

ENSC 180 - Assignment 3

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1.

Function 1

```
-----  
%This function calculates the depth of a sphere submerged in fluid by  
%following steps  
%1.prompting for radius of sphere, the densities of sphere and fluid  
%2.calculate the volume submerged using the inputed values and with  
%different values of depth  
%3.Take the difference of the volumes from two different calculations done  
%in 2. to find the root (difference <= eps)  
%variables are listed below  
%depth is the depth the sphere sinks  
%radius is the radius of the sphere  
%densityS and densityF are the densities of sphere and fluid respectively  
%volumeSub is the volume of sphere below fluid calculated using Eqn1  
function depthSub  
%Prompt for inputs  
radius=input('Enter the radius of sphere (mm)\n');  
densityS=input('Enter the density of sphere (g/mm^3)\n');  
densityF=input('Enter the density of fluid (g/mm^3)\n');  
if densityS > densityF  
    error('This program is not designed for cases when the sphere keeps sinking; density of  
sphere <= density of fluid');  
end  
%Calculations  
volumeSub=(densityS/densityF)*((4/3)*pi*(radius^3)); %Eqn1  
  
h=0:0.01:(radius*2);  
difference=(pi.*(3.*radius.*(h.^2)-(h.^3))./3-(volumeSub); %Eqn2 - Eqn1  
  
for i=1:(radius*2/0.01)  
    if densityS==densityF  
        depth=radius*2;  
    elseif difference(i)*difference(i+1)<0  
        depth=h(i);  
    end  
end  
fprintf('The sphere depth below the fluid surface is: %.2f (mm)\n',depth);  
end  
-----
```

Output when $r=40\text{mm}$, $\rho_S=0.6\text{ g/mm}^3$ and $\rho_0=1.0\text{ g/mm}^3$

```
-----  
>> depthSub  
Enter the radius of sphere (mm)  
40
```

Enter the density of sphere (g/mm³)

0.6

Enter the density of fluid (g/mm³)

1

The sphere depth below the fluid surface is: 45.36 (mm)

Function 2

%This function calculates the rate of h/r VS P_s/P_0

%The function can use an arbitrary radius in this case 4

%The maximum of the depth is the diameter of the sphere

%variables are listed below

%radius is the radius of the sphere

%h is the depth submerged

%ratio_PsP0 is P_s/P_0

%ratio_hr is h/r

function ratio

radius=4; %An arbitrary radius

h=0:0.01:(radius^2);

ratio_PsP0=(3.*radius.*(h.^2)-(h.^3))./(4.*(radius.^3)); % P_s/P_0 in terms of r and h

ratio_hr=h./radius;

plot(ratio_PsP0,ratio_hr)

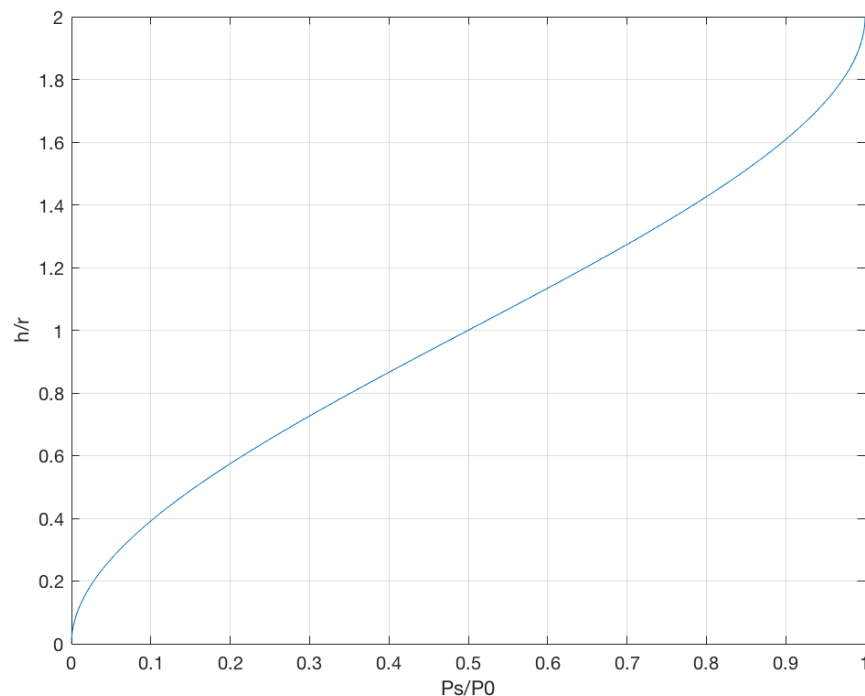
grid

xlabel('Ps/P0')

ylabel('h/r')

end

Output



When the density ratio is 1 $h/r=2$ meaning h is the radius of the sphere and the whole sphere is submerged. When density ratio is 0.5 only half of the sphere is submerged and as the density ratio decreases h/r decreases meaning less part of sphere sinks.

