



Mechanics of Materials III:

Beam Bending

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Module 15 Learning Outcome

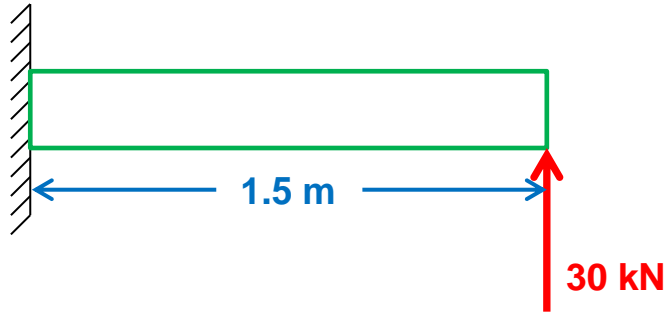
- Solve an elastic beam bending problem

Elastic Beam Bending



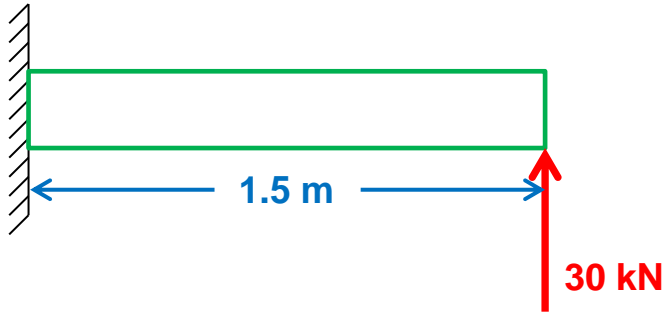
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Try to draw a model on your own



We are going to analyze the situation using a steel S Type I-Beam.
We will need the structure properties to complete this analysis.
Let's choose an S 305 X 74 beam.

Do research on your own and find the area moment of inertia, I , the section modulus, S , and the depth of the I-beam, D , for an S 305 X 74 I-beam.



For an S 305 X 74 I-beam:

$$I = 127 \times 10^6 \text{ mm}^4$$

$$S = 832 \times 10^3 \text{ mm}^3$$

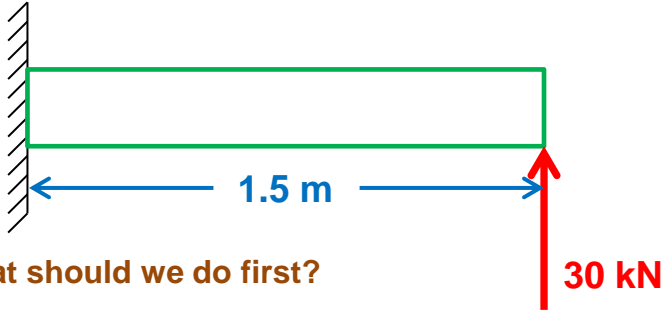
$$D = 304.8 \text{ mm}$$

Also note that the cross section is symmetrical and the neutral axis is through the center

Worksheet:

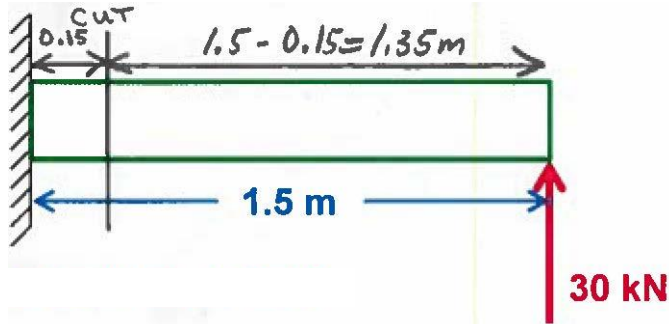
At a point 0.15 meters to the right of the left fixed end, find:

- the normal stress due to bending at a point 50 mm below the top of the beam
- the maximum normal stress experienced in the beam



What should we do first?

Draw a FBD and solve for the moment experienced at a point 0.15 meters to the right of the left fixed end.

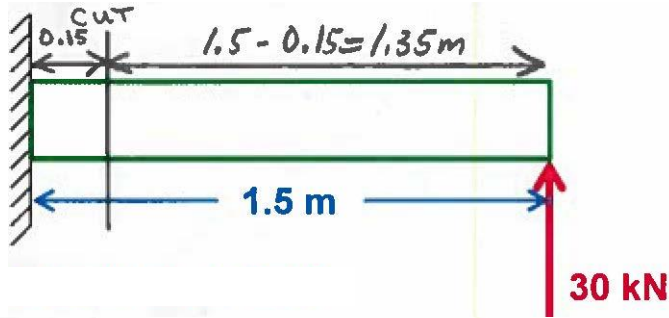


Worksheet:

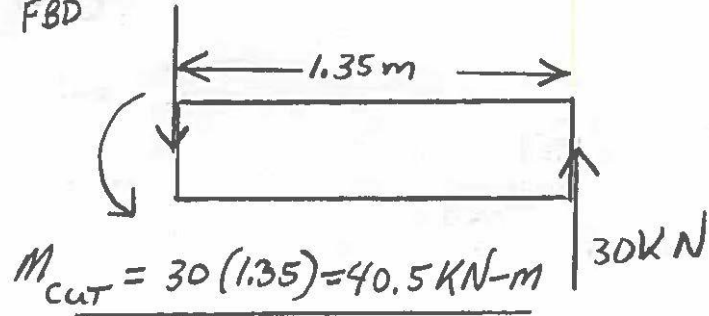
At a point 0.15 meters to the right of the left fixed end, find:

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Draw a FBD and solve for the moment experienced at a point 0.15 meters to the right of the left fixed end.



