



# ADVANCED ASSEMBLY PROGRAMMING

*PIC Microcontroller: An Introduction to  
Software & Hardware Interfacing*

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## Signed Arithmetic

- Some quantities can be positive or negative.
- A negative number is represented by the 2's complement of its magnitude.
- The subtract and add instructions can handle negative number properly when they are represented in 2's complement format.

## Modulo Math

- All computers uses limited number of bits to represent numbers.
- Adding  $2^8$  to a number in an 8-bit computer does not affect the result.
- Similarly, adding  $2^{16}$  and  $2^{32}$  to a number in a 16-bit and 32-bit computer do not affect the result.

## Procedure for Signed 8-bit Multiplication

### Step 1

Multiply two operands ( $op1 \times op2$ ) disregarding their signs.

### Step 2

If  $op1$  is negative, then subtract  $op2$  from the upper byte of the product.

### Step 3

if  $op2$  is negative, then subtract  $op1$  from the upper byte of the product.

## Procedure for Signed 16-bit Multiplication

### Step 1

Multiply two operands ( $op1 \times op2$ ) disregarding their signs.

### Step 2

If  $op1$  is negative, then subtract  $op2$  from the upper 16 bits of the product.

### Step 3

if  $op2$  is negative, then subtract  $op1$  from the upper 16 bits of the product.

**Example 4.1** Write a program to compute the product of two 8-bit signed numbers represented by data memory locations op1 and op2 and leave the product in file registers PRODH and PRODL.

**Solution:**

```
#include <p18F8720.inc>

op1    set    0x00    ; the first operand
op2    set    0x01    ; the second operand
num1   equ    0x87    ; test number 1
num2   equ    0x98    ; test number 2

org     0x00    ; reset vector
goto    start
org     0x08    ; high priority interrupt service routine
retfie
org     0x18    ; low priority interrupt service routine
retfie

start  movlw   num1    ; set up op1 for testing purpose
       movwf  op1,A   ;
       movlw  num2    ; set up op2 for testing purpose
       movwf  op2,A   ;
       movf   op1,W,A
```

```

mulwf    op2,A
btfsc    op2,7,A      ; test the sign bit of the second
operand
subwf    PRODH,F,A    ; if negative, eliminate extra term
movf     op2,W,A
btfsc    op1,7,A      ; test the sign bit of the first operand
subwf    PRODH,F,A    ; if negative, eliminate extra term
nop
end

```

**Example 4.2** Write a program to compute the product of two 16-bit signed integers and leave the product in memory locations represented by **result ... result+3**.

**Solution:**

```

#include <p18F8720.inc>
arg1_hi  set    0x00      ; high byte of the first argument
arg1_lo  set    0x01      ; low byte of the first argument
arg2_hi  set    0x02      ; high byte of the second argument
arg2_lo  set    0x03      ; low byte of the second argument
result   set    0x04      ; location to hold the product
num1_hi  equ    0x83      ; test number 1
num1_lo  equ    0x45      ;
num2_hi  equ    0x81      ; test number 2
num2_lo  equ    0x47      ;

```

```

                                org      0x00                ; reset vector
                                goto     start
                                ...                          ; interrupt service routines
start    movlw    num1_hi                ; set up test numbers
                                movwf   arg1_hi              ;
                                movlw    num1_lo              ;
                                movwf   arg1_lo              ;
                                movlw    num2_hi              ;
                                movwf   arg2_hi              ;
                                movlw    num2_lo              ;
                                movwf   arg2_lo              ;
                                movf     arg1_lo,W            ;
                                mulwf   arg2_lo              ; compute arg1_lo x arg2_lo
                                movff   PRODL,result
                                movff   PRODH,result+1
                                movf     arg1_hi,W
                                mulwf   arg2_hi              ; compute arg1_hi x arg2_hi
                                movff   PRODL,result+2
                                movff   PRODH,result+3
                                movf     arg1_lo,W
                                mulwf   arg2_hi              ; compute arg1_lo x arg2_hi
                                movf     PRODL,W
                                addwf   result+1,F

```

	movf	PRODH,W	
	addwfc	result+2,F	
	clrf	WREG	
	addwfc	result+3,F	; add carry to the most significant byte
	movf	arg1_hi,W	
	mulwf	arg2_lo	; compute $\text{arg1\_hi} \times \text{arg2\_lo}$
	movf	PRODL,W	
	addwf	result+1,F	
	movf	PRODH,W	
	addwfc	result+2,F	
	clrf	WREG	; add carry to the most significant byte
	addwfc	result+3,F	; "
	btfss	arg2_hi,7	; check the sign of arg2
	goto	sign_arg1	
	movf	arg1_lo,W	
	subwf	result+2,F	; delete extra term
	movf	arg1_hi,W	; "
	subwfb	result+3,F	; "
sign_arg1	btfss	arg1_hi,7	; check the sign of arg1
	goto	more	; continue to perform other operation
	movf	arg2_lo,W	
	subwf	result+2,F	; delete extra term

```
        movf    arg2_hi,W,A
        subwfb  result+3,F,A
more     nop
        end
```

## Unsigned Divide Operation

- Performed by repeated subtraction using the circuit shown in Figure 4.1.
- Registers N, R, and Q are initialized to the **divisor**, **0**, and the **dividend**.
- R and Q will hold the remainder and quotient at the end of the division operation.

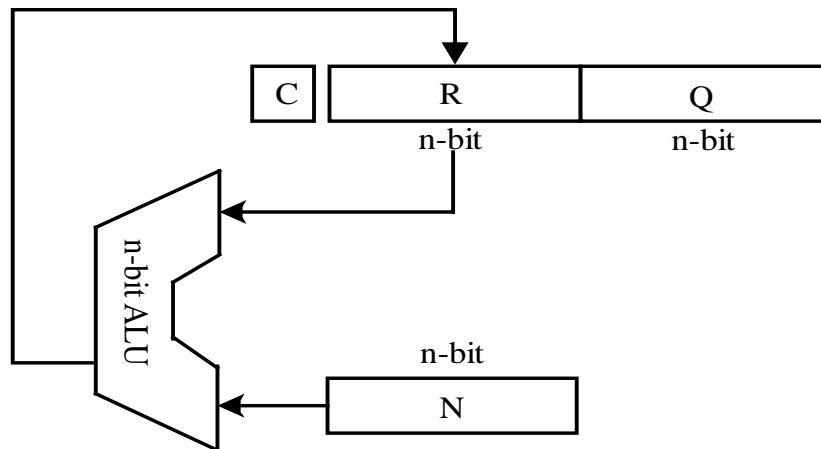


Figure 4.1 Division hardware



## Algorithm for Unsigned Division

Repeat the following steps  $n$  times

### Step 1

Shift the register pair (R, Q) one place to the left.

### Step 2

Subtract the contents of N from R and put the result back to R if the result is nonnegative.

### Step 3

If the result of Step 2 is negative, then set the least significant bit of Q to 0. Otherwise, set the least significant bit of Q to 1.

**Example 4.4** Write a program to divide an unsigned 16-bit number into another unsigned 16-bit number.

```
#include <p18F8720.inc>
```

```
radix    dec    ; set default radix to decimal
lp_cnt   set    0x00    ; loop count
temp     set    0x01    ; temporary storage
dsr       set    0x04    ; divisor
quo       set    0x06    ; quotient
rem       set    0x08    ; remainder
dd_h     equ    0x68    ; high byte of dividend test number
dd_l     equ    0x20    ; low byte of dividend test number
dr_h     equ    0x01    ; high byte of divisor test number
dr_l     equ    0x48    ; low byte of divisor test number
org       0x00
goto     start
org       0x08
retfie
org       0x18
retfie
start    movlw   dd_h    ; initialize Q register in Figure 4.1
         movwf   quo+1,A ;
         movlw   dd_l    ;
         movwf   quo,A   ;
         movlw   dr_h    ; initialize N register in Figure 4.1
         movwf   dsr+1,A ;
```



```

                                movlw    dr_l      ;   "
                                movwf    dsr,A        ;   "
                                clrf     rem,A        ; initialize R register in Figure 4.1 to 0
                                clrf     rem+1,A      ;   "
                                movlw    16
                                movwf    lp_cnt,A    ; initialize loop count to 16
loop    bcf     STATUS,C,A    ; clear the C flag
                                rlc      quo,F,A      ; rotate (R, Q) pair to the left one place
                                rlc      quo+1,F,A    ;   "
                                rlc      rem,F,A      ;   "
                                rlc      rem+1,F,A    ;   "
                                movf     dsr,W,A
                                subwf    rem,W,A
                                movwf    temp,A      ; save the low byte of the difference
                                movf     dsr+1,W,A
                                subwfb   rem+1,W,A
                                btfss    STATUS,C    ; skip if carry is 1
                                goto     less
                                bsf      quo,0,A      ; set the quotient bit to 1
                                movwf    rem+1,A      ; place the difference in R register
                                movff    temp,rem     ;   "

```

```

                goto    next
less           bcf      quo,0,A      ; set the quotient bit to 0
next          decfsz   lp_cnt,F,A    ; decrement the loop count and skip is zero
                goto    loop
                nop
                end

```

## Signed Division

- When dividend and divisor differs in sign, the sign of the quotient is minus.
- The sign of the remainder agrees with the dividend.

**Example 4.5** Write a PIC18 assembly program to perform the 8-bit signed divide operation and leave the quotient and remainder in registers labeled as **quo** and **rem**, respectively.

```
#include <p18F8720.inc>
```

```
radix    dec
sign     set    0x00
dvd      set    0x01    ; dividend
dsr      set    0x02    ; divisor
quo      set    0x03    ; quotient
rem      set    0x04    ; remainder
lp_cnt   set    0x05    ; loop count
dd       equ    0x82    ; test number for dividend
dr       equ    0xf5    ; test number for divisor

org      0x00
goto     start
org      0x08

retfie

org      0x18
retfie

start    bcf     sign,2,A    ; initialize the sign of quotient to positive
         bcf     sign,1,A    ; initialize the sign of dividend to positive
         bcf     sign,0,A    ; initialize the sign of divisor to positive
         movlw   dd
         movwf   dvd,A
         movlw   dr
         movwf   dsr,A
```



```

                btfss    dvd,7,A      ; check the sign of dividend
                goto     second
                btg      sign,2      ; change the sign of quotient
                bsf      sign,1      ; record the sign bit of the dividend
                negf     dvd,A        ; compute the magnitude of dividend
second          btfss    dsr,7,A      ; check the sign of the divisor
                goto     do_it
                btg      sign,2,A    ; change the sign of quotient
                bsf      sign,0,A    ; set the sign of the divisor
                negf     dsr,A        ; compute the magnitude of divisor
do_it          movf     dvd,W,A
                movwf    quo,A
                clrf     rem,A        ; initialize R register in Figure 4.1
                movlw    8
                movwf    lp_cnt,A    ; initialize loop count to 8
loop           bcf      STATUS,C,A   ; clear the C flag
                rlcf     quo,F,A     ; rotate (R, Q) pair to the left one place
                rlcf     rem,F,A     ;
                movf     dsr,W,A
                subwf    rem,W,A     ; subtract and leave the difference in WREG
                btfss    STATUS,C,A  ; skip if carry is 1

```

```

                goto    negative
                bsf     quo,0,A      ; set the least significant bit of Q1 to 1
                movwf   rem,A        ; place the difference in R1
                goto    next
negative       bcf     quo,0,A      ; set the quotient bit to 0
next          decfsz   lp_cnt,F,A   ; decrement the loop count and skip if zero
                goto    loop
                btfss   sign,2,A    ; skip if sign of quotient is negative
                goto    check_re    ;
                negf     quo,A
check_re      btfss   sign,1,A      ; skip if dividend is negative
                goto    ok_skip     ;
                negf     rem,A
ok_skip       nop
                end

```

## The Stack

- A first-in-last-out data structure.
- Has a stack pointer that points to the top byte or the byte above its top byte.
- A block of RAM of adequate size is required.
- The most common operations performed on the stack are **push** and **pop**.
- The push operation grows the stack while the pop operation shrinks the stack.
- A stack is often used to hold return address for subroutine calls or interrupt handling and temporary storage.



