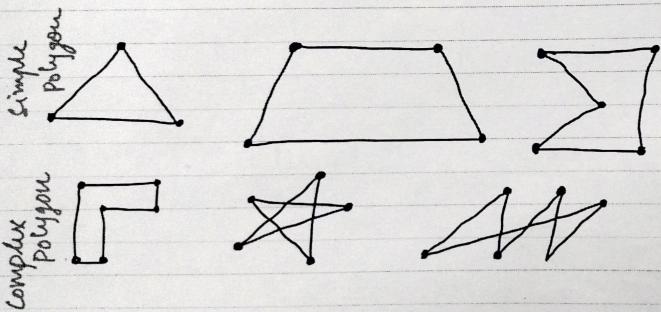


POLYGON

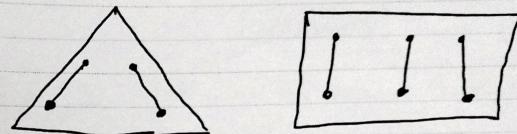
Properties of Polygon

- ↳ It consists of line segments.
- ↳ It must be closed circuit.



Types of Polygon

- ① Convex Polygon:- If the two interior points of the lines lies inside the polygon then it is convex.



② Concave Polygon:- If the two interior points of the lines lies outside the polygon then it is called concave polygon.



Remarks:- If the angle of polygon is less than 180° then it is called as convex polygon.

Else, It is called concave greater than 180° .

Inside Test (Polygon)

→ It is used to identify the pixel/ point is within the polygon or outside the polygon.

Algorithm:- Ray Casting

- ① Draw the horizontal line from the point to cover max vertices.
- ② Count the number of times the line intersects with the edge.
- ③ If the number of count is number = odd

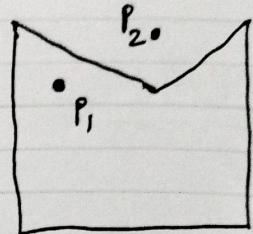
then it is inside

else,

number == even

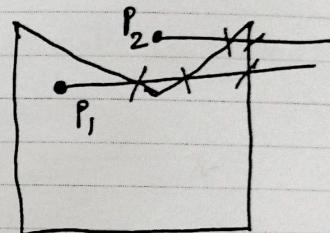
then it is outside.

Q



check the point is inside or outside of Polygon using Ray casting Algo

Sol :-



<u>Point</u>	<u>Intersection</u>	<u>OP</u>
P ₁	3	inside
P ₂	2	outside

Spatial case:- If the line pass/cross at the vertex' or' cross-section point of two lines.

We used the Winding Number Algorithm

① Check the respective line segment of that point.

② Check the other end of the line segment.

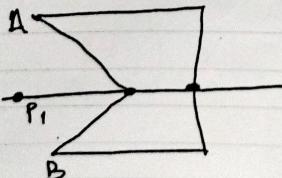
③ Check if both points are in same side 'or' different side of the line segment.

④ If the point is on same side then we consider as even.

If the point is not on same side then we consider as odd

So $\frac{4}{4}$:- Not on the same side = odd

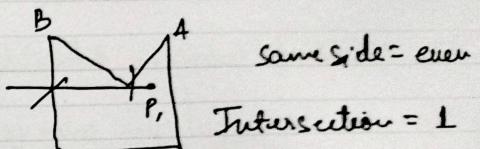
Intersection = 1



Then, $= 1 + \text{odd} = \text{even no of intersection}$

Conclusion :- Then point is outside.

Q.



Then $= 1 + \text{even} = \text{odd}$

Conclusion = odd no of intersection.

Therefore point is inside.

Polygon Boundary Fill Algorithm

- ↳ Color Fill Algorithm.
- ↳ Boundary color is different
- ↳ Within the polygon color is different.

Algorithm:-

- ① Let 'P' take the point inside the polygon.
- ② Start with co-ordinate (x, y)
- ③ Inside color is 'F' ← Fill color.
- ④ Boundary color is 'b'

Algorithm steps:-

{ boundary (x, y, F, b)

if (get pixel $(x, y) \neq b$) {

(get pixel $(x, y) \neq F$)

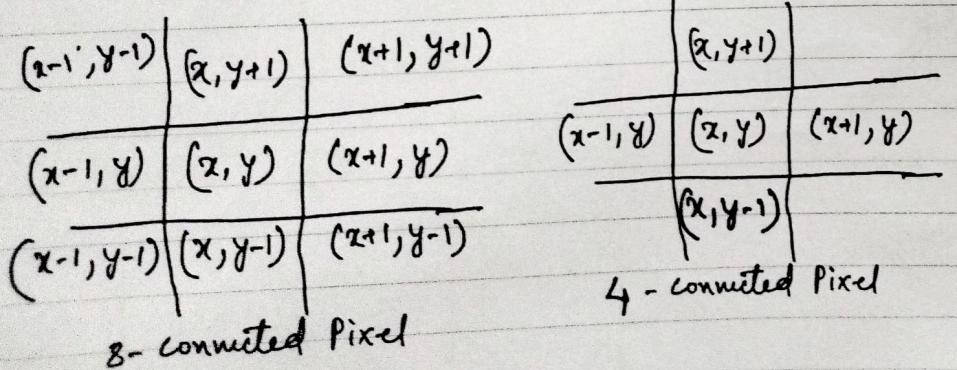
}

put pixel (x, y, F)