FBD



Worksheet:

At a point 0.15 meters to the right of the left fixed end, find:

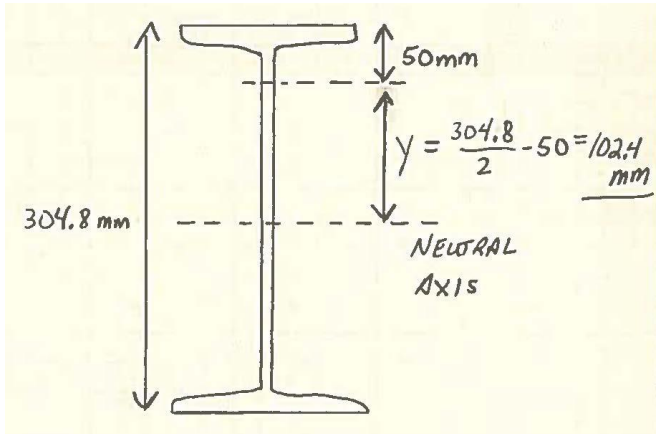
- the normal stress due to bending at a point 50 mm below the top of the beam
- the maximum normal stress experienced in the beam

$$\underline{M_{CUT} = 40.5 \text{ kN} \cdot \text{m} \text{ CCW}}$$

What should we do next?

Elastic Flexural Formula

$$\sigma_x = - \frac{M y}{I} \quad I = 127 \times 10^6 \text{ mm}^4$$



Worksheet:

At a point 0.15 meters to the right of the left fixed end, find:

- the normal stress due to bending at a point 50 mm below the top of the beam
- the maximum normal stress experienced in the beam

Elastic Flexural Formula

$$\sigma_x = - \frac{M y}{I}$$

$$M_{CUT} = 40.5 \text{ kN} \cdot \text{m} \text{ CCW}$$

$$y = 102.4 \text{ mm}$$

$$I = 127 \times 10^6 \text{ mm}^4$$

$$\sigma_x = \frac{40.5 \text{ kN} \cdot \text{m} \left(\frac{1000 \text{ N}}{\text{kN}} \right) \left(\frac{1000 \text{ mm}}{\text{m}} \right) 102.4 \text{ mm}}{127 \times 10^6 \text{ mm}^4}$$

$$\sigma_x = 32.7 \frac{\text{N}}{\text{mm}^2} = 32.7 \text{ MPa} \quad (C)$$

at a point 50 mm below
the top of the beam

ANS

Worksheet:

At a point 0.15 meters to the right of the left fixed end, find:

- the normal stress due to bending at a point 50 mm below the top of the beam
- the maximum normal stress experienced in the beam

What should we do next?

Section Modulus

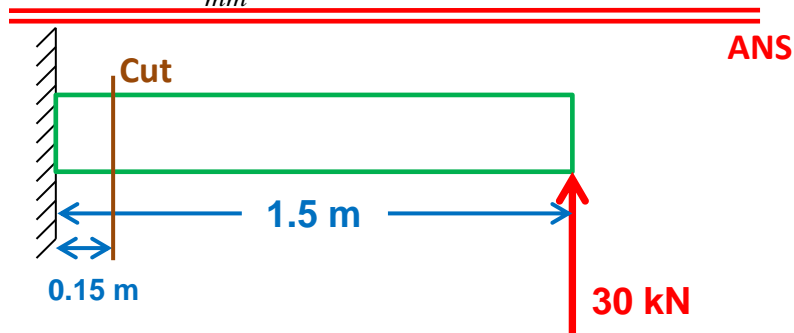
$$M_{CUT} = 40.5 \text{ kN} \cdot \text{m} \text{ CCW}$$

$$S \equiv \frac{M}{c} \quad \sigma_{MAX} = \frac{M}{S} \quad S = 832 \times 10^3 \text{ mm}^3$$

$$\sigma_{MAX} = \frac{40.5 \text{ kN} \cdot \text{m} \left(\frac{1000 \text{ N}}{\text{kN}} \right) \left(\frac{1000 \text{ mm}}{\text{m}} \right)}{832 \times 10^3 \text{ mm}^3}$$

$$\sigma_{MAX} = 48.7 \frac{\text{N}}{\text{mm}^2} = 48.7 \text{ MPa}$$

compression on top
tension on bottom



Worksheet:

At a point 0.15 meters to the right of the left fixed end, find:

- the normal stress due to bending at a point 50 mm below the top of the beam
- the maximum normal stress experienced in the beam

What should we do next?

$$\sigma_{MAX} = 48.7 \frac{N}{mm^2} = 48.7 \text{ MPa}$$

compression on top
tension on bottom

ANS

Make sure the beam remained in the elastic region!

$$48.7 \text{ MPa} < 250 \text{ MPa} = \sigma_{YIELD \text{ STEEL}}$$

Ok!