2.

a)

Function

```
-----  
%This function calculates the height and speed of a rocket at a given time  
%Where height is given by  $2.13 \cdot \text{time}^2 - 0.0013 \cdot \text{time}^4 + 0.000034 \cdot \text{time}^{4.751}$   
%and speed is given by the absolute value of the 1st order derivative of  
%height with respect to time  
function R_motion(time)  
if time > 63.01  
    error('The rocket lands approximately at t=63.01s. Time must be less than 63.01s');  
end  
height=2.13*time^2 - 0.0013*time^4 + 0.000034*time^4.751;  
speed=abs(4.26*time - 0.0052*time^3 + 0.000161534*time^3.751);  
  
fprintf('Height=%f (m)\nSpeed=%f (m/s)\n', height, speed);  
end  
-----
```

Output when time = 50

```
-----  
>> R_motion(50)  
Height=1211.302439 (m)  
Speed=55.846042 (m/s)  
-----
```

b)

```
>> f=@R_motion
```

f =

function_handle with value:

@R_motion

```
>> f(60) %Test the function handle with time=60  
Height=358.399488 (m)  
Speed=112.317734 (m/s)
```

c)

Function

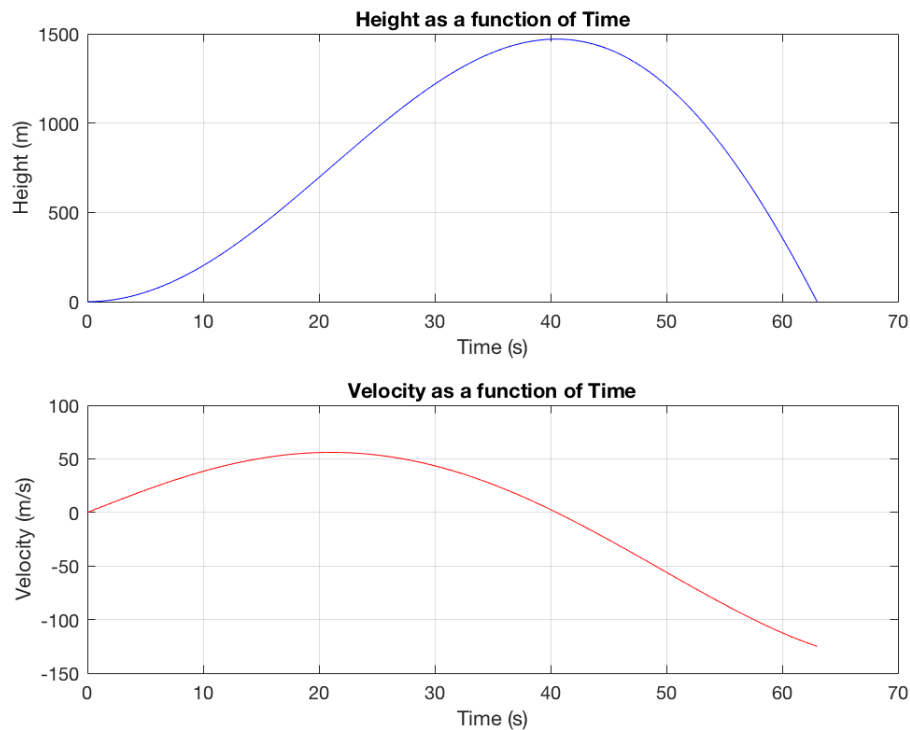
```
-----  
%This function plot height and velocity as a function of time from t=0 to  
%t=63.01(the landing time)  
%height is given by  $2.13 \cdot \text{time}^2 - 0.0013 \cdot \text{time}^4 + 0.000034 \cdot \text{time}^{4.751}$   
%speed is given by the absolute value of the 1st order derivative of height with respect to time  
function R_motionplot  
time=0:0.01:63.01;  
  
height=2.13.*time.^2 - 0.0013.*time.^4 + 0.000034.*time.^4.751;
```

```
velocity=4.26.*time - 0.0052.*time.^3 + 0.000161534.*time.^3.751;
```

```
s(1) = subplot(2,1,1);
height=2.13.*time.^2 - 0.0013.*time.^4 + 0.000034.*time.^4.751;
plot(time,height,'b')
grid
title('Height as a function of Time')
xlabel('Time (s)')
ylabel(s(1),'Height (m)')
```

```
s(2) = subplot(2,1,2);
velocity=4.26.*time - 0.0052.*time.^3 + 0.000161534.*time.^3.751;
plot(time,velocity,'r')
grid
title('Velocity as a function of Time')
xlabel('Time (s)')
ylabel(s(2),'Velocity (m/s)')
end
```

