Summer Internship Project Report

Formal verification of programs with pointers

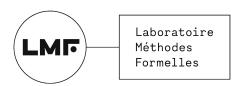
Submitted by

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1 Introduction

1.1 The Laboratoire Méthodes Formelles (LMF)

LMF is a joint research centre of University Paris-Saclay, CNRS, ENS Paris-Saclay, Inria, and CentraleSupélec. it's divided to multiple departments interested in various topics such as type systems, topology and quantum computing. My research project took place within Toccata's team of the formal methods department. I worked on verification of programs with pointers under the supervision of Jean-Cristophe Filliâtre, Arnaud Golfouse and Paul Patault.

There are multiple verification tools widely used and developed at the LMF research center. Among these tools, we find Creusot and Why3.

1.2 Le langage de preuve Creusot

1.2.1 Introduction

CREUSOT is a formal verification language used to verify RUST code. It checks the safety of code against compile-time errors and runtime panics, integer overflows, and, more importantly, the logical correctness of the code, ensuring it adheres to its specifications.

CREUSOT operates on top of Why3 indirectly by translating Rust code into an intermediate verification language known as Coma. It facilitates the verification, and it also gives Creusot access to the full access to Why3's features.

Below is a simple example of CREUSOT code that verifies the correctness of the SUM_FIRST_N function.

```
1
    extern crate creusot_contracts;
2
    use creusot_contracts::*;
3
    #[requires(n@ * (n@ + 1) / 2 < u32::MAX@)]
4
    #[ensures(result0 == n0 * (n0 + 1) / 2)]
5
    pub fn sum_first_n(n: u32) -> u32 {
6
         let mut sum = 0;
7
         #[invariant(sum@ * 2 == produced.len() * (produced.len() + 1))]
8
         for i in 1..=n {
9
             sum += i;
10
        }
11
12
         sum
    }
13
```

Figure 1: Creusot verification example: sum of first n natural numbers

Explanation:

The function SUM_FIRST_N shown above computes the sum of the first n natural numbers. The expressions highlighted in yellow represent its specification:

- **Precondition:** It asserts that the sum of the first n natural numbers where n is provided as a parameter, does not overflow the capacity of the result type. This ensures that the final sum, which will be stored in the return variable will not exceed the capacity of the return type. The operator @ converts machine integers into mathematical integers, which are unlimited, allowing us to use arithmetic theory.
- Postcondition: It states that the returned result is equal to the expected mathematical value: n * (n + 1) / 2
- Loop invariant: The expression produced.len() corresponds to the number of iterations performed so far, it effectively can play the role of the loop index by applying a transformation.

The reason we cannot refer directly to the loop index is due to scoping limitations.

1.2.2 Ghost code in CREUSOT

Rust's ownership and borrowing principles make it difficult to use pointers in proofs. where the need for a notion of ghost code in such a language. Ghost code allows us to perform proofs that are not possible using only raw code and the logical world, especially when dealing with existential quantification, if we know how to construct the value we are seeking for the existential quantifier.

Recently, ghost code has been introduced in CREUSOT. The subtlety lies in the fact that ghost code is separate from the original code. Therefore, it can be safely erased at compile time, allowing only the original code and the corresponding logical formulas to be executed. This results in faster and safer proof verification. Below are some examples of how to write ghost code in CREUSOT.

2 State of art

2.1 Reynolds article

Reynolds' article introduced a new concept in formal program verification: Separation Logic, an extension of Hoare Logic that facilitates automatic proofs on low-level imperative programs that use shared mutable data structures, by reasoning about disjoint parts of the heap. It greatly simplifies the formalization and verification of many problems that are otherwise difficult to handle using traditional Hoare Logic, such as concurrency, memory management, and aliasing.

Reynolds is particularly interested in the in_place_reversal† algorithm. He frequently discusses it in his research, as it is a very interesting algorithm for exploring formal proofs on mutable data structures with pointers.

