

Introduction to Quantum Theory

* Hydrogen Spectra - classical theory

- Lyman, Balmer, Paschen, Brackett, Pfund \rightarrow Series of spectra
1 2 3 4 5

Rydberg's formula - $\frac{1}{\lambda} = R_H Z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$ $R_H = 1.097 \times 10^7 \text{ m}^{-1}$ - Energy conservation
Rydberg's constant

* Photo Electric Effect - Quantization

• $E_{\max} = h\nu - \phi = h(\nu - \nu_0) \rightarrow$ frequency decides energy of ejected e^-

$h =$ plank's constant $= 6.63 \times 10^{-34}$ units

* Blackbody Radiation

• Atoms vibrate with a frequency f , and they can exchange energy in multiples of hf , where h - plank's constant.

- Wein's Displacement Law $\rightarrow \lambda_m T = \text{constant} = 2898 \mu\text{m-K}$

Stefan-Boltzmann Law $\rightarrow P = \sigma A e T^4$; $\sigma = 5.67 \times 10^{-8}$ units

(3) Rayleigh-Jeans Law

• Given that mode density $N(\nu)d\nu = \frac{8\pi\nu^2}{c^3} d\nu$

By equipartition theorem, each mode has avg energy $\frac{1}{2} k_B T$

But the modes are caused due to vibration $(PE + KE) = 2 \times \frac{1}{2} k_B T = k_B T$

\therefore Energy density $= u(\nu)d\nu = \left[\frac{8\pi\nu^2}{c^3} \right] (k_B T)$

• Valid only for low ν , because we haven't considered that the atoms can emit/absorb only in multiples of $h\nu$.

* Planck's Law!

- Emission of energy takes place in discrete multiples of $h\nu$, and the probability that energy E is emitted is proportional to $e^{-E/k_B T}$.

$$P(E) \propto e^{-E/k_B T} \quad \text{— Boltzmann Distribution}$$

$$\Rightarrow \langle E \rangle = \frac{\sum e^{-nh\nu/k_B T} \cdot nh\nu}{\sum e^{-nh\nu/k_B T}} \Rightarrow \langle E \rangle = \frac{h\nu}{e^{\frac{h\nu}{k_B T}} - 1} \quad (\text{using GP and differential of GP})$$

- Using this, energy density $\Rightarrow u(\nu) = \frac{8\pi\nu^2}{c^3} \cdot \frac{h\nu}{e^{\frac{h\nu}{k_B T}} - 1}$

- Represent Planck's energy density as $u_P(\nu)$, Rayleigh-Jeans as $u_{RJ}(\nu)$

$$u_P(\nu) = u_{RJ}(\nu) \cdot \frac{h\nu/k_B T}{e^{\frac{h\nu}{k_B T}} - 1} \quad \rightarrow \text{Quantum Correction.}$$