Output



3.

```
x=-1:0.001:1;
LegendreP=(693.*x.^6-945.*x.^4+315.*x.^2-15)./48;
ChebyshevP=32.*x.^6-48.*x.^4+18.*x.^2-1;
fprintf('Roots\tLegendre\tChebyshev\n');
```

```

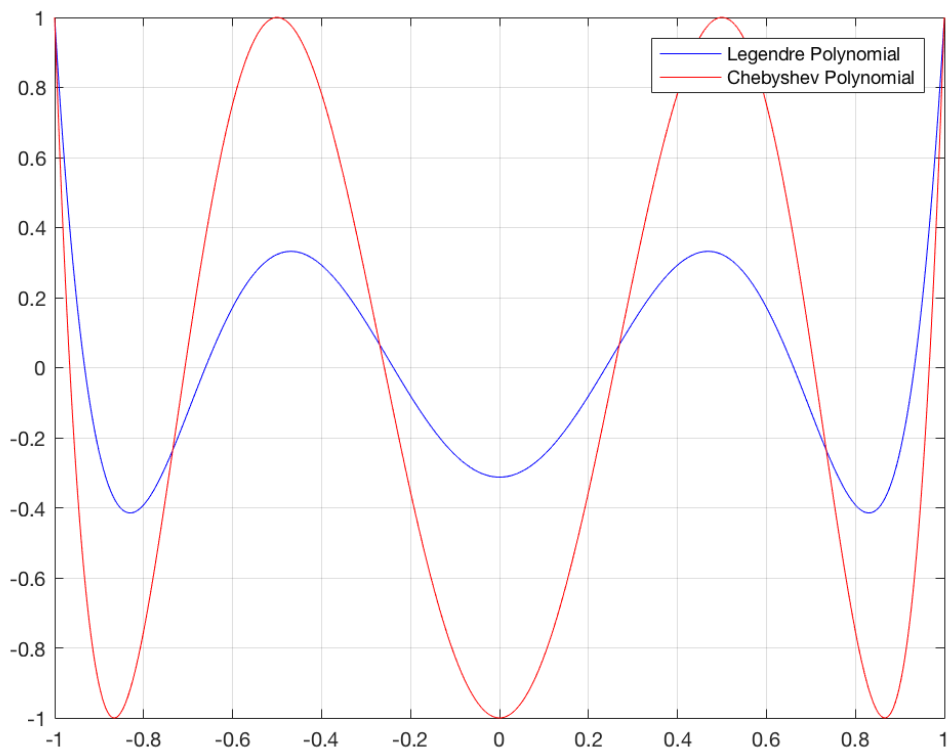
plot(x,LegendreP,'b',x,ChebyshevP,'r')
grid
legend('Legendre Polynomial','Chebyshev Polynomial')

for i=1:2000
    if LegendreP(i)*LegendreP(i+1)<0 %Product is negative if function crosses x-axis
        fprintf('\t%.3f\n',x(i));
    elseif ChebyshevP(i)*ChebyshevP(i+1)<0
        fprintf('\t\t\t%.3f\n',x(i));
    end
end
end

```

Output

Roots	Legendre	Chebyshev
		-0.966000.3
-0.933		-0.708000.3
-0.662		-0.259000.3
-0.239		
0.238		0.258000.3
0.661		0.707000.3
0.932		0.965000.3



Both polynomials are oscillating and are symmetrical over the y-axis, thus the absolute values of the roots with the same distance of x from 0 are the same.

