

(Short solutions to HW on Quantum mechanics)

① Straightforward

$$\text{ans: } \lambda = 1.04 \times 10^{-12} \text{ m}$$

② Straightforward

$$\text{ans: } V = 2.4 \times 10^6 \text{ volt}$$

③ Get mass of single C-60 molecule as $m = \frac{M}{N_0}$

$$\lambda = 2.52 \times 10^{-12} \text{ m}$$

since this value is well-within the experimental limits of measurement, the claim is verifiable experimentally. (It is been verified, actually)

④ Angular momentum $L = mvr$ so $\Delta L = m\Delta vr$
 assume radius with no uncertainty. Get $\Delta \theta$ by uncertainty principle $\Delta L \Delta \theta \geq \frac{\hbar}{4\pi}$

$$\text{ans: } \Delta \theta \approx 2189 \text{ rad}$$

⑤ Get Δp first. $\Delta p = m\Delta v$ and then $\Delta x = \Delta v t$

$$\text{ans: } \Delta x = 4.15 \times 10^{-7} \text{ m}$$

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Note: Solution for this problem exists on internet - but that uses Bohr's theory. Here, we'll get it using the uncertainty principle.

$$\text{First get } \Delta E \approx 5.28 \times 10^{-27} \text{ J}$$

$$\text{Let } E \approx \Delta E ; E = p^2/2m$$

$$\text{and } v = \frac{p}{m} = \frac{\sqrt{2mE}}{m}$$

$$v \approx 107.7 \text{ m/s}$$

$$\text{Dist to cover in 2^{nd} orbit} = 2\pi r_2$$

$$r_n \propto n^2 \text{ i.e. } r_n = n^2 r_p ; n=2$$

$$r_p : \text{radius of first orbit} = 0.53 \times 10^{-10} \text{ m}$$

$$\text{Time taken for 1 rev} = \frac{2\pi \times (2)^2 r_1}{v}$$

$$\approx 1.236 \times 10^{-11} \text{ sec}$$

$$\text{time it stays in } n=2 \text{ is } 10^{-8} \text{ sec}$$

$$\therefore \text{no of rev.} = \frac{10^{-8}}{1.236 \times 10^{-11}} \approx 809$$

This is the minimum no. of revolution the electron makes before jumping to $n=1$

$$\textcircled{7} \quad \Delta E = 1.056 \times 10^{-17} \text{ J} \approx 66 \text{ eV}$$

$$\Delta v = \frac{1}{4\pi \Delta t} \approx 1.6 \times 10^{16} \text{ Hz}$$

This is huge bandwidth covers all the way from UV to visible to IR region of EM spectrum
 The broadened bandwidth is due to very short time pulse.

\textcircled{8} Use wavefunction of particle in a box

$$\phi(x) = \sqrt{\frac{\pi}{L}} \cdot \sin\left(\frac{n\pi x}{L}\right)$$

for ground state, $n=1$
 solve like # 15 of solved examples on QM

ans : probability $\approx 39.25\%$.

$$\textcircled{9} \quad E_n = \frac{n^2 h^2}{8 m L^2} \quad E = E_2 - E_1$$

$$E = \frac{hc}{\lambda} \quad \text{get } L$$

ans : 20.1 nm

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This can be quantitatively solved by taking some value of L say 1 nm

~~then~~ then $\Delta L = \pm 0.1 nm$

L varies from 0.9 nm to 1.1 nm

$$E = \frac{n^2 h^2}{8mL^2}$$

get variation in E for these values and for $L = 1$ nm

% variation goes from 17.2% to 28.9%.

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