

Final

Write a C/MPI program that implements the **block matrix version** of Fox's matrix multiplication algorithm (see Lecture Notes 5). Your program should be able to multiply two $n \times n$ matrices on a $p \times p$ Cartesian grid, where $p \leq n$. For simplicity, you may assume that n is divisible by p .

In your program, process 0 of the 2D grid should read the matrices **A** and **B** from a file. The input file should be formatted as follows:

```
< matrix dimension n >
< elements of matrix A >
< elements of matrix B >
```

A sample input file might look like this:

```
8
3.0  -10.0  22.0  -4.0   3.0  23.0  -9.0  15.0
11.0 -21.0  22.0  12.0  12.0 -21.0  6.0  -24.0
11.0  13.0  11.0   5.0  11.0  4.0  6.0  -18.0
-8.0   6.0  10.0  18.0   3.0  4.0  13.0  10.0
-11.0 -3.0  20.0  13.0   1.0  18.0  5.0   2.0
1.0   23.0 -21.0  11.0   5.0   1.0  1.0   5.0
-20.0 13.0  15.0   4.0   5.0  19.0  5.0   7.0
6.0   -8.0  -7.0   6.0  -2.0   3.0  3.0   9.0
12.0   2.0 -14.0  10.0 -23.0 -21.0 14.0 -24.0
16.0   8.0  16.0   4.0   8.0  11.0 -10.0 -21.0
5.0   4.0  24.0  22.0  23.0   1.0  -1.0  21.0
-22.0 24.0  24.0   5.0  24.0  17.0  14.0  11.0
22.0 -17.0   5.0   2.0   6.0  23.0  4.0 -16.0
24.0 -16.0  24.0 -16.0  -3.0  13.0  7.0   8.0
7.0   17.0 -13.0   3.0  11.0  22.0  17.0  7.0
14.0  23.0  15.0   6.0  16.0  22.0 -14.0  15.0
```

After reading **A** and **B**, your program should distribute the matrices among the processes of the 2D grid using **block checkerboard decomposition**, perform matrix multiplication on the sub-matrices locally in each process, then gather the sub-matrices into the entire product matrix **C** in process 0. Finally, print the original matrices **A** and **B**, and the product matrix **C**, from process 0.

Test your program using the accompanying files named **inmatrix<n>** which contains $n \times n$ matrices **A** and **B**. The correct output of the program for input file **inmatrix<n>** is in file **outmatrix<n>**.

The output of your program should follow the format depicted in the sample output below for the input file **inmatrix8** (8 x 8 matrices).

```
% mpirun -n 4 blockfox
% Enter filename: inmatrix8

Matrix size = 8 x 8
Grid size = 2 x 2

Matrix A:
  3.0 -10.0  22.0  -4.0   3.0  23.0  -9.0  15.0
 11.0 -21.0  22.0  12.0  12.0 -21.0   6.0 -24.0
 11.0  13.0  11.0   5.0  11.0   4.0   6.0 -18.0
 -8.0   6.0  10.0  18.0   3.0   4.0  13.0  10.0
-11.0  -3.0  20.0  13.0   1.0  18.0   5.0   2.0
  1.0  23.0 -21.0  11.0   5.0   1.0   1.0   5.0
-20.0  13.0  15.0   4.0   5.0  19.0   5.0   7.0
  6.0  -8.0  -7.0   6.0  -2.0   3.0   3.0   9.0

Matrix B:
 12.0   2.0 -14.0  10.0 -23.0 -21.0  14.0 -24.0
 16.0   8.0  16.0   4.0   8.0  11.0 -10.0 -21.0
  5.0   4.0  24.0  22.0  23.0   1.0  -1.0  21.0
-22.0  24.0  24.0   5.0  24.0  17.0  14.0  11.0
 22.0 -17.0   5.0   2.0   6.0  23.0   4.0 -16.0
 24.0 -16.0  24.0 -16.0  -3.0  13.0   7.0   8.0
  7.0  17.0 -13.0   3.0  11.0  22.0  17.0   7.0
 14.0  23.0  15.0   6.0  16.0  22.0 -14.0  15.0

Product Matrix C:
 839.0 -309.0 1139.0  155.0  351.0  281.0 -126.0  854.0
-892.0  -88.0 -556.0  804.0  190.0 -629.0  849.0   93.0
 413.0 -273.0  241.0  297.0   56.0   49.0  509.0 -623.0
  47.0  840.0  972.0  295.0 1203.0 1177.0  191.0  699.0
 151.0  172.0 1300.0  124.0 1040.0  850.0  225.0 1083.0
 244.0  397.0  225.0 -278.0   60.0  658.0  -67.0 -817.0
 654.0   77.0 1465.0  -35.0 1145.0 1272.0 -229.0  778.0
-48.0  308.0  -78.0  -85.0  -63.0  138.0  193.0  155.0

%
```

Submitting Your Assignment

- Be sure to properly comment your code. Points will be taken off for improperly commented or uncommented code.
- Upload your program as a plain text file. Write your full name clearly in comments at the top of your program.
- Include screenshot of how the code ran.