## PIC18 Software Stack

- PIC18 does not have a hardware stack (no dedicated stack pointer).
- One of the FSR registers can be used as the stack pointer. By convention, FSR1 is used as the stack pointer by the PIC18 C compiler.
- The PIC18 stack is shown in Figure 4.2

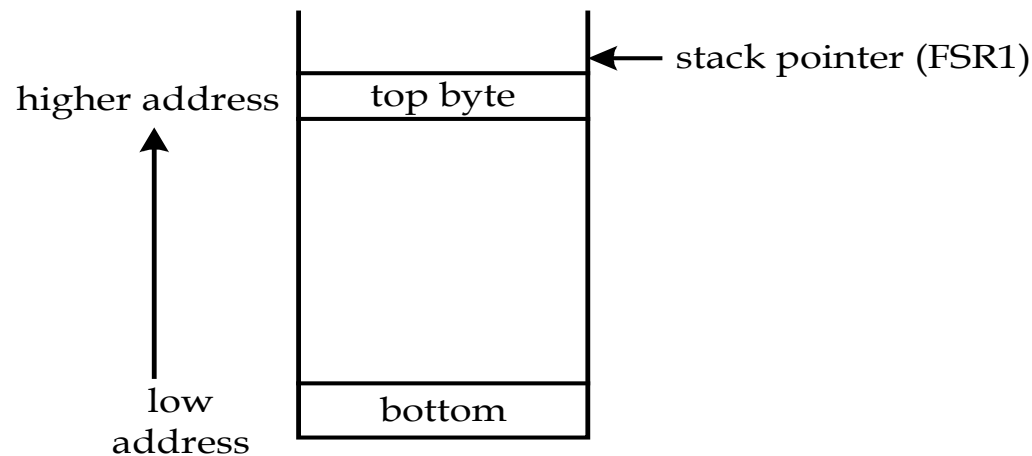


Figure 4.2 The PIC18 Software Stack

## Stack Macros

- **Push** and **pop** operations are often performed during a subroutine call.
- The user often needs to allocate and deallocate stack space during a subroutine call.
- Allocation and deallocation of stack space are performed during subroutine calls.

```
pushr macro      arg                ; macro to push the arg register
    movff         arg,POSTINC1
endm
```

```
popr  macro      arg                ; arg is a file register
    movff         POSTDEC1,arg        ; decrement the stack pointer
    movff         INDF1,arg           ; pop off a byte from the stack onto arg
endm
```

```
push_dat
macro      dat                ; this macro push the value dat onto the
stack
    movlw        dat
    pushr        WREG
endm
```

## Stack Macros (continued)

**alloc\_stk**      macro      n                      ; this macro allocates n bytes in stack  
                 movlw      n  
                 addwf      FSR1L,F,A  
                 movlw      0x00  
                 addwfc      FSR1H,F,A  
                 endm

**dealloc\_stk**      macro      n                      ; this macro deallocates n bytes from stack  
                 movlw      n  
                 subwf      FSR1L,F,A  
                 movlw      0  
                 subwfb      FSR1H,F,A              ; subtract borrow from high byte of FSR1  
                 endm

## Examples of Stack Macros Applications

1. Push PRODL into the software stack

```
pushr      PRODL
```

2. Pop PRODL from the software stack

```
popr      PRODL
```

3. Push the value 0x20 onto the software stack

```
push_dat   0x20
```

4. Allocate 10 bytes of stack space

```
alloc_stk   10
```

5. Deallocate 10 bytes from the stack

```
dealloc_stk 10
```

## Subroutines

- A sequence of instructions that can be called from many different places in a program.
- Parameters can be passed to the subroutine so that it can perform operations on different variables.
- Allows the user to use divide-and-conquer strategy to solve complicated problems.
- Using subroutines can in some cases reduce the code size significantly.

## Structured Programming methodology

- Start with a main program that outlines the logical flow of the algorithm
- Assign program details to subroutines
- A subroutine may also call other subroutines

## PIC18 Mechanisms to Support Subroutine Calls

- A 31-slot **return address stack** for saving and restoring return address
- A **return address stack pointer** points to the top of the return address stack.
- The **push** and **pull** instructions for pushing values onto the return address stack and pulling values into program counter from the return address stack
- A one-layer deep **fast register stack** for fast saving and restoring the STATUS, WREG, and BSR registers during interrupts and subroutine calls
- The **rcall n** and **call k[,s]** instructions for making subroutine calls.
- The **return [s]** instruction for returning from the subroutine
- The **retlw n** instruction for table lookup
- The **s** bit option allows one to save WREG, STATUS, and BSR in the fast register stack when making subroutine calls and restore them before returning from the subroutine

## The CALL n[,s] Instruction

- A 2-cycle, 32-bit instruction
- **n** is a 20-bit value that specifies the word address of the subroutine.
- The **s** bit allows the PIC18 to save WREG, STATUS, BSR in the fast register stack.

## The RCALL n instruction

- **n** is an 11-bit signed integer that specifies the distance of the subroutine to be called.
- Allows the PIC18 to call a subroutine that is 1-KW away
- The address of the subroutine to be called is at  $PC+2+2n$ .
- A 16-bit, two-cycle instruction

## The return [s] instruction

- Return from subroutine
- When **s** is 1, the contents of the fast return stack will be popped off to WREG, STATUS, and BSR registers.
- The top entry of the return address stack will be popped off and loaded into the PC.

## The retlw k instruction

- The WREG register is loaded with k.
- The top entry of the return address stack will be popped off and loaded into the PC.



## Examples of Subroutine Calls and Returns

```
        call    sub_x, FAST    ; save BSR, STATUS, and WREG in fast
        ...                  ; register stack
        ...
sub_x    ...
        ...
        return  FAST          ; restore values saved in fast register stack
```

### Table Lookup Instruction: retlw

```
        movlw   i              ; prepare to lookup the ith entry
        call    look_up
        ...
        ...
look_up  addwf   PCL            ; jump to one of the following entries
        retlw   k0
        retlw   k1
        ...
        retlw   kn            ; end of table
```

## Issues Related to Subroutine Calls

- **Parameter passing.**

1. Use general-purpose registers
2. Use the stack
3. Use global memory (same as method 1 for PIC18)

- **Result returning**

1. Use general-purpose registers
2. Use the stack
3. Use global memory (same as method 1 for PIC18)

- **Allocation and deallocation of local variables**

1. Local variables are allocated when the subroutine is entered.
2. Local variables are deallocated before returning from the subroutine

## The Stack Frame

- Stack frame is a data structure that holds the incoming parameters, saved registers, and local variables for the subroutine.
- A frame pointer is beneficial for managing the stack frame.
- The **stack pointer** may change during the lifetime of a subroutine, which sometimes makes the access of stack element tricky.
- The **frame pointer** points to a fixed location in the stack and does not change during the lifetime of the subroutine.
- By convention, the FSR2 register is used as the frame pointer.
- The PIC18 stack frame is shown in Figure 4.5.

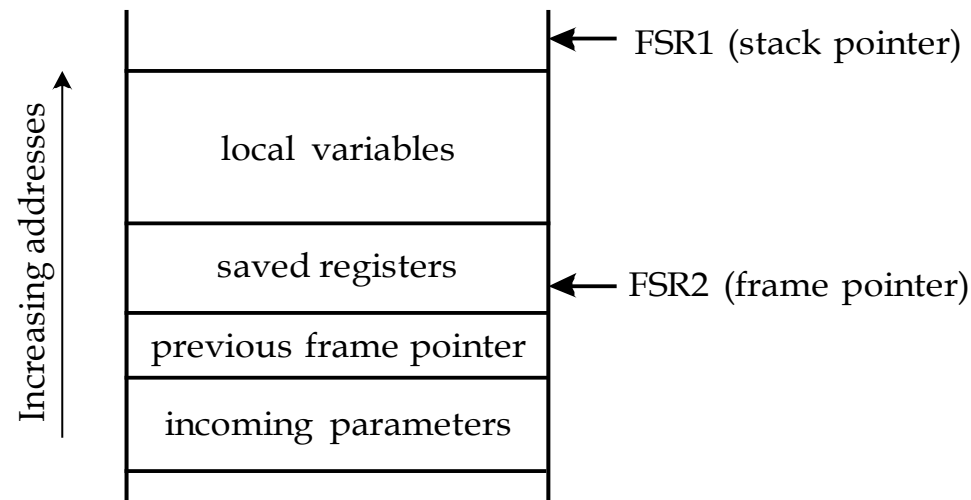


Figure 4.5 PIC18 Stack frame

## Functioning of the Stack Frame

- Upon entry to a subroutine, the value of FSR2 is pushed onto the stack and the value of FSR1 is copied into FSR2.
- Some registers are pushed onto the stack.
- Local variables are allocated in the stack.
- Incoming parameters have negative offsets relative to the FSR2 register.
- Local variables have positive offsets relative to FSR2.