{ 4-connected pixels used to check the co-ordinates }
boundary $(x+1, y, F, b)$
boundary $(x, y+1, F, b)$
boundary $(x-1, y, F, b)$
boundary $(x, y-1, F, b)$
boundary $(x-1, y-1, F, b)$
boundary $(x-1, y+1, F, b)$
boundary $(x+1, y+1, F, b)$
boundary $(x+1, y-1, F, b)$
}}

} 8-connected Pixel Algorithm

	R	R	R	R				
R		R						
R		R	R	R				
R	R	R		R				
R	R	R	R	R				



Flood fill Algorithm:-

Flood (x, y, N, θ)

{

if (getpixel(x, y) == θ)

{

4-connected { Flood ($x+1, y, N, \theta$)
Flood ($x, y+1, N, \theta$)
Flood ($x-1, y, N, \theta$)
Flood ($x, y-1, N, \theta$) }

8-connected { } }

Flood ($x-1, y-1, N, \theta$)

Flood ($x-1, y+1, N, \theta$)

Flood ($x+1, y-1, N, \theta$)

Flood ($x-1, y+1, N, \theta$)

}

}

Here, N = New Color.

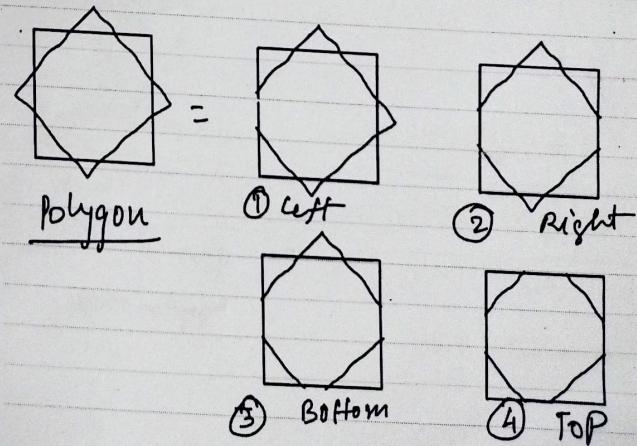
θ = Old Color.

R	R	R	R
R		B	
R		B	R
R	B	B	R
B			R
R	R	R	R

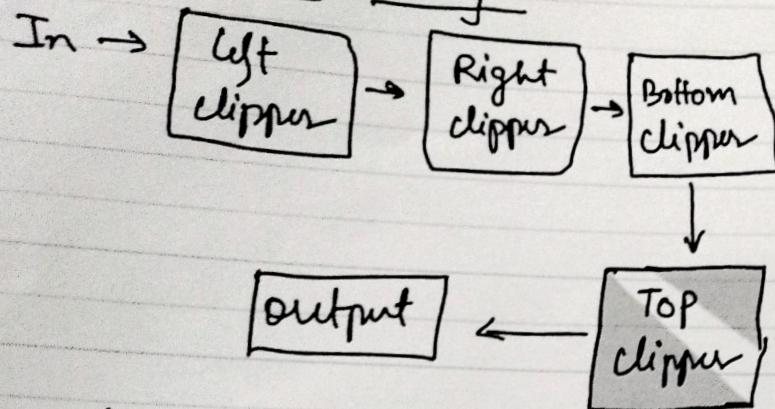
Sutherland Hodgeman Polygon Clipping Algorithm

- ↳ It is used for clipping polygon.
- ↳ In this we have given a polygon & window.
- ↳ Testing of Algorithm with respect to reference of Frame (RoF)

Ex 1-



Algorithm Processing



- Clipping is done based on the boundary.
- Edge is considered as boundary and respective inside and outside of point is considered for clipping.

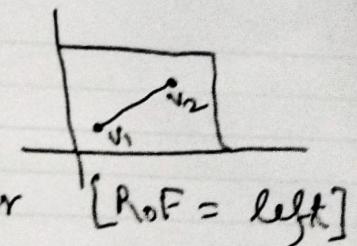
There are four cases for processing of vertices :-

Case 1 :- When both input vertices are inside the window boundary (WB)

Input = v_1, v_2

Output = v_2

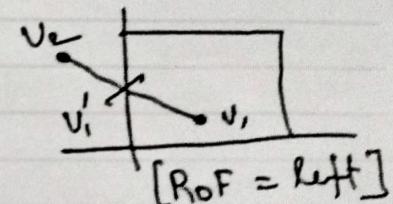
Consider 2nd vertex for the O/P.



Case 2 :- First vertex is inside and second is outside of (WB).

