# FinancePy 0.33

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## **Chapter 1**

## **Introduction to FinancePy**

#### **Latest News and Versions**

- 1. 33 released
- Tidied up key rate code Fixed unit tests for pytest Fixed vectorisation of barrier options Various pep8 fixes
  - 1. 32 released
- Fixed bug in Bond OAS and ASW
  - 1. 31 released

Schedule - Corrected bug in schedule generation - Corrected bug in CDS protection leg integral Many Bond Classes have been amended - Changed FULL price to DIRTY price in functions UPDATE YOUR CODE PLEASE. APOLS for inconvenience. - Removed face amount from bond class - how much you buy is not intrinsic to a bond - Made number of ex-dividend days a member of bond class - Added adjustment for ex-dividend dates to yield calculations - Revised accerued and principal functions to take face amount as input - Updated document

- 1. 30 released
- Added PrettyPrint to required dependencies
  - 1. 22 Nov 22

Version 0.260 has been released and pushed to PyPI - Create Date from python datetime - Zero coupon bond class - Fixed bug in bond payment date

1. 31-Aug-2022

Version 0.240 has just been released and pushed to PyPI with changes - Negative terms in date class - Recovery rates do not default to standard value for CDS curves

#### **DISCLAIMER**

This software is distributed FREE AND WITHOUT ANY WARRANTY.

Report any bugs or suggestions here as an issue.

### **CONTRIBUTORS WANTED!**

If you have a knowledge of Quantitative Finance and a reasonable knowledge of Python, then please consider contributing to this project. There are small tasks and big tasks to be done. Just look in the list of Issues and you may find something you can do. Before you begin, please comment in the issue thread in case someone else may be working on that issue. Or you can contact me directly at dominic.okane at edhec.edu.

If you are a user and require some additional functionality, then please add it as an issue.

#### **Quick Start Guide**

FinancePy can be installed from pip using the following command:

'pip install financepy'

To upgrade an existing installation type:

'pip install -upgrade financepy'

I have encountered problems using Anaconda3-2020.07 due to some Numba and LLVMLite problems. However Anaconda3-2020.02 works.

### Using FinancePy in a Jupyter Notebook

Once financepy has been installed, it is easy to get started.

Just download the project and examine the set of Jupyter Notebooks in the notebooks folder.

A pdf manual describing all of the functions can be found in the project directory.

#### Overview

FinancePy is a python-based library that is currently in beta version. It covers the following functionality:

• Valuation and risk models for a wide range of equity, FX, interest rate and credit derivatives.

Although it is written entirely in Python, it can achieve speeds comparable to C++ by using Numba. As a result the user has both the ability to examine the underlying code and the ability to perform pricing and risk at speeds which compare to a library written in C++.

The target audience for this library includes:

- Students of finance and students of python
- Academics teaching finance or conducting research into finance
- Traders wishing to price or risk-manage a derivative.
- Quantitative analysts seeking to price or reverse engineer a price.
- Risk managers wishing to replicate and understand price sensitivity.

- Portfolio managers wishing to check prices or calculate risk measures.
- Fund managers wanting to value a portfolio or examine a trading strategy.

Users should have a good, but not advanced, understanding of Python. In terms of Python, the style of the library has been determined subject to the following criteria:

- 1. To make the code as simple as possible so that those with a basic Python fluency can understand and check the code.
- 2. To keep all the code in Python so users can look through the code to the lowest level.
- 3. To offset the performance impact of (2) by leveraging Numba to make the code as fast as possible without resorting to Cython.
- 4. To make the design product-based rather than model-based so someone wanting to price a specific product can easily find that without having to worry too much about the model â€" just use the default â€" unless they want to. For most products, a Monte-Carlo implementation has been provided both as a reference for testing and as a way to better understand how the product functions in terms of payments, their timings and conditions.
- 5. To make the library as complete as possible so a user can find all their required finance-related functionality in one place. This is better for the user as they only have to learn one interface.
- 6. To avoid complex designs. Limited inheritance unless it allows for significant code reuse. Some code duplication is OK, at least temporarily.
- 7. To have good documentation and easy-to-follow examples.
- 8. To make it easy for interested parties to contribute.

In many cases the valuations should be close to if not identical to those produced by financial systems such as Bloomberg. However for some products, larger value differences may arise due to differences in date generation and interpolation schemes. Over time it is hoped to reduce the size of such differences.

Important Note:

- IF YOU HAVE ANY PRICING OR RISK EXAMPLES YOU WOULD LIKE REPLICATED, SEND SCREENSHOTS OF ALL THE UNDERLYING DATA, MODEL DETAILS AND VALUATION.
- IF THERE IS A PRODUCT YOU WOULD LIKE TO HAVE ADDED, SEND ME THE REQUEST.
- IF THERE IS FUNCTIONALITY YOU WOULD LIKE ADDED, SEND ME A REQUEST.

## The Library Design

The underlying Python library is split into a number of major modules:

 Utils - These are utility functions used to assist you with modelling a security. These include dates (Date), calendars, schedule generation, some finance-related mathematics functions and some helper functions.

- Market These are modules that capture the market information used to value a security. These include interest rate and credit curves, volatility surfaces and prices.
- Models These are the low-level models used to value derivative securities ranging from Black-Scholes to complex stochastic volatility models.
- Products These are the actual securities and range from Government bonds to Bermudan swaptions.

Any product valuation is the result of the following data design:

• \*VALUATION\*\* = \*\*PRODUCT\*\* + \*\*MODEL\*\* + \*\*MARKET\*\*

The interface to each product has a value() function that will take a model and market to produce a price.

#### **Author**

Dominic O'Kane. I am a Professor of Finance at the EDHEC Business School in Nice, France. I have 12 years of industry experience and over 15 years of academic experience.

Contact me at dominic.okane at edhec.edu.

#### **Dependencies**

FinancePy depends on Numpy, Numba, Scipy and basic python libraries such as os, sys and datetime.

## Changelog

See the changelog for a detailed history of changes.

#### **Contributions**

Contributions are very welcome. There are a number of requirements:

- The code should be Pep8 compliant.
- Comments are required for every class and function and they should be a clear description.
- At least one broad test case and a set of unit tests must be provided for every function.
- Avoid very pythonic constructions. For example a loop is as good as a list comprehension. And with numba it can be faster. Readability is the priority.

