT OF  $(X=x) = -\text{LOG}(P(X=x))$

AVERAGE VALUE OF THE INFORMATION  
CONTENT (ALSO CALLED THE EXPECTED  
VALUE)=

$$\sum P(X=x) (-\text{LOG}(P(X=x)))$$

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ENTROPY IS THE AMOUNT OF  
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NUMBER OF POSSIBLE ANSWERS  
2) THE EVENNESS OF THE PROBABILITY DISTRIBUTION

$P(\text{YES}) = 0 \Rightarrow \text{THERE IS NO UNCERTAINTY} \Rightarrow \text{ENTROPY} = 0$

YES AND NO HAVE EQUAL PROBABILITY  $\Rightarrow$  VERY HIGH ENTROPY

INFORMATION CONTENT OF ( $X=x$ ) =  $-\text{LOG}(P(X=x))$

AVERAGE VALUE OF THE INFORMATION

**ENTROPY  $H(X)$**  = CONTENT (ALSO CALLED THE EXPECTED

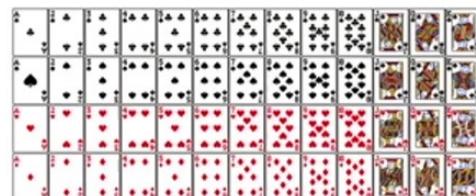
VALUE)=  $\sum P(X=x) (-\text{LOG}(P(X=x)))$

THE GAME IS TO ANSWER THE QUESTION

**WHICH CARD DO YOU HOLD?**

INITIALLY, THERE ARE  
52 POSSIBLE  
OUTCOMES IN ALL

EACH HAS SAME  
PROBABILITY =  $1/52$

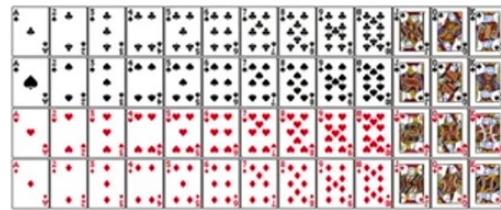


**ENTROPY=** $H(X)=$   
 $\sum (1/52)(-\text{LOG}(1/52)) =$   
 $\text{LOG}(52)$

THERE ARE 52  
POSSIBLE  
OUTCOMES IN ALL  
EACH HAS  
PROBABILITY = 1/52

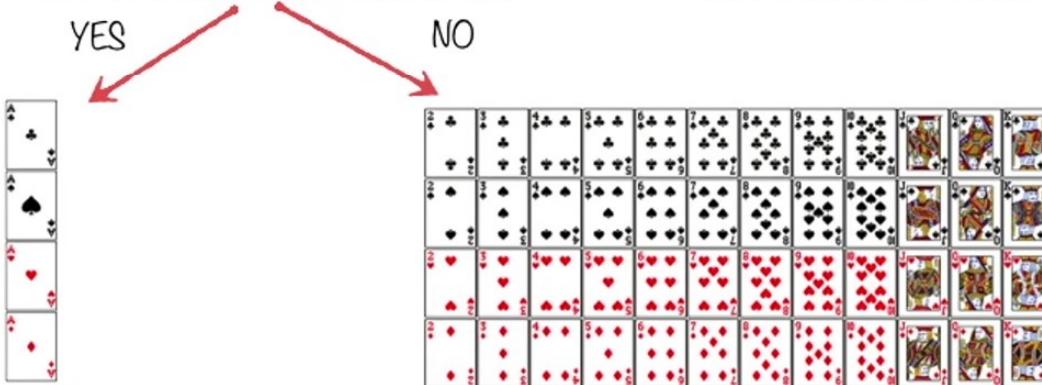
$$\text{ENTROPY} = \\ H(X/Q|Q=\text{YES}) = \\ \text{LOG}(4)$$

BEFORE WE HAVE ASKED ANY YES/NO QUESTIONS, THE  
UNCERTAINTY (ENTROPY) IN OUR GUESS IS VERY HIGH



$$\text{ENTROPY} = H(X) = \text{LOG}(52)$$

ONCE YOU ASK  
IS THE CARD AN ACE?



X

BEFORE WE HAVE ASKED ANY YES/NO QUESTIONS, THE  
UNCERTAINTY (ENTROPY) IN OUR GUESS IS VERY HIGH

$$\text{ENTROPY} = H(X) = \log(52)$$

ONCE YOU ASK IS THE CARD AN ACE?

