

The image above is Craiyon.Al generated in response to "predicting market return".

Predicing Asset Price Direction

Dr Richard Diamond, PhD, CQF, ARPM

Foreword. This demonstration is a stylised, simplified example of running classifiers (supervised learning) on equity returns. The demo be relevant to CQF Assignment/Examination/one kind of Final Project. For that purpose, is a very starting point. The task is purposefuly limited to prediction of return sign and binomial classification (up/down).

Here, we consider a large-cap equities, however in practice, the high frequency returns of large caps and market indices are the most difficult quantities to predict. Otherwise, the 70-90% traders in CFD accounts would not routinely lose their depostis.

One is more likely to find a sensible scheme in predicting specialised assets and comovement (spread) rather than returns (prices) of an individual assets. Academic asset pricing theory concerns itself with estimating (prediction) of beta, which is relation between asset returns and the market.

• To organise the prediction (your machine learning workflow) we start with features: generate 7-10 price-related features (columns) and run Classifier.fit() on them. This is no different than running a regression on several variables. For each classifier, you can produce ROC, Confusion Matrix, Transition Probabilities -- the startard evaluation techniques of supervised learning.

This demo derives features (lagged returns) from the asset price. Price-derived information is limited and there is large discussion about its predictive powers vs. fundamentals, macro economic, and alternative data.

However, the forecasting can be technically improved by using the measures of Average and Momentum. You will need to make reasonable choices of time period (rolling window) for SMA, EMA, Momentum. This link, gives one example on how to do Exponential Moving Average from the first principles. The choice of smoothing factor $lpha=2/(N_{obs}+1)$.

Positive or Negative?

• Setting up prediction classes, you are likely to encounter the high count of uncertain moves/'no move', where the movement took less than 1/10th of a percentage point.

Remember that for a global market index, the daily average return can be O(0.04%). [-1,0,1] trinomial classification might be more appropriate, but there is **no trading action** that follows from the prediction of no move in the asset.

One but not a universal approach, is to lable 'no moves' as positive. This keeps continuity 1) isolating information carried by empirical negative returns; Models

2) better quality in negative market moves prediction.

The second is because of the assymetry of negative feeling reward for losing money (which one wants to avoid), as compared to the reward for gaining.

Note that we can't simply drop 'no move' observations from the data because that will our ability to predict for each next trading day -- therefore, P\&L backtesting will be affected.

 This demo is NOT about regression on past returns per se, and it is NOT about regression analysis. In fact, we will show how spurious Ordinary Least Squares resutls are, for this simple binomial classification.

OLS given for the illustration only. Regressing on past returns (=lagged values) is the common model-free setup known as Vector Autoregression (VAR). VAR does not work to predict daily return -- the order of error will be 150-200%.

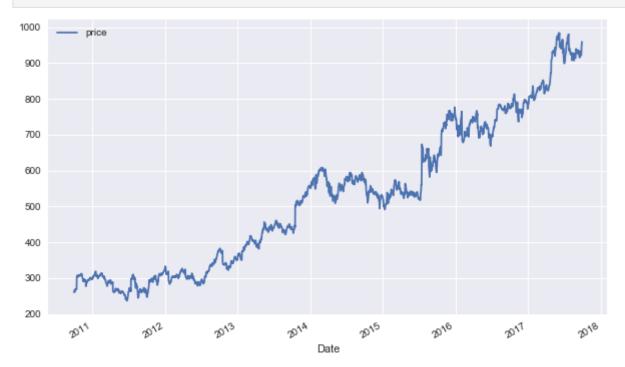
Second, OLS is not a valid regression model for binary dependent variable {0, 1}. To have non-linear link between dependent variable (such as binary 0,1 or Probability 0.01..0.99) the

`Genearalized Linear Models' approach was theoretically developed and Logistic Regression.

```
In [1]: import numpy as np
   import pandas as pd
   from pylab import plt
   plt.style.use('seaborn')
   %matplotlib inline
```

Getting Historical Data

In [7]: data.plot(figsize=(10, 6));



```
In [26]: # SEPARATE for Features Correlation
         data_advf = data.copy() #save a copy for advanced look at lagged returns over in
         data_advf['Returns'] = np.log(data_advf).diff()
         data_advf.head()
Out[26]:
                      price
                              Returns
                Date
         2010-09-30 261.91
                                 NaN
          2010-10-01 261.83 -0.000305
          2010-10-04 260.20 -0.006245
          2010-10-05 268.11
                            0.029947
          2010-10-06 266.18 -0.007225
         data['return'] = np.log(data / data.shift(1))
In [19]:
In [9]:
         data.head()
 Out[9]:
                      price
                               return
                Date
         2010-09-30 261.91
                                 NaN
          2010-10-01 261.83 -0.000305
          2010-10-04 260.20 -0.006245
          2010-10-05 268.11
                            0.029947
          2010-10-06 266.18 -0.007225
In [10]: lags = 5
         cols = []
         for lag in range(1, lags+1):
             col = 'ret %d' % lag
             data[col] = data['return'].shift(lag)
             cols.append(col)
         # Column indexation is from 0, so we effectively have range(1, 6) for returns
         # CHECK NOT TO USE Return IN ACTUAL PREDICTION
In [11]: data.head(10)
```

