

```

In[ ]:= h+[p_, θ_, n_] := p^n / (p^n + θ^n)
h-[p_, θ_, n_] := 1 - h+[p, θ, n]

```

```

tmax = 200;

```

```

With[{ma = 1., mb = 1., mc = 1.,
      na = 2.2, nb = 2.2, nc = 2.2,
      θa = 0.28, θb = 0.28, θc = 0.28,
      ka = 1., kb = 1., kc = 1.,
      γa = 1., γb = 1., γc = 1.,
      δa = 1., δb = 1., δc = 1.},
  sol = NDSolve[{r_a'[t] == ma * (h+[p_c[t], θc, nc]) - γa * r_a[t],
                 r_b'[t] == mb * (h+[p_a[t], θa, na]) - γb * r_b[t],
                 r_c'[t] == mc * (h-[p_b[t], θb, nb]) - γc * r_c[t],
                 p_a'[t] == ka * r_a[t] - δa * p_a[t],
                 p_b'[t] == kb * r_b[t] - δb * p_b[t],
                 p_c'[t] == kc * r_c[t] - δc * p_c[t],
                 r_a[0] == 0,
                 r_b[0] == 0, r_c[0] == 0, p_a[0] == 0, p_b[0] == 0, p_c[0] == 0},
                {r_a, r_b, r_c, p_a, p_b, p_c}, {t, 0, tmax}]]];

```

```

ParametricPlot[Evaluate[{p_a[t], p_b[t]} /. First[sol]], {t, 0, tmax},
  AxesLabel → {p_a, p_b}, ColorFunction → "Rainbow", PlotRange → Full]

```

```

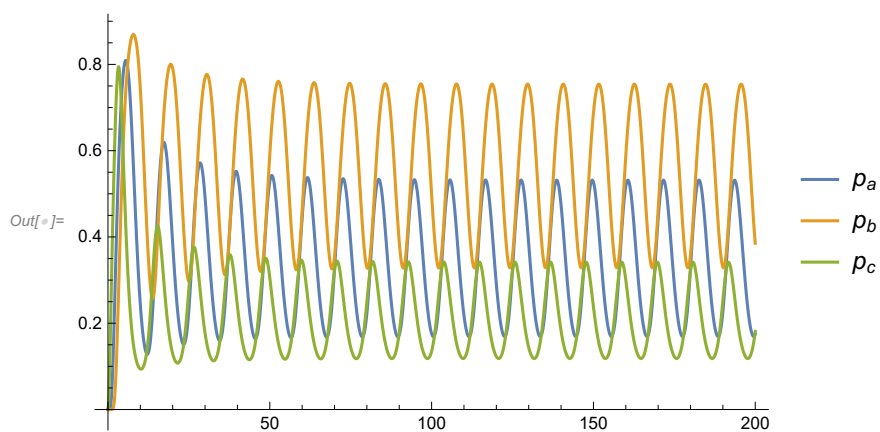
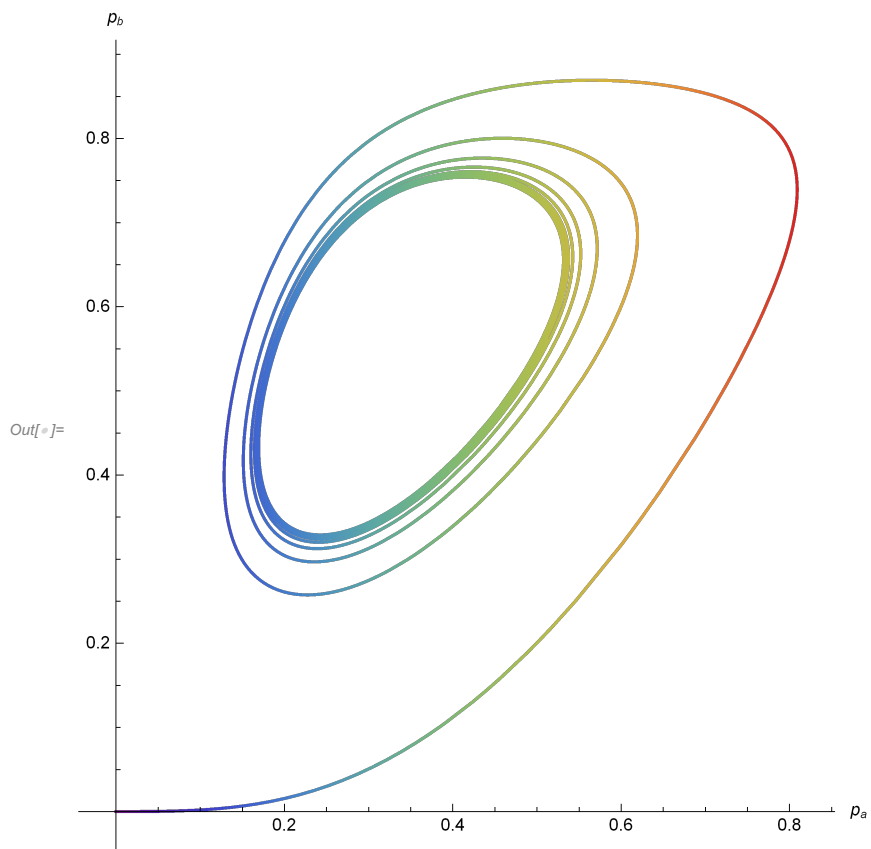
Plot[Evaluate[{p_a[t], p_b[t], p_c[t]} /. First[sol]],
  {t, 0, tmax}, PlotLegends → {"p_a", "p_b", "p_c"}]

```

```

Animate[ParametricPlot[Evaluate[
  {p_a[t], p_b[t]} /. First[NDSolve[{r_a'[t] == ma * (h+[p_c[t], θc, nc]) - γa * r_a[t],
                                     r_b'[t] == mb * (h+[p_a[t], θa, na]) - γb * r_b[t],
                                     r_c'[t] == mc * (h-[p_b[t], θb, nb]) - γc * r_c[t],
                                     p_a'[t] == ka * r_a[t] - δa * p_a[t],
                                     p_b'[t] == kb * r_b[t] - δb * p_b[t],
                                     p_c'[t] == kc * r_c[t] - δc * p_c[t],
                                     r_a[0] == 0,
                                     r_b[0] == 0, r_c[0] == 0, p_a[0] == 0, p_b[0] == 0, p_c[0] == 0},
                                     {r_a, r_b, r_c, p_a, p_b, p_c}, {t, 0, tmax}]]], {t, 0, tmax},
  AxesLabel → {p_a, p_b}, ColorFunction → "Rainbow", PlotRange → Full], {ma, 1., 10.},
{mb, 1., 10.}, {mc, 1., 10.}, {na, 2., 5.}, {nb, 2., 5.}, {nc, 2., 5.},
{θa, 0.2, 1.}, {θb, 0.2, 1.}, {θc, 0.2, 1.},
{ka, 1., 5.}, {kb, 1., 5.}, {kc, 1., 5.},
{γa, 1., 5.}, {γb, 1., 5.}, {γc, 1., 5.}, {δa, 1., 5.},
{δb, 1., 5.}, {δc, 1., 5.}, AnimationRunning → False]

```



Out[ ]=

