

Engineering Mathematics Homework 7 Solution

1. Find : $\mathcal{L}^{-1}\left\{\frac{-2s+6}{s^2+4}\right\}$

Sol:

$$\begin{aligned}\mathcal{L}^{-1}\left\{\frac{-2s+6}{s^2+4}\right\} &= \mathcal{L}^{-1}\left\{\frac{-2s}{s^2+4} + \frac{6}{s^2+4}\right\} \\ &= -2\mathcal{L}^{-1}\left\{\frac{s}{s^2+4}\right\} + 3\mathcal{L}^{-1}\left\{\frac{2}{s^2+4}\right\} \\ &= -2\cos 2t + 3\sin 2t\end{aligned}$$

2. Find : $\mathcal{L}^{-1}\left\{\left(\frac{2}{s} - \frac{1}{s^3}\right)^2\right\}$

Sol:

$$\begin{aligned}\mathcal{L}^{-1}\left\{\left(\frac{2}{s} - \frac{1}{s^3}\right)^2\right\} &= \mathcal{L}^{-1}\left\{\left(4 \times \frac{1}{s} - \frac{4}{3!} \times \frac{3!}{s^4} + \frac{1}{5!} \times \frac{5!}{s^6}\right)\right\} \\ &= 4t - \frac{2}{3}t^3 + \frac{1}{120}t^5\end{aligned}$$