#### License

GPL-3.0 License - See the license file in this folder for details.

## Chapter 2

## financepy.utils

## Introduction

This is a collection of modules used across a wide range of FinancePy functions. Examples include date generation, special mathematical functions and useful helper functions for performing some repeated action

- Date is a class for handling dates in a financial setting. Special functions are included for computing IMM dates and CDS dates and moving dates forward by tenors.
- Calendar is a class for determining which dates are not business dates in a specific region or country.
- DayCount is a class for determining accrued interest in bonds and also accrual factors in ISDA swaplike contracts.
- Error is a class which handles errors in the calculations done within FinancePy
- annual\_frequency takes in a annual\_frequency type and then returns the number of payments per year
- global\_vars holds the value of constants used across the whole of FinancePy
- helper\_functions is a set of helpful functions that can be used in a number of places
- math is a set of mathematical functions specific to finance which have been optimised for speed using Numba
- FinSobol is the implementation of Sobol quasi-random number generator. It has been speeded up using Numba.
- FinRateConverter converts rates for one compounding annual\_frequency to rates for a different annual\_frequency
- FinSchedule generates a sequence of cashflow payment dates in accordance with financial market standards
- FinStatistics calculates a number of statistical variables such as mean, standard deviation and variance
- FinTestCases is the code that underlies the test case framework used across FinancePy

## **FinDayCount**

The year fraction function can take up to 3 dates, D1, D2 and D3 and a annual\_frequency in specific cases. The current day count methods are listed below.

- THIRTY 360 BOND 30E/360 ISDA 2006 4.16f, German, Eurobond(ISDA 2000)
- THIRTY E 360 ISDA 2006 4.16(g) 30/360 ISMA, ICMA
- THIRTY E 360 ISDA ISDA 2006 4.16(h)
- THIRTY E PLUS 360 A month has 30 days. It rolls D2 to next month if D2 = 31
- ACT ACT ISDA Splits accrued period into leap and non-leap year portions.
- ACT ACT ICMA Used for US Treasury notes and bonds. Takes 3 dates and a annual\_frequency.
- ACT 365 F Denominator is always Fixed at 365, even in a leap year
- ACT 360 Day difference divided by 360 always
- ACT 365L the 29 Feb is counted if it is in the date range

2.1. AMOUNT 9

#### 2.1 amount

Class: Amount

#### **Amount**

Create Amount object.

```
Amount(notional: float = ONE_MILLION, currency_type: CurrencyTypes = CurrencyTypes.NONE):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
notional	float	-	ONE_MILLION
currency_type	CurrencyTypes	-	CurrencyTypes.NONE

#### \_\_repr\_\_

Print out the details of the schedule and the actual dates. This can be used for providing transparency on schedule calculations.

```
__repr__():
```

The function arguments are described in the following table.

#### amount

PLEASE ADD A FUNCTION DESCRIPTION

```
amount():
```

The function arguments are described in the following table.

#### \_print

Print out the details of the schedule and the actual dates. This can be used for providing transparency on schedule calculations.

```
_print():
```

## 2.2 calendar

## Enumerated Type: BusDayAdjustTypes

This enumerated type has the following values:

- NONE
- FOLLOWING
- MODIFIED\_FOLLOWING
- PRECEDING
- MODIFIED\_PRECEDING

## Enumerated Type: CalendarTypes

This enumerated type has the following values:

- NONE
- WEEKEND
- AUSTRALIA
- CANADA
- FRANCE
- GERMANY
- ITALY
- JAPAN
- NEW\_ZEALAND
- NORWAY
- SWEDEN
- SWITZERLAND
- TARGET
- UNITED\_STATES
- UNITED\_KINGDOM

## Enumerated Type: DateGenRuleTypes

This enumerated type has the following values:

- FORWARD
- BACKWARD

#### Class: Calendar

Class to manage designation of payment dates as holidays according to a regional or country-specific calendar convention specified by the user. It also supplies an adjustment method which takes in an adjustment convention and then applies that to any date that falls on a holiday in the specified calendar.

#### Calendar

Create a calendar based on a specified calendar type.

Calendar(cal\_type: CalendarTypes):

2.2. CALENDAR

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
cal_type	CalendarTypes	-	-

## adjust

Adjust a payment date if it falls on a holiday according to the specified business day convention.

```
adjust(dt: Date, bd_type: BusDayAdjustTypes):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	Date	-	-
bd_type	BusDayAdjustTypes	-	-

## add\_business\_days

Returns a new date that is numDays business days after Date. All holidays in the chosen calendar are assumed not business days.

```
add_business_days(start_dt: Date, numDays: int):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
start_dt	Date	-	-
numDays	int	-	-

## is\_business\_day

Determines if a date is a business day according to the specified calendar. If it is it returns True, otherwise False.

```
is_business_day(dt: Date):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
dt	Date	-	-

## is\_holiday

Determines if a date is a Holiday according to the specified calendar. Weekends are not holidays unless the holiday falls on a weekend date.

```
is_holiday(dt: Date):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	Date	-	-

## holiday\_weekend

Weekends by themselves are a holiday.

```
holiday_weekend():
```

The function arguments are described in the following table.

## holiday\_australia

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_australia():
```

The function arguments are described in the following table.

## holiday\_united\_kingdom

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_united_kingdom():
```

The function arguments are described in the following table.

## holiday\_france

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_france():
```

2.2. CALENDAR

#### holiday\_sweden

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_sweden():
```

The function arguments are described in the following table.

## holiday\_germany

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_germany():
```

The function arguments are described in the following table.

## holiday\_switzerland

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_switzerland():
```

The function arguments are described in the following table.

## holiday\_japan

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_japan():
```

The function arguments are described in the following table.

## holiday\_new\_zealand

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_new_zealand():
```

The function arguments are described in the following table.

## holiday\_norway

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_norway():
```

The function arguments are described in the following table.

## holiday\_united\_states

Only bank holidays. Weekends by themselves are not a holiday. This is a generic US calendar that contains the superset of holidays for bond markets, NYSE, and public holidays. For each of these and other categories there will be some variations.

```
holiday_united_states():
```

The function arguments are described in the following table.

## holiday\_canada

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_canada():
```

The function arguments are described in the following table.

## holiday\_italy

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_italy():
```

The function arguments are described in the following table.