Out[11]:		price	return	ret_1	ret_2	ret_3	ret_4	ret_5
	Date							
	2010-09-30	261.91	NaN	NaN	NaN	NaN	NaN	NaN
	2010-10-01	261.83	-0.000305	NaN	NaN	NaN	NaN	NaN
	2010-10-04	260.20	-0.006245	-0.000305	NaN	NaN	NaN	NaN
	2010-10-05	268.11	0.029947	-0.006245	-0.000305	NaN	NaN	NaN
	2010-10-06	266.18	-0.007225	0.029947	-0.006245	-0.000305	NaN	NaN
	2010-10-07	264.02	-0.008148	-0.007225	0.029947	-0.006245	-0.000305	NaN
	2010-10-08	267.17	0.011860	-0.008148	-0.007225	0.029947	-0.006245	-0.000305
	2010-10-11	268.41	0.004631	0.011860	-0.008148	-0.007225	0.029947	-0.006245
	2010-10-12	269.68	0.004720	0.004631	0.011860	-0.008148	-0.007225	0.029947
	2010-10-13	270.64	0.003553	0.004720	0.004631	0.011860	-0.008148	-0.007225

```
In [12]: data.dropna(inplace=True)
          data = data.drop(columns="price")
          data['return_sign'] = np.sign(data['return'].values)
          data adv = data.copy() #save a copy for advanced methods (classifiers), as comp
In [13]:
          data.head()
Out[13]:
                        return
                                    ret_1
                                             ret_2
                                                       ret_3
                                                                 ret_4
                                                                           ret_5 return_sign
                Date
            2010-10-
                      0.011860 -0.008148 -0.007225 0.029947 -0.006245 -0.000305
                                                                                        1.0
                 80
          2010-10-11
                     0.004631
                                0.011860 -0.008148 -0.007225 0.029947 -0.006245
                                                                                        1.0
```

0.004631

0.003553 0.004720 0.004631

0.011860 -0.008148 -0.007225

0.011860 -0.008148

ASIDE: Correlation in Lagged Returns

0.004720

```
In [27]: # Create features (predictors) list
features_list = []
for r in range(10, 65, 5):
    data_advf['Ret_'+str(r)] = data_advf.Returns.rolling(r).sum()
    data_advf['Std_'+str(r)] = data_advf.Returns.rolling(r).std()
    features_list.append('Ret_'+str(r))
    features_list.append('Std_'+str(r))

# Drop NaN values
data_advf.dropna(inplace=True)
```

2010-10-12 0.004720

2010-10-13 0.003553

2010-10-14 -0.004370

1.0

1.0

-1.0

```
In [28]: # Derive features correlation
import seaborn as sns
corrmat = data_advf.drop(['price', 'Returns'],axis=1).corr()

# Visualize feature correlation
fig, ax = plt.subplots(figsize=(20,10))
sns.heatmap(corrmat, annot=True, annot=kws=("size": 10}, fmt="0.2f", linewidths
ax.set_title('Feature Correlation', fontsize=12, color='black');

**Feature Correlation**
**Retio**
*
```

Maximum Likelihood for Regression (Ordinary Least Squares)

Below work is illustration-only. Do not run OLS in your assignments and projects.

When the assumption of Normality of residuals holds: ϵ_t is iid $N(0, \sigma^2)$, the linear regression $y_t = \hat{\beta} x_t + \epsilon_t$ has MLE properties.

That means estimated coefficients $\hat{oldsymbol{eta}}$ are

- consistent (i.e., close to unknown true estimates $\boldsymbol{\beta}$ with low tolerance) and
- asymptotically efficient (i.e., their variance is known and minimised).