$$\begin{aligned}\text{ENTROPY} &= \\ H(X/QI=\text{YES}) &= \\ \log(4) & \\ p(\text{YES}) &= 4/52\end{aligned}$$

$$\begin{aligned}\text{ENTROPY} &= \\ H(X/QI=\text{NO}) &= \\ \log(48) & \\ p(\text{NO}) &= 48/52\end{aligned}$$

$$\text{ENTROPY AFTER QI} = H(X/QI) =$$

$$p(\text{YES}) * H(X/QI=\text{YES}) + p(\text{NO}) * H(X/QI=\text{NO}) =$$

$$4/52 * \log(4) + 48/52 * \log(48)$$

BEFORE WE HAVE ASKED ANY YES/NO QUESTIONS, THE  
UNCERTAINTY (ENTROPY) IN OUR GUESS IS VERY HIGH

$$\text{ENTROPY} = H(X)$$

ONCE YOU ASK IS THE CARD AN ACE?

$$\text{ENTROPY AFTER Q1} = H(X/Q1)$$

INFORMATION GAIN =

REDUCTION IN  
ENTROPY  
OVERALL

$$= H(X) - H(X/Q1)$$

AS YOU SAW, WHENEVER YOU ASK A  
QUESTION, SUBSETS ARE FORMED

WHEN EACH OF THOSE SUBSETS ARE  
HOMOGENOUS, THE INFORMATION GAIN IS  
MAXIMUM

$$\text{ENTROPY} = H(X)$$

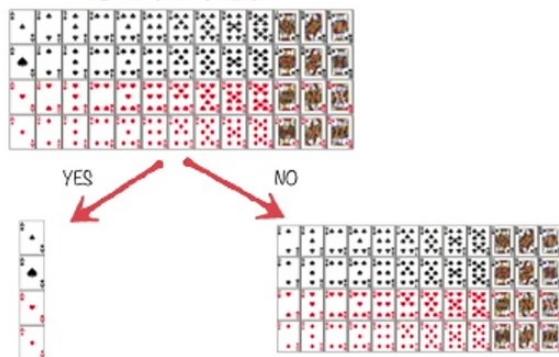
$$\text{ENTROPY AFTER QI} = H(X/QI)$$

AS YOU SAW, WHENEVER YOU  
ASK A QUESTION, SUBSETS ARE  
FORMED

$$\text{INFORMATION GAIN} = \frac{\text{REDUCTION IN ENTROPY}}{\text{OVERALL}} = H(X) - H(X/QI)$$

WHEN EACH OF THOSE SUBSETS ARE  
HOMOGENOUS, THE INFORMATION GAIN  
IS MAXIMUM

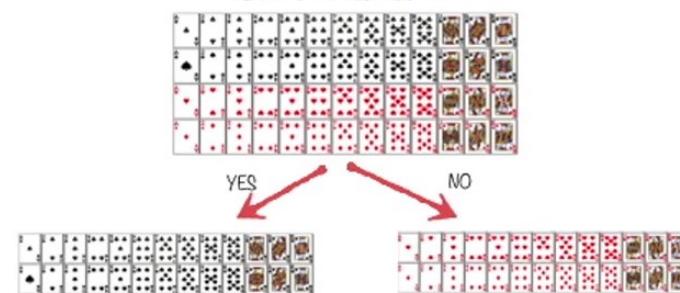
IS IT AN ACE?



$$H(X/QI) = 4/52 * \log(4) + 48/52 * \log(48)$$

$$IG = H(X) - H(X/QI) = 0.12$$

IS IT A BLACK?



$$H(X/QI) = \log(26)$$

$$IG = H(X) - H(X/QI) = \log(52) - \log(26) = 0.30$$

# Decision Tree Learning

- Recursive partitioning is the most common strategy for decision tree learning
- Decision tree learning algorithms
  - CART
  - ID3
  - C4.5
  - CHAID



# Decision Tree Learning

- Recursive partitioning is the most common strategy for decision tree learning
  - Decision tree learning algorithms
    - CART
    - ID3
    - C4.5
    - CHAID
- EACH HAS A SLIGHTLY DIFFERENT WAY OF ARRIVING AT THE BEST ATTRIBUTE (OR) MEASURING THE HOMOGENEITY OF A SUBSET

# Decision Tree Learning

- Recursive partitioning is the most common strategy for decision tree learning
- Decision tree learning algorithms
  - CART
  - ID3
  - C4.5
  - CHAID

INFORMATION GAIN

# Decision Tree Learning

- Recursive partitioning is the most common strategy for decision tree learning
- Decision tree learning algorithms

- **CART**

**GINI IMPURITY**

- ID3

- C4.5

- CHAID

CART IS ANOTHER DECISION TREE LEARNING METHOD  
(CLASSIFICATION AND REGRESSION TREES) IT USES A DIFFERENT WAY TO  
CHOOSE AN ATTRIBUTE

### MINIMIZING GINI IMPURITY

THE IDEA BEHIND, GINI  
IMPURITY IS SIMPLE



CHOOSE THE ATTRIBUTE SUCH THAT -  
IF YOU STOP THE DECISION TREE WITH  
THAT ATTRIBUTE AND GO NO FURTHER

THE PROBABILITY OF A FALSE LABEL IS  
MINIMIZED

## **Key takeaways from this chapter**

Building a Decision Tree - Information Gain a Gini Impurity

Entropy is the amount of Uncertainty/Unpredictability there is in the Answer.

