

44 →

12

$$R = \begin{bmatrix} 1 & 2 & 4 & 8 \\ 1 & 3 & 9 & 27 \\ 1 & 4 & 16 & 64 \\ 1 & 5 & 25 & 125 \end{bmatrix}$$

Product of Eigen Value of R

Solⁿ

$$\begin{bmatrix} 1 & 2 & 4 & 8 \\ 0 & 3-2 & 3^2-2^2 & 3^3-2^3 \\ 0 & 4-2 & 4^2-2^2 & 4^3-2^3 \\ 0 & 5-2 & 5^2-2^2 & 5^3-2^3 \end{bmatrix}$$

$$= (3-2)(4-2)(5-2) \begin{bmatrix} 1 & 2 & 2^2 & 2^3 \\ 0 & 1 & 3+2 & 19 \\ 0 & 1 & 4+2 & 28 \\ 0 & 1 & 5+2 & 39 \end{bmatrix}$$

$$= 1 \times 2 \times 3 \times \begin{bmatrix} 1 & 5 & 19 \\ 0 & 1 & 9 \\ 0 & 2 & 20 \end{bmatrix}$$

$$= 1 \times 2 \times 3 \times 2$$

→ Eigen Values

$$= \underline{\underline{12}} \text{ Ans}$$

45 →

160

Total time to transfer = $1 + 3 + 8 = 12$ cycles
8 W ————— 12 cycles
8 x 4 bytes ————— 12 cycles

$$\frac{\text{in 1 sec}}{\text{}} = \frac{32 \text{ B}}{12 \times \left(\frac{1}{60} + 10^{-6} \right) \text{ sec}}$$

$$= 160 \times 10^6 \text{ bytes/sec}$$

Ans

46 →

T → 8 levels Full Binary Tree

4.857

choose two leaf a & b at random.
Distance b/w a & b in T. is —

Solⁿ

Select two node — ${}^8C_2 = 28 \text{ ways}$

X	2	4	6
P(X)	$\frac{4}{28}$	$\frac{8}{28}$	$\frac{16}{28}$

$$E(X) = 2 \left(\frac{4}{28} \right) + 4 \left(\frac{8}{28} \right) + 6 \times \left(\frac{16}{28} \right)$$

$$= \frac{8 + 32 + 96}{28} = \frac{136}{28}$$

$$= 4.857$$

Ans

47

Suppose X distributed uniformly in the open interval $(1, 6)$. The probability that the polynomial $3x^2 + 6xY + 3Y + 6$ has only real root is

Solⁿ

$$3x^2 + (6Y)x + (3Y+6)$$

$$b^2 - 4ac \geq 0$$

$$(6Y)^2 - 4 \times 3 \times (3Y+6) \geq 0$$

$$Y^2 - Y + 2 \geq 0$$

$$Y \in (-\infty, -1] \cup [2, \infty)$$

$$Y \in [2, 6)$$

Y distributed — $(1, 6)$

$$f(Y) = 1/5, \quad 1 < Y < 6$$

$$P(2 \leq Y < 6) = \int_2^6 f(Y) dY$$

$$= \frac{1}{5} [Y]_2^6$$

$$= \frac{4}{5}$$

$$= 0.8 \text{ Ans}$$

48 Σ is set of bijection - $\{1, \dots, 5\}$ to $\{1, \dots, 5\}$
 $id(j) = j, \forall j$
 $x = x_1 x_2 \dots x_n \in \Sigma^n, n \geq 0$

120

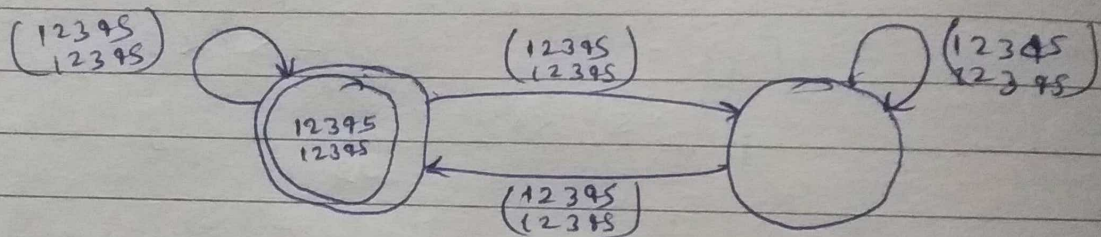
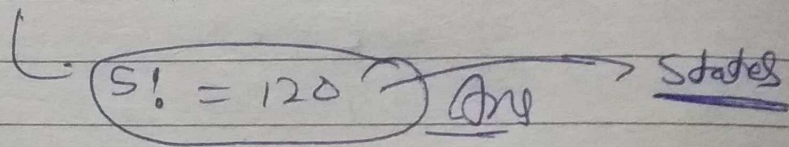
$$\pi(x) = x_1 \circ x_2 \circ x_3 \circ \dots \circ x_n$$

