

题号	一	二	三	四	五	六	七	八	九	十	总分	阅卷人
得分												

备注：闭卷，可以带计算器

得分	阅卷人

一、Fill the blanks(40%)

1. Let there is a continuous time sequences $x(t) = x_1(t) + x_2(t) + x_3(t)$ with two continuous components, $x_1(t) = \cos(3\pi t)$, $x_2(t) = \cos(7\pi t)$, $x_3(t) = \cos(10\pi t)$, if the combined digital signal is $x[n] = x_1[n] + x_2[n] + x_3[n]$, then

- (1) if sampled by 10Hz, then the signal will get aliasing or not ① and then sampled signal in time domain $x[n] =$ ② ;
- (2) based on (1), to filter the $x_1[n]$ by passing $x[n]$ through a digital filter, choose one kind of digital filter ③ and determine its cut-off frequency ④
- (3) based on (2), determine the period of $x_1[n]$, $N =$ ⑤

2. If $x[n] = \{1, 4, 5, -4, -1\}$, $-2 \leq n \leq 2$, then

- (1) $x[n]$ can be expressed in terms of the unit impulse signal $\delta[n]$ as ⑥ ;
- (2) If the impulse response of a LTI system is $h[n] = \{1, 4, 5\}$, $0 \leq n \leq 3$, then given by $x[n]$, the output sequence $y[1] =$ ⑦ and the range of $y[n]$ is between ⑧ and ⑨ ;
- (3) if calculate $y_c[n]$ by 6-points circulation convolution, the value of $y_c[1] =$ ⑩ ;
- (4) without computing the DTFT, $X(e^{j0}) =$ ⑪ ; $\int_{-\pi}^{\pi} |X(e^{j\omega})|^2 d\omega =$ ⑫ ;

(5) to make $h[n]$ to be a Type1 linear phrase FIR, then write out one of the possible new linear phase $h'[n] =$ ⑬

(5) Without computing the DTFT, determine what kind of $X(e^{j\omega})$ is ⑭ ; (real-valued or imaginary-valued or others types of DTFT).

3. If $x[n]$ is a length-120 sequence and $h[n]$ is a FIR filter with $0 \leq n \leq 4$. If using 10-points overlap method to computer $y[n]$, then the length of each small segment of $x[n]$ is ⑮ and their whole length output $y[n]$ is ⑯

4. Some samples of the 5-point DFT of a length-5 real sequence are given by $X[0] = -4.7$, $X[2] = 1.2 - j2$, $X[4] = -3.5 + j3$. The $X[1]$ should be ⑰

5. An IIR digital filter has the unit pulse response $h[n] = (0.5)^n \mu[-n] + (0.2)^n \mu[n]$, then

- (1) z-transform of $H(z)$ in closed form is ⑱ and its R.O.C is ⑲
- (2) whether $h[n]$ is BIBO stable or not ⑳

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二、Comprehensive problems(60%)

1. (40%) A causal LTI system is described by the recursive difference equation

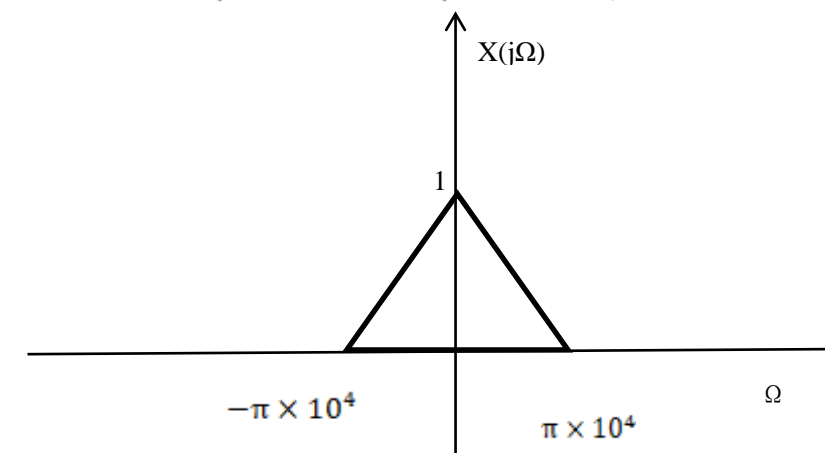
$$y[n] = 2x[n] - x[n-1] + \frac{7}{12}y[n-1] - \frac{1}{12}y[n-2]$$

- (1) Find the transfer function of $H(z)$ and its R.O.C.(6%)
- (2) Draw the diagram of the system in parallel form. (8%)
- (3) If using bilinear form to transfer the digital filter to analog filter, write out the transform equation.

(4%)

- (4) Find the impulse response $h[n]$ by solving differential equations. (8%)
- (5) Write out the magnitude function of the frequency response $H(e^{j\omega})$. (6%)
- (6) If using FIR filter to approximate $h[n]$ and $N=10$, then what its magnitude function of the frequency response $H(e^{j\omega})$ will be. (6%)
- (7) How to make (6) to be linear phase. (2%)

2. (20%) For a continuous time signal $x(t)$ with frequency spectrum $X(j\Omega)$, which $-\pi \times 10^4 \text{ rad/s} \leq \Omega \leq \pi \times 10^4 \text{ rad/s}$ as following.



- (1) Plot corresponding frequency spectrum of $X(e^{j\omega})$ and $X_s(j\Omega)$ with a proper sampling period $T = 0.5 \times 10^{-4} \text{ s}$. (5%)
- (2) If there is a LPF $H(e^{j\omega})$ with cut-off frequency $-\pi/4 \leq \omega_c \leq \pi/4$, Plot the frequency spectrum of $Y(e^{j\omega})$ and its 10-points DFT $Y[k]$. (5%)
- (3) Determine the range of sampling rate Ω_s if $Y_s(j\Omega)$ is reconstructed by filter in (2) without aliasing and Draw the $Y_s(j\Omega)$. (5%)
- (4) Design an antialiasing filter if $T = 0.2 \times 10^{-4} \text{ s}$ and plot the frequency spectrum of $X_s(j\Omega)$ after using anti-aliasing filter. (5%)