## A stack frame example

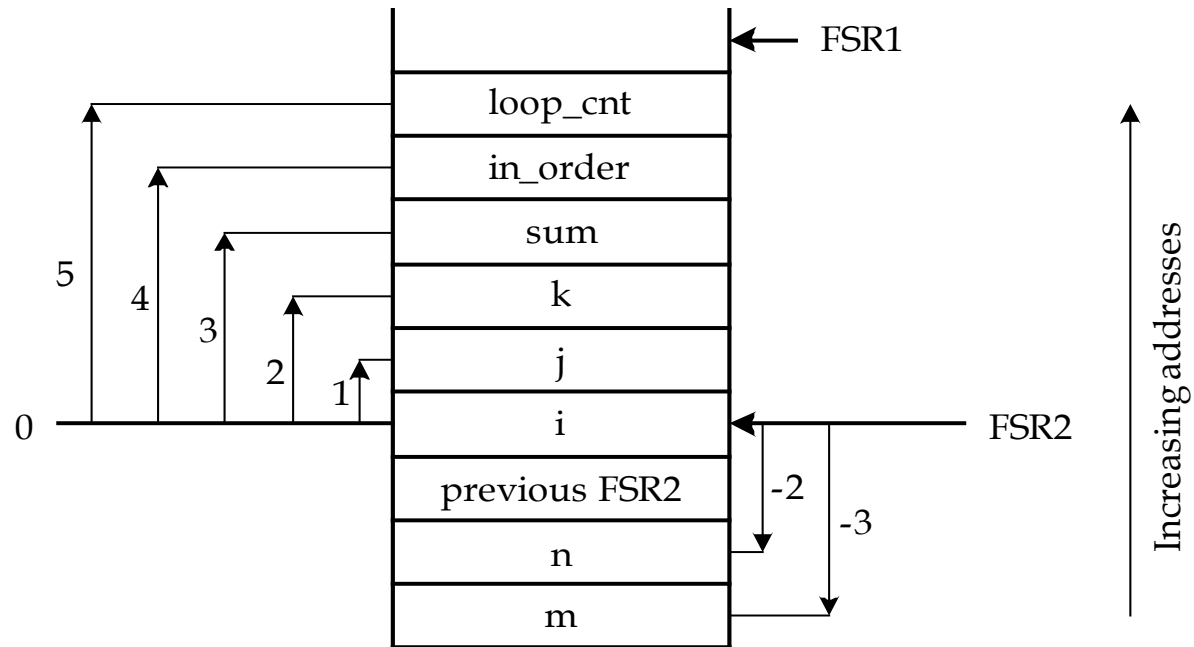


Figure 4.6 Stack frame and variable offsets

## Accessing Locations in the Stack Frame

- Each stack frame slot has an offset relative to the slot pointed to by FSR2
- Assign a name to each stack frame slot by using the **equ** directive
- Execute the **movf PLUSW2,W** instruction

```
loop_cnt equ    5        ; offset of loop_cnt from frame pointer
in_order equ    4        ; offset of in_order from frame pointer
sum      equ    3        ; offset of sum from frame pointer
k        equ    2        ; offset of k from frame pointer
j        equ    1        ; offset of j from frame pointer
i        equ    0        ; offset of i from frame pointer
n        equ   -2        ; offset of n from frame pointer
m        equ   -3        ; offset of m from frame pointer
; loading sum into WREG
        movlw    sum
        movf     PLUSW2,W
; loading m into WREG
        movlw    m
        movf     PLUSW2,W
```

**Example 4.9** Write a subroutine to find the maximum element of an array of 8-bit elements in program memory. Pass the array count and starting address in the software stack.

**Solution:**

The caller of this subroutine will

1. Push the low part of the array starting address onto the stack.
2. Push the high part of the array starting address onto the stack.
3. Push the upper part of the array starting address onto the stack.
4. Push the array count onto the stack.

The subroutine will

1. Push FSR2L and FSR2H onto the stack
2. Copy FSR1 to FSR2
3. Push TBLPTRL, TBLPTRH, and TBLPTRU onto the stack
4. Allocate two bytes in the stack for local variables (one byte for **lp\_cnt**, and one byte for **ar\_max**)

These operations need planning and thinking.

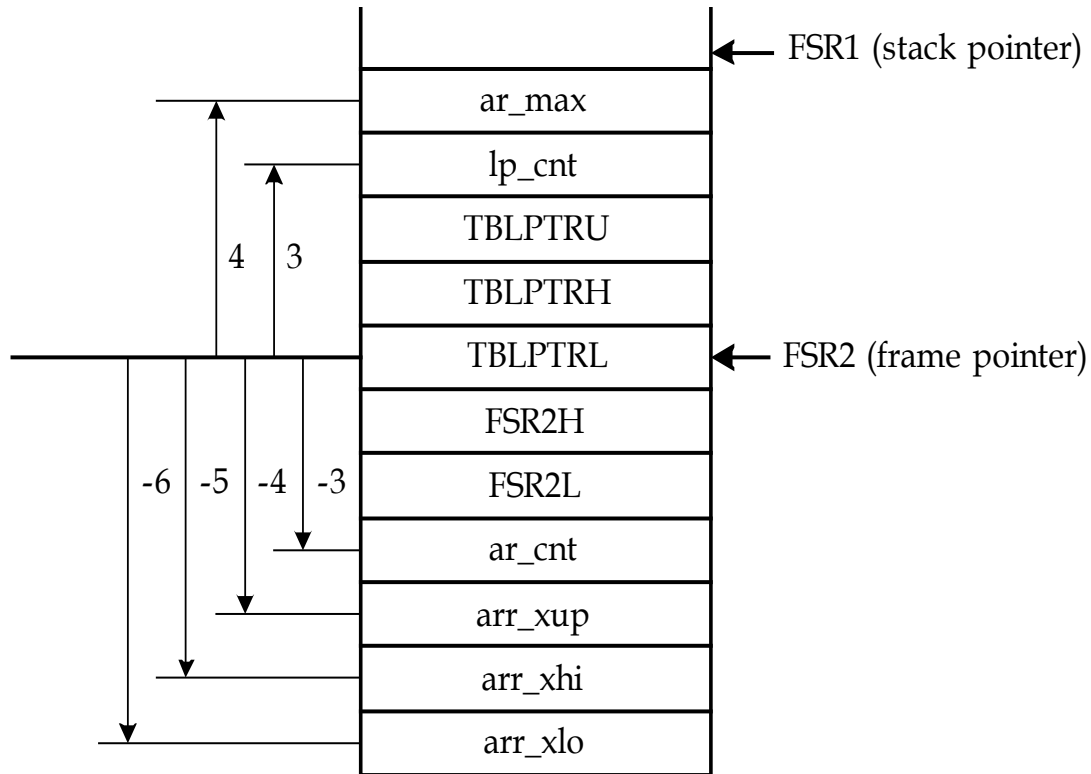


Figure 4.7 Stack frame for Example 4.9



```
#include <p18F8720.inc>
```

```
radix    dec
acnt     equ    32          ; array count
lp_cnt   equ    3          ; stack frame offset for lp_cnt
ar_max   equ    4          ; stack frame offset for array max
ar_cnt   equ    -3         ; stack frame offset for array count
arr_xup  equ    -4         ; stack frame offset for array base
arr_xhi  equ    -5         ;      "
arr_xlo  equ    -6         ;      "
array_max set    0x00      ; register to hold array max
org      0x00              ; reset vector
goto     start
org      0x08
retfie
org      0x18
retfie
start    lfsr    FSR1,0xE00 ; set up software stack pointer
movlw    low arr_x          ; pass array base in the stack
pushr    WREG               ;      "
movlw    high arr_x         ;      "
pushr    WREG               ;      "
movlw    upper arr_x        ;      "
```

```

pushr    WREG          ;
movlw    acnt           ; pass array count in stack
pushr    WREG          ;
call     find_amax,FAST ; call the subroutine
movff    PRODL,array_max ; save the result
dealloc_stk      4      ; clean up the allocated stack

```

space

```

nop

```

```

here     bra     here

```

```

. *****
;

```

; This subroutine finds the maximum element of an 8-bit array and returns it in PRODL.

```

. *****
;

```

```

find_max pushr    FSR2L      ; save caller's frame pointer
           pushr    FSR2H      ;
           movff    FSR1L,FSR2L ; set up new frame pointer
           movff    FSR1H,FSR2H ;
           pushr    TBLPTRL     ; save table pointer in stack
           pushr    TBLPTRH     ;
           pushr    TBLPTRU     ;
           alloc_stk 2          ; allocate 2 bytes for local variables
           movlw    ar_cnt
           movff    PLUSW2,PRODL ; copy array count into PRODL

```

```

    decf    PRODL,F,A
    movlw   lp_cnt
    movff   PRODL,PLUSW2    ; initialize lp_cnt to arcnt-1
    movlw   arr_xlo          ; place array pointer in TBLPTR
    movff   PLUSW2,TBLPTRL   ;
    movlw   arr_xhi          ;
    movff   PLUSW2,TBLPTRH   ;
    movlw   arr_xup          ;
    movff   PLUSW2,TBLPTRU   ;
    tblrd*+          ; assign arr_x[0] as the initial array max
    movlw   ar_max           ;
    movff   TABLAT,PLUSW2    ;
cmp_lp:  movlw   lp_cnt
    tstfsz  PLUSW2
    goto    next
    goto    done
next:    movlw   lp_cnt
    decf    PLUSW2,F          ; decrement the loop index
    tblrd*+          ; read in the next array element
    movlw   ar_max
    movf    PLUSW2,W,A
    cpfsgt  TABLAT

```

```

        movlw    ar_max
        movff    TABLAT,PLUSW2    ; update the current array max
        goto    cmp_lp
done    movlw    ar_max
        movff    PLUSW2,PRODL
        dealloc_stk                2; deallocate local variables
        popr     TBLPTRU
        popr     TBLPTRH
        popr     TBLPTRL
        popr     FSR2H
        popr     FSR2L
        return    FAST
; define an array of 32 8-bit elements.
arr_x   db       1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16
        db       17,18,19,20,21,22,23,24,25,26,27,28,29,30,31,32
        end

```

## Binary Search

- Searching an array or a file is a common operation.
- An efficient search algorithm can be applied to a sorted array or file.
- Binary search is a very efficient search algorithm.
- Divide the sorted array into three parts: upper half, middle element, and lower half.
- Use three array indices to guide the search of the array: min, mean, and max.
- The index **min** refers to the lowest array index for searching.
- The index **max** refers to the highest array index for searching.
- The index **mean** is the average of **min** and **max**.

## Binary Search Algorithm

### Step 1

Use *max* and *min* as the upper and lower indices of the array for searching and initialize *max* and *min* to  $n - 1$  and  $0$ , respectively.

### Step 2

If  $max < min$ , then stop. No element matches the key.

### Step 3

Let  $mean = (min + max)/2$ .

### Step 4

If  $key = array\_y[mean]$ , then key is found; stop.

### Step 5

If  $key < array\_y[mean]$ , then set *max* to **mean - 1** and go to Step 2.

### Step 6

If  $key > array\_y[mean]$ , then set *min* to **mean + 1** and go to Step 2.

**Example 4.10** Write a subroutine to implement the binary search algorithm. The starting address of the array, array count, and search key are passed in the stack. A value of 1 will be returned in PRODL if the key is found in the array. Otherwise, a value of 0 will be returned.

**Solution:**

- This subroutine saves the table pointer in the stack and allocates four bytes for local variables.

