

Assignment - 2

① for (i=0 ; i < length ; i++)

{ if (arr[i] == target)

 return 0;

}

 else if (arr[i] > target)

{

 return -1;

}

}

② void iterative_insertion (int arr[], int n)

{ for (int i=1 ; i < n ; i++)

 int key = arr[i];

 int j = i-1;

 while (j >= 0 && arr[j] > key)

 arr[j+1] = arr[j];

 j = j - 1;

 arr[j+1] = key;

{

}

}

```

void recursive-insertionhelper (int arr[],  

int n)  

{
    if (n <= 1)
        return;  

    }  

recursive-insertionhelper (arr, n-1);  

int lost-element = arr[n-1];  

int i = n-2;  

while (i > j && arr[j] > lost-  

element)  

{
    arr[j+1] = arr[j];  

    i = j-1;  

}  

arr[j+1] = lost-element;  

}
}

```

```

void recursive-insertion (int arr[], int n)  

{
    int n/ recursive-insertion (arr, n);
}

```

(3)

Insertion sort

T.C :
Best $O(n)$
Avg $O(n^2)$
Worst $\Omega(n^2)$

S.C : $O(1)$ Selection sort

T.C :
Best $O(n^2)$
Avg $O(n^2)$
Worst $\Omega(n^2)$

S.C : $O(1)$ Bubble sort

T.C :
Best $O(n^2)$
Avg $O(n^2)$
Worst $\Omega(n^2)$

S.C : $O(1)$

Quick sort

T.C :

Best $O(n \log n)$
Avg $O(n \log n)$
Worst $O(n^2)$

Space :

$O(\log n)$

Merge sort

T.C :

Best $O(n \log n)$
Avg $O(n \log n)$
Worst $O(n \log n)$

Space :

$O(n)$

(4)

Algorithm

In-place

stable

online

Bubble sort

Yes

Yes

No

Selection sort

Yes

No

No

Inversion sort

Yes

Yes

Yes

Merge sort

No

Yes

No

Quick sort

Yes

No

No

Heap sort

Yes

No

No

Count sort

No

Yes

No

Radix sort

No

Yes

No

(5)

(5) int recursive_binary_search (int arr[], int target, int low, int high)
{
 if (low > high)
 return -1;
 }
 int mid = low + (high - low) / 2;
 if (arr[mid] == target)
 {
 return mid;
 }
 else if (arr[mid] > target)
 {
 return recursive_binary_search (arr, target, low, mid - 1);
 }
 else
 {
 return recursive_binary_search (arr, target, mid + 1, high);
 }
}

int iterative_binary_search (int arr[], int target, int n)
{

 int low = 0;
 int high = n - 1;
 while (low <= high)
 {

 int mid = low + (high - low) / 2;

⑥

```

if [ arr[mid] == target )
{
    return mid;
}
else if ( arr[mid] < target )
{
    low = mid + 1;
}
else
{
    high = mid - 1;
}
return -1;
}

```

Linear search

Recursive

$$T.C \rightarrow O(n)$$

$$S.C \rightarrow O(1)$$

Iterative

$$T.C \rightarrow O(n)$$

$$S.C \rightarrow O(1)$$

Binary search

Recursive

$$T.C \rightarrow O(\log n)$$

$$S.C \rightarrow O(\log n)$$

Iterative

$$T.C \rightarrow O(\log n)$$

$$S.C \rightarrow O(1)$$

⑥ In each recursive call, the search space is halved. Therefore, the time taken to search an array of size n can be expressed as follows:

If the element is found at the middle index, the time taken is constant.

If this element is not found and we continue the search.

$$T(n) = T(n/2) + O(1)$$

$T(n) \rightarrow$ time taken to search an array of size n ,

$T(n/2) \rightarrow$ time taken to search an array of $n/2$,

$O(1) \rightarrow$ time taken for constant operation.

Time complexity of binary search is $O(\log n)$.

⑦ void twoSum(int arr[], int n), int target)

{ int l = 0;

int h = n - 1;

sort(arr, arr + n);

for (while (l <= n))

{

if ((arr[l] + arr[h]) == target)

return cout << l << " " << h;

{ else if (arr[i] + arr[h]) > target)

}

i++, h--;

else

{

i++;

}

3

⑧

- Quick sort is best for practical uses, because efficient for large datasets and generally outperforms other sorting algorithms.
- Performs well in average and best case ~~scenarios~~ scenarios.
- Not stable, but it can be modified to achieve stability at the cost of additional overhead.
- Requires less additional space compared to merge sort, making it suitable for memory-constrained environments.