Estimates $\hat{\boldsymbol{\beta}}$ in fact, maximise the following **joint Normal** likelihood:

$$\mathbf{L} = \left(rac{1}{\sqrt{2\pi\sigma^2}}
ight)^T \exp{-rac{1}{2}igg[rac{\epsilon_1^2}{\sigma^2} + rac{\epsilon_2^2}{\sigma^2} + \cdots + rac{\epsilon_T^2}{\sigma^2}igg]}$$

Substituting $\epsilon_t = y_t - \hat{\beta} x_t$ and taking log gives for an individual observation -- I call this quantity a contribution of likelihood from an observation (data row values of features) at

time t

$$\log L_t = -rac{1}{2} \log 2\pi \sigma^2 - rac{1}{2} rac{(y_t - \hat{oldsymbol{eta}} oldsymbol{x_t})^2}{\sigma^2}$$

Total log-likelihood for a regression model is the sum of contributions from each observation $\log \mathbf{L} = \sum_{t=1}^T L_t.$

Numerical MLE varies $\hat{\beta}$ to maximise $\log \mathbf{L}$. This can be done by any non-specific optimisation routine, such as Excel Solver. It is clear to spot that log-likelihood is maximised by **minimising** the residual sum of squares

sum of squares
$$RSS = \sum_{t=1}^{T} \epsilon_t^2 = \sum_{t=1}^{T} (y_t - \hat{\boldsymbol{\beta}} \boldsymbol{x_t})^2$$
 for definition the first formulae $\boldsymbol{\beta}$

Residual sum of squares (RSS) is also known as the sum of squared residuals (SSR) or the sum of squared estimate of errors (SSE).

CAUTION OLS is an **invalid** model for binary dependent variable {0, 1}. Think about a change in MLE function for such variable.

In [13]: # Regression from NUMPY library
reg_coef = np.linalg.lstsq(data[cols].values, data['return_sign'])[0]
PREFER delegates to use STATSMOTELS
#import statsmodels.api as sm

/anaconda3/lib/python3.6/site-packages/ipykernel_launcher.py:2: FutureWarning: `rcond` parameter will change to the default of machine precision times ``max (M, N)`` where M and N are the input matrix dimensions.

To use the future default and silence this warning we advise to pass `rcond=No ne`, to keep using the old, explicitly pass `rcond=-1`.

In [14]: reg coef

Out[14]: array([1.13255353, 0.34409898, -2.87238464, -0.40975749, -1.38671844])

In [15]: data['ols_pred'] = np.sign(np.dot(data[cols].values, reg_coef)) #dot product

In [16]: data.head(15)

Out[16]:

	return	ret_1	ret_2	ret_3	ret_4	ret_5	return_sign	ols_pre
Date								
2010- 10-08	0.011860	-0.008148	-0.007225	0.029947	-0.006245	-0.000305	1.0	-1.
2010- 10-11	0.004631	0.011860	-0.008148	-0.007225	0.029947	-0.006245	1.0	1.
2010- 10-12	0.004720	0.004631	0.011860	-0.008148	-0.007225	0.029947	1.0	-1.
2010- 10-13	0.003553	0.004720	0.004631	0.011860	-0.008148	-0.007225	1.0	-1.
2010- 10-14	-0.004370	0.003553	0.004720	0.004631	0.011860	-0.008148	-1.0	-1.
2010- 10-15	0.106028	-0.004370	0.003553	0.004720	0.004631	0.011860	1.0	-1.
2010- 10-18	0.026677	0.106028	-0.004370	0.003553	0.004720	0.004631	1.0	1.
2010- 10-19	-0.016119	0.026677	0.106028	-0.004370	0.003553	0.004720	-1.0	1.
2010- 10-20	0.000231	-0.016119	0.026677	0.106028	-0.004370	0.003553	1.0	-1.
2010- 10-21	0.006582	0.000231	-0.016119	0.026677	0.106028	-0.004370	1.0	-1.
2010- 10-22	0.000885	0.006582	0.000231	-0.016119	0.026677	0.106028	1.0	-1.
2010- 10-25	0.006468	0.000885	0.006582	0.000231	-0.016119	0.026677	1.0	-1.
2010- 10-26	0.003381	0.006468	0.000885	0.006582	0.000231	-0.016119	1.0	1.
2010- 10-27	-0.003446	0.003381	0.006468	0.000885	0.006582	0.000231	-1.0	1.
2010- 10-28	0.003446	-0.003446	0.003381	0.006468	0.000885	0.006582	1.0	-1.

Count number of predicted moves UP and DOWN

```
In [17]: data['ols_pred'].value_counts()
    #c.value_counts()[1] / (c.value_counts().sum()) #We were UP this percentage of
Out[17]: -1.0    938
    1.0    819
    Name: ols_pred, dtype: int64
```

False Negatives -- Type II Error

The probelm transpires: the model is likely to be bad at predicting negative returns, there are a lot of **false negatives** with -1.0 label.

In terms of generated asset path: in case of bad prediction of negative returns (moves down) we can observe the path drifting downwards and downwards. But that is for later.