## holiday\_target

Only bank holidays. Weekends by themselves are not a holiday.

```
holiday_target():
```

The function arguments are described in the following table.

## holiday\_none

No day is a holiday.

```
holiday_none():
```

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## get\_holiday\_list

generates a list of holidays in a specific year for the specified calendar. Useful for diagnostics.

```
get_holiday_list(year: float):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
year	float	-	-

## easter\_monday

Get the day in a given year that is Easter Monday. This is not easy to compute so we rely on a pre-calculated array.

```
easter_monday(year: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
year	float	-	-

\_\_str\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__str__():
```

The function arguments are described in the following table.

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

## 2.3 currency

## Enumerated Type: CurrencyTypes

This enumerated type has the following values:

- USD
- EUR
- GBP
- CHF
- CAD
- AUD
- NZD
- DKK
- SEK
- HKD
- NONE

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## 2.4 date

## Enumerated Type: DateFormatTypes

This enumerated type has the following values:

- BLOOMBERG
- US\_SHORT
- US\_MEDIUM
- US\_LONG
- US\_LONGEST
- UK\_SHORT
- UK\_MEDIUM
- UK\_LONG
- UK\_LONGEST
- DATETIME

## Class: Date()

A date class to manage dates that is simple to use and includes a number of useful date functions used frequently in Finance.

#### **Date**

Create a date given a day of month, month and year. The arguments must be in the order of day (of month), month number and then the year. The year must be a 4-digit number greater than or equal to 1900. The user can also supply an hour, minute and second for intraday work. Example Input:  $start_dt = Date(1, 1, 2018)$ 

```
Date(d, m, y, hh=0, mm=0, ss=0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
d	-	-	-
m	-	-	-
У	-	-	-
hh	-	-	0
mm	-	-	0
SS	-	-	0

## from\_string

Create a Date from a date and format string. Example Input: start\_dt = Date('1-1-2018', '

```
from_string(cls, date_string, formatString):
```

Argument Name	Type	Description	<b>Default Value</b>
cls	-	-	-
date_string	-	-	-
formatString	-	-	-

## from\_date

Create a Date from a python datetime.date object or from a Numpy datetime64 object. Example Input: start\_dt = Date.from\_dt(datetime.date(2022, 11, 8))

```
from_date(cls, date: [datetime.date, np.datetime64]):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
cls	-	-	-
date	[datetime.date,np.datetime64]	-	-

#### \_refresh

Update internal representation of date as number of days since the 1st Jan 1900. This is same as Excel convention.

```
_refresh():
```

The function arguments are described in the following table.

 $\_\_gt_-$ 

PLEASE ADD A FUNCTION DESCRIPTION

```
__gt__(other):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
other	-	-	-

\_\_lt\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__lt__(other):
```

Argument Name	Type	Description	Default Value
other	-	-	-

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\_\_ge\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

\_\_ge\_\_(other):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
other	-	-	-

\_\_le\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

\_\_le\_\_(other):

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
other	-	-	-

\_\_sub\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

\_\_sub\_\_(other):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
other	-	-	-

\_\_rsub\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

\_rsub\_\_(other):

Argument Name	Type	Description	Default Value
other	-	-	-

\_\_eq\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__eq__(other):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
other	-	-	-

#### is\_weekend

returns True if the date falls on a weekend.

```
is_weekend():
```

The function arguments are described in the following table.

#### is\_eom

returns True if this date falls on a month end.

```
is_eom():
```

The function arguments are described in the following table.

#### eom

returns last date of month of this date.

```
eom():
```

The function arguments are described in the following table.

#### add\_hours

Returns a new date that is h hours after the Date.

```
add_hours(hours):
```

Argument Name	Type	Description	Default Value
hours	-	-	-

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## add\_days

Returns a new date that is numDays after the Date. I also make it possible to go backwards a number of days.

```
add_days(numDays: int = 1):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numDays	int	-	1

## add\_weekdays

Returns a new date that is numDays working days after Date. Note that only weekends are taken into account. Other Holidays are not. If you want to include regional holidays then use add\_business\_days from the FinCalendar class.

```
add_weekdays(numDays: int):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numDays	int	-	-

#### add\_months

Returns a new date that is mm months after the Date. If mm is an integer or float you get back a single date. If mm is a vector you get back a vector of dates.

```
add_months(mm: (list, int)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
mm	list or int	-	-

### add\_years

Returns a new date that is yy years after the Date. If yy is an integer or float you get back a single date. If yy is a list you get back a vector of dates.

```
add_years(yy: (np.ndarray, float)):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
уу	np.ndarray or float	-	-

#### next\_cds\_date

Returns a CDS date that is mm months after the Date. If no argument is supplied then the next CDS date after today is returned.

```
next_cds_date(mm: int = 0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
mm	int	-	0

### third\_wednesday\_of\_month

For a specific month and year this returns the day number of the 3rd Wednesday by scanning through dates in the third week.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
m	int	Month number	-
у	int	Year number	-

#### next\_imm\_date

This function returns the next IMM date after the current date This is a 3rd Wednesday of Jun, March, Sep or December. For an IMM contract the IMM date is the First Delivery Date of the futures contract.

```
next_imm_date():
```

The function arguments are described in the following table.

#### add\_tenor

Return the date following the Date by a period given by the tenor which is a string consisting of a number and a letter, the letter being d, w, m, y for day, week, month or year. This is case independent. For example 10Y means 10 years while 120m also means 10 years. The date is NOT weekend or holiday calendar adjusted. This must be done AFTERWARDS.

```
add_tenor(tenor: (list, str)):
```

Argument Name	Type	Description	<b>Default Value</b>
tenor	list or str	-	-

2.4. DATE 23

#### datetime

Returns a datetime of the date

```
datetime():
```

The function arguments are described in the following table.

#### str

returns a formatted string of the date

```
str(format):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
format	-	-	-

#### \_\_repr\_\_

returns a formatted string of the date

```
__repr__():
```

The function arguments are described in the following table.

## \_print

prints formatted string of the date.

```
_print():
```

The function arguments are described in the following table.

#### set\_date\_format

Function that sets the global date format type.