The entropy typically changes when we use a node in a decision tree to partition the training instances into smaller subsets

Entropy increase with number of possible answers and the evenness of the probability distribution.

Entropy,  $H(X) = \sum -P(E)\log_2(P(E))$

Information gain is a measure of this change in entropy.

So in our case, it is the difference in entropy before the question is asked and after the question is asked.

Constructing a decision tree is all about finding an attribute that returns the highest information gain (i.e., the most homogeneous branches)

## **Key Takeaways from this chapter**

### Decision Tree Lab:Building our First Decision Tree

- 1) import pandas and numpy libraries
- 2) Download Datset file:<https://archive.ics.uci.edu/ml/machine-learning-databases/wine-quality/winequality-white.csv>
- # Even though the file comes with headers, we still specify them so that they are in our desired format
- use read\_csv and view the data
- 3)Since all the values are numeric we do not have to do encoding
- 4)import seaborn and matplotlib to plot he corelation heatmap
- 5) define x variable with all the available features except Quality and Y with just the labels
- 6)Use Split function to split using for training and testing.
- 7)Run the decision tree classifier in sklearn
- 8)print the accuracy of the trained model with respect to the test data

# Jupyter SVM-census Last Checkpoint: 14 hours ago



File Edit View Run Kernel Settings Help

Trusted

File + X □ ▶ ■ C ▶ Code ▾

JupyterLab ▾ Python 3 (ipykernel) ▾

```
[43]: import pandas as pd  
import numpy as np  
import math
```

⟳ ⌛ ⌂ ⌃ ⌄ ⌅ ⌆ ⌇

```
[10]: original_data=pd.read_csv("adult.csv",names =[ "Age", "Workclass", "fnlwgt", "Education", "Education-Num", "Marital Status", "Occupation", "Relationship",  
sep=r'\s*,\s*',  
engine='python',  
na_values="?")  
original_data.head()  
#sep -- may or not have white space
```

	Age	Workclass	fnlwgt	Education	Education-Num	Marital Status	Occupation	Relationship	Race	Gender	Capital Gain	Capital Loss	Hours per week	country	Target
0	39	State-gov	77516	Bachelors	13	Never-married	Adm-clerical	Not-in-family	White	Male	2174	0	40	United-States	<=50K
1	50	Self-emp-not-inc	83311	Bachelors	13	Married-civ-spouse	Exec-managerial	Husband	White	Male	0	0	13	United-States	<=50K
2	38	Private	215646	HS-grad	9	Divorced	Handlers-cleaners	Not-in-family	White	Male	0	0	40	United-States	<=50K

## **Key takeaways from this chapter**

Decision Tree Lab: Viewing and Tweaking our Decision Tree

- You can use `classifier.n_features_` attribute to view the number of features used in the decision tree.
- Tweak the `max_depth` attribute to observe the change in accuracy and minimise the size of the tree.
- You can use `tree.export_graphviz()` to output the decision tree as PNG file
- Tweak `max_features` to 4 has decreased the accuracy
- Specify Criterion As Entropy in order to use Information gain rather than Gini impurity to train the model and observe the accuracy against the test data.

Below are the 8 actual values of target variable in the train file.

[0,0,0,1,1,1,1,1]

What is the entropy of the target variable?

Options

- $(5/8 \log(5/8) + 3/8 \log(3/8))$

$5/8 \log(5/8) + 3/8 \log(3/8)$

$3/8 \log(5/8) + 5/8 \log(3/8)$

$5/8 \log(3/8) 3/8 \log(5/8)$

**For which of the following hyper parameters, higher value is better for decision tree algorithm?**

- 1)Number of samples used for split**
- 2)Depth of tree**
- 3)Samples for leaf**

**Options**

1 and 2

2 and 3

1 and 3

1, 2 and 3

Cant say

Following are the advantage/s of Decision Trees. Choose that apply.

#### Options

Possible Scenarios can be added

Use a white box model, If given result is provided by a model

Worst, best and expected values can be determined for different scenarios

All of the mentioned.

can't say.

Decision Trees can be used for Classification Tasks

Options

True

False

# Decision Tree is

## Options

Flow-Chart

Structure in which internal node represents test on an attribute, each branch represents outcome of test and each leaf node represents class label

Flow-Chart & Structure in which internal node represents test on an attribute, each branch represents outcome of test and each leaf node represents class label

None of the mentioned

Movie Recommendation systems are not a case of:

**Options**

Reinforcement learning

Regression

Clustering

Classification

Sentiment analysis is a natural language processing (NLP) technique used to determine and analyze the sentiment expressed in a piece of text. It involves classifying the text into categories such as positive, negative, or neutral, and sometimes into more nuanced categories like joy, anger, or sadness.

Sentiment Analysis is not an example of:

**Options**

Reinforcement learning

Regression

Clustering

Classification