Vectorised	l Backtesting = R	ebalancing	h period	
	'ols_pred'	'return'	Result P\&L	
	NEGATIVE 'ols_pred'	NEGATIVE 'return'	POSITIVE P\&L	
	NEGATIVE 'ols_pred'	POSITIVE 'return' (move up)	NEGATIVE P\&L, Loss	
	POSITIVE 'ols_pred'	NEGATIVE 'return'	NEGATIVE P\&L, Loss	
	POSITIVE 'ols pred'	POSITIVE 'return' (move up)	POSITIVE P\&L	

Exercise care with Dr Hilpisch code, particularly on 'vectorised backtesting' where correctly predicted negative sign translates into the Positive P\&L -- that assumes daily rebalancing (betting) rather than replication of the actual asset path.

So above multiplication represents a sequence of daily bets, based on the sign (up/down move) predicted from past returns.

The actual return that realises today t, is \% P\&L that one makes (loses) on the bet of \$100, for example if return today is POSITIVE 0.018 and predcited sign was POSITIVE, then P\&L is 1.18%.

$$Return_{pred} = Z^* imes \sigma$$

Assume we want to have more model-like prediction. Then, we will use standard deviation, which gives some measure of randomness.

- We use std dev from the dataset but that can be estimated from any prevoius holdout period/window. Such backtesting requires past data but not regular daily update of return -- the latter is historical backtesting.
- $Z^*=\pm 0.7$ of the standard deviation translates into betting \%70 of one sigma -- the Actual P\&L which would still depend on actual return. But we can plot cumulative P\&L from 'ols_pred_move' to see if matches with the asset path. It also is possible to do P\&L Attribution test on such std dev model:

'ols_pred_move' is in effect, our Theoretical P\&L

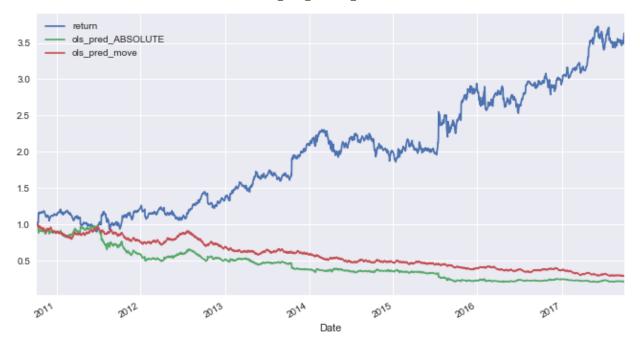
'return' is the Actual P\&L

- Why z-score of ± 0.7 ? This is because empirical asset returns are not well-Normal and between ± 2 standard deviation, but their density/histogram is high-peak (high mode). If you standardise returns $z_t=(r_t-\mu)/\sigma$ the histogram of z_t will have bars within ± 0.7 .
- Instead of ± 0.7 and to provide negative outcomes, we can use simulated values of Random Normal ϕ which can be positive or negative.

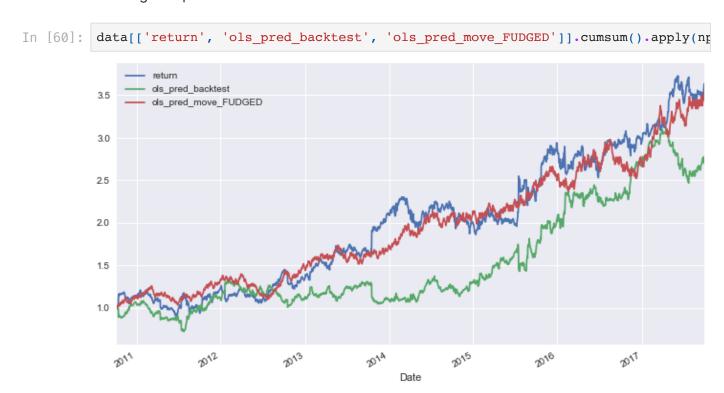
Out[53]:

	return	ret_1	ret_2	ret_3	ret_4	ret_5	return_sign	ols_pre
Date	•							
2010- 10-08	0.011860	-0.008148	-0.007225	0.029947	-0.006245	-0.000305	1.0	-1
2010- 10-11	0.004631	0.011860	-0.008148	-0.007225	0.029947	-0.006245	1.0	1
2010- 10-12	0.004720	0.004631	0.011860	-0.008148	-0.007225	0.029947	1.0	-1
2010- 10-13	0.003553	0.004720	0.004631	0.011860	-0.008148	-0.007225	1.0	-1
2010- 10-14	-0.004370	0.003553	0.004720	0.004631	0.011860	-0.008148	-1.0	-1
2010- 10-15	0.106078	-0.004370	0.003553	0.004720	0.004631	0.011860	1.0	-1
2010- 10-18	0.026677	0.106028	-0.004370	0.003553	0.004720	0.004631	1.0	1
2010- 10-19	-0.016119	0.026677	0.106028	-0.004370	0.003553	0.004720	-1.0	1
2010- 10-20	0.000231	-0.016119	0.026677	0.106028	-0.004370	0.003553	1.0	-1
2010- 10-21	0.006582	0.000231	-0.016119	0.026677	0.106028	-0.004370	1.0	-1
2010- 10-22	0.000885	0.006582	0.000231	-0.016119	0.026677	0.106028	1.0	-1
2010- 10-25	0.006/168	0.000885	0.006582	0.000231	-0.016119	0.026677	1.0	-1
2010- 10-26	0.003381	0.006468	0.000885	0.006582	0.000231	-0.016119	1.0	1
2010- 10-27		0.003381	0.006468	0.000885	0.006582	0.000231	-1.0	1
2010- 10-28	0.003/1/16	-0.003446	0.003381	0.006468	0.000885	0.006582	1.0	-1
2010- 10-29		0.003446	-0.003446	0.003381	0.006468	0.000885	-1.0	-1
2010- 11-01	0.007124	-0.007950	0.003446	-0.003446	0.003381	0.006468	1.0	-1
2010- 11-02	mmaza	0.002124	-0.007950	0.003446	-0.003446	0.003381	1.0	-1
2010- 11-03	0.007408	0.000979	0.002124	-0.007950	0.003446	-0.003446	1.0	1
2010- 11-04	H H H H H H K /	0.007408	0.000979	0.002124	-0.007950	0.003446	1.0	1

In [59]: data[['return', 'ols_pred_ABSOLUTE', 'ols_pred_move']].cumsum().apply(np.exp).r



• 'ols_pred_ABSOLUTE' and 'ols_pred_move' from std dev do not reproduce the asset price path at all. This plot reveals the poor quality of prediction. **FINDING:** correct negatives plus false negatives make for a bad prediction. OLS seems to produce a lot of negative predictions which do not realise.



INTERIM QUESTIONS

Why 'pred_return' does not match the asset path ('return'). ANSWER: because our
prediction is not a prediction but Daily Rebalanced P\&L, where correctly predicted
Negative move results in Positive P\&L increment.

 We have done worse than buy and hold: simply investing \$100 and holding the position.

FUDGED inverted sign applied to OLS prediction worked better at reproducing the asset price path. Whoa!

ANSWER: that's likely because of cancelled false negatives, ie, OLS produces a lot of negative predicitons which do not realise.

Remember OLS is an **invalid** regression model for binary dependent variable {0, 1}. **DO NOT** run OLS in your ML assignments and projects.

Logistic Classifier (in detail) // Support Vectors (comparison, no detail)

```
In [35]: from sklearn import linear_model
    from sklearn.svm import SVC #you can import ANY OTHER CLASSIFIER and proceed :
In [36]: lm = linear_model.LogisticRegression(C = 1e5)
    svcm = SVC(C= 1e5, probability=True)
```

As your vary the main penalty hyparameter C -- what happens to your coefficients for features?

• Logistic Classifier

C= 1e5 is nearly no L2 Penalty because parater set in inverse.

Try strong penalisation C=1 or 0.5 (or 0.01 for mild penalty.

What about L1 Penalty? (Answer: default setting is L2 penalty and you need to invoke another hyperparameter)

SVM Classifier

C= 1e5 NOT inverse for Support Vector Machines. This is Hard Margins.

Try Soft Margins which supposed to work better on time series.

Try smaller number of features -- SVM might work better

Maximum Likelihood in Binomial Classification (Logistic Classifier/Regression)

Let's find an analytical solution to the maximum likelihood estimation problem for a mix of independent identically distributed Bernoulli draws in the regression (prediction) setting.

Each $\{0,1\}$ putcome has a set of its own explanatory variables X_i .

$$y_i|m{X_i}\sim ext{Bernoulli}(p_i)$$
 $\mathbb{E}\left[y_i|m{X_i}
ight]=p_i$ $ext{Pr}\left(y_i=1,0
ight)=\left\{egin{array}{cccc} p_i & ext{whole} & ext{Transho} \ 1-p_i & ext{down} & ext{word} \end{array}
ight\}$ for $f(y_i;p_i)=p_i^{y_i}(1-p_i)^{1-y_i}$

Each outcome is determined by the probability of default p_i , which is unobserved (latent) in the regression model.