```
set_date_format(format_type):
```

Argument Name	Type	Description	Default Value
format_type	-	-	-

## is\_leap\_year

Test whether year y is a leap year - if so return True, else False

```
is_leap_year(y: int):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
у	int	-	-

#### parse\_dt

PLEASE ADD A FUNCTION DESCRIPTION

```
parse_dt(date_str, date_format):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
date_str	-	-	-
date_format	-	-	-

#### calculate\_list

Calculate list of dates so that we can do quick lookup to get the number of dates since 1 Jan 1900 (inclusive) BUT TAKING INTO ACCOUNT THE FACT THAT EXCEL MISTAKENLY CALLS 1900 A LEAP YEAR. For us, agreement with Excel is more important than this leap year error and in any case, we will not usually be calculating day differences with start dates before 28 Feb 1900. Note that Excel inherited this "BUG" from LOTUS 1-2-3.

```
calculate_list():
```

The function arguments are described in the following table.

#### date\_index

PLEASE ADD A FUNCTION DESCRIPTION

```
date_index(d, m, y):
```

Argument Name	Type	Description	Default Value
d	-	-	-
m	-	-	-
y	-	-	-

2.4. DATE 25

#### date\_from\_index

Reverse mapping from index to date. Take care with numba as it can do weird rounding on the integer. Seems OK now.

```
date_from_index(idx):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
idx	-	-	-

## weekday

PLEASE ADD A FUNCTION DESCRIPTION

```
weekday(day_count):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
day_count	-	-	-

## vectorisation\_helper

PLEASE ADD A FUNCTION DESCRIPTION

```
vectorisation_helper(func):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
func	-	-	-

## $daily\_working\_day\_schedule$

Returns a list of working dates between start\_dt and end\_dt. This function should be replaced by dateRange once add\_tenor allows for working days.

<b>Argument Name</b>	Type	Description	Default Value
self	-	-	-
start_dt	Date	-	-
end_dt	Date	-	-

#### datediff

Calculate the number of days between two Findates.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
d1	Date	-	-
d2	Date	-	-

#### from\_datetime

Construct a Date from a datetime as this is often needed if we receive inputs from other Python objects such as Pandas dataframes.

```
from_datetime(dt: Date):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	Date	-	-

## days\_in\_month

Get the number of days in the month (1-12) of a given year y.

```
days_in_month(m, y):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
m	-	-	-
y	-	-	-

## date\_range

Returns a list of dates between start\_dt (inclusive) and end\_dt (inclusive). The tenor represents the distance between two consecutive dates and is set to daily by default.

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Argument Name	Type	Description	Default Value
start_dt	Date	-	-
end_dt	Date	-	-
tenor	str	-	"1D"

## $test\_type$

## PLEASE ADD A FUNCTION DESCRIPTION

test\_type():

## 2.5 day\_count

## Enumerated Type: DayCountTypes

This enumerated type has the following values:

- ZERO
- THIRTY\_360\_BOND
- THIRTY\_E\_360
- THIRTY\_E\_360\_ISDA
- THIRTY\_E\_PLUS\_360
- ACT\_ACT\_ISDA
- ACT\_ACT\_ICMA
- ACT\_365F
- ACT\_360
- ACT\_365L
- SIMPLE

## Class: DayCount

Calculate the fractional day count between two dates according to a specified day count convention.

## **DayCount**

Create Day Count convention by passing in the Day Count Type.

```
DayCount(dccType: DayCountTypes):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dccType	DayCountTypes	-	-

## year\_frac

This method performs two functions: 1) It calculates the year fraction between dates dt1 and dt2 using the specified day count convention which is useful for calculating year fractions for Libor products whose flows are day count adjusted. In this case we will set dt3 to be None 2) This function is also for calculating bond accrued where dt1 is the last coupon date, dt2 is the settlement date of the bond and date dt3 must be set to the next coupon date. You will also need to provide a coupon frequency for some conventions. Note that if the date is intraday, i.e. hh,mm and ss do not equal zero then that is used in the calculation of the year frac. This avoids discontinuities for short dated intra day products. It should not affect normal dates for which hh=mm=ss=0. This seems like a useful source: https://www.eclipsesoftware.biz/DayCountConventions.html Wikipedia also has a decent survey of the conventions https://en.wikipedia.org/wiki/Day\_count\_convention and http://data.cbonds.info/files/cbondscalc/Calculator.pdf

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```
freq_type: FrequencyTypes = FrequencyTypes.ANNUAL,
isTerminationDate: bool = False): # Is dt2 a termination date
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt1	Date	Start of coupon period	-
dt2	Date	Settlement (for bonds) or period end(swaps)	-
dt3	Date	End of coupon period for accrued	None
freq_type	FrequencyTypes	-	FrequencyTypes.ANNUAL
isTerminationDate	bool	Is dt2 a termination date	False

## \_\_repr\_\_

Returns the calendar type as a string.

```
__repr__():
```

The function arguments are described in the following table.

## is\_last\_day\_of\_feb

PLEASE ADD A FUNCTION DESCRIPTION

```
is_last_day_of_feb(dt: Date):
```

Argument Name	Type	Description	<b>Default Value</b>
dt	Date	-	-

## 2.6 distribution

Class: FinDistribution()

## **FinDistribution**

*Initialise FinDistribution with x values and associated vector of density times dx values.* 

```
FinDistribution(x, y):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	-	-	-
у	-	-	-

#### sum

This should equal 1.0 for the entire distribution.

```
sum():
```

2.7. ERROR 31

#### 2.7 error

## Class: FinError(Exception)

Simple error class specific to FinPy. Need to decide how to handle FinancePy errors. Work in progress.

#### **FinError**

Create FinError object by passing a message string.

```
FinError(message: str):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
message	str	-	-

## \_print

PLEASE ADD A FUNCTION DESCRIPTION

```
_print():
```

The function arguments are described in the following table.

## \_hide\_traceback

PLEASE ADD A FUNCTION DESCRIPTION

```
_hide_traceback(exc_tuple=None, filename=None, tb_offset=None, exception_only=False, running_compiled_code=False):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
exc_tuple	-	-	None
filename	-	-	None
tb_offset	-	-	None
exception_only	-	-	False
running_compiled_code	-	-	False

#### func\_name

PLEASE ADD A FUNCTION DESCRIPTION

```
func_name():
```

# $suppress\_traceback$

PLEASE ADD A FUNCTION DESCRIPTION

suppress\_traceback():

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# 2.8 frequency

# Enumerated Type: FrequencyTypes

This enumerated type has the following values:

- ZERO
- SIMPLE
- ANNUAL
- SEMI\_ANNUAL
- TRI\_ANNUAL
- QUARTERLY
- MONTHLY
- CONTINUOUS

# annual\_frequency

This is a function that takes in a Frequency Type and returns a float value for the number of times a year a payment occurs.

```
annual_frequency(freq_type: FrequencyTypes):
```

Argument Name	Type	Description	<b>Default Value</b>
freq_type	FrequencyTypes	-	-

# 2.9 global\_types

# Enumerated Type: FinLongShort

This enumerated type has the following values:

- LONG
- SHORT

### Enumerated Type: OptionTypes

This enumerated type has the following values:

- EUROPEAN\_CALL
- EUROPEAN\_PUT
- AMERICAN\_CALL
- AMERICAN\_PUT
- DIGITAL\_CALL
- DIGITAL\_PUT
- ASIAN\_CALL
- ASIAN\_PUT
- COMPOUND\_CALL
- COMPOUND\_PUT

# Enumerated Type: EquityBarrierTypes

This enumerated type has the following values:

- DOWN\_AND\_OUT\_CALL
- DOWN\_AND\_IN\_CALL
- UP\_AND\_OUT\_CALL
- UP\_AND\_IN\_CALL
- UP\_AND\_OUT\_PUT
- UP\_AND\_IN\_PUT
- DOWN\_AND\_OUT\_PUT
- DOWN\_AND\_IN\_PUT

# Enumerated Type: FinCapFloorTypes

This enumerated type has the following values:

- CAP
- FLOOR

# Enumerated Type: SwapTypes

This enumerated type has the following values:

- PAY
- RECEIVE

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### Enumerated Type: ReturnTypes

This enumerated type has the following values:

- TOTAL\_RETURN
- PRICE\_RETURN

# Enumerated Type: FinExerciseTypes

This enumerated type has the following values:

- EUROPEAN
- BERMUDAN
- AMERICAN

# Enumerated Type: FinSolverTypes

This enumerated type has the following values:

- CONJUGATE\_GRADIENT
- NELDER\_MEAD
- NELDER\_MEAD\_NUMBA

### Enumerated Type: TouchOptionTypes

This enumerated type has the following values:

- DOWN\_AND\_IN\_CASH\_AT\_HIT
- UP\_AND\_IN\_CASH\_AT\_HIT
- DOWN\_AND\_IN\_CASH\_AT\_EXPIRY
- UP\_AND\_IN\_CASH\_AT\_EXPIRY
- DOWN\_AND\_OUT\_CASH\_OR\_NOTHING
- UP\_AND\_OUT\_CASH\_OR\_NOTHING
- DOWN\_AND\_IN\_ASSET\_AT\_HIT
- UP\_AND\_IN\_ASSET\_AT\_HIT
- DOWN\_AND\_IN\_ASSET\_AT\_EXPIRY
- UP\_AND\_IN\_ASSET\_AT\_EXPIRY
- DOWN\_AND\_OUT\_ASSET\_OR\_NOTHING
- UP\_AND\_OUT\_ASSET\_OR\_NOTHING

# 2.10 global\_vars

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# 2.11 helpers

#### \_func\_name

Extract calling function name - using a protected method is not that advisable but calling inspect.stack is so slow it must be avoided.

```
_func_name():
```

The function arguments are described in the following table.

### grid\_index

PLEASE ADD A FUNCTION DESCRIPTION

```
grid_index(t, grid_times):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t	-	-	-
grid_times	-	-	-

#### beta\_vector\_to\_corr\_matrix

Convert a one-factor vector of factor weights to a square correlation matrix.

```
beta_vector_to_corr_matrix(betas):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
betas	-	-	-

### pv01\_times

Calculate a bond style pv01 by calculating remaining coupon times for a bond with t years to maturity and a coupon frequency of f. The order of the list is reverse time order - it starts with the last coupon date and ends with the first coupon date.

Argument Name	Type	Description	<b>Default Value</b>
t	float	-	-
f	float	-	-

#### times\_from\_dates

If a single date is passed in then return the year from valuation date but if a whole vector of dates is passed in then convert to a vector of times from the valuation date. The output is always a numpy vector of times which has only one element if the input is only one date.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	Date or list	-	-
value_dt	Date	-	-
day_count_type	DayCountTypes	-	None

#### check\_vector\_differences

Compare two vectors elementwise to see if they are more different than tolerance.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	np.ndarray	-	-
y	np.ndarray	-	-
tol	float	-	1e-6

#### check\_date

Check that input d is a Date.

```
check_date(d: Date):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
d	Date	-	-

# dump

PLEASE ADD A FUNCTION DESCRIPTION

```
dump(obj):
```

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
obj	-	-	-

### print\_tree

Function that prints a binomial or trinonial tree to screen for the purpose of debugging.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
array	np.ndarray	-	-
depth	int	-	None

# input\_time

Validates a time input in relation to a curve. If it is a float then it returns a float as long as it is positive. If it is a Date then it converts it to a float. If it is a Numpy array then it returns the array as long as it is all positive.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
dt	Date	-	-
curve	-	-	-

#### listdiff

Calculate a vector of differences between two equal sized vectors.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
a	np.ndarray	-	-
b	np.ndarray	-	-

# dotproduct

Fast calculation of dot product using Numba.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
xVector	np.ndarray	-	-
yVector	np.ndarray	-	-

# frange

fast range function that takes start value, stop value and step.

```
frange(start: int,
     stop: int,
     step: int):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
start	int	-	-
stop	int	-	-
step	int	-	-

# normalise\_weights

Normalise a vector of weights so that they sum up to 1.0.

```
normalise_weights(wt_vector: np.ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
wt_vector	np.ndarray	-	-

# label\_to\_string

Format label/value pairs for a unified formatting.

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
label	str	-	-
value	float or str	-	-
separator	str	-	"
n"			
list_format	bool	-	False

# table\_to\_string

Format a 2D array into a table-like string.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
header	str	-	-
value_table	-	-	-
float_precision	-	-	"10.7f"

### format\_table

Format a 2D array into a table-like string. Similar to "table\_to\_string", but using a wrapper around PrettyTable to get a nice formatting.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
header	list or tuple	-	-
rows	list or tuple	-	-

# $to\_usable\_type$

Convert a type such that it can be used with 'isinstance'

```
to_usable_type(t):
```

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-

### uniform\_to\_default\_time

Fast mapping of a uniform random variable to a default time given a survival probability curve.