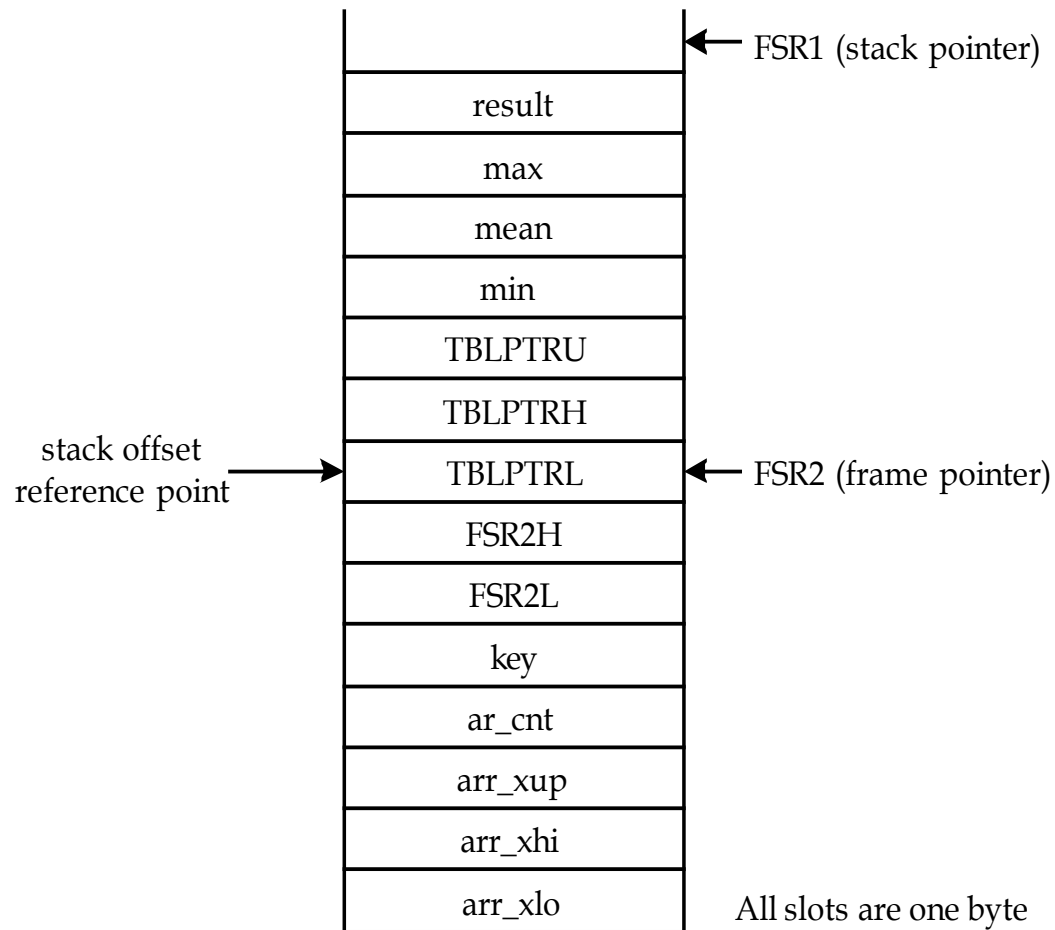


Figure 4.8 Stack frame of example 4.10



## Binary Search Subroutine and Test Program

```
#include <p18F8720.inc>
radix    dec

; -----
; include stack macros pushr, push_dat, popr, alloc_stk, and dealloc_stk here
; -----
acnt      equ    32          ; array count
local_var equ    4          ; number of bytes for local variables
skey      equ    7          ; key for search
min       equ    3          ; offset for lower bound of search range index
mean      equ    4          ; offset for middle element index
max       equ    5          ; offset for upper bound of search range index
result    equ    6          ; offset for search result
key       equ    -3         ; offset for search key
ar_cnt    equ    -4         ; stack frame offset for array count
arr_xup   equ    -5         ; stack frame offset for array base
arr_xhi   equ    -6         ;      "
arr_xlo   equ    -7         ;      "
find_it   set     0x00       ; register to hold array max
          org     0x00       ; reset vector
          goto    start
          org     0x08
          retfie
```

```

                                org      0x18
                                retfie

start    lfsr      FSR1,0xE00    ; set up software stack pointer
         movlw    low arr_x      ; pass array base in the stack
         pushr    WREG           ;
         movlw    high arr_x     ;
         pushr    WREG           ;
         movlw    upper arr_x    ;
         pushr    WREG           ;
         movlw    acnt           ; pass array count in stack
         pushr    WREG           ;
         movlw    skey           ; pass key for search
         pushr    WREG
         call     bin_search,FAST ; call the subroutine
         movff    PRODL,find_it  ; save the result
         dealloc_stk      5      ; clean up the stack space used by param
         nop

here     bra      here

bin_search    pushr    FSR2L    ; save callers frame pointer
              pushr    FSR2H    ;
              movff    FSR1L,FSR2L ; set up frame pointer
              movff    FSR1H,FSR2H ;

```

```

pushr    TBLPTRL      ; save table pointer in stack
pushr    TBLPTRH      ; "
pushr    TBLPTRU      ; "
alloc_stk local_var    ; allocate space for local variables
movlw    ar_cnt        ; max ← (ar_cnt – 1)
movff    PLUSW2,PRODL  ; "
decf     PRODL,F,A     ; "
movlw    max           ; "
movff    PRODL,PLUSW2  ; "
movlw    min           ; min ← 0
clrf     PLUSW2,A      ; "
movlw    result
clrf     PLUSW2        ; set the search result to not found
bloop    movlw    max
movff    PLUSW2,PRODL  ; place max index in PRODL
movlw    min
movff    PLUSW2,WREG   ; place min index in W
cpfslt   PRODL         ; is max < min?
goto     do_it         ; max >= min and continue
goto     done          ; no match is found in the array
do_it    addwf     PRODL,F,A ; compute (min+max), this may set C flag
bfc      STATUS,C     ; compute (min+max)/2 and place it

```

```

rrcf      PRODL,F,A      ; in PRODL
movlw     mean
movff     PRODL,PLUSW2    ; place mean index in the stack frame slot
; compare array[mean] with the search key
movlw     arr_xlo         ; place array base in TBLPTR
movff     PLUSW2,TBLPTRL;      "
movlw     arr_xhi         ;      "
movff     PLUSW2,TBLPTRH;     "
movlw     arr_xup         ;      "
movff     PLUSW2,TBLPTRU;     "
; add mean to TBLPTR to compute the address of arr_x[mean]
movf      PRODL,W,A      ; add lower 8 bits of mean to
addwf     TBLPTRL,F,A     ; TBLPTR
movlw     0               ;      "
addwfc    TBLPTRH,F,A     ;      "
addwfc    TBLPTRU,F,A     ;      "
tblrd*                    ; read array[mean] into TABLAT
; compare key with array[mean]
movlw     key
movf      PLUSW2,W,A      ; place key in WREG
cpfseq    TABLAT,A
goto     not_equal

```

```

                                movlw    result
                                incf      PLUSW2,F          ; set search result to "found"
                                goto      done
not_equal cpfslt              TABLAT,A
                                goto      go_low
                                movlw     mean
                                movff     PLUSW2,PRODL
                                incf      PRODL,F,A
                                movlw     min
                                movff     PRODL,PLUSW2      ; set min to mean+1 to
go_low  goto                  bloop                          ; search upper half
                                movlw     mean
                                movff     PLUSW2,PRODL
                                decf      PRODL,F,A
                                movlw     max
                                movff     PRODL,PLUSW2      ; set max to mean - 1 and
                                goto      bloop              ; search lower half
done  movlw                   result
                                movff     PLUSW2,PRODL      ; place the result in PRODL before return
                                dealloc_stk                  local_var ; deallocate local variables
                                popr       TBLPTRU
                                popr       TBLPTRH

```

```
    popr    TBLPTRL
    popr    FSR2H
    popr    FSR2L
    return  FAST
```

; define an array of 32 8-bit elements for testing purpose. The element arr\_x[i] is  
; located at arr\_x[0] + i

```
arr_x    db      1,2,3,4,5,6,7,8,9,10
          db      11,12,13,14,15,16,17,18,19,20
          db      21,22,23,24,25,26,27,28,29,30
          db      31,32
end
```

**Example 4.11** Convert the unsigned 16-bit division program into a subroutine. The caller of this subroutine will push the dividend and divisor into the stack and make a hole in the stack for this subroutine to return the remainder and the quotient.

**Solution:**

The caller of this subroutine will do the following

- Push the dividend onto the stack
- Make a hole of two bytes to hold the remainder
- Push the divisor onto the stack

The **divu16** subroutine will do the following

- Push the FSR2 onto the stack
- Copy FSR1 to FSR2 (set up new frame pointer)
- Save PRODL in the stack
- Allocate space for local variables

The stack frame of this subroutine is shown in Figure 4.9.

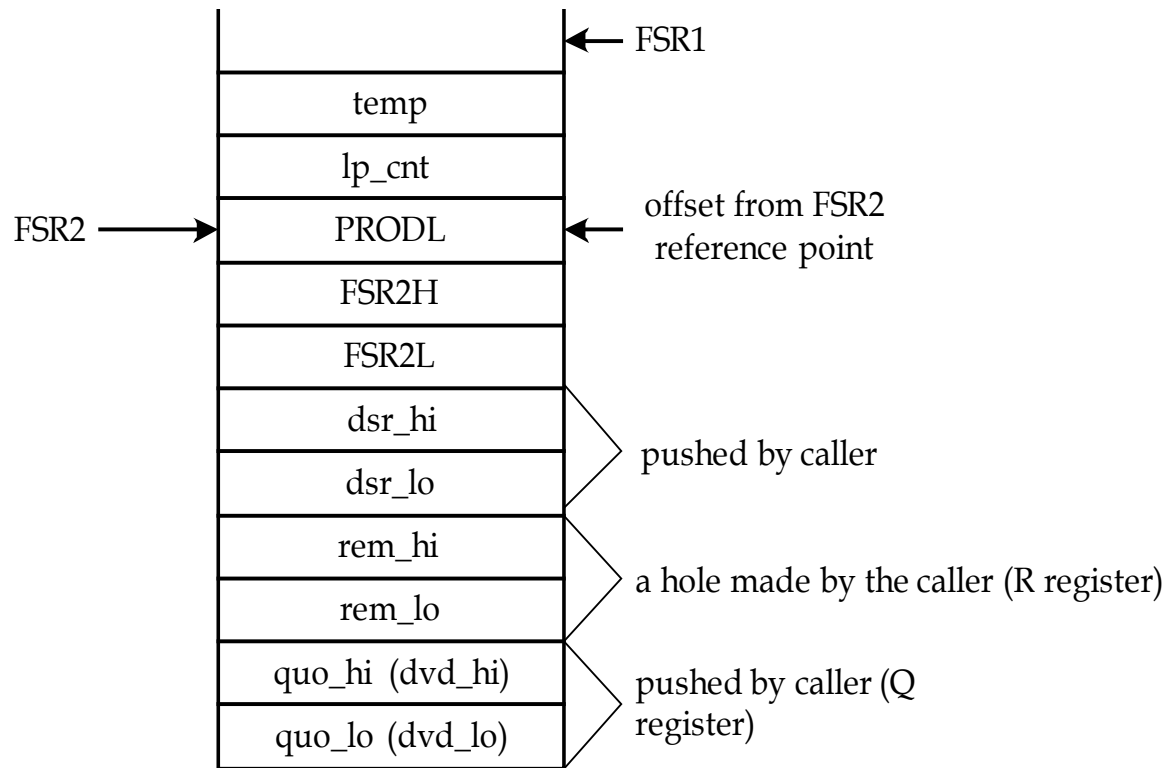


Figure 4.9 Stack frame of example 4.11



```
#include <p18F8720.inc>
```

```
radix      dec
```

```
; ---
```

```
; include macros pushr, popr, alloc_stk, and dealloc_stk here
```

```
; ---
```

```
loc_var    equ      2          ; local variable size
```

```
lp_cnt     equ      1          ; loop count
```

```
temp       equ      2          ; temporary storage
```

```
quo_hi     equ     -7          ; offset for quotient and dividend
```

```
quo_lo     equ     -8          ;      "
```

```
rem_hi     equ     -5          ; offset for remainder
```

```
rem_lo     equ     -6          ;      "
```

```
dsr_hi     equ     -3          ; offset for divisor
```

```
dsr_lo     equ     -4          ;      "
```

```
dd_h       equ     0xEC        ; high byte of dividend test number
```

```
dd_l       equ     0x46        ; low byte of "
```

```
dr_h       equ     0x00        ; high byte of divisor test number
```

```
dr_l       equ     0x87        ; low byte of "
```

```
quo        set     0x00        ; memory space to hold the quotient
```

```
rem        set     0x02        ; memory space to hold the remainder
```

```
org        0x00
```

```
goto       start
```

```