To prove properties of algorithms on data structures, it's usually not enough to rely only on the program's representation. We often build a logical model of the data and connect it to the program state using predicates. It's better if the logical model is inductive, because provers generally work better with inductive data structures, for instance, the intuitive logical modeling of lists are sequences, therefore we can write the following predicate to represent a list:

$$list \epsilon i \stackrel{\text{def}}{=} i = nil \tag{1}$$

$$\mathtt{list}\;(a.\alpha)\;\mathtt{i}\stackrel{\mathrm{def}}{=}\;\exists\;\mathtt{j},\;\mathtt{list}\;\alpha\;\mathtt{j}\wedge\;\mathtt{i}\hookrightarrow\mathtt{a} \tag{2}$$

 $i \hookrightarrow a$ means i points to a

We can generalize the definition of a list to list segments by passing a tuple of pointers instead of a single one. In this case, the first pointer represents the head of the sub-list, and the second pointer represents the queue of the sub-list.

One of key uses of separation logic can be show in case if we prohibit using in_place_reversal† on shared data structures, in this context, given the following precondition for in-place reversal: list $p \alpha$, the post-condition list $p \overline{\alpha}$ is not sufficient to ensure the correctness of the algorithm. consider the example in the figure below.

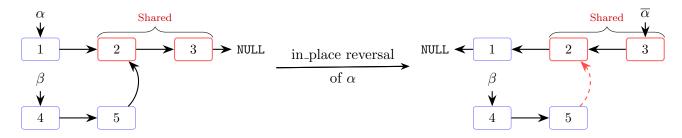


Figure 2: in_place reversal on shared lists

So we need to provide a stronger precondition that prevents such cases. One possible way is:

list p
$$\alpha \land \forall x, \alpha'$$
. list $x \alpha' \rightarrow \text{conflicting}(x, \alpha', p, \alpha) \rightarrow x = \text{nil}$

where conflicting (p: Pointer) (seq: Sequence) (p': Pointer) (seq': Sequence) is a predicate that returns True if the two provided lists share any nodes. It is defined as follows:

conflicting p emp p'
$$\alpha' \stackrel{\text{def}}{=} (p = \text{nil})$$
 (3)

conflicting
$$p \alpha p' emp \stackrel{\text{def}}{=} (p' = nil)$$
 (4)

conflicting p
$$(a.\alpha)$$
 p' $(a'.\alpha') \stackrel{\text{def}}{=} (p = p') \lor$

conflicting p
$$\alpha$$
 [p'+1] $\alpha' \vee$ conflicting [p+1] α p' α' (5)

Here, [e] denotes the content of the address e.

We can clearly notice that the precondition, but also the invariant, and the post-condition become extremely complicated, even more, when the program runs in a concurrent context. This is where separation logic proves invaluable. By leveraging heap separation, the specifications become significantly clearer and simpler.

Although CREUSOT does not support Separation Logic, its principles can be emulated through the use of the RUST type system and ghost code. The latter can be used to carry over separation logic principles that are implicitly guaranteed by the Rust type system into the logical world. To be more precise, let us consider the interface of PtrOwn<T>::disjoint_lemma as an illustrative example.

```
/// Ensures two PtrOwns reference different memory locations
#[ghost]
#[ensures(own1.ptr().addr_logic() != own2.ptr().addr_logic())]
#[ensures(*own1 == ^own1)]
pub fn disjoint_lemma(own1: &mut PtrOwn<T>, own2: &PtrOwn<T>)
```

Figure 3: PtrOwn<T>::disjoint_lemma interface

This lemma is admitted as an axiom in CREUSOT, and what it does is verify that the two permissions correspond to two distinct pointers on the heap. If this lemma were logical, it would not hold, because we quantify universally over own1 and own2; therefore, one could be equal to the other, and the first post-condition would not be satisfied. However, if we admit it as a ghost lemma, the Rust type system, within the context of ghost code prohibits having a mutable borrow and an immutable borrow to the same value. Therefore, own1 and own2 are necessarily distinct, and the validity of the axiom follows (the second post-condition is not essential for conveying the idea).