```
uniform_to_default_time(u, t, v):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
u	-	-	-
t	-	-	-
V	-	-	-

# $accrued\_tree$

Fast calulation of accrued interest using an Actual/Actual type of convention. This does not calculate according to other conventions.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
grid_times	np.ndarray	-	-
grid_flows	np.ndarray	-	-
face	float	-	-

# check\_argument\_types

Check that all values passed into a function are of the same type as the function annotations. If a value has not been annotated, it will not be checked.

```
check_argument_types(func, values):
```

Argument Name	Type	Description	Default Value
func	-	-	-
values	-	-	-

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# 2.12 latex

# convert To Latex Table

PLEASE ADD A FUNCTION DESCRIPTION

```
convertToLatexTable(txt, sep="", header_list=[]):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
txt	-	-	-
sep	-	-	"
header_list	-	-	[]

### 2.13 math

# accrued\_interpolator

Fast calculation of accrued interest using an Actual/Actual type of convention. This does not calculate according to other conventions.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
tset	float	Settlement time in years	-
cpn_times	np.ndarray	-	-
cpn_amounts	np.ndarray	-	-

### is\_leap\_year

Test whether year y is a leap year - if so return True, else False

```
is_leap_year(y: int):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
у	int	-	-

#### scale

Scale all of the elements of an array by the same amount factor.

```
scale(x: np.ndarray,
     factor: float):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	np.ndarray	-	-
factor	float	-	-

# test\_monotonicity

Check that an array of doubles is monotonic and strictly increasing.

```
test_monotonicity(x: np.ndarray):
```

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	np.ndarray	-	-

# test\_range

Check that all of the values of an array fall between a lower and upper bound.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	np.ndarray	-	-
lower	float	-	-
upper	float	-	-

#### maximum

Determine the array in which each element is the maximum of the corresponding element in two equally length arrays a and b.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
a	np.ndarray	-	-
b	np.ndarray	-	-

#### maxaxis

Perform a search for the vector of maximum values over an axis of a 2D Numpy Array

```
maxaxis(s: np.ndarray):
```

Argument Name	Type	Description	<b>Default Value</b>
S	np.ndarray	-	-

#### minaxis

Perform a search for the vector of minimum values over an axis of a 2D Numpy Array

```
minaxis(s: np.ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
S	np.ndarray	-	-

#### covar

Calculate the Covariance of two arrays of numbers. TODO: check that this works well for Numpy Arrays and add NUMBA function signature to code. Do test of timings against Numpy.

```
covar(a: np.ndarray, b: np.ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
a	np.ndarray	-	-
b	np.ndarray	-	-

# pair\_gcd

Determine the Greatest Common Divisor of two integers using Euclid's algorithm. TODO - compare this with math.gcd(a,b) for speed. Also examine to see if I should not be declaring inputs as integers for NUMBA.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
v1	float	-	-
v2	float	-	-

### nprime

Calculate the first derivative of the Cumulative Normal CDF which is simply the PDF of the Normal Distribution

```
nprime(x: float):
```

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Argument Name	Type	Description	Default Value
X	float	-	-

#### heaviside

Calculate the Heaviside function for x

```
heaviside(x: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	float	-	-

# frange

Calculate a range of values from start in steps of size step. Ends as soon as the value equals or exceeds stop.

```
frange(start: int,
     stop: int,
     step: int):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
start	int	-	-
stop	int	-	-
step	int	-	-

### normpdf

Calculate the probability density function for a Gaussian (Normal) function at value x

```
normpdf(x: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	float	-	-

#### N

Fast Normal CDF function based on Hull OFAODS 4th Edition Page 252. This function is accurate to 6 decimal places.

```
N(x):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	-	-	-

#### n\_vect

#### PLEASE ADD A FUNCTION DESCRIPTION

```
n_vect(x):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	-	-	-

### n\_prime\_vect

#### PLEASE ADD A FUNCTION DESCRIPTION

```
n_prime_vect(x):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	-	-	-

# normcdf\_integrate

Calculation of Normal Distribution CDF by simple integration which can become exact in the limit of the number of steps tending towards infinity. This function is used for checking as it is slow since the number of integration steps is currently hardcoded to 10,000.

```
normcdf_integrate(x: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	float	-	-

#### normcdf\_slow

Calculation of Normal Distribution CDF accurate to 1d-15. This method is faster than integration but slower than other approximations. Reference: J.L. Schonfelder, Math Comp 32(1978), pp 1232-1240.

```
normcdf_slow(z: float):
```

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
Z	float	-	-

# phi3

Bivariate Normal CDF function to upper limits b1 and b2 which uses integration to perform the innermost integral. This may need further refinement to ensure it is optimal as the current range of integration is from -7 and the integration steps are dx = 0.001. This may be excessive.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
b1	float	-	-
b2	float	-	-
b3	float	-	-
r12	float	-	-
r13	float	-	-
r23	float	-	-

#### norminvcdf

This algorithm computes the inverse Normal CDF and is based on the algorithm found at (http:#home.online.no/pjacklam/notes/invnorm/) which is by John Herrero (3-Jan-03)

```
norminvcdf(p):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
p	-	-	-

#### M

#### PLEASE ADD A FUNCTION DESCRIPTION

```
M(a, b, c):
```

Argument Name	Type	Description	<b>Default Value</b>
a	-	-	-
b	-	-	-
С	-	-	-

# phi2

Drezner and Wesolowsky implementation of bi-variate normal

```
phi2(h1, hk, r):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
h1	-	-	-
hk	-	-	-
r	-	-	-

# cholesky

Numba-compliant wrapper around Numpy cholesky function.

```
cholesky(rho):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
rho	-	-	-

# corr\_matrix\_generator

Utility function to generate a full rank  $n \times n$  correlation matrix with a flat correlation structure and value rho.