```

```

rlcf      PLUSW2,F      ; "
movlw     rem_lo        ; get the low byte of the remainder in
movff     PLUSW2,PRODL  ; PRODL
movlw     dsr_lo        ; get the low byte of the divisor in WREG
movf      PLUSW2,W      ; "
subwf     PRODL,F,A
movlw     temp
movff     PRODL,PLUSW2  ; save the low byte of difference at temp
movlw     rem_hi
movff     PLUSW2,PRODL
movlw     dsr_hi
movf      PLUSW2,W
subwfb    PRODL,F      ; subtract the high byte
btfss     STATUS,C      ; skip if carry is 1
goto      less
movlw     quo_lo
bsf       PLUSW2,0      ; set the quotient bit to 1
movlw     rem_hi
movff     PRODL,PLUSW2  ; place the difference in the R register
movlw     temp          ; "
movff     PLUSW2,PRODL  ; "
movlw     rem_lo        ; "

```

```

        movff    PRODL,PLUSW2 ;      "
        goto     next
less    movlw    quo_lo
        bcf      PLUSW2,0      ; set the quotient bit to 0
next    movlw    lp_cnt
        decfsz   PLUSW2,F      ; decrement the loop count and skip if zero
        goto     loop
        dealloc_stk loc_var    ; deallocate local variables
        popr     PRODL
        popr     FSR2H
        popr     FSR2L
        return   FAST
        end

```

## String Processing

- A string is a sequence of characters terminated by a NULL character.
- A character is encoded in ASCII code.
- Strings are needed in input and output.
- A number must be converted to ASCII code before it can be output.
- The decimal number 10805 will be converted to 0x31 0x30 0x38 0x30 0x35
- A binary number can be converted to its equivalent decimal string by performing repeated division by 10.
- The remainder of the first division is the least significant digit, the last division will separate the most significant digit and second most significant digit.

**Example 4.12** Write a subroutine to convert a 16-bit signed number to an ASCII string that represents its equivalent decimal value.

**Solution:** Let **p**, **rem**, **quo**, and **sign** represent the integer to be converted, remainder after the divide-by-10 operation, the quotient after the divide-by-10 operation, and the sign of **p**, respectively. The algorithm for converting a binary number into a decimal string is as follows:

**Step 1**

If  $p = 0$ , then store '\$30' and '\$00' in the buffer and stop.

**Step 2**

If  $p < 0$ , then set **sign** to 1 and compute **p**'s 2's complement. Otherwise, set **sign** to 0.

**Step 3**

Divide **p** by 10 and leave the remainder and the quotient in **rem** and **quo**, respectively.

**Step 4**

Add '\$30' to the remainder and save it in the next available space in the buffer.

**Step 5**

If  $quo \neq 0$  then  $p \leftarrow quo$  and go to Step 3.

**Step 6**

Push the characters in the buffer into the stack.

**Step 7**

If **sign** is 1, then store the ASCII code of the minus sign as the first character in the buffer.

**Step 8**

Pop out all the decimal digits from the stack into the buffer.

The stack frame of this subroutine is in Figure 4.10.

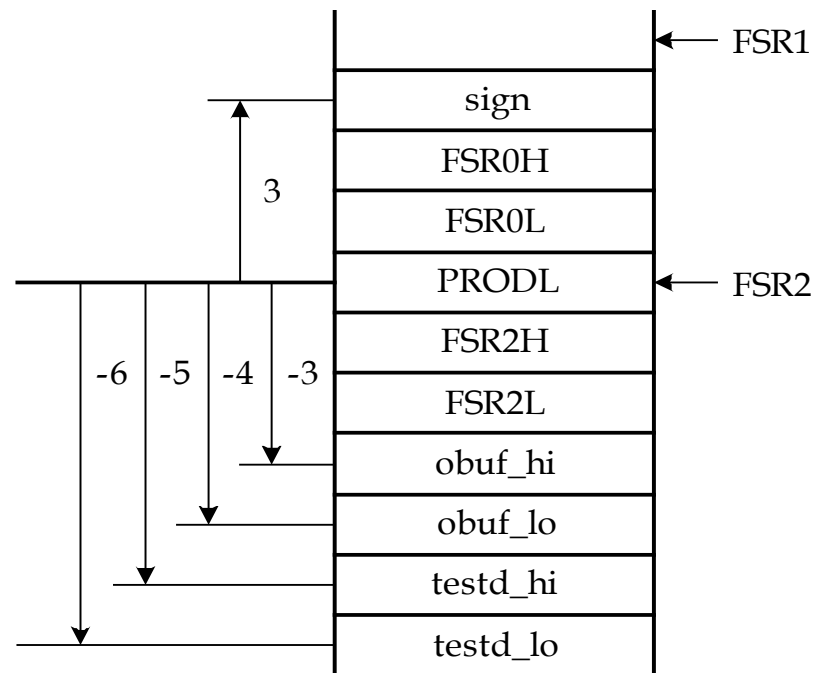


Figure 4.10 Stack frame for example 4.12

```

#include <p18F8720.inc>
radix    dec                ; set default radix to decimal
; ---
; include macro definitions of pushr, popr, push_dat, alloc_stk, and dealloc_stk here
; ---
tstd_hi   equ    0x88        ; test data high byte
tstd_lo   equ    0x89        ; test data low byte
sign      equ    3           ; stack offset for sign in bin2dec
testd_lo  equ    -6          ; stack offset for test data in bin2dec
testd_hi  equ    -5          ;      "
obuf_lo   equ    -4          ; stack offset for conversion buffer
obuf_hi   equ    -3          ;      "
minus     equ    0x2D        ; ASCII code of minus sign
loc_varc  equ    1           ; local variable size of bin2dec routine
obuf      set    0x0100
          org    0x00
          goto   start

```



The test program is as follows:

```

                org      0x08          ; high-priority interrupt vector
                retfie
                org      0x18          ; low-priority interrupt vector
                retfie
start   lfsr      FSR1,0xE00          ; set up stack pointer
        push_dat  tstd_lo             ; pass test data in stack
        push_dat  tstd_hi             ;
        push_dat  low obuf            ;
        push_dat  high obuf           ;
        call      bin2dec,FAST         ; call bin2dec subroutine
        dealloc_stk 4                 ; clean up stack space
con_loop      nop
                bra      con_loop
```

```

bin2dec  pushr    FSR2L      ; save previous frame pointer
           pushr    FSR2H      ; "
           movff    FSR1L,FSR2L ; set up new frame pointer
           movff    FSR1H,FSR2H ; "
           pushr    PRODL
           pushr    FSR0L      ; save FSR0 in stack
           pushr    FSR0H      ; "
           alloc_stk loc_varc   ; allocate local variable space
; set FSR0 as the pointer to the buffer that holds the conversion result
           movlw    obuf_lo
           movff    PLUSW2,FSR0L
           movlw    obuf_hi
           movff    PLUSW2,FSR0H
; initialize the sign of the number to be converted to positive
           movlw    sign        ; "
           clrf     PLUSW2       ; "
; test to find out if the number is negative. If yes, compute its
; two's complement.
           movlw    testd_hi
           btfss    PLUSW2,7      ; compute the magnitude when negative
           goto     tst_zero      ; no need to complement when positive
           comf     PLUSW2,F      ; complement the upper byte when negative

```

```

        clrf      PRODL,A          ; add carry to testd_hi (carry may be 0)
        movlw    testd_lo          ; compute the two's complement of data
        negf     PLUSW2            ; to be converted
        movlw    testd_hi          ;
        movf     PLUSW2,W          ; "
        addwfc   PRODL,F          ; "
        movlw    testd_hi          ; "
        movff    PRODL,PLUSW2     ; "
; change sign to 1 to indicate minus
        movlw    sign              ; "
        incf     PLUSW2,F         ; "
        bra      normal
; check if the number to be tested is zero
tst_zero  movlw    testd_hi          ; test high byte
          tstfsz   PLUSW2            ; "
          bra      normal
          movlw    testd_lo          ; test low byte
          tstfsz   PLUSW2            ; "
          bra      normal
          movlw    0x30
          movwf    POSTINC0
          clrf     INDF0            ; terminate the buffer with NULL character

```

```

        goto        done
; normal repeated divide-by-10 loop starts here
normal   movlw      testd_lo          ; pass the dividend
        movf        PLUSW2,W         ;
        pushr       WREG              ;
        movlw       testd_hi         ;
        movf        PLUSW2,W         ;
        pushr       WREG              ;
div_lp   alloc_stk   2                ; make room for remainder
        push_dat    10                ; push 10 into the stack as divisor
        push_dat    0                ;
        call        div16u            ; call subroutine to perform division
        dealloc_stk 3                ; deallocate the stack space (3 bytes rem
        popr        WREG              ; pop off low byte of remainder
        addlw       0x30              ; convert the remainder into ASCII code
        movwf       POSTINC0          ; and save it in buffer
; is quotient equal to 0?
        movlw       -1
        tstfsz      PLUSW1
        goto        div_lp
        movlw       -2
        tstfsz      PLUSW1

```

```

        goto      div_lp
        clrf      INDF0          ; terminate the buffer with NULL
        dealloc_stk      2      ; clean up the stack
; set FSR0 to point to the start of the buffer to reverse the string
        movlw     obuf_lo        ;
        movff     PLUSW2,FSR0L   ;
        movlw     obuf_hi        ;
        movff     PLUSW2,FSR0H   ;
        push_dat  0              ; push a NULL character onto the stack
push_lp  movf      POSTINC0,W
        bz        to_pop        ; is this the NULL character
        pushr     WREG
        goto      push_lp
; reverse the converted string
to_pop  movlw     obuf_lo        ; set FSR0 to point to the start of buffer
        movff     PLUSW2,FSR0L   ;
        movlw     obuf_hi        ;
        movff     PLUSW2,FSR0H   ;
        movlw     sign
        movf      PLUSW2,W       ; is the converted data negative?
        bz        pop_loop      ;
; add a minus sign if the number is negative

```

```

        movlw    minus
        movwf    POSTINC0
pop_loop popr    WREG        ; reverse string loop
        movwf    POSTINC0
        tstfsz   WREG,A      ; reach the end of string?
        goto     pop_loop
done     popr    WREG        ; get rid of sign
        popr     FSR0H
        popr     FSR0L
        popr     PRODL
        popr     FSR2H
        popr     FSR2L
        return    FAST

```

**Example 4.13** Write a subroutine that computes the product of two unsigned 16-bit integers. The numbers to be multiplied and the pointer to the buffer for storing the product are passed in the stack.