There are, however, more specialized tools designed specifically for reasoning with Separation Logic. One such tool is VIPER, a Rust verifier that supports Separation Logic. It is built on top of BOOGIE, an intermediate verification language (IVL) developed by Microsoft Research, and is widely used in the field of formal verification. The illustration below clarifies the relationships between these languages and their connection to Separation Logic.

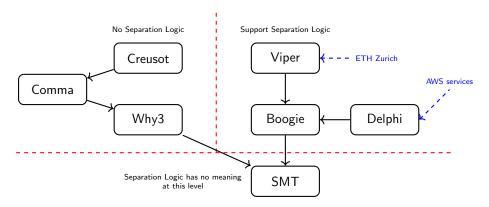


Figure 4: Illustration of the relationship between verification tools and intermediate languages.

2.2 Different ways of implementing the problem

The list reversal problem has already been proven in two different ways in CREUSOT, but both methods have certain limitations:

- BOX method: This approach models lists using Rust Box type. However, it imposes strong restrictions on the memory model by prohibiting any form of sharing or aliasing, since Box does not support multiple references to the same memory location. As a result, the specification is simple and the proof goes through easily.
- Memory model method: This approach relies on modular reasoning over the memory. In other words, it involves passing an object that models the entire memory as a parameter to each method to be verified. As a result, verification requires reasoning about the complete memory state. This can quickly lead to complex proofs even for simple algorithms. For example, suppose we have two disjoint lists in the heap, each verified using a list predicate. If we reverse one of them, the list predicate on the other is not preserved automatically, and we must explicitly include it in the proof. This makes the verification process tedious. This is where separation logic becomes useful, and the solution we propose implicitly uses its principles, thanks to Rust type system.

3 Problem definition and proposed solution

3.1 Problem definition

Formal verification of mutable data structures with pointers is one of the most challenging aspects of formal methods. The in-place list reversal algorithm is a canonical example of this challenge, as it can easily lead to memory leaks, dangling pointers, or logical errors.

The core problem is that, for a given list implementation in Rust using raw pointers, we need to formally verify the correctness of an in-place reversal algorithm not only that, but also the preservation of memory safety and the proper handling of shared lists.

3.2 Proposed solution

3.2.1 PtrOwn and RawPtr

Formally called linear algebraic types, they are used by CREUSOT to manipulate pointers in proofs. PtrOwn models ownership of memory cells in the ghost world and can be used in parallel with RawPtr, which represents the corresponding address of the cell represented by PtrOwn. The internal representation of PtrOwn is as follows:

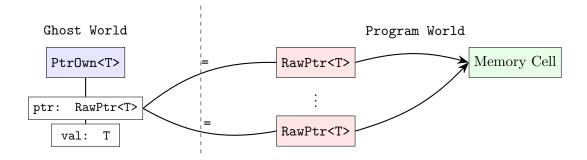


Figure 5: Internal structure of PtrOwn<T>.

Our solution relies on the use of linear algebraic types in CREUSOT, specifically, PtrOwn and RawPtr. This allows us to prove the correctness of in-place reversal even in the presence of shared data structures, making it better than the BOX method†. Moreover, it also outperforms the memory model† approach, our method requires to reason locally on memory. In other words, we only need to verify the parts of the heap we are manipulating, without having to reason about independent regions. This provides a form of separation logic, implicitly enforced by the Rust type system. In the following we will present our solutions in steps.

