

Time! 1 hour

Attempt all Questions

Q. 1

Evaluate  $\int_0^{\frac{\pi}{2}} \sqrt{\cos \theta} d\theta$  using Simpson's  $\frac{1}{3}$  rule by taking 9 ordinates.

Q. 2

Using Runge-Kutta method of fourth order, solve

$$\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2} \text{ with } y(0) = 1 \text{ at } x = 0.2, 0.4$$

Q. 3

fit a second degree parabola  $y = a + bx + cx^2$  in the following data  $(x; y)$ :  $(-1, 2), (0, 0), (0, 1), (1, 2)$

Q. 4

Suppose that  $f(x) = \sin x$  to be approximated on  $[0, 1]$  by an interpolating polynomial on  $n+1$  equally spaced points. What step size  $h$  ensure that linear interpolation gives an absolute error of at most  $10^{-6} \forall x \in [0, 1]$