

# Adders, Encoders, and Decoders

More sophisticated applications of circuits

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# Agenda

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## 2 Adders

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- Half Adders
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# Announcements

# Project 2

- Project 2 has been released, and can be found on the course website under 'Week 3' on the calendar.
- Everything you need to complete the project will be covered in today's lecture, with optional supplementary material provided on the course website under Week 3's resources section.

# Some Reminders

- As the projects become more involved, we'd like to remind you to reach out and attend office hours if you are struggling.
- Additionally, here's a reminder that all projects can be group projects, but you'll have to let us know **4 days** prior to the project's due date if you'll be working in a group. (Max size of 3)

# Adders

# Addition

How would you add the following binary numbers?  
11101 & 11011

# Addition

- Let's visualize the computation as long addition
- How would you go about solving it this way?

$$\begin{array}{r} 11101 \\ + 11011 \\ \hline \end{array}$$



# Addition

- Let's visualize the computation as long addition
- How would you go about solving it this way?

$$\begin{array}{r} 1 \\ 11101 \\ + 11011 \\ \hline 0 \end{array}$$

- This phenomenon is known as a **carry**
- This occurs when the numbers we are adding exceed the limit imposed by the number system we are using
- Where else during this computation would this phenomenon occur?

# Half Adders

- First, let's represent the 1s as TRUEs and the 0s as FALSEs
- Think back to last week when we talked about designing circuits that dealt with booleans
- The big question: can we perform the addition process that we just talked about using such gates?
- The answer: **absolutely**

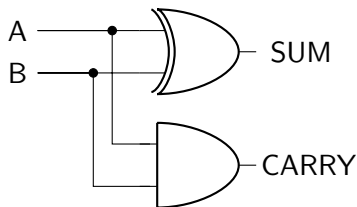
# Half Adders

- Let's take this step by step.
- Looking at the addition example, what's the simplest operation we can take away from that?
- Let's see if we can build something that can take two one-bit numbers and add them, producing a carry if applicable
  - In terms of inputs, we will need two booleans
  - In terms of outputs, we will need two booleans (one for our sum, and one for the carry)
- Incidentally, we have been describing a **Half Adder**
- We have defined our inputs and outputs- try to design a Half Adder using the gates we've learned

# Half Adders

- Below is the formal truth table and circuit diagram for an optimal Half-Adder
- In this case, we can see that the Sum and Carry can be represented by an XOR and AND gate, respectively

Half Adder		
In	Sum	Carry
0 0	0	0
0 1	1	0
1 0	1	0
1 1	0	1



# Full Adders

- The Half Adder is great, but limited in functionality
- Let's work on 'scaling' it for use with multi-digit addition.
- How do we accomplish such a task?
- All we need to do is create a circuit that can:
  - Add two one-bit numbers and produce a sum and carry
  - In case the previous addition resulted in a carry, be able to add in that third number as well
- Essentially, we need a logical circuit that can add three one-bit numbers. We can then use this circuit for each digit in our addition.

# Full Adders

- Below is a full adder that meets our previously outlined specifications exactly.