3.2.2 Data Structure

The list type is represented by RawPtr<Node<T>> where Node<T> is defined like the following:

```
struct Node<T> {
    elem: T,
    pub next: RawPtr<Node<T>>,
    }
}
```

3.2.3 Predicates

• List Predicate code†

list predicate takes a pointer of type RawPtr and the abstract ghost sequence of permission PtrOwn that represents the list algebraically seq. it checks recursively that the pointers inside the permissions in the sequence correspond to the pointers in the progam world, and that the list ends with nil.

$$list p nil \stackrel{\text{def}}{=} p = null_ptr()$$
 (6)

list p (a.
$$\alpha$$
) $\stackrel{\text{def}}{=}$ p = a.ptr() \wedge list [p+1] α (7)

• inverse Predicate code†

The predicate inverse takes two sequences of PtrOwn objects and determines whether the elements of the first sequence appear in reverse order in the second. One might notice that we could express this predicate more simply using the built-in rev function, as in inverse(s1, s2) == inverse'(s1, s2) where inverse'(s1, s2) := s1.rev() == s2. However, this is not the case due to our choice of the algebraic representation of the list and the invariants implied by the algorithm. We chose to model it as Seq<PtrOwn<Node<T>>>, before explaining why the rev function is not applicable in this context, we first present a figure showing the structure of a Seq<PtrOwn<Node<T>>> and its corresponding representation in the program's memory model.

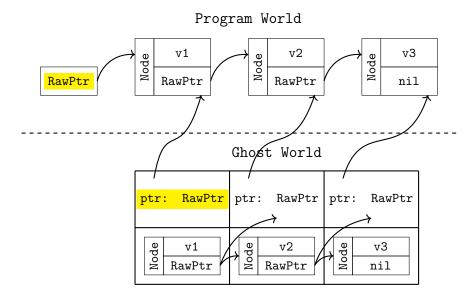


Figure 6: Memory representation of a list with 3 elements with raw pointers and Creusot sequences.

inverse and inverse' are not equivalent predicates. The key difference is that inverse is independent of the second field of PtrOwn (Node field), whereas inverse' is not. In the in_place_reversal algorithm, we reverse the direction of the pointers inside the Node field of each PtrOwn. As a result, if we use the built-in rev function to reverse the sequence, it will not reconstruct the original version as it was at the beginning of the function, since the internal pointers now point in the opposite direction. The predicate inverse avoids this problem by ignoring the second field entirely. It only checks the ordering of the elements in the list, which is the only relevant information we need to verify. This is precisely why we define and use this predicate.

4 Conclusion and perspectives

4.1 Conclusion

This work successfully addresses the challenge of formally verifying in-place linked list reversal in the presence of shared data structures using CREUSOT. I have learned many concepts through this research work, not only about formal verification but also about programming semantics and formal verification language compilation.

4.2 Perspectives

We are looking forward to extending the proof to lasso structures and, more importantly, to proving the Morris tree traversal algorithm, which was my initial subject. Unfortunately, due to the complexity of the proof compared to the given time, I had to work on a simpler but very important algorithm, which is the list reversal.

References

- [1] John C. Reynolds, Separation Logic: A Logic for Shared Mutable Data Structures, Proceedings of the 17th Annual IEEE Symposium on Logic in Computer Science (LICS), 2002.
- [2] Joseph M. Morris, *Traversing Binary Trees Simply and Cheaply*, Information Processing Letters, Vol. 9, No. 5, December 1979, pp. 197–200.