**Solution:** The subroutine will save all the used registers in the stack and allocates four bytes for local variables to hold the product. The stack frame is shown in Figure 4.11.

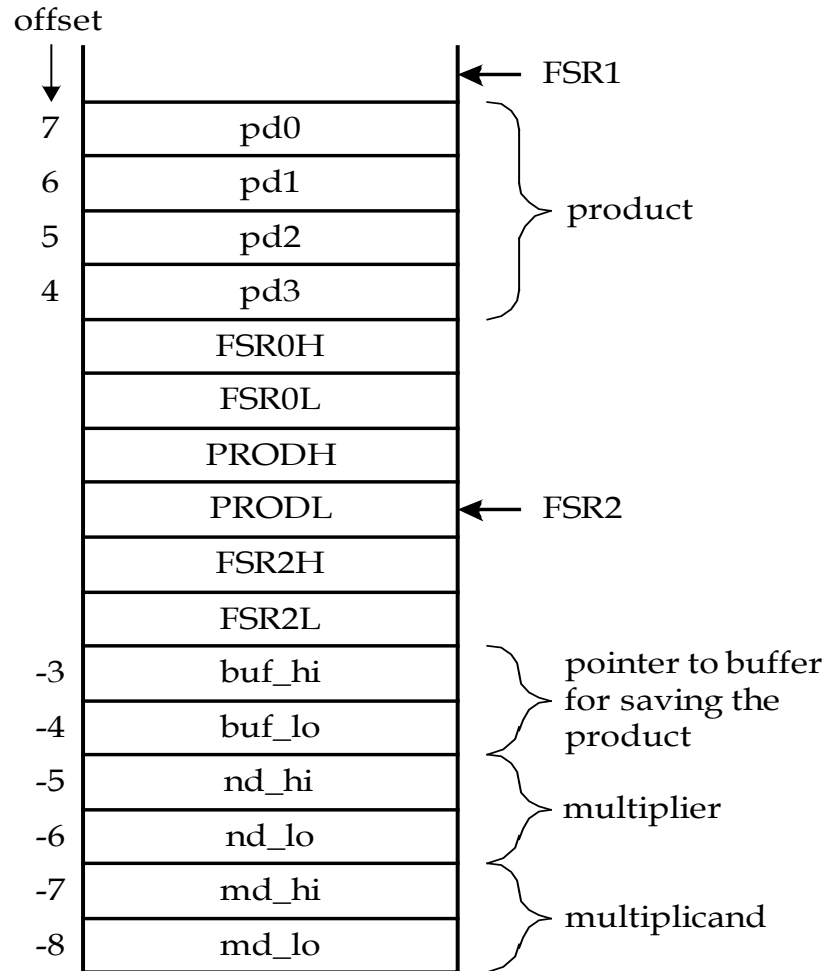


Figure 4.11 Stack frame for Example 4.13



```

mul_16u pushr    FSR2L      ; save previous frame pointer
        pushr    FSR2H      ; "
        movff    FSR1L,FSR2L ; set up new frame pointer
        movff    FSR1H,FSR2H ; "
        pushr    PRODL      ; save PRODL in stack
        pushr    PRODH      ; save PRODH in stack
        pushr    FSR0L      ; save FSR0 in stack
        pushr    FSR0H      ; "
        alloc_stk loc_varm
; compute md_lo x nd_lo and place in pd1..pd0
        movlw    md_lo
        movff    PLUSW2,PRODL ; place md_lo in PRDOL
        movlw    nd_lo
        movf     PLUSW2,W      ; place nd_lo in WREG
        mulwf    PRODL        ; compute nd_lo * md_lo
        movlw    pd0
        movff    PRODL,PLUSW2
        movlw    pd1
        movff    PRODH,PLUSW2
; compute md_hi x nd_hi and place the product in pd3..pd2
        movlw    md_hi
        movff    PLUSW2,PRODL ; place md_hi in PRODL

```

```

movlw    nd_hi
movf     PLUSW2,W          ; place nd_hi in WREG
mulwf    PRODL             ; compute nd_hi * md_hi
movlw    pd2
movff    PRODL,PLUSW2
movlw    pd3
movff    PRODH,PLUSW2
; compute md_lo x nd_hi
movlw    md_lo
movff    PLUSW2,PRODL
movlw    nd_hi
movf     PLUSW2,W
mulwf    PRODL
movlw    pd1              ; add to pd1
movf     PLUSW2,W          ;      "
addwf    PRODL,F          ;      "
movlw    pd1              ;      "
movff    PRODL,PLUSW2     ;      "
movlw    pd2
movf     PLUSW2,W
addwfc   PRODH,F
movlw    pd2

```

```

movff    PRODH,PLUSW2  ;
clrf     PRODL
movlw    pd3
movf     PLUSW2,W
addwfc   PRODL,F
movlw    pd3
movff    PRODL,PLUSW2
; compute md_hi × nd_lo
movlw    md_hi
movff    PLUSW2,PRODL
movlw    nd_lo
movf     PLUSW2,W
mulwf    PRODL
movlw    pd1            ; add to pd1
movf     PLUSW2,W        ;      "
addwf    PRODL,F        ;      "
movlw    pd1            ;      "
movff    PRODL,PLUSW2   ;      "
movlw    pd2            ; add to pd2
movf     PLUSW2,W        ;      "
addwfc   PRODH,F        ;      "
movlw    pd2            ;      "

```

```

movff    PRODH,PLUSW2    ;      "
clrf     PRODL           ; add carry to most significant byte
movlw    pd3             ;      "
movf     PLUSW2,W        ;      "
addwfc   PRODL,F         ;      "
movlw    pd3             ;      "
movff    PRODL,PLUSW2    ;      "

```

; use FSR0 as a pointer to the buffer that holds the product

```

movlw    buf_lo
movff    PLUSW2,FSR0L
movlw    buf_hi
movff    PLUSW2,FSR0H

```

; save product in the buffer

```

popr     WREG
movwf    POSTINC0
popr     WREG
movwf    POSTINC0
popr     WREG
movwf    POSTINC0
popr     WREG
movwf    POSTINC0
popr     FSR0H

```

```
popr    FSR0L
popr    PRODH
popr    PRODL
popr    FSR2H
popr    FSR2L
return  FAST
end
```

## Input Data Conversion Issue

- A number entered from the keyboard is encoded in ASCII code.
- Each input character represents a decimal digit.
- The input number can be positive or negative.
- A negative number is entered using signed magnitude format.
- Illegal characters must be checked.
- The following algorithm uses three variables to facilitate the conversion:
  - sign:** keeps track of the sign of the number
  - error:** indicates whether the input string has any error
  - number:** stores the converted number

## ASCII String to Binary Conversion Algorithm

### Step 1

sign  $\leftarrow$  0  
error  $\leftarrow$  0  
number  $\leftarrow$  0

### Step 2

If the character pointed to by *in\_ptr* is the minus sign, then

sign  $\leftarrow$  1  
in\_ptr  $\leftarrow$  in\_ptr + 1

### Step 3

If the character pointed to by *in\_ptr* is the NULL character, then go to Step 4.

else if the character is not a BCD digit (i.e.,  $m[in\_ptr] > \$39$  or  $m[in\_ptr] < \$30$ ), then

error  $\leftarrow$  1;  
go to Step 4;

else

number  $\leftarrow$  number  $\times$  10 +  $m[in\_ptr] - \$30$ ;  
in\_ptr  $\leftarrow$  in\_ptr + 1;  
go to Step 3;

### Step 4

If sign = 1 and error = 0, then

number  $\leftarrow$  two's complement of number;

else stop;



**Example 4.14** Write a subroutine that converts a decimal digit string into the binary number that it represents. The string is stored in the data memory and its starting address is passed to this function in the FSR0 register. The string may represent a positive or a negative number and is no longer than 7 bytes. Thus, the converted binary number can be accommodated in two bytes. The converted result will be returned in PRODL and PRODH. Do not check for illegal characters.

**Solution:**

- This subroutine needs to call **mul\_16u** subroutine to perform multiplication.
- This subroutine passes a pointer to a buffer to hold the product.
- The buffer is reserved in the stack frame.

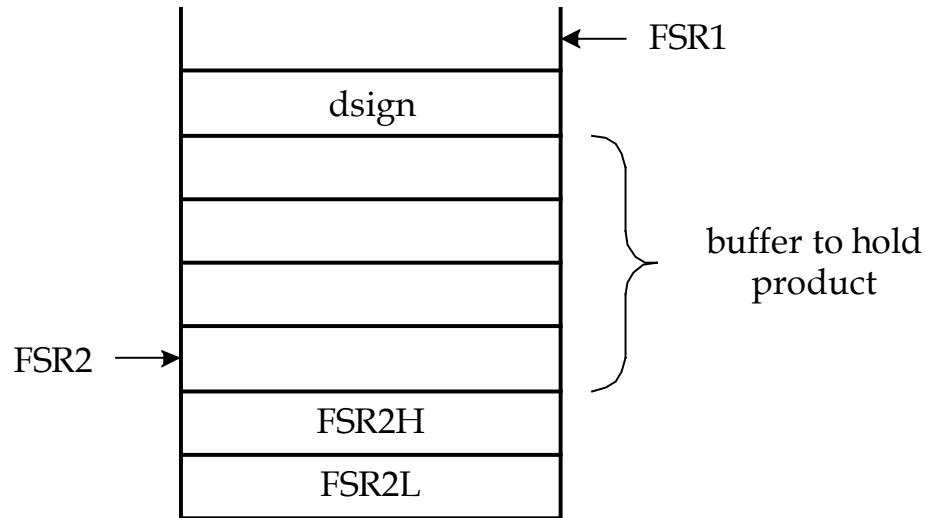


Figure 4.12 Stack frame for Example 4.14

The subroutine is as follows:

```
loc_vard equ    5           ; size of local variables for d2b
dsign     equ    4           ; offset of dsign from FSR2
dec_strg  set    0x10        ; address of the buffer for the decimal string
```



```

dec2bin  pushr    FSR2L      ; save the current frame pointer
           pushr    FSR2H      ; "
           movff    FSR1L,FSR2L ; set up new frame pointer
           movff    FSR1H,FSR2H ; "
           alloc_stk loc_var    ; allocate 5 bytes for local variables
           movlw    0
           clrf     PLUSW2      ; clear the buffer that holds the product
           incf     WREG,W       ; "
           clrf     PLUSW2      ; "
           incf     WREG,W       ; "
           clrf     PLUSW2      ; "
           incf     WREG,W       ; "
           clrf     PLUSW2      ; "
           movlw    dsign        ; initialize sign to positive
           clrf     PLUSW2      ; "
           movff    INDF0,PRODL  ; get a character from string
           movlw    0x2D         ; place minus sign in WREG
           cpfseq    PRODL       ; is the first character a minus sign?
           goto     con_lp
           movlw    dsign
           incf     PLUSW2      ; set sign to minus
           movf     POSTINC0,W   ; move pointer to next character

