## Assignment 10

## AKHILA, CS21BTECH11031

## **Question:**

The random variable x is uniformly distributed in the interval  $\theta - 2 < x < \theta + 2$ . We observe 100 samples  $x_i$  and find that their average equals  $\bar{x} = 30$ . Find the 0.95 confidence interval of  $\theta$ .

## **Solution:**

In this problem, x is uniform with  $E\left\{x\right\}=\theta$  and  $\sigma^2=\frac{4}{3}.$ 

We can use , however, the normal approximation for  $\bar{x}$  because n =100.

Here,  $\gamma = 0.95$ 

We know,

$$\gamma = 1 - \delta \tag{1}$$

$$\implies \delta = 1 - \gamma = 1 - 0.95 = 0.05$$
 (2)

Also,

$$u = 1 - \frac{\delta}{2} = 1 - \frac{0.05}{2} = 0.975$$
 (3)

Standard normal percentile  $z_u$  for  $u=1-\frac{\delta}{2}$  is  $z_{0.975}$  which is equal to 1.967

We obtain the interval

$$\bar{x} \pm z_{0.975} \frac{\sigma}{\sqrt{n}} = 30 \pm 1.967 \frac{\frac{2}{\sqrt{3}}}{\sqrt{100}}$$
 (4)

$$=30\pm 1.967\frac{1}{5\sqrt{3}}\tag{5}$$

$$=30\pm0.227$$
 (6)