

## HW3 參考解答

### 5.41

```
1 - clear all
2 - close all
3
4 - %-----Plot distribution-----%
5 - n = 18;
6 - p = 0.7;
7 - x = 0 : n;
8 - %binomial distribution
9 - yb = binopdf(x, n, p);
10 - figure; plot(x, yb);
11 - xlabel('number of seniors');
12 - ylabel('probability');
13 - title('Binomial distribution');
14 - %hypergeometric distribution
15 - yh = hygepdf(x, 17000, n, 17000*p);
16 - figure; plot(x, yh);
17 - xlabel('number of seniors');
18 - ylabel('probability');
19 - title('Hypergeometric distribution');
20
21 - %-----Probability-----%
22 - pb = binocdf(13, n, p) - binocdf(9, n, p);
23 - ph = hygecdf(13, 17000, n, 17000*p) - hygecdf(9, 17000, n, 17000*p);
24 - fprintf('Probability of binomial : %f', pb);
25 - fprintf('\nProbability of hypergeometric : %f\n', ph);
```

Comparison :

If  $n$  is small compared to  $N$ , the nature of the  $N$  items changes very little in each draw. (when  $\frac{n}{N} \leq 0.05$ )

Then binomial distribution can be used to approximate the hypergeometric distribution.

## 5.87

```
1 - clear all
2 - close all
3
4 %-----Plot distribution-----%
5 - n = 200;
6 - p = 0.03;
7 - x = 0 : n;
8 %binomial distribution
9 - yb = binopdf(x, n, p);
0 - figure; plot(x, yb);
1 - xlabel('number of seniors');
2 - ylabel('probability');
3 - title('Binomial distribution');
4 %Poisson distribution
5 - yp = poisspdf(x, n*p);
6 - figure; plot(x, yp);
7 - xlabel('number of seniors');
8 - ylabel('probability');
9 - title('Poisson distribution');
:0
:1 %-----Probability-----%
:2 - pb = binocdf(0, n, p);
:3 - pp = poisscdf(0, n*p);
:4 - fprintf('Probability of binomial : %f', pb);
:5 - fprintf('\nProbability of Poisson : %f\n', pp);
```

Comparison :

When  $n \rightarrow \infty$ ,  $p \rightarrow 0$ , and  $\mu = np$  remains constant.

$$b(x; n, p) \rightarrow p(x; \mu).$$