Logistic ML Part 1

The Bernoulli density above translates to the log-likelihood (contribution from one observation i).

$$\log L_i = \log f(y_i; p_i) = y_i \log p_i + (1-y_i) \log (1-p_i)$$

The joint og-likelihood for multiple events observed together and treated as independent, is given by the Product Rule of probabilties:

$$\log f(y_1,y_2,\ldots,y_N) = \log \prod_{i=1}^{N_{obs}} f(y_i;p_i)$$

$$= \sum_{i=1}^{N_{obs}} \log f(y_i;p_i)$$

$$\log L = \sum_{i=1}^{N_{obs}} \left[y_i \log p_i + (1-y_i) \log (1-p_i) \right]$$

$$y_i \text{ is known from dataset.}$$

$$p_i \text{ requires inverse of the link } p_i = g^{-1}(\boldsymbol{X}_i \boldsymbol{\beta}')$$

$$\text{Logistic ML Part 2}$$
 We can express Bernoulli density for a random variable $y = \{1,0\}$ in a more canonical form he are as a member of the Exponential family of distributions.

-- as a member of the Exponential family of distributions.

$$f(y;p) = p^y (1-p)^{1-y} = \exp\left[y\log\left(rac{p}{1-p}
ight) + \log(1-p)
ight]$$

Choice of a link function is \underline{the same for any categorical Y}

$$g(p) = \log\left(\frac{p}{1-p}\right)$$

 $g(p) = \log\left(\frac{p}{1-p}\right)$ Link Function

This is a logit function (different from logistic function!), which can be read as the ``log of odds". The inverse of logit function is logistic function, which we are interested in.

$$p = \frac{1}{1 + e^{-g}}$$



Under the hood: the choice of Link Function

To adapt the linear regression to non-linear output variable $y_i=0,1$ or Binomial $y_i = 0, 1, 2, 3, 4, \dots$ or in general case to probability we introduce a non-linear link function

Dependent Variable = Link Function (Probability)



$$PD \equiv \mathbb{E}[\mathbf{Y}|\mathbf{X}] = \mathbf{X}\boldsymbol{\beta}' \tag{3}$$

$$PD \equiv \mathbb{E}[\mathbf{Y}|\mathbf{X}] = \mathbf{X}\boldsymbol{\beta}'$$

$$g(p) = (\mathbf{X}\boldsymbol{\beta}')^{-1}$$
and
$$g(q) = g(\mathbf{X}\boldsymbol{\beta}')^{-1}$$
(5)

$$p = q(\mathbf{X}\boldsymbol{\beta}')^{-1} \tag{5}$$

Probability = **Inverse Link Function** (Dependent Variable)

- This covers default/no default $y_i = \{1,0\}$ and ordinal ratings $y_i = 1,2,3,4,5$. In fact, response variable Y can have any distribution from Exponential family (quasi MLE).
- Linear part βX is linked to a non-linear, latent variable (probability).

$$p = g(\boldsymbol{X}\boldsymbol{\beta}')^{-1}$$

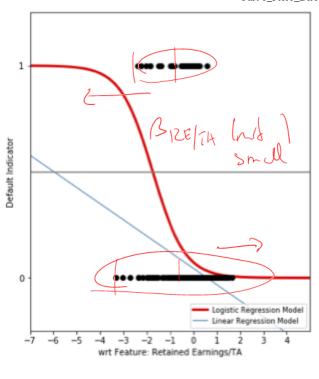
A link function is the clever bit that allows to convert a categorical event indicator $y_i = \{1, 0\}$ to the probability p_i

$$p_i = g^{-1}(\boldsymbol{X_i}\boldsymbol{eta}')$$

$$\begin{pmatrix} y_1 \\ \vdots \\ y_n \end{pmatrix} \Rightarrow \begin{pmatrix} g(\boldsymbol{X}_1 \boldsymbol{\beta}')^{-1} \\ \vdots \\ g(\boldsymbol{X}_n \boldsymbol{\beta}')^{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \operatorname{Prob}_1 \\ \vdots \\ \operatorname{Prob}_n \end{pmatrix}$$

Let's make a step forward and say that the inverse of our link will be the logistic sigmoid function,

$$p = \frac{1}{1 + e^{-X\beta'}} = \frac{e^{X\beta'}}{1 + e^{X\beta'}}$$



Firantial (RE/TA)=) Z-sc.

Platos

2D: Prediction

One

Pertur

Simill.

