

# CS 410- QL Database App Dev Assignment: Relational Algebra - Bag semantics, complex expressions, and extended Algebra

I, Baba Avinash Puppala (bpuppala), declare that I have completed this assignment completely and entirely on my own, without any consultation with others. I understand that any breach of the UAB Academic Honor Code may result in severe penalties.

## Solution to Question 1: Bag Projection and Intersection

Given relation  $R(A, B, C)$  with the following tuples:

$A$	$B$	$C$
1	2	3
1	2	3
2	3	1
3	1	2
2	2	3
2	3	3

We need to compute the intersection:

$$\text{PROJ}_{A,B}(R) \cap \text{RENAME}_{S(A,B)}(\text{PROJ}_{B,C}(R)),$$

where  $S$  is used to rename the attributes of  $\text{PROJ}_{B,C}(R)$  to match the schema of  $A, B$ .

## Step 1: Projection

- The projection  $\text{PROJ}_{A,B}(R)$  results in:

$$(1, 2), (1, 2), (2, 3), (3, 1), (2, 2), (2, 3).$$

Since we are considering a bag (multiset), duplicates are preserved.

- The projection  $\text{PROJ}_{B,C}(R)$  results in:

$$(2, 3), (2, 3), (3, 1), (1, 2), (2, 3), (3, 3).$$

## Step 2: Renaming

Rename  $\text{PROJ}_{B,C}(R)$  to have the same schema as  $A, B$ :

$$(2, 3), (2, 3), (3, 1), (1, 2), (2, 3), (3, 3).$$

## Step 3: Intersection

Find the intersection between  $\text{PROJ}_{A,B}(R)$  and the renamed  $\text{PROJ}_{B,C}(R)$ :

$$(1, 2), (2, 3), (3, 1).$$

The result contains only the tuples that appear in both projections.

## Solution to Question 2: Set and Bag Operations

Let  $R(A, B, C)$  and  $S(A, B, C)$  be two relations where no attributes can have a null value. Determine whether the given equations hold for both sets and bags.

**Part (a):**  $(R \cap S) = (RS)$

- **Set Operations:** In general,  $R \cap S$  returns the common tuples in both  $R$  and  $S$ , while  $RS$  produces a join result based on matching tuples across all attributes. The join is equivalent to  $R \cap S$  only if  $R$  and  $S$  contain exactly the same tuples with matching attributes. - **Bag Operations:** Even when considering bags, a join operation can produce multiple occurrences based on matching criteria, whereas  $R \cap S$  counts occurrences in both relations. Hence, they are not guaranteed to be equal.

**Part (b):**  $((R - S) \cup (S - R)) \cap (R \cap S) = \emptyset$

- **Set Operations:** This equation is always true because  $(R - S) \cup (S - R)$  represents the symmetric difference, which includes elements not common to both sets. Since  $R \cap S$  contains elements common to both, their intersection will indeed be an empty set. - **Bag Operations:** For bags, even if there are duplicate elements, the symmetric difference and intersection will remain disjoint. Therefore, the equation still holds true.

**Part (c):**  $\Delta(R) = \Gamma_{A,B,C}(R)$

- **Set Operations:** The operator  $\Delta$  returns the distinct tuples from  $R$ . When applying the grouping operator  $\Gamma$ , the resulting grouped tuples are the same as the distinct elements in  $R$ , thus making  $\Delta(R)$  and  $\Gamma_{A,B,C}(R)$  equivalent. - **Bag Operations:** In the case of bags, both operations will return the distinct tuples without considering duplicates, hence they are equal.

**Part (d):**  $R \cup S = R$

- **Set Operations:** This equation holds if and only if  $S \subseteq R$ . In other words, all tuples in  $S$  must also be present in  $R$ . - **Bag Operations:** For bags, each tuple in  $S$  must appear in  $R$  at least as many times as in  $S$  for this equation to hold.

## Solution to Question 3: Database Queries Using Relational Algebra

Given the following relations:

- **Person** ( $ID, name, age, gender$ ) where  $ID$  is a key.
- **Shop\_list** ( $ID, item$ ) where  $(ID, item)$  is the key.
- **Sell** ( $supermarket, item, price$ ) where  $(supermarket, item)$  is the key.

**Part (a): Find all the items on the shop\_list of at least one person over the age of 18**

$$\text{PROJ}_{item}(\sigma_{age > 18}(\text{Person}) \bowtie \text{Shop\_list})$$

This expression filters the persons who are over 18, joins the result with the shop\_list, and projects the items.

**Part (b): Find the names of all males who have at least one item in their shop\_list sold at Walmart**

$$\text{PROJ}_{name}(\sigma_{gender='M'}(\text{Person}) \bowtie \text{Shop\_list} \bowtie \sigma_{supermarket='Walmart'}(\text{Sell}))$$

The query first filters for male persons, joins with their shopping lists, then joins with items sold at Walmart, and finally projects their names.

**Part (c): Find for each person, the lowest price of items on his/her shop\_list**

$$\Gamma_{ID, \text{MIN}(price)}(\text{Person} \bowtie \text{Shop\_list} \bowtie \text{Sell})$$

The expression performs a join across the three relations and then uses a grouping to find the minimum price for each person based on their ID.