

Q 11. for (I=1 ; I<=n ;I ++)
for (J=1 ; J<= I ; J++)
printf(“pankaj”);

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for (i = 1 ; i <= n ; i++)

for (j = 1 ; j <= i ; j++)

printf ("Pankaj");

$$\sum_{i=1}^n \sum_{j=1}^i 1 = \sum_{i=1}^n i$$

$$= \frac{n(n+1)}{2}$$

Ans

Q 12. for (I=1 ; I<=n ; I =I*2)
 for (J=1 ; J<= I ; J++)
 for(K=1 ; K<=10 ; K++)
 printf("pankaj");

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for (i = 1; i <= n; i = i * 2) {

for (j = 1; j <= i; j++) {

printf("panka %d", j);

for (k = 1; k <= 10; k++) → $\frac{\log_2 n}{2} + 1$

printf("panka %d", k);

$$= \left(\frac{\log_2 n}{2} + 1 \right) \times 55$$

Q 13. for (I=1 ; I<=n ;I ++)
 for (J=1 ; J<= I * I ; J++)
 for(K=1 ; K<=n ; K++)
 printf(“pankaj”);

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for (i=1; i<=n; i++)

for (j=1; j<=n; j++)

for (k=1; k<=n; k++)

printf("Pankaj");

$$\sum_{i=1}^n \sum_{j=1}^{i^2} \sum_{k=1}^n 1 = \sum_{i=1}^n \sum_{j=1}^{i^2} 1 \cdot n$$

$$= \sum_{i=1}^n (n + n + \dots + (i^2 - 1 + 1))$$

$$= n \sum_{i=1}^n i^2$$

$$= \frac{n^2 (n+1) (2n+1)}{6}$$

Q 14. for (I=1 ; I<=n ;I++)
 for (J=I ; J<= 3*I ; J++)
 printf(“pankaj”);

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for (i=1; i<=n; i++)  
    for (j=1; j<=3*i; j++)  
        printf("Pankaj");
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$$\sum_{i=1}^n \sum_{j=1}^{3i} 1 = \sum_{i=1}^n (2i+1) = \frac{2n(n+1)}{2} + n$$

$$= \boxed{n^2 + 2n}$$

Q 15. for (I=1 ; I<=n ;I=I*3)
for (J=I ; J<= n ; J++)
printf(“pankaj”);

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for (i=1; i<=n; i=i*3)
    for (j=1; j<=n; j++)
        printf("Pankaj ");
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$$\begin{aligned} \text{No.} &= (n-1) + 1 + (n-3) + 1 + \dots + (n-3^{k-1}) + 1 \\ &= (n+1)(k+1) - \frac{3^{k+1} - 1}{3 - 1} \end{aligned}$$

$$= \left(\left\lfloor \log_3 n \right\rfloor + 1 \right) (n+1) + \frac{3^{\left\lfloor \log_2 n \right\rfloor + 1} - 1}{2}$$

Q 16. for (I=0 ; I<=n-1 ; I ++)
 for (J=2 ; J<= I + 1 ; J++)
 for(K=J + 1 ; K<=I + J ; K++)
 printf(“pankaj”);

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 for (i = 1; i <= n; i++)
 for (j = 2; j <= i; j++)
 for (k = j + 1; k <= i; k++)
 printf("Parkaj")

$$\sum_{i=1}^n \sum_{j=2}^{i-1} \sum_{k=j+1}^{i-1} 1 \neq \sum \sum i$$

$$= \sum ((i+1) - 2 + 1) \times 1$$

$$= \sum i^2$$

$$= \frac{n(n+1)(2n+1)}{6}$$

Q 17. for (I=1 ; I<=n ;I ++)
 for (J=1 ; J<= I ; J++)
 for(K=J ; K<=I + J ; K++)
 printf("pankaj");

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for (i=1; i<=n; i++)

for (j=1; j<=i; j++)

for (k=1; k<=i+j; k++)

printf("Pankaj");

$$\sum_{i=1}^n \sum_{j=1}^i \sum_{k=1}^{i+j} 1 = \sum_{i=1}^n \sum_{j=1}^i (i+j+1)$$

$$= \sum_{i=1}^n \sum_{j=1}^i (i+j)$$

$$= \sum_{i=1}^n (i-1+1)(i+1)$$

$$= \sum_{i=1}^n i^2 + 1$$

$$= \frac{n(n+1)}{2} + \frac{2n+1}{3}$$

Ans

Q 18. for (I=1 ; I<=n ; I++)
 for (J=I ; J<=2*I ; J++)
 printf("pankaj");

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for ($i = 1$; $i \leq n$; $i++$)

for ($j = 1$; $j \leq 2i$; $j++$)

printf("Pankaj ");

$$\sum_{i=1}^n \sum_{j=1}^{2i} 1 = \sum_{i=1}^n (i + i)$$

$$= \frac{n(n+1)}{2}$$

Q 19. for (I=1 ; I<=n ; *I*++)
 for (J=I +1 ; J<=n ; J++)
 for (K=1 ; K<=J ; K++)
 printf("pankaj");

19-8 for (i=1; i<=n; i++)
 for (j=i+1; j<=n; j++)
 for (k=1; k<=j; k++)
 printf("paukqj");

$$\sum_{i=1}^n \sum_{j=i+1}^n \sum_{k=1}^j 1 = \sum_{i=1}^n \sum_{j=i+1}^{n-i} j$$

$$= (i+1) + (i+2) + \dots + n$$

$$= \frac{n(n+1)}{2} - \frac{i(i+1)}{2}$$

$$= \sum_{i=1}^n \frac{n(n+1)}{2} - \sum_{i=1}^n \frac{i(i+1)}{2}$$

$$= \frac{n^2(n+1)}{2} - \frac{1}{2} \times \frac{n(n+1)(n+1)}{6} = \frac{n^2(n+1)}{2} - \frac{n(n+1)^2}{12}$$

$$= \frac{n(n+1)(n-1)}{3}$$

Q 20. What is the total number of multiplication : $D=2$;
for ($I=1$; $I \leq n$; $I++$)
 for ($J=I$; $J \leq n$; $J++$)
 for ($K=J+1$; $K \leq n$; $K++$)
 $D=D * 3$;

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for ($i = 1; i \leq n; i++$)

for ($j = 1; j \leq n; j++$)

for ($k = j+1; k \leq n; k++$)

$$O(n^3)$$

$$\sum_{i=1}^n \sum_{j=1}^n \sum_{k=j+1}^n (1) = \sum_{i=1}^n \sum_{j=1}^{(n-i)}$$

$$= (n-i) + (n-i-1) + \dots + 1$$

$$= 1 + 2 + \dots + (n-i)$$

$$= \frac{(n-i)(n-i+1)}{2}$$

$$\sum_{i=1}^n \frac{1}{2} (n^2 + i^2 - 2in + n - i)$$

$$= \frac{1}{2} \left[\sum n^2 + \sum i^2 - \sum 2in + \sum n - \sum i \right]$$

$$= \frac{1}{2} \left[\frac{n^2 n(n+1)(2n+1)}{6} - \frac{2n^2(n+1)}{2} + n^2 - \frac{n(n+1)}{2} \right]$$

$$= \frac{1}{2} \left[\frac{n(n+1)(2n+1)}{6} - \frac{n(n+1)}{2} \right]$$

$$= \frac{n(n+1)}{12} [2n+1-3]$$

$$= \frac{n(n+1)(n-1)}{6}$$

Teacher's Signature