Albernahre

```
In [37]: # use data adv copy of the dataset
         lm.fit(data_adv[cols], data_adv['return_sign'])
         LogisticRegression(C=100000.0, class_weight=None, dual=False,
Out[37]:
                            fit intercept=True, intercept scaling=1, l1 ratio=None,
                            max_iter=100, multi_class='auto', n_jobs=None, penalty='l
         2',
                            random state=None, solver='lbfgs', tol=0.0001, verbose=0,
                            warm start=False)
In [41]: svcm.fit(data adv[cols], data adv['return sign'])
         SVC(C=100000.0, break ties=False, cache size=200, class weight=None, coef0=0.
Out[41]:
             decision function shape='ovr', degree=3, gamma='scale', kernel='rbf',
             max iter=-1, probability=True, random state=None, shrinking=True, tol=0.00
         1,
             verbose=False)
In [29]:
         def logistic_sigmoid(xb):
             return (1 / (1 + np.exp(-xb)))
```

In [119... #Procedure RELIES X_Features, Y_Response variables to be existing
def logistic_plot(X_min, X_max, FeatureName, FeatureBetaIdx):

 plt.clf() #clears the figure drawing space, nothing to do with classifier!
 fig, ax = plt.subplots(figsize=(18,10)) #fig = plt.figure(figsize=(18,10))

1. Plot two clusters of observations at Y={-1,1} on a scatter
 ax.scatter(data_adv[FeatureName], data_adv['logit_pred'], c=(data_adv['logi

2. Plot CALIBRATED sigmoid function -- with the correctly picked coeffice
 X_Sim = np.linspace(X_min, X_max, 100) #fill in values for the range of Axe
 Y_Loss = logistic_sigmoid(X_Sim * lm.coef_[0,FeatureBetaIdx] + lm.intercept
 # Y_Loss = logistic_sigmoid(X_Sim * logit.coef_[0,FeatureBetaIdx] + logit.:
 ax.plot(X_Sim, Y_Loss, color='red', linewidth=3) # plot sigmoid in Red

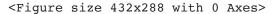
```
In [123... # Error message below will remain due to difference in data types passed into to
# TypeError: 'float' object cannot be interpreted as an integer

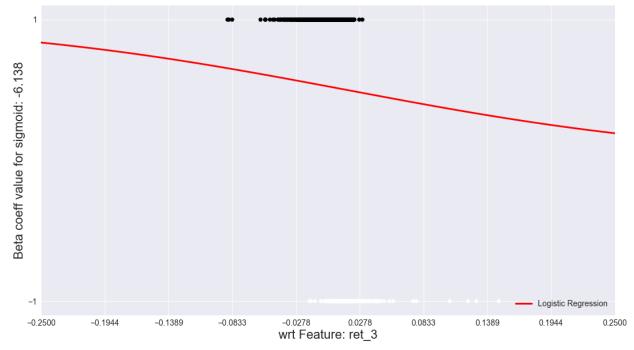
logistic_plot(-0.25, 0.25, 'ret_3', 2)

# 'ret_1' has lm.coef_[0,0]

# 'ret_3' has lm.coef_[0,2], the coefficient for our GOOG is -6.13818103, the integer
```

Out[123]: <matplotlib.axes._subplots.AxesSubplot at 0x7fe0dc157950>





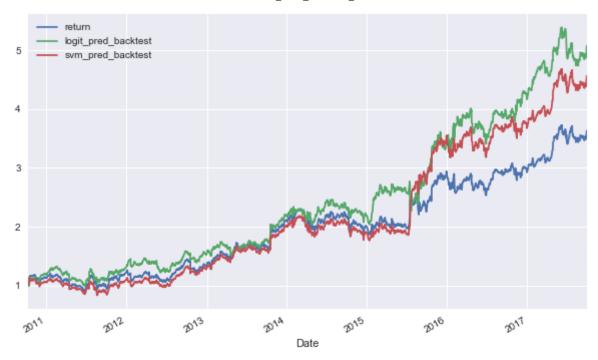
Above plot implements the inverse of our link will be the logistic sigmoid function,

$$p = \frac{1}{1 + e^{-X\beta'}}$$

```
In [122... data_adv['logit_pred'] = lm.predict(data_adv[cols])
    data_adv['logit_pred_backtest'] = data_adv['return'] * data_adv['logit_pred']
    data_adv['svm_pred'] = svcm.predict(data_adv[cols])
    data_adv['svm_pred_backtest'] = data_adv['return'] * data_adv['svm_pred']
In [62]: data_adv.head(20)
```