Input :- v_1, v_2

Output :- v'_1

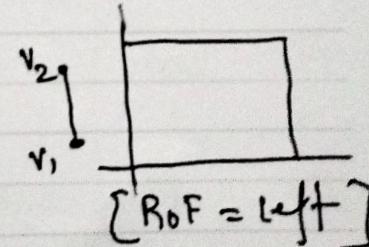


Consider the intersection point w.r.t first point.

Case 3 :- Both input vertices are outside the (WB).

Input :- v_1, v_2

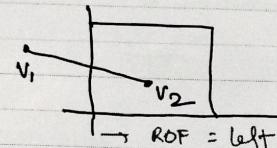
Output :- Nil



Case 4:- If first vertex is outside and second vertex is inside of WB.

Input = v_1, v_2

Output = v'_1, v_2

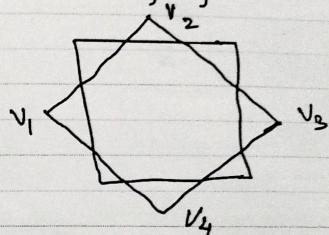


Take the intersection point of first point.

Based on the cases we have generate the truth table:-

	vertices		O/P of vertices
	v_1	v_2	
①	In	In	v_2
②	out	out	Nil
③	In	out	v'_1 (Intersection of First Point)
④	out	In	$v'_1 \& v_2$ (Intersection of first Point)

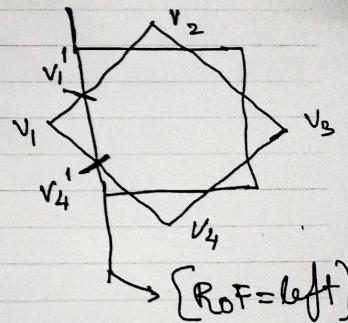
Q. Perform the clipping using Sutherland Hodgeman clipping Algorithm.



Sol^u :- Start from the [ROF = left]

① ROF = Left

$$\begin{array}{ll}
 \text{I/P} & \text{O/P} \\
 v_1, v_2 & = v'_1 \& v_2 \\
 v_2, v_3 & = v_3 \\
 v_3, v_4 & = v_4 \\
 v_4, v_1 & = v'_4
 \end{array}$$



[ROF=left]

② R_{OF} = Right

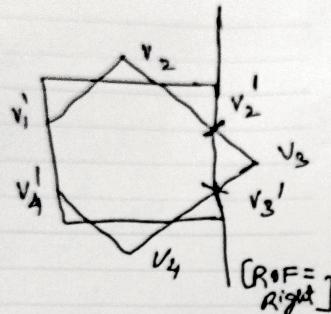
$$V_1' V_2 = V_2'$$

$$V_2 V_3 = V_2'$$

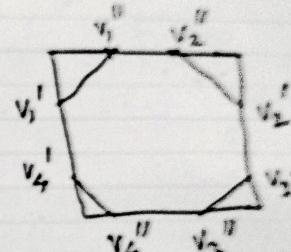
$$V_3 V_4 = V_3' \text{ & } V_4$$

$$V_4 V_1' = V_4'$$

$$V_4' V_1' = V_1'$$



D/P



③ R_{OF} = Bottom

$$V_1' V_2' = V_2'$$

$$V_2 V_2' = V_2'$$

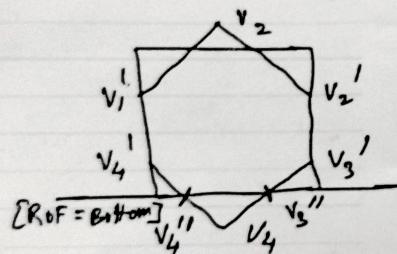
$$V_2' V_3' = V_3'$$

$$V_3' V_4 = V_3''$$

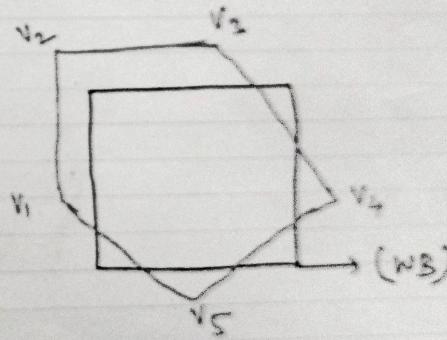
$$V_3' V_4 = V_3''$$

$$V_4 V_4' = V_4''$$

$$V_4' V_1' = V_1'$$



Q



④ R_{OF} = TOP

$$V_1' V_2 = V_1''$$

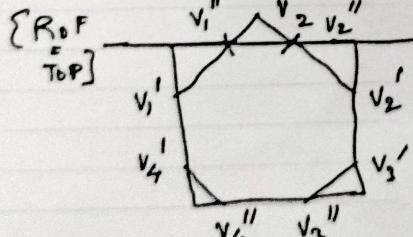
$$V_2 V_2' = V_2'' \text{ & } V_2'$$

$$V_2' V_3' = V_3'$$

$$V_3' V_3'' = V_3''$$

$$V_3'' V_4'' = V_4''$$

$$V_4'' V_4' = V_4'$$



$$V_4' V_1' = V_1'$$