⑨

- In the context of sorting algorithms, an inversion occurs when two elements in an array are out of order relative to each other. Formally, in an array $\text{arr}[\cdot]$, $\text{arr}[i], \text{arr}[j]$ forms a pair

inversion if $i < j$ but $arr[i] > arr[j]$

for example, in the array {7, 21, 31, 8, 10, 1, 20, 6, 4, 5} there are several inversions.

- (7, 8)
- (21, 8)
- (31, 8)
- (21, 10)
- (31, 10)
- (31, 20)
- (8, 6)
- (21, 6)
- (31, 6)
- (21, 4)
- (31, 4)
- (20, 6)
- (20, 4)
- (6, 5)

24 inversions

⑩

Quick sort's time complexity varies depending on the input data and the chosen pivot elements. In the tree

Best-case time complexity:

Quick sort achieves its best - case time complexity when the pivot element is consistently chosen such that it divides the array into two sub - arrays. In this scenario, the algorithm's partitioning process efficiently divides the array into smaller sub - arrays. The best case time complexity of Quick sort is $O(n \log n)$, where n is the number of elements. This scenario typically occurs when the input array is already sorted or nearly sorted.

Worst - case time complexity :

- Quick sort exhibits its worst - case time complexity when the pivot element is consistently chosen in a way that one sub - array has significantly more elements. In this scenario, the algorithm performs poorly as it fails to divide the array into smaller sub - arrays. The worst case time complexity of Quick sort is $O(n^2)$.
- This scenario typically occurs when the input array is already sorted and pivot selection is first or last element as pivot.

11) 1. merge sort :

- recurrence relations

$$T(n) = 2T(n/2) + O(n)$$

2. quick sort :

- recurrence relation (average case)

$$T(n) = T(k) + T(n-k-1) + O(n)$$

- recurrence relation (worst case)

$$T(n) = T(n-1) + O(n)$$

similarities :

- Both merge sort and quick sort have a time complexity of $O(n \log n)$ in the average case.
- Both algorithms divide the input array into smaller sub-arrays, recursively split the sub-arrays and then merge or combine the sorted sub-arrays.
- Both algorithms have a worst-case time complexity of $O(n^2)$.

Differences :

- merge sort guarantees a time complexity of $O(n \log n)$ in all cases (best, average and worst case), making it a reliable choice.
- quick sort has a worst-case time complexity of $O(n^2)$ but typically performs better in practice than merge sort.
- merge sort is stable, meaning it preserves the relative order of equal

elements, while quick sort is not stable by default.
Merge sort requires additional space for the merge step, while quick sort is an in-place sorting algorithm.

(13)

(12) void selection-sort (int arr[], int n)
{
 for (int i=0; i<n-1; i++)
 int min-index = i;
 for (int j= i+1; j < n; j++)
 if (arr[j] < arr[min-index])
 min-index = j;
 }
 int key = arr[min-index];
 while (min-index > 0)
 {
 arr[min-index] = arr[min-index - 1];
 min-index --;
 }
 arr[0] = key;
 }
}

(13) void bubble - sort (int arr[] , int n)

```
    {  
        bool swapped ;  
        for ( int i = 0 ; i < n - 1 ; i ++ )
```

```
            swapped = false ;  
            for ( int j = 0 ; j < n - i - 1 ; j ++ )
```

```
                if ( arr [ j ] > arr [ j + 1 ] )
```

```
                    swap ( arr [ j ] , arr [ j + 1 ] )  
                    swapped = true ;
```

```
    }  
}
```

```
    if ( ! swapped )
```

```
        break ;
```

```
}
```

```
}
```

(14)

In this scenario we need to use the external sorting like merge sort. Merge sort is well suited for external sorting because it divides the data into smaller so chunks that can fit into the available RAM.

- Internal sorting

- Internal sorting refers to sorting

data that can fit entirely into the main memory. Algorithms like quick sort, merge sort are commonly used in internal sorting, all data resides in the main memory.

- External sorting
- External sorting refers to storing data that exceeds the available RAM and requires external storage.
- Algorithms like merge sort.
- In external sorting data is divided into smaller chunks that can fit into the available RAM.
- External sorting is essential for handling large datasets that cannot be processed entirely in memory.

② continued

Insertion sort is often referred to as an "online sorting" algorithm because it can sort a list as it receives it. Other sorting algorithms discussed in lecture include

1. Bubble sort
2. Selection sort
3. Merge sort
4. Quick sort