```
corr_matrix_generator(rho, n):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
rho	-	-	-
n	-	-	-

#### npv

Function to calculate the npv given irr and cashflow. It can be used to do root search in IRR. times\_cfs is a list of tuples. The tuple is in the form of (years from first date, cashflow)

2.13. MATH 51

```
npv(irr: float, times_cfs: list):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
irr	float	-	-
times_cfs	list	-	-

# band\_matrix\_multiplication

PLEASE ADD A FUNCTION DESCRIPTION

```
band_matrix_multiplication(A, m1, m2, b):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
A	-	-	-
m1	-	-	-
m2	-	-	-
b	-	-	-

# solve\_tridiagonal\_matrix

Solve  $A \ u = r$  for vector u when A is tridiagonal The matrix A is split into vectors a, b, and c contain the three non-zero elements of each row of A, in order. i.e. the vector b is the main diagonal of A, with a and c the elements either side of the main diagonal. Note that a[0] and c[-1] are not used, and so can be any value.

```
solve_tridiagonal_matrix(A, r):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
A	-	-	-
r	-	-	-

# $transpose\_tridiagonal\_matrix$

PLEASE ADD A FUNCTION DESCRIPTION

```
transpose_tridiagonal_matrix(A):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
A	-	-	-

# 2.14 polyfit

#### \_coeff\_mat

PLEASE ADD A FUNCTION DESCRIPTION

```
_coeff_mat(x, deg):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	-	-	-
deg	-	-	-

#### \_fit\_x

PLEASE ADD A FUNCTION DESCRIPTION

```
_fit_x(a, b):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-

# fit\_poly

PLEASE ADD A FUNCTION DESCRIPTION

```
fit_poly(x, y, deg):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	-	-	-
у	-	-	-
deg	-	-	-

# $eval\_polynomial$

Compute polynomial P(x) where P is a vector of coefficients, highest order coefficient at P[0]. Uses Horner's Method.

```
eval_polynomial(P, x):
```

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Argument Name	Type	Description	Default Value
P	-	-	-
X	-	-	-

### 2.15 schedule

#### Class: Schedule

A schedule is a set of dates generated according to ISDA standard rules which starts on the next date after the effective date and runs up to a termination date. Dates are adjusted to a provided calendar. The zeroth element is the previous coupon date (PCD) and the first element is the Next Coupon Date (NCD). We reference ISDA 2006.

#### **Schedule**

Create Schedule object which calculates a sequence of dates following the ISDA convention for fixed income products, mainly swaps. If the date gen rule type is FORWARD we get the unadjusted dates by stepping forward from the effective date in steps of months determined by the period tenor - i.e. the number of months between payments. We stop before we go past the termination date. If the date gen rule type is BACKWARD we get the unadjusted dates by stepping backward from the termination date in steps of months determined by the period tenor - i.e. the number of months between payments. We stop before we go past the effective date. - If the EOM flag is false, and the start date is on the 31st then the unadjusted dates will fall on the 30 if a 30 is a previous date. - If the EOM flag is false and the start date is 28 Feb then all unadjusted dates will fall on the 28th. - If the EOM flag is false and the start date is 28 Feb then all unadjusted dates will fall on their respective EOM. We then adjust all of the flow dates if they fall on a weekend or holiday according to the calendar specified. These dates are adjusted in accordance with the business date adjustment. The effective date is never adjusted as it is not a payment date. The termination date is not automatically business day adjusted in a swap - assuming it is a holiday date. This must be explicitly stated in the trade confirm. However, it is adjusted in a CDS contract as standard. Inputs first\_dt and next\_to\_last\_dt are for managing long payment stubs at the start and end of the swap but \*have not yet been implemented\*. All stubs are currently short, either at the start or end of swap.

```
Schedule(effective_dt: Date,  # Also known as the start date
  # This is UNADJUSTED (set flag to adjust it)
  termination_dt: Date,
  freq_type: FrequencyTypes = FrequencyTypes.ANNUAL,
  cal_type: CalendarTypes = CalendarTypes.WEEKEND,
  bd_type: BusDayAdjustTypes = BusDayAdjustTypes.FOLLOWING,
  dg_type: DateGenRuleTypes = DateGenRuleTypes.BACKWARD,
  adjust_termination_dt: bool = True,  # Default is to adjust
  end_of_month: bool = False,  # All flow dates are EOM if True
  first_dt=None,  # First coupon date
  next_to_last_dt=None):  # Penultimate coupon date
```

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Argument Name	Type	Description	Default Value
effective_dt	Date	Also known as the start date	-
termination_dt	Date	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.ANNUAL
cal_type	CalendarTypes	-	Calendar Types. WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
adjust_termination_dt	bool	Default is to adjust	True
end_of_month	bool	All flow dates are EOM if True	False
first_dt	-	First coupon date	None
next_to_last_dt	-	Penultimate coupon date	None

#### schedule\_dts

Returns a list of the schedule of Dates.

```
schedule_dts():
```

The function arguments are described in the following table.

### \_generate

Generate schedule of dates according to specified date generation rules and also adjust these dates for holidays according to the specified business day convention and the specified calendar.

```
_generate():
```

The function arguments are described in the following table.

#### \_\_repr\_\_

Print out the details of the schedule and the actual dates. This can be used for providing transparency on schedule calculations.

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Print out the details of the schedule and the actual dates. This can be used for providing transparency on schedule calculations.

```
_print():
```

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# 2.16 singleton

# Class: Singleton(type)

Singleton type which is used to ensure there is only one instance across the whole project.

\_\_call\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__call__(cls, *args, **kwargs):
```

<b>Argument Name</b>	Type	Description	Default Value
cls	-	-	-
*args	-	-	-
**kwargs	-	-	-

### 2.17 solver 1d

#### \_results

rSelect from a tuple of(root, funccalls, iterations, flag)

```
_results(r):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
r	-	-	-

#### newton\_secant

```
newton_secant(func, x0, args=(), tol=1.48e-8, maxiter=50, disp=True):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
func	-	-	-
x0	-	-	-
args	-	-	()
tol	-	-	1.48e-8
maxiter	-	-	50
disp	-	-	True

#### newton

#### PLEASE ADD A FUNCTION DESCRIPTION

```
newton(func, x0, fprime=None, args=None, tol=1.48e-8, maxiter=50, fprime2=None, x1=None, rtol=0.0, full_output=False, disp=False):
```

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Type	Description	Default Value
-	-	-
-	-	-
-	-	None
-	-	None
-	-	1.48e-8
-	-	50
-	-	None
-	-	None
-	-	0.0
-	-	False
-	-	False
		Type Description

#### brent\_max

#### PLEASE ADD A FUNCTION DESCRIPTION

```
brent_max(func, a, b, args, xtol=1e-5, maxiter=500):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
func	-	-	-
a	-	-	-
b	-	-	-
args	-	-	-
xtol	-	-	1e-5
maxiter	-	-	500

# bisection

Bisection algorithm. You need to supply root brackets x1 and x2.