Out [62]: return ret_1 ret_2 ret_3 ret_4 ret_5 return_sign logit_p

	return	161_1	161_2	161_3	161_4	161_5	return_sign	iogit_p
Date								
2010- 10-08	0.011860	-0.008148	-0.007225	0.029947	-0.006245	-0.000305	1.0	
2010- 10-11	0.004631	0.011860	-0.008148	-0.007225	0.029947	-0.006245	1.0	
2010- 10-12	0.004720	0.004631	0.011860	-0.008148	-0.007225	0.029947	1.0	
2010- 10-13	0.003553	0.004720	0.004631	0.011860	-0.008148	-0.007225	1.0	
2010- 10-14	-0.004370	0.003553	0.004720	0.004631	0.011860	-0.008148	-1.0	
2010- 10-15	0.106028	-0.004370	0.003553	0.004720	0.004631	0.011860	1.0	
2010- 10-18	0.026677	0.106028	-0.004370	0.003553	0.004720	0.004631	1.0	
2010- 10-19	-0.016119	0.026677	0.106028	-0.004370	0.003553	0.004720	-1.0	
2010- 10-20	0.000231	-0.016119	0.026677	0.106028	-0.004370	0.003553	1.0	
2010- 10-21	0.006582	0.000231	-0.016119	0.026677	0.106028	-0.004370	1.0	
2010- 10-22	0.000885	0.006582	0.000231	-0.016119	0.026677	0.106028	1.0	
2010- 10-25	0.006468	0.000885	0.006582	0.000231	-0.016119	0.026677	1.0	
2010- 10-26	0.003381	0.006468	0.000885	0.006582	0.000231	-0.016119	1.0	
2010- 10-27	-0.003446	0.003381	0.006468	0.000885	0.006582	0.000231	-1.0	
2010- 10-28	0.003446	-0.003446	0.003381	0.006468	0.000885	0.006582	1.0	
2010- 10-29	-0.007950	0.003446	-0.003446	0.003381	0.006468	0.000885	-1.0	
2010- 11-01	0.002124	-0.007950	0.003446	-0.003446	0.003381	0.006468	1.0	
2010- 11-02	0.000979	0.002124	-0.007950	0.003446	-0.003446	0.003381	1.0	
2010- 11-03	0.007408	0.000979	0.002124	-0.007950	0.003446	-0.003446	1.0	
2010- 11-04	0.006582	0.007408	0.000979	0.002124	-0.007950	0.003446	1.0	



```
In []: # Instead of 0.7 we should use simulated Normal Random Variable
#or we end up with just gives exponentially rising plots, no down moves predict
#data_adv['logit_pred_move'] = 0.7 * stdev * (data_adv['logit_pred'])
#data_adv['svm_pred_move'] = 0.7 * stdev * (data_adv['svm_pred'])
```

Further Steps

- Do not rush to a quick conclusion as to which is better SVM/Decision Tree/Logistic Classifer. This is dependent on data history, frequency, historical regime (eg high volatility) and the model itself. SVM estimation with more than 2-3 features becomes very slow.
- Consider the accuracy and pattern of prediction within each class. This is mandatory.
- Investigate the Recall for negative moves, ie, False Negatives problem.
- Since this is binomial prediction $\{0,1\}$, you can plot **area under the ROC curve** and **confusion matrix** to investigate predictions within each class.
- Think of advantages and disadvantages of moving onto multinomial classification $\{-1,0,1\}$. For example what would you do if most of observations (daily return) will fall into category of 'no move'.

END OF DEMONSTRATION

In []:

More Features

Below is an initial set of features, which econometricans typically utilise, and a good starting-level textbook is Forecasting Methods and Applications by Hyndman, Makridakis, and Wheelwright. They dilligently consider lags, each relevant test such as F-statistic, ARIMA and how to implement seasonality. However that is typical econometrics aimed at quarterly, cyclically-dependent indicators such as GDP.

It is possible to get professional and utilise a Python wrapper for something like TA-Lib. However, we would like to be able to compupte technical analysis indicators from the first princiles, whenever possible.

```
In [ ]:
        def createFeatures(df):
             Below code features to an existing data frame
             df = df.rename(columns={df.columns[0]: 'price'})
             df['return'] = df.pct_change()
             df['log return'] = np.log(df['price']/df['price'].shift(periods=1))
             df['sign'] = df['log_return'].apply(lambda x: 0 if x<0 else 1)</pre>
            df['return_1d'] = df['return'].shift(periods=1)
            df['return_2d']= df['return'].shift(periods=2)
            df['return_5d'] = df['return'].shift(periods=5)
            df['momentum 1d']=df['price']-df['price'].shift(periods=1)
            df['momentum_2d']=df['price']-df['price'].shift(periods=2)
            df['momentum_5d']=df['price']-df['price'].shift(periods=5)
            df['MA_5d']=df['price'].rolling(5).mean()
            df['MA 10d']=df['price'].rolling(10).mean()
            df['MA 20d']=df['price'].rolling(20).mean()
            df['MA 50d']=df['price'].rolling(20).mean()
            df['EMA 5d']=df['price'].ewm(5, adjust=False).mean()
            df['EMA 10d']=df['price'].ewm(10, adjust=False).mean()
            df['EMA_20d']=df['price'].ewm(20, adjust=False).mean()
            df['EMA 50d']=df['price'].ewm(50, adjust=False).mean()
             return df
In [ ]:
```

```
In [ ]:
```