

Andrew Liddle



An Introduction to

MODERN COSMOLOGY

Third Edition

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Andrew Liddle

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To my grandmothers

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