```



con_lp	movff	POSTINC0,PRODL	
	tstfsz	PRODL,A	; reach the NULL character?
	goto	normal	; not yet
	goto	done	; yes, reach NULL character
normal	movlw	0x30	
	subwf	PRODL,F,A	; convert to digit value
	movlw	0	; push multiplicand
	movf	PLUSW2,W	; "
	pushr	WREG	; "
	movlw	1	; "
	movf	PLUSW2,W	; "
	pushr	WREG	; "
	push_dat	10	; push multiplier 10 into stack
	push_dat	0	; "
	pushr	FSR2L	; push buffer pointer
	pushr	FSR2H	; "
	call	mul_16U	; multiply the current result by 10
	dealloc_stk	6	; clean up stack space
	movf	PRODL,W	
	addwf	INDF2,F	; add the converted digit to the product
	clrf	PRODL,A	; "
	movlw	1	

```

        movf    PLUSW2,W      ; place the upper byte of the product in WREG
        addwfc  PRODL,F       ;
        movlw   1             ;
        movff   PRODL,PLUSW2  ;
        goto    con_lp

; check the sign of the converted binary number before return
done    dealloc_stk          3      ; move down the stack pointer
        popr    PRODH        ; place upper byte of product in PRODH
        popr    PRODL        ; place lower byte of product in PRODL
        movlw   dsign        ; check the sign
        tstfsz  PLUSW2       ;
        goto    negate
        goto    getback
negate  negf     PRODL        ; find 2's complement of the result
        comf    PRODH        ;
        movlw   0            ;
        addwfc  PRODH,F      ;
getback popr    FSR2H
        popr    FSR2L
        return

; ----
; include MUL16U and its associated equ directives here.

```

## Bubble Sort

- Sorting makes searching operation easy to perform.
- Bubble sort is simple, widely known, but inefficient.
- Go through the array or file several iterations with each iteration placing one element in the right position.
- The main operation is to compare each array element  $x[i]$  with its immediate successor  $x[i+1]$  and swap them if they are not in proper order.
- For an array of  $n$  elements,  $n - 1$  comparisons are performed in the first iteration.
- As more and more iterations are performed, more and more elements are in their right positions. Fewer comparisons are needed.
- If there is no swapping done during an iteration, then the array is already in order and comparisons can be terminated.

**Example 4.15** Write a subroutine to implement the bubble sort algorithm and a sequence of instructions along with a set of test data for testing this subroutine. Use an array in data memory that consists of  $n$  8-bit unsigned integers for testing purpose.

**Solution:** The bubble sort subroutine needs three local variables:

- **in\_order:** a flag indicating whether the array is in order after an iteration
- **inner:** number of comparisons remained to be performed in an iteration
- **iteration:** number of iterations remained to be performed

The caller of bubble sort subroutine pushed the array base address and array count in the stack.

The following program declares an array of  $n$  8-bit elements in program memory and copies it to the data memory for testing purpose.

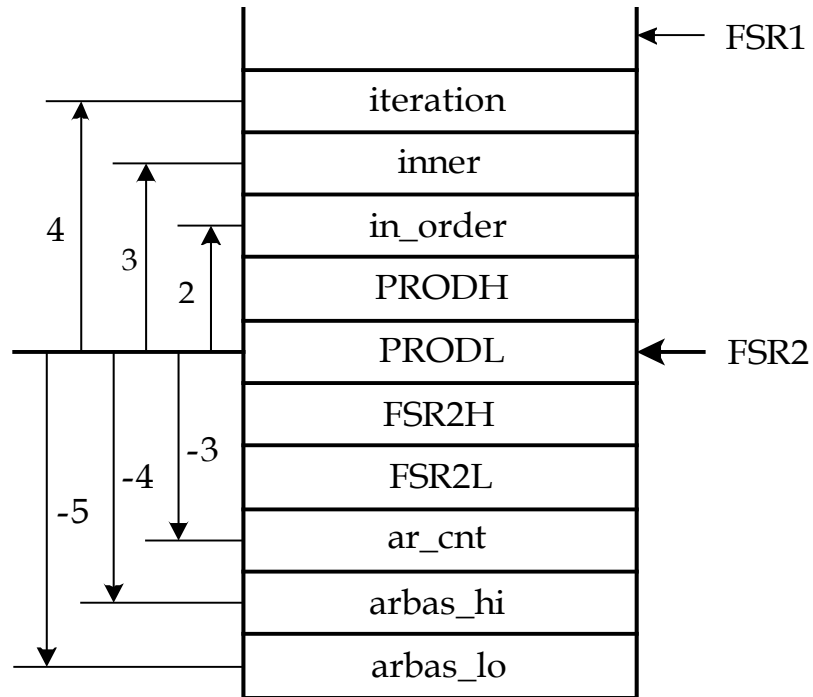


Figure 4.14 Stack frame of Example 4.15

```

#include <p18F8720.inc>
radix      dec

; ----
; include macro definitions pushr, push_dat, popr, alloc_stk, and dealloc_stk here
; ----
NN          equ      30                ; array count
loc_varb    equ      3                ; number of bytes of local variables
arbas       equ      0x0100           ; array base address
lp_cnt      set      0                ; use data memory location 0 for loop count
in_order    equ      2                ; offset of local variable from frame pointer
inner       equ      3                ; "
iteration    equ      4                ; "
ar_cnt      equ      -3               ; "
arbas_hi    equ      -4               ; "
arbas_lo    equ      -5               ; "
org         0x00
goto        start
org         0x08                ; high-priority interrupt vector
retfie
org         0x18                ; low-priority interrupt vector
retfie

```

```

start    lfsr      FSR1,0xE00      ; set up stack pointer
         movlw     high arbas      ; use FSR0 as the pointer to the array
         movwf     FSR0H,A         ; to be sorted
         movlw     low arbas       ;
         movwf     FSR0L,A         ;
         movlw     upper xarr      ; set up table pointer to point to
         movwf     TBLPTRU,A       ; the array in program memory
         movlw     high xarr       ;
         movwf     TBLPTRH,A       ;
         movlw     low xarr        ;
         movwf     TBLPTL,A        ;
         movlw     NN
         movwf     lp_cnt
; *****
;
; copy an array from program memory to data memory to test the bubble
; sort subroutine.
; *****
;
copy_lp   tblrd*+                ; read a byte into the table latch
         movff     TABLAT,POSTINC0 ; copy one byte
         decfsz    lp_cnt,F,A
         bra       copy_lp
         movlw     low arbas      ; push array base address onto stack

```



```

        pushr    WREG                ;
        movlw    high arbas          ;
        pushr    WREG                ;
        push_dat NN                  ; push array count
        call     bubble,FAST         ; call the bubble sort function
forever  nop
        bra     forever

bubble  pushr    FSR2L                ; save the current frame pointer
        pushr    FSR2H                ;
        movff    FSR1L,FSR2L          ; set up new frame pointer
        movff    FSR1H,FSR2H          ;
        pushr    PRODL                ; save PRODL in stack
        pushr    PRODH                ; save PRODH in stack
        alloc_stk loc_varb
        movlw    ar_cnt
        movff    PLUSW2,PRODL
        decf     PRODL,F,A
        movlw    iteration            ; set iteration to array count – 1
        movff    PRODL,PLUSW2        ;

```

```

ploop    movlw    in_order
         clrf     PLUSW2          ; set in_order flag to true (0)
         movlw    iteration
         movff    PLUSW2,PRODL
         movlw    inner
         movff    PRODL,PLUSW2    ; initialize inner loop count
         movlw    arbas_lo        ; use FSR0 as the array pointer
         movff    PLUSW2,FSR0L    ;
         movlw    arbas_hi        ;
         movff    PLUSW2,FSR0H    ;
cloop    movff    INDF0,PRODL      ; place arr[i] in PRODL
         movlw    1
         movf     PLUSW0,W         ; place arr[i+1] in WREG
         cpfsgt   PRODL,A
         goto     looptst
         movwf    PRODH            ; swap arr[i] with arr[i+1]
         movlw    1                ;
         movff    PRODL,PLUSW0    ;
         movff    PRODH,INDF0     ;
         movlw    in_order        ; set the in_order flag to false (1)
         incf     PLUSW2,F        ;
looptst  movf     POSTINC0,W       ; increment array pointer

```

```

        movlw    inner            ; decrement inner loop count and skip if it
        decfsz   PLUSW2,F         ; has been decremented to zero
        goto     cloop
        movlw    in_order
        tstfsz   PLUSW2          ; is the array in order?
        goto     nexti           ; not yet
        goto     done            ; yes, return.
nexti    movlw    iteration
        decfsz   PLUSW2,F
        goto     ploop
done     dealloc_stk loc_varb
        popr     PRODH
        popr     PRODL
        popr     FSR2H
        popr     FSR2L
        return   FAST
xarr     db       0x56,0x1F,0x01,0x08,0x11,0x47,0x21,0x20,0x30,0x07
        db       0x19,0x18,0x17,0x16,0x15,0x14,0x13,0x12,0x29,0x28
        db       0x27,0x26,0x25,0x24,0x23,0x22,0x06,0x05,0x04,0x03
        end

```

## Square Root Computation

- A simple but efficient way to compute the approximate integral square root of an integer is successive approximation method.
- The square root of an **2n**-bit number would be **n**-bit.
- Let **SAR** be an n-bit number, **Q** be a 2n-bit number of which the square root is to be computed.

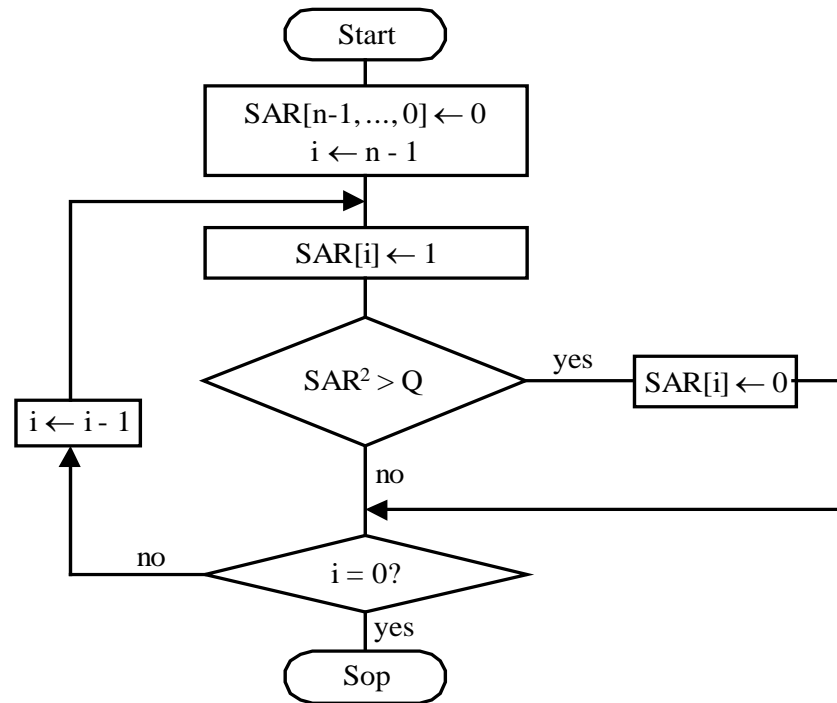


Figure 4.15 Successive approximation method for computing the square root of a 2n-bit number Q.

