

Graphs – Graph Representation

1. Introduction

Graph Representation refers to the way a graph is stored in computer memory.

Since a graph consists of **vertices and edges**, we need an efficient method to represent their relationships.

Choosing the right representation is important because it affects:

- Memory usage
 - Traversal speed
 - Algorithm efficiency
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2. Why Graph Representation is Needed

Graph representation is required to:

- Perform graph traversals (BFS, DFS)
- Apply shortest path algorithms
- Store large networks efficiently
- Process relationships between nodes

Different problems require different representations.

3. Types of Graph Representation

There are **two main methods** to represent graphs:

1. **Adjacency Matrix**
 2. **Adjacency List**
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4. Adjacency Matrix

What is an Adjacency Matrix?

An **Adjacency Matrix** is a **2D array** of size $V \times V$, where:

- V is the number of vertices
- Each cell indicates whether an edge exists

Representation Rule

$\text{matrix}[i][j] = 1 \rightarrow \text{edge exists}$

$\text{matrix}[i][j] = 0 \rightarrow \text{no edge}$

Example

Graph:

```
A — B
|
C
```

Adjacency Matrix:

```
  A B C
A [ 0 1 1 ]
B [ 1 0 0 ]
C [ 1 0 0 ]
```

Advantages of Adjacency Matrix

- Easy to implement
- Fast edge lookup ($O(1)$)
- Suitable for dense graphs

Limitations of Adjacency Matrix

- Uses large memory
- Wastes space for sparse graphs

- Not efficient for large graphs
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5. Adjacency List

What is an Adjacency List?

An **Adjacency List** stores:

- Each vertex
- A list of all vertices connected to it

It is usually implemented using **arrays or linked lists**.

Example

Graph:

```
A — B
|
C
```

Adjacency List:

```
A → B → C
B → A
C → A
```

Advantages of Adjacency List

- Memory efficient
 - Suitable for sparse graphs
 - Easy to traverse neighbors
 - Most commonly used
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Limitations of Adjacency List

- Edge lookup is slower than matrix
- Slightly complex to implement
- Not ideal for very dense graphs

6. Adjacency Matrix vs Adjacency List

| Feature | Adjacency Matrix | Adjacency List |
|----------------|------------------|----------------|
| Memory Usage | High | Low |
| Edge Lookup | $O(1)$ | $O(V)$ |
| Traversal | Slower | Faster |
| Best For | Dense Graphs | Sparse Graphs |
| Implementation | Simple | Moderate |

7. Representation for Directed Graphs

Adjacency Matrix

$\text{matrix}[i][j] = 1 \rightarrow \text{edge from } i \text{ to } j$

Adjacency List

$i \rightarrow j$

Direction is explicitly stored.

8. Representation for Weighted Graphs

Adjacency Matrix

- Store weight instead of 1

$\text{matrix}[i][j] = \text{weight}$

Adjacency List

- Store pairs (vertex, weight)
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9. Which Representation to Use?

| Scenario | Best Choice |
|-----------------|------------------|
| Dense graph | Adjacency Matrix |
| Sparse graph | Adjacency List |
| Fast edge check | Adjacency Matrix |
| Fast traversal | Adjacency List |

10. Applications of Graph Representation

- Social networks
 - Road maps
 - Network routing
 - Dependency graphs
 - Scheduling problems
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11. Summary

- Graphs need memory representation
 - Two main methods: matrix and list
 - Matrix is simple but memory-heavy
 - List is efficient and widely used
 - Choice depends on problem requirements
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