5 Appendix

5.1 in_place_reversal algorithm

```
j := nil; while i <> nil do
                     (k := [i + 1]; [i + 1] := j; j := i; i := k).
  5.2 Code
#![allow(dead_code)]
extern crate creusot_contracts;
use ::std::ptr;
use creusot_contracts::ptr_own::{PtrOwn, RawPtr};
use creusot_contracts::*;
pub struct Node<T> {
    elem: T,
    pub next: RawPtr<Node<T>>,
}
impl<T> Node<T> {
    #[predicate]
    #[variant(perm_seq.len())]
    fn list(1: RawPtr<Self>, perm_seq: Seq<PtrOwn<Node<T>>>) -> bool {
        pearlite! {
            if l.is_null_logic() {
                perm_seq.len() == 0
            } else {
                 if perm_seq.len() > 0 {
                     let ptr = perm_seq[0].ptr();
                     1 == ptr && Self::list(perm_seq[0].val().next, perm_seq.tail())
                } else {
                     false
                }
            }
        }
    }
    #[ensures(Self::list(result.0, *result.1))]
    #[ensures(result.0.is_null_logic())]
    pub fn empty() -> (RawPtr<Self>, Ghost<Seq<PtrOwn<Node<T>>>>) {
        (ptr::null(), Seq::new())
    }
    #[requires(Self::list(l, **seq))]
    #[ensures(Self::list(result, *^seq))]
    \#[ensures(forall < i:Int > 0 <= i \& i < (\hat{seq}).tail().len() ==> seq[i] == (\hat{seq}).tail()[i])
    \#[ensures((\hat{seq})[0].val().elem == e)]
    \#[ensures((\hat{seq})[0].ptr() == result)]
    \#[ensures((\hat{seq}).len() == seq.len() + 1)]
    pub fn cons(e: T, 1: RawPtr<Self>, seq: &mut Ghost<Seq<PtrOwn<Node<T>>>>) -> RawPtr<Self>
        let (raw, own) = PtrOwn::new(Node { elem: e, next: 1 });
        let _seq2 = snapshot!(**seq);
```

```
ghost!(seq.push_front_ghost(own.into_inner()));
    proof_assert!(*_seq2 == seq.tail());
    raw
}
#[requires(Self::list(p, **seq))]
#[requires(0 <= nth@ && nth@ < seq.len() )]
#[ensures(seq[nth@].val().elem == *result)]
pub fn nth(mut p: RawPtr<Self>, nth: i128, seq: &Ghost<Seq<PtrOwn<Node<T>>>>) -> &T {
    //requires nth >= 0
    let mut i = 0;
    proof_assert!(**seq == seq.subsequence(0, seq.len()));
    #[invariant(0 <= i@ && i@ <= nth@)]
    #[invariant(Self::list(p, seq.subsequence(i@, seq.len())))]
    loop {
        let rw = unsafe {
            PtrOwn::as_ref(p, ghost!(seq.get_ghost(Int::new(i).into_inner()).unwrap()))
        };
        if i == nth {
            return &rw.elem;
        p = rw.next;
        proof_assert!(seq.subsequence(i@, seq.len()).tail() == seq.subsequence(i@+1, seq.
        i += 1;
    }
}
#[predicate]
pub fn inverse(seq: Seq<PtrOwn<Node<T>>>, other: Seq<PtrOwn<Node<T>>>, lb: Int, lh: Int)
where
    T: Sized,
{
    pearlite! {
         forall<i: Int>
        lb <= i && i < lh
        ==> seq[i].val().elem == other[other.len() - i - 1].val().elem
    }
}
#[requires(Self::list(p, **seq))]
#[ensures(Self::list(result, *^seq))]
\#[ensures(seq.len() == (^seq).len())]
#[ensures(Self::inverse(**seq, *^seq, 0, (*^seq).len()))]
pub fn reverse_in_place(
    mut p: RawPtr<Self>,
    seq: &mut Ghost<Seq<PtrOwn<Node<T>>>>,
) -> RawPtr<Self> {
    //requires p n'est pas un lasso
    snapshot! {
```

```
};
        let mut q: *const Node<T> = ptr::null();
        let mut reverted_seq = Seq::new();
        let _seq0 = snapshot!(**seq);
        #[invariant(Self::list(q, *reverted_seq))]
        #[invariant(Self::list(p, **seq))]
        #[invariant(Self::inverse(_seq0.subsequence(0, reverted_seq.len()), *reverted_seq, 0,
        #[invariant(reverted_seq.len() + seq.len() == _seq0.len())]
        #[invariant(**seq == _seq0.subsequence(reverted_seq.len(), _seq0.len()))]
        #[invariant(inv(seq))]
        #[invariant(inv(reverted_seq))]
        while !p.is_null() {
            let _sloop_entry = snapshot!(**seq);
            let _revs_loop_entry = snapshot!(*reverted_seq);
                unsafe { PtrOwn::as_mut(p, ghost!(seq.get_mut_ghost(*ghost!(0int)).unwrap()))
            let next = p2.next;
            p2.next = q;
            q = p;
            p = next;
            let _sloop_exit = snapshot!(**seq);
            ghost!((*reverted_seq).push_front_ghost(seq.pop_front_ghost().unwrap()));
            //a0156: Assertion used to prove invariant #1 (we can remove it and use use_th se
            proof_assert!(reverted_seq.tail() == *_revs_loop_entry);
            //Hypothesis: invariant(Self::list (p, **seq))
            // We need to add to the hypothesis the fac that the tail of the previous seq is
            //a1369
            proof_assert!((*_sloop_exit).tail() == **seq);
            //In order to proof the last assertion, we need the following assertion
            //It esnures that seq.tail() didn't change between the beginig of the loop and th
            proof_assert!((*_sloop_exit).tail() == (*_sloop_entry).tail());
            //this should be enough to prove #[invariant(Self::list (p, **seq))], whith using
            //proof_assert!(Self::list(p, (*snap2).tail()));
            proof_assert!(Self::list(p, (*_sloop_exit).tail()));
            // ==> invariant #1 checks for iteration n+1
        //Pour montrer ensures#1 (ensures(seq.len() == (^seq).len() && Self::inverse(**seq, *
        //a4224
        proof_assert!(_seq0.subsequence(0, reverted_seq.len()) == *_seq0);
        ghost!(**seq = reverted_seq.into_inner());
   }
}
```