- The algorithm in Figure 4.15 computes an approximate integer square root smaller than or equal to the actual one. The better approximation could be  $[SAR]$  or  $[SAR]+1$ .
- The better approximate square root can be found by comparing  $Q - [SAR*SAR]$  and  $([SAR]+1)*([SAR]+1)$ .

**Example 4.16** Write an assembly routine to implement the successive approximation method for computing the square root of a 16-bit integer. The 16-bit integer will be pushed into the stack. The square root is returned in PRODL.

**Solution:** The subroutine has three local variables:

1. sar: Successive approximation register
2. mask: A value used to set the **ith** bit
3. lp\_cnt: loop count

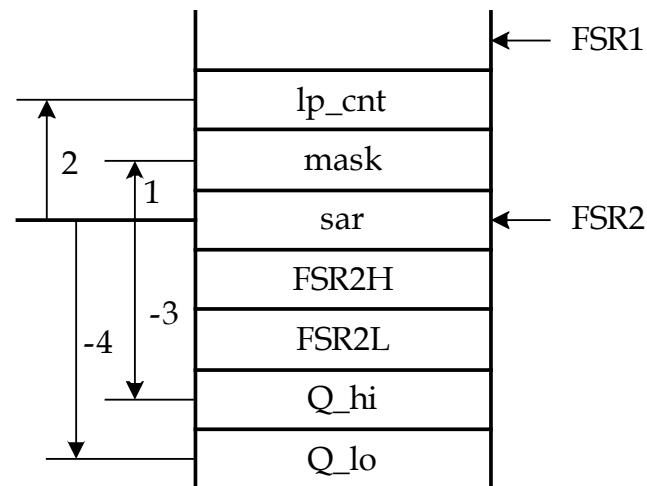


Figure 4.16 Stack frame for Example 4.16

```
#include <p18F8720.inc>
```

```
radix    dec
```

```
; ----
```

```
; include macro definitions pushr, push_dat, popr, alloc_stk, and dealloc_stk here
```

```
; ----
```

```
testd_hi equ    0x41          ; data to be tested
testd_lo equ    0x2E          ; "
loc_vars equ    3             ; number of bytes for local variable
Q_hi     equ    -3            ; offsets of Q from frame pointer
Q_lo     equ    -4            ; "
sar       equ    0            ; "
mask     equ    1             ; "
lp_cnt    equ    2             ; "
sq_root   set    0x00          ; memory location to save square root
...        ; insert testing program here
```

```
find_sqr pushr    FSR2L
           pushr    FSR2H
           movff    FSR1L,FSR2L
           movff    FSR1H,FSR2H
           alloc_stkloc_vars
           movlw    8           ; initialize loop count
           movwf    PRODL,A     ; "
```



```

                                ;
movlw    lp_cnt                ;
movff    PRODL,PLUSW2         ;
movlw    0x80                  ; start with the mask 0x80
movwf    PRODL                 ;
movlw    mask                  ;
movff    PRODL,PLUSW2         ;
clrf     INDF2                 ; initialize SAR to 0
loop     movlw    mask
        movf     PLUSW2,W      ; place mask in WREG
        iorwf    INDF2,W      ; set the ith bit of SAR
        mulwf    WREG,A        ; compute SAR*SAR
        movlw    Q_lo         ; compute SAR*SAR - Q
        movf     PLUSW2,W      ;
        subwf    PRODL,F       ;
        movlw    Q_hi         ;
        movf     PLUSW2,W      ;
        subwfb   PRODH,F       ;
        btfsc    STATUS,C      ; skip if Q > SAR*SAR
        goto     nextbit
        movlw    mask          ; the guess is right, so
        movf     PLUSW2,W      ; set bit i of SAR
        iorwf    INDF2,F       ;

```

```

nextbit    movlw    lp_cnt            ; decrement the loop count
           decf     PLUSW2,F          ;
           bz       done              ; it is done if lp_cnt = 0
           bcf      STATUS,C,A        ; clear the C flag
           movlw    mask
           rrcf     PLUSW2,F          ; shift the mask to the right
           goto     loop

. *****
;
; Before return, find out if SAR*SAR or (SAR+1)**2 is closer to Q and
; return [SAR] or [SAR]+1 accordingly.
. *****
done        movf     INDF2,W           ; get the estimated square root
           mulwf    WREG,A            ; compute SAR*SAR
           movlw    Q_lo              ; compute SAR*SAR - Q (is < 0)
           movf     PLUSW2,W          ;
           subwf    PRODL,F,A         ;
           movlw    Q_hi              ;
           movf     PLUSW2,W          ;
           subwfb   PRODH,F,A         ;
           comf     PRODH,F,A         ; compute the magnitude of
           negf     PRODL,A           ; |SAR*SAR - Q|
           movlw    0                 ;

```



```

addwfc    PRODH,F,A      ;
movlw     lp_cnt         ; copy |SAR*SAR - Q| into lp_cnt
movff     PRODH,PLUSW2   ; and mask
movlw     mask           ;
movff     PRODL,PLUSW2   ;
movf      INDF2,W        ; compute SAR+1
incf      WREG,W,A       ;
mulwf     WREG,A         ; compute (SAR+1)**2
movlw     Q_lo           ; compute (SAR+1)**2 - Q
movf      PLUSW2,W       ; and leave the difference in
subwf     PRODL,F,A      ; PRODH:PRODL
movlw     Q_hi           ;
movf      PLUSW2,W       ;
subwfb    PRODH,F,A      ;
movlw     mask           ; compare [Q-(SAR*SAR)] with
movf      PLUSW2,W       ; (SAR+1)**2 - Q
subwf     PRODL,F,A      ;
movlw     lp_cnt         ;
movf      PLUSW2,W       ;
subwfb    PRODH,F,A      ;
btfsc     STATUS,C       ;
goto      sel_SAR        ;

```

```

incf          INDF2,F          ; increment SAR by 1
sel_SAR dealloc_stk 2          ; remove lp_cnt and mask from stack
popr          PRODL           ; place SAR in PRODL
popr          FSR2H
popr          FSR2L
return
end

```

### Prime Number Test

- An integer is prime if it cannot be divided by any of the prime numbers smaller or equal to its square root.
- A less efficient method is to divide the given number by all the integers from 2 to its approximate integral square root.

**Example 4.17** Write a subroutine to test whether a 16-bit unsigned integer is a prime number. The integer to be tested is pushed into the stack and the test result is returned in the WREG register. If the number is prime, the subroutine returns a one. Otherwise, it returns a zero.

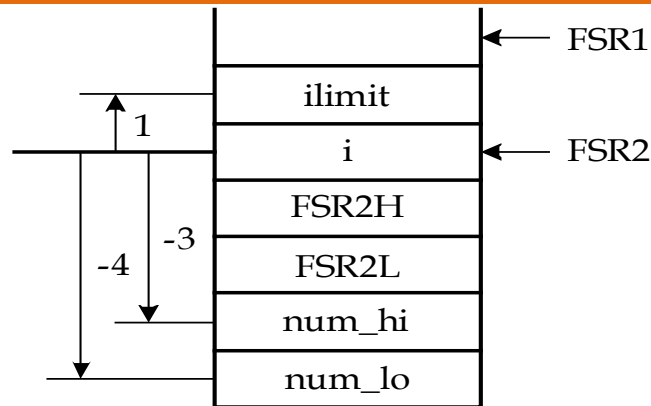


Figure 4.17 Stack frame for example 4.17

```
#include <p18F8720.inc>
radix      dec

; ----
; include macro definitions pushr, push_dat, popr, alloc_stk, and dealloc_stk here
; ----
loc_varp   equ      2           ; local variable size for prime_test
ilimit     equ      1           ; offset of ilimit from FSR2
num_hi     equ     -3           ; offset of test number high byte from FSR2
num_lo     equ     -4           ; offset of test number low byte from FSR2
```

<b>prime_tst</b>	<b>pushr</b>	<b>FSR2L</b>	
	pushr	FSR2H	
	movff	FSR1L,FSR2L	; set up frame pointer
	movff	FSR1H,FSR2H	; "
	alloc_stk	loc_varp	; allocate local variables
	movlw	num_lo	; get a copy of the low byte
	movf	PLUSW2,W	; of the incoming number
	pushr	WREG	
	movlw	num_hi	; get a copy of the high byte
	movf	PLUSW2,W	; "
	pushr	WREG	
	call	find_sqr	; compute the upper limit for prime test
	dealloc_stk	2	; clean up the pushed data from stack
	movlw	ilimit	; set up the upper limit for prime
	movff	PRODL,PLUSW2	; test
	movlw	2	
	movwf	INDF2	; initialize i to 2
loop	movlw	ilimit	; place the ilimit in WREG
	movf	PLUSW2,W	; "
	cpfsqt	INDF2	; is i > ilimit?
	goto	inloop	
	goto	isprime	; it is prime if i > ilimit

```

inloop    movlw    num_lo        ; push the number to be test for prime
          movf     PLUSW2,W      ; onto the stack
          pushr    WREG          ;
          movlw    num_hi        ;
          movf     PLUSW2,W      ;
          pushr    WREG          ;
          alloc_stk 2            ; allocate two bytes for R register
          movf     INDF2,W       ; get the value of i
          pushr    WREG          ; push i into the stack
          push_dat 0            ; push 0 as the upper byte of divisor
          call     div16u
          dealloc_stk 3          ; remove the pushed top three bytes
          movlw    -1            ; the low byte of the remainder is one
          tstfsz   PLUSW1        ; below the byte pointed to by FSR1
          goto     nexti         ; remainder is not zero, test next i
nexti     goto     not_prime
          incf     INDF2,F
          dealloc_stk 3          ; deallocate the pushed remaining 3 bytes
          goto     loop
not_prime dealloc_stk 2+loc_varp ; deallocate the pushed remaining 3 bytes
                                   ; and two bytes of local variables
          popr     FSR2H
          popr     FSR2L

```

```

        movlw    0                ; return a 0 to indicate non_prime
        return
isprime dealloc_stk              loc_varp ; deallocate local variables
        popr     FSR2H
        popr     FSR2L
        movlw    1
        return
; ----
; include subroutine find_sqr and its associated equ directives here
; ----
; ----
; include subroutine div16u and its associated equ directives here
; ----
        end

```