$$L = \{x \in \Sigma^* \mid \pi(x) = id\}$$

minimum no. of state in any DFA accept L

Solⁿ

DFA accept L will have



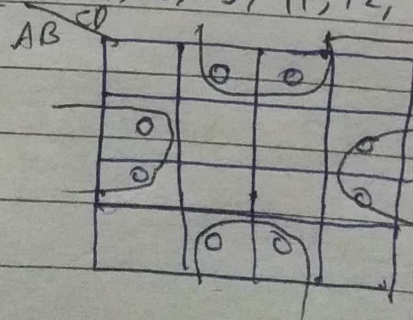
49

50 Minimum no. 2 i/p NOR gate

3 Ans $f = \Sigma (0, 2, 5, 7, 8, 10, 13, 15)$

Assume all element & their complement available

Solⁿ $F = \Pi (1, 3, 4, 6, 9, 11, 12, 14)$



$$B + \bar{D}$$

$$\bar{B} + D$$

$$f = (B + \bar{D})(\bar{B} + D)$$

3 NOR GATE

51 →

5

Student	
Roll-No.	Student-Name
1	Amit
2	Priya
3	Vinit
4	Rohan
5	Smita

Performance		
Roll-No.	Sub-Code	Marks
1	A	86 ✓
1	B	95 ✓
1	C	90 ✓
2	A	89 ✓
2	C	92 ✓
3	C	88 ✓

SQL-

```
SELECT S.Student-Name, sum(P.Marks)
FROM Student S, Performance P
WHERE P.Marks > 89
GROUP BY S.Student-Name;
```

Return No. of rows.

→ 5 Ans

52 →

```
#include <stdio.h>
```

```
int main() {
```

```
float sum = 0.0, j = 1.0, i = 2.0;
```

```
while (i/j > 0.0625)
```

```
    j = j + j;
```

```
    sum = sum + i/j;
```

```
    printf("%f \n", sum);
```

```
} return 0; }
```

No. of times sum printed = 5 Ans

53

#include <stdio.h>

int main()

{ int a[] = {2, 4, 6, 8, 10};

int i, sum = 0, *b = a + 4;

for (i = 0; i < 5; i++)

sum = sum + (*b - i) - *(b - i);

printf("%i", sum);

return 0;

}

→ 0/p = 10 Ans

54

In an RSA, public modulus parameters $n = 3007$,
 $\phi(n) = 2880$, prime factor of n greater than 50

Soln

$$n = p \times q = 3007$$

$$\phi(n) = (p-1)(q-1) = 2880$$

using RSA algo

$$n = 31 \times 97 = 3007$$

→ greater than 50 → 31
97

So

97

Ans

55 ⇒

1

P			Q			R	
X	Y	Z	X	Y	T	Y	V
x ₁	y ₁	z ₁	x ₂	y ₁	2	y ₁	v ₁
x ₁	y ₁	z ₂	x ₁	y ₂	5	y ₃	v ₂
x ₂	y ₂	z ₂	x ₁	y ₁	6	y ₂	v ₃
x ₂	y ₄	z ₄	x ₃	y ₃	1	y ₂	v ₂

How many tuples returned ~

$$\Pi \left(\sigma_{(P.Y = R.Y \wedge R.V = V_2)} (P \times R) \right) - \Pi \left(\sigma_{(Q.Y = R.Y \wedge Q.T = 2)} (Q \times R) \right)$$

$$\frac{\text{Set}^n}{2} = \frac{X}{x_2} = \frac{X}{x_1}$$

$$\Rightarrow \frac{X}{x_2}$$

No of tuples in 1st is 1 Are