

# DIGITAL LOGIC

TM

## Chapter - 1 : Number Systems

- Q.1** Consider n-bit (including sign bit) 2's complement representation of integer numbers. The range of integer value N, that can be represented is  $-2^{n-1} \leq N \leq 2^{n-1} - 1$ . [GATE : 1994]
- Q.2** The number of 1's in the binary representation of  $(3 \times 4096 + 15 \times 256 + 5 \times 16 + 3)$  is [GATE : 1994]  
(A) 8 (B) 9 (C) 10 (D) 12
- Q.3** The number 43 in 2's complement representation is [GATE : 2000]  
(A) 01010101 (B) 11010101 (C) 00101011 (D) 10101011
- Q.4** The decimal value 0.25 [GATE : 2002]  
(A) Is equivalent to binary value 0.1 (B) Is equivalent to binary value 0.01  
(C) Is equivalent to binary value 0.00111..... (C) Can not be represented precisely in binary
- Q.5** The 2's complement representation of the decimal value - 15 is [GATE : 2002]  
(A) 1111 (B) 11111 (D) 111111 (E) 10001
- Q.6** Assuming all numbers are in 2's complement representation, which of the following numbers is divisible by 11111011? [GATE : 2003]  
(A) 11100111 (B) 11100100 (C) 11010111 (D) 11011011
- Q.7** If  $73_x$  (in base - x number system) is equal to  $54_y$  (in base - y number system), the possible values of x and y are [GATE : 2004]  
(A) 8, 16 (B) 10, 12 (C) 9, 13 (D) 8, 11
- Q.8** The range of integers that can be represented by an n bit 2's complement number system is: [GATE : 2005]  
(A)  $-2^{n-1}$  to  $+(2^{n-1} - 1)$  (B)  $-(2^{n-1} - 1)$  to  $(2^{n-1} - 1)$   
(C)  $-2^{n-1}$  to  $2^{n-1}$  (D)  $-(2^{n-1} + 1)$  to  $(2^{n-1} - 1)$
- Q.9** The hexadecimal representation of  $657_8$  is: [GATE : 2005]  
(A) 1AF (B) D78 (C) D71 (D) 32F

- Q.10 Let  $r$  denote number system radix. The only value(s) of  $r$  that satisfy the equation  $\sqrt{121}_r = 11_r$  is/are  
 $\sqrt{1+2r+r^2} = 1+r$  [GATE : 2008]  
 (A) Decimal 10 (B) Decimal 11 (C) Decimal 10 and 11 (D) Any value  $> 2$
- Q.11  $(1217)_8$  is equivalent to [GATE : 2009]  
 (A)  $(1217)_{16}$  (B)  $(028F)_{16}$  (C)  $(2297)_{10}$  (D)  $(0B17)_{16}$
- Q.12 The smallest integer that can be represented by an 8-bit number in 2's complement form is [GATE : 2013]  
 (A) -256 (B) -128 (C) -127 (D) 0
- Q.13 The base (or radix) of the number system such that the following equation holds is  $\frac{312}{20} = 13.1$   
 $478 \leftarrow x=5 \leftarrow \frac{3x^2 + x + 2}{2x + 3 + \frac{1}{x}} = \frac{3 \cdot 5^2 + 5 + 2}{2 \cdot 5 + 3 + \frac{1}{5}} = \frac{78}{13.1} = 6$  [GATE : 2014]
- Q.14 Consider the equation  $(123)_5 = (x8)_y$ , with  $x$  and  $y$  as unknown. The number of possible solutions is  
 $\frac{3}{25+10+3} = \frac{x}{y+8} \Rightarrow xy = 30$  [GATE : 2014]
- Q.15 The 16-bit 2's complement representation of an integer is 1111 1111 1111 0101; its decimal representation is [GATE : 2016]
- Q.16 Let  $X$  be the number of distinct 16-bit integers in 2's complement representation. Let  $Y$  be the number of distinct 16-bit integers in sign magnitude representation. Then  $X-Y$  is [GATE : 2016]  
 $2^n - (2^n - 1) = 1$
- Q.17 The representation of the value of a 16-bit unsigned integer  $X$  in hexadecimal number system is BCA9. The representation of the value of  $X$  in octal number system is [GATE : 2017]  
 (A) 571244 (B) 736251 (C) 571247 (D) 136251
- Q.18 Consider the number given by the decimal expression. [GATE : 1991]  
 $16^3 \times 9 + 16^2 \times 7 + 16 \times 5 + 3 \rightarrow (9753)_{16} \rightarrow (1001011101010011)_2$   
 The number of 1's in the unsigned binary representation of the number is 9
- Q.19 Given  $\sqrt{(224)_r} = (13)_r$ , [GATE : 1997]  
 $\Rightarrow \sqrt{2r^2 + 2r + 4} = r + 3$   
 $r^2 + r - 5 = 0 \Rightarrow r = 2, 5, -1$   
 The value of the radix  $r$  is : (A) 10 (B) 8 (C) 5 (D) 6
- Q.20 Zero has two representations in : [GATE : 1999]  
 (A) Sign magnitude (B) 1's complement (C) 2's complement (D) None of the above