let _ = Seq::<T>::ext_eq;

```
#[ensures(Node::list(result.0, *result.1))]
#[ensures(result.1.len() == vec.view().len())]
\#[ensures(forall < i: Int > 0 <= i \ \& \ i < vec.view().len() == > (*result.1)[i].val().elem == vec.
pub fn list_of_vector1<T>(mut vec: Vec<T>) -> (RawPtr<Node<T>>>, Ghost<Seq<PtrOwn<Node<T>>>>)
    //Takes possession of elements in the vector
    let (mut 1, mut seq) = Node::empty();
    let _vec0 = snapshot!(vec);
    #[invariant(forall<i: Int>
        vec.view().len() \le i \otimes i < vec0.view().len() \Longrightarrow seq[i - vec.view().len()].val().en() 
    #[invariant(Node::list(l, *seq))]
    #[invariant(vec.view().len() + seq.len() == _vec0.view().len())]
    \#[invariant(forall < i: Int > 0 <= i &  i < vec.view().len() == > vec.view()[i] == _vec0.view()
    #[invariant(inv(seq))]
    loop {
        if let Some(v) = vec.pop() {
            1 = Node::cons(v, 1, &mut seq);
        } else {
            break;
    }
    (1, seq)
}
pub fn tr() {
    let v1 = creusot_contracts::vec![1, 5, 3];
    let (list1, mut _seq1) = list_of_vector1(v1.clone());
    assert!(*Node::nth(list1, 0, &_seq1) == 1);
    assert!(*Node::nth(list1, 1, &_seq1) == 5);
    assert!(*Node::nth(list1, 2, &_seq1) == 3);
    let 12 = Node::reverse_in_place(list1, &mut _seq1);
    assert!(*Node::nth(12, 2, &_seq1) == 1);
    assert!(*Node::nth(12, 1, &_seq1) == 5);
    assert!(*Node::nth(12, 0, &_seq1) == 3);
   print!("ok");
}
```