The acados software package

Fast, embeddable solvers for nonlinear optimal control

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acados overview for new developers

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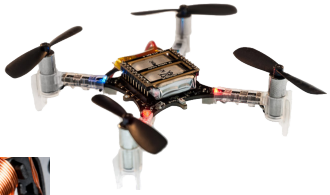
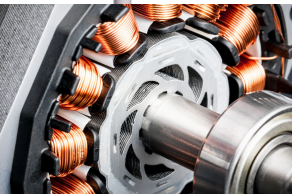
Workshop Outline

- Presentation
  - Introduction
  - acados optimal control problem formulation
  - Overview on acados
  - QP solvers
  - integration methods
  - Python interface
- Interactive Exercise / Demo Session

Intro





- Real world optimal control applications with
  - fast dynamics,
  - nonlinear optimal control problem formulations,
  - strict hardware limitations

  require tailored high-performance algorithms.
- acados implements such algorithms based on
  - Sequential Quadratic Programming (SQP)
  - Real-Time Iteration (RTI)
- Application projects include
  - Wind turbines
  - Drones
  - Race cars
  - Driving assistance systems
  - Electric drives (PMSM)

Continuous-time optimal control problem (OCP):

$$\begin{aligned} \underset{x(\cdot),z(\cdot),u(\cdot)}{\text{minimize}} \quad & \int_{t=0}^{T} \ell(x(t), z(t), u(t))\,\mathrm{d}t + M(x(T)) \\ \text{subject to} \quad & x(0) = \bar{x}_0, \\ & 0 = f(\dot{x}(t), x(t), z(t), u(t)), \quad t \in [0, T], \\ & 0 \geq g(x(t), z(t), u(t)), \qquad\quad t \in [0, T]. \end{aligned} \tag{1}$$

In MPC, instances of these problems are solved repeatedly, with current state $\bar{x}_0$.

OCP structured NLP handled in acados

$$\underset{\substack{x_0,\dots,x_N,\\ u_0,\dots,u_{N-1},\\ z_0,\dots,z_{N-1},\\ s_0,\dots,s_N}}{\text{minimize}} \quad \sum_{k=0}^{N-1} l_k(x_k,u_k,z_k) + M(x_N) + \sum_{k=0}^{N} \rho_k(s_k) \tag{2a}$$

$$\text{subject to} \quad \begin{bmatrix} x_{k+1} \\ z_k \end{bmatrix} = \phi_k(x_k,u_k), \qquad k=0,\dots,N-1, \tag{2b}$$

$$0 \geq g_k(x_k,z_k,u_k) - J_{\mathrm{s},k}s_k \quad k=0,\dots,N-1, \tag{2c}$$

$$0 \geq g_N(x_N) - J_{\mathrm{s},N}s_N, \tag{2d}$$

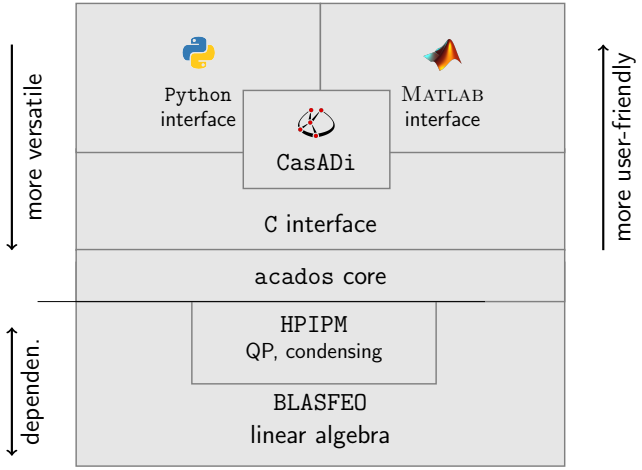
$$0 \leq s_k \qquad k=0,\dots,N. \tag{2e}$$

- ϕ_k – discrete time dynamics on $[t_k, t_{k+1}]$ – typically acados integrator from ODE or DAE
- l_k discrete version of Lagrange cost term ℓ on $[t_k, t_{k+1}]$
- slack variables s_k separate from controls – handled efficiently
- inequality constraints g_k
- problem functions can vary stage wise in C
- from high-level interfaces
  - initial and terminal shooting node handled separately – MHE support
  - parameters can be varied conveniently
- more detailed problem formulation can be found *here*.