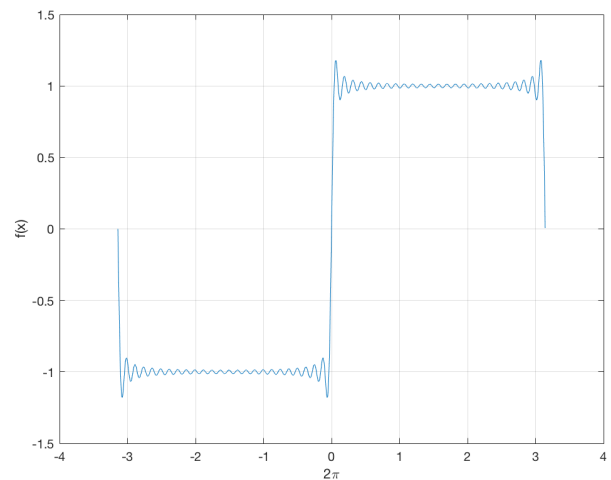
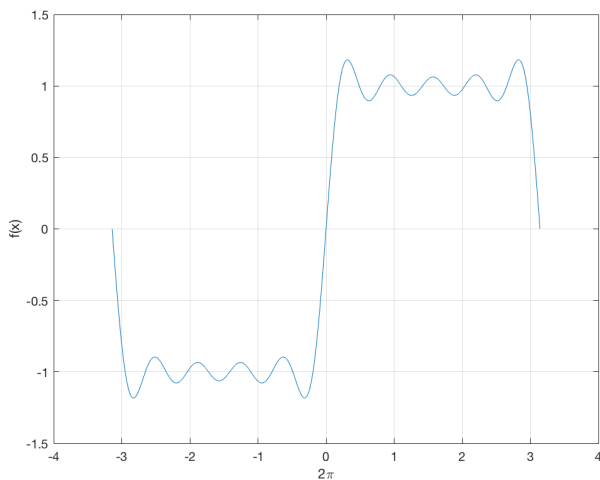
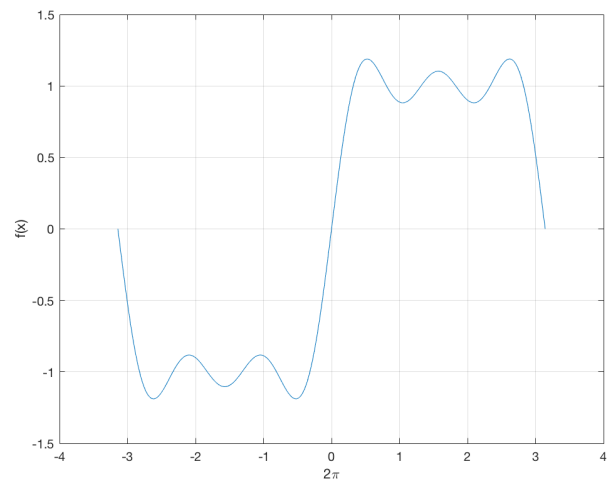
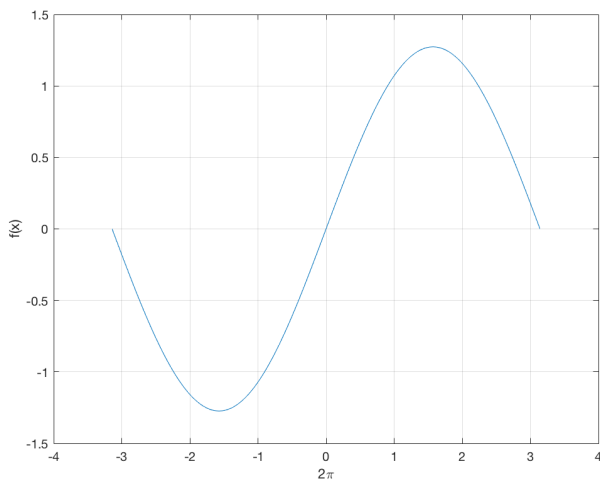
4.

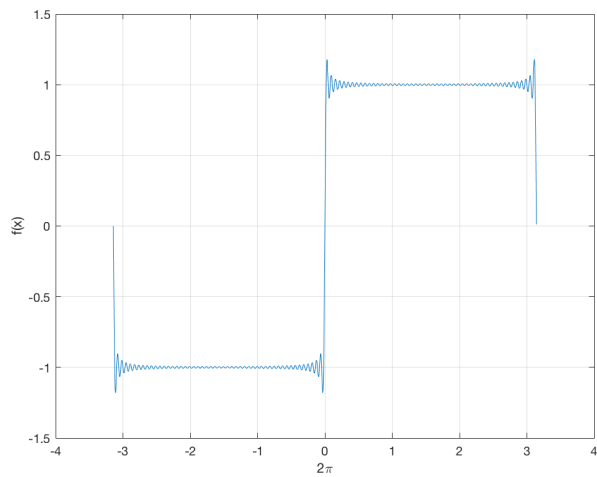
```
k=1;
series = 0;
x = -pi:0.001:pi;

for n=1:100 %sum of series from n=1 to n=100
    series = series + sin(n.*x).*(2.*k.*(1-cos(n.*pi))./(n.*pi));
end

plot(x, series)
grid
xlabel('2\pi')
ylabel('f(x)')
```

Output N=2,5,10,50,100 respectively





As N becomes larger value the solution graph looks more like $f(x) = -k$ when $-\pi < x < 0$ $=k$ when $0 < x < \pi$. The portion of the solution at k and $-k$ in this case 1 and -1 becomes flatter as well. The biggest error is the glitch close to the ends of those flat lines, namely: around π , 0 , $-\pi$.