Philosophy & History

- Solvers and interfaces for
  - OCP structured NLP (2)
  - Initial value problems for ODEs and DAEs – integrators
- Exploit block-sparse structure inherent in OCP / MHE formulation $\rightarrow$ specialized solver
- Successor of the `ACADO Toolkit`
  - Code generation for all parts of the SQP method
- Principles of `acados`
  - efficiency – `BLASFEO`, `HPIPM`, `C`
  - flexibility – general formulation
  - modularity – encapsulation
  - portability – self-contained `C` library with little dependencies
- Model functions code generation using `CasADi`
- Problem formulation in high-level interface (`Python`, MATLAB, `Octave`)
- Generate corresponding `C` code for problem specific solver
  - uses only `acados C` interface
  - first developed in `Python` interface
  - used for `S-function` generation – `Simulink` interface

Structure of the acados software



The interplay between the acados dependencies, the 'core' C library and its interfaces.

- BLASFEO: Basic Linear Algebra for Embedded Optimization
- HPIPM: High-Performance Interior Point Method

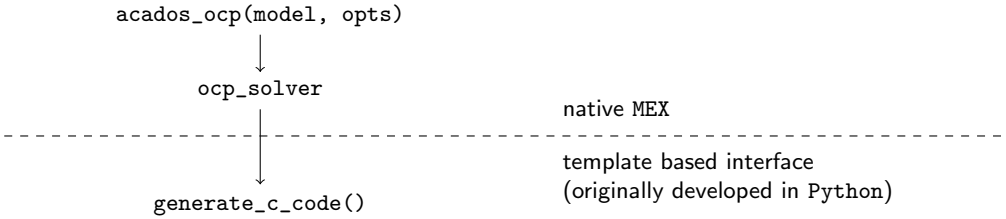
Template based Interfaces in Detail

1. problem specification & solver generation
   - defaults, model formulation, "easy" to specify OCP, IVP
   - Python: Classes with properties and setters
2. post process user input
   - detect dimensions
   - sanity checks
   - fill missing fields
   - dump description to `json` file
3. generate C solver + X
4. compile
5. create objects
6. interaction with solver
   - `get()`, `set()`, `solve()`

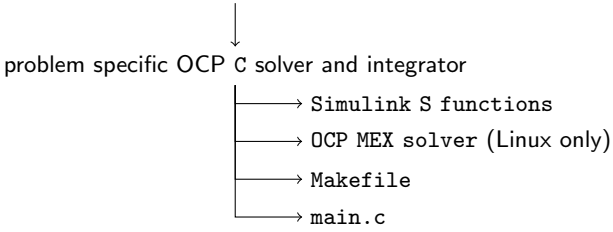
Generate C solver + X

- `CasADi` functions
- write model and options to `.json` file
- template based – `Tera` based templated files `https://tera.netlify.app/`
  - the problem specific solver (`*.c`, `*.h`) ♠
  - additional wrappers around ♠
    - minimal main, `Cython`, `Simulink`, `MEX` (Matlab, Octave), ROS?
  - build file: `Make`, `CMake`, Simulink: `make_sfun`, MEX make

MATLAB template based interface



- builds `ocp_json` object, mimicing acados OCP formulation in Python
- `ocp_json` → `.json` file



QP solver types and sparsity – an overview

	Active-Set	Interior-Point	First-Order
dense	qpOASES, DAQP	HPIPM	
sparse	[PRESAS]	CVXGEN, OOQP	FiOrdOs, OSQP
OCP structure	qpDUNES, [ASIPM]	HPMPC, HPIPM, [ASIPM], [FORCES]	

Table: Overview: QP solver types and their way to handle sparsity.
underline: available in acados + support in Simulink
gray: not interfaced in acados, [proprietary]

efficient condensing from HPIPM:

- condensing: OCP structured $\rightarrow$ dense, expand solution
- partial condensing: OCP structured with horizon $N \rightarrow$ OCP structured with horizon $N_2 < N$, expand solution, $N_2 \hat{=}$ qp_solver_cond_N

Integration methods in acados

- solve Initial Value Problems (IVP) for
  - Ordinary Differential Equations (ODE)
  - Differential-Algebraic Equations (DAE)
  - + sensitivity propagation (derivative of result with respect to initial state, control input)
- integrators in Python, are `'ERK'`, `'IRK'`, `'IRK_GNSF'`
- size of Butcher table: `sim_method_num_stages`
- time step is divided into `sim_method_num_steps` intervals, use the integration method on each interval
- ERK: explicit Runge-Kutta
  - integration order `sim_method_num_stages` $= 1, 2, 4$
- IRK: implicit Runge-Kutta
  - Gauss-Legendre Butcher tableaus
    - integration order $2 \cdot$ `sim_method_num_stages`, A-stable, but not L-stable
  - Gauss-Radau IIA
    - integration order is $2 \cdot$ `sim_method_num_stages` $- 1$, L-stable
- IRK_GNSF: structure-exploiting implicit Runge-Kutta method
  - Butcher tableaus as IRK
  - Detecting and Exploiting Generalized Nonlinear Static Feedback Structures in DAE Systems for MPC, J. Frey, R. Quirynen, D. Kouzoupis, G. Frison, J. Geisler, A. Schild, M. Diehl, ECC 2019

Python interface

- Continuous time formulation
  - Discretization flexible, cost multiplied with time step, nonuniform grid possible
- Model functions provided as `CasADi` expressions
- Template workflow
  - Model function and derivatives generated using `CasADi`
  - `C` code to set up the OCP solver using the `C` interface
  - `Makefile` to compile everything into a shared library
  - Shared library is loaded in `Python` and used via a wrapper
  - Generated solver can be used in alternative wrapper and embedded framework, `C++`, `ROS`

Important Ressources

- https://docs.acados.org/
  - Python API - documents all options in template interface: https://docs.acados.org/python_api
  - Installation instructions https://docs.acados.org/installation
- acados MATLAB problem formulation PDF: https://github.com/acados/acados/blob/master/docs/problem_formulation/problem_formulation_ocp_mex.pdf
- latest acados publication:
  acados – a modular open-source framework for fast embedded optimal control R. Verschueren, G. Frison, D. Kouzoupis, J. Frey, N. van Duijkeren, A. Zanelli, B. Novoselnik, T. Albin, R. Quirynen, M. Diehl Mathematical Programming Computation 2021
- acados forum https://discourse.acados.org
- Github examples https://github.com/acados/acados/tree/master/examples

Problem Shooting – OCP

- check OCP solver status, 0 – Success, other values defined in `types.h`
- `ocp_solver.print_statistics()`
  - KKT residuals: `stat` stationarity – Lagrange gradient, `eq`: equality constraints, `ineq`: inequality constraints, `comp`: complementarity
  - `qp_stat`: status of the QP solver, should be 0
  - `qp_iter`: number of iterations in QP solver
- initialization: `set()` – x, u, multipliers
- infeasibility: introduce slacks (soft constraints)
- check failing QP: `get_from_qp_in()`
- try different Hessian approximations: Definiteness & Exactness
  - `ocp.solver_options.hessian_approx = 'GAUSS_NEWTON'` or `'EXACT'`
  - Option to turn off exact hessian contributions from cost, constraints or dynamics
  - Set numerical approximation for cost hessian
  - add a Levenberg Marquardt term, `ocp.solver_options.levenberg_marquardt`
- iterates don't converge:
  - reduce the step size, `ocp_opts.set('step_size', alpha)` with `alpha` < 1.
  - globalization (preliminary implementation) of a merit function based backtracking:
    - `ocp.solver_options.globalization = 'FIXED_STEP'` or `'MERIT_BACKTRACKING'`
    - Second order correction: set `globalization_use_SOC` to 1
    - Armijo condition: set `line_search_use_sufficient_descent` to 1.