```
bisection(func, x1, x2, args, xtol=1e-6, maxIter=100):
```

Argument Name	Type	Description	<b>Default Value</b>
func	-	-	-
<u>x1</u>	-	-	-
x2	-	-	-
args	-	-	-
xtol	-	-	1e-6
maxIter	-	-	100

### minimize\_wolfe\_powel

Minimize a differentiable multivariate function. Parameters ——- f: function to minimize. The function must return the value of the function (float) and a numpy array of partial derivatives of shape (D,) with respect to X, where D is the dimensionality of the function. X: numpy array - Shape: (D, 1) initial guess. length: int The length of the run. If positive, length gives the maximum number of line searches, if negative its absolute value gives the maximum number of function evaluations, args: tuple Tuple of parameters to be passed to the function f. reduction: float The expected reduction in the function value in the first linesearch (if None, defaults to 1.0) verbose: bool If True - prints the progress of minimize. (default is True) concise: bool If True - returns concise convergence info, only the minimium function value (necessary when optimizing a large number of parameters) (default is False) Return — Xs: numpy array - Shape: (D, 1) The found solution. convergence: numpy array - Shape: (i, D+1) Convergence information. The first column is the function values returned by the function being minimized. The next D columns are the guesses of X during the minimization process. If concise = True, convergence information is only the minimum function value. This is necessary only when optimizing a large number of parameters. i: int Number of line searches or function evaluations depending on which was selected. The function returns when either its length is up, or if no further progress can be made (ie, we are at a (local) minimum, or so close that due to numerical problems, we cannot get any closer) Copyright (C) 2001 - 2006 by Carl Edward Rasmussen (2006-09-08). Converted to python by David Lines (2019-23-08)

minimize\_wolfe\_powel(f, X, length, fargs=(), reduction=None, verbose=False, concise=
 False):

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	()
-	-	None
-	-	False
-	-	False
	Type	Type Description

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# 2.18 solver\_cg

#### Class: OptimizeResult(dict)

\_\_getattr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_getattr\_\_(name):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
name	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

The function arguments are described in the following table.

dir

PLEASE ADD A FUNCTION DESCRIPTION

\_\_dir\_\_():

The function arguments are described in the following table.

# polak\_ribiere\_powell\_step

PLEASE ADD A FUNCTION DESCRIPTION

```
polak_ribiere_powell_step(alpha, gfkp1=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
gfkp1	-	-	None

### descent\_condition

#### PLEASE ADD A FUNCTION DESCRIPTION

```
descent_condition(alpha, xkp1, fp1, gfkp1):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
alpha	-	-	-
xkp1	-	-	-
fp1	-	-	-
gfkp1	-	-	-

# fmin\_cg

#### PLEASE ADD A FUNCTION DESCRIPTION

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	None
-	-	()
-	-	1e-5
-	-	Inf
-	-	_epsilon
-	-	None
-	-	0
-	-	1
-	-	0
-	-	None
	Type	Type         Description           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -

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### \_check\_unknown\_options

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_check_unknown_options(unknown_options):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
unknown_options	-	-	-

### \_prepare\_scalar\_function

Creates a ScalarFunction object for use with scalar minimizers (BFGS/LBFGSB/SLSQP/TNC/CG/etc). Pa-an 1-D array with shape (n,) and "args" is a tuple of the fixed parameters needed to completely specify the function. x0: ndarray, shape (n,) Initial guess. Array of real elements of size (n,), where 'n' is the number of independent variables. jac: callable, '2-point', '3-point', 'cs', None, optional Method for computing the gradient vector. If it is a callable, it should be a function that returns the gradient vector: "jac(x, \*args) - i" array\_like, shape (n,)" If one of ''2-point', '3-point', 'cs' is selected then the gradient is calculated with a relative step for finite differences. If 'None', then two-point finite differences with an absolute step is used. args: tuple, optional Extra arguments passed to the objective function and its derivatives ('fun', 'jac' functions). bounds: sequence, optional Bounds on variables. 'new-style' bounds are required. eps: float or ndarray If 'jac is None' the absolute step size used for numerical approximation of the jacobian via forward differences. finite\_diff\_rel\_step: None or array\_like, optional If 'jac in ['2-point', '3-point', 'cs']' the relative step size to use for numerical approximation of the jacobian. The absolute step size is computed as "h =  $rel\_step * sign(x0) * max(1, abs(x0))$ ", possibly adjusted to fit into the bounds. For "method='3-point'" the sign of 'h' is ignored. If None (default) then step is selected automatically. hess: callable, '2-point', '3-point', 'cs', None Computes the Hessian matrix. If it is callable, it should return the Hessian matrix: "hess(x, \*args) -; LinearOperator, spmatrix, array, (n, n)" Alternatively, the keywords '2-point', '3-point', 'cs' select a finite difference scheme for numerical estimation. Whenever the gradient is estimated via finitedifferences, the Hessian cannot be estimated with options '2-point', '3-point', 'cs' and needs to be estimated using one of the quasi-Newton strategies. Returns ——- sf: ScalarFunction

```
_prepare_scalar_function(fun, x0, jac=None, args=(), bounds=None, epsilon=None, finite_diff_rel_step=None, hess=None):
```

Argument Name	Type	Description	<b>Default Value</b>
fun	-	-	-
x0	-	-	-
jac	-	-	None
args	-	-	()
bounds	-	-	None
epsilon	-	-	None
finite_diff_rel_step	-	-	None
hess	-	-	None

#### vecnorm

#### PLEASE ADD A FUNCTION DESCRIPTION

```
vecnorm(x, ord=2):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	-	-	-
ord	-	-	2

# \_line\_search\_wolfe12

Same as line\_search\_wolfe1, but fall back to line\_search\_wolfe2 if suitable step length is not found, and raise an exception if a suitable step length is not found. Raises — LineSearchError If no suitable step size is found

```
_line_search_wolfe12(f, fprime, xk, pk, gfk, old_fval, old_old_fval, **kwargs):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
f	-	-	-
fprime	-	-	-
xk	-	-	-
pk	-	-	-
gfk	-	-	-
old_fval	-	-	-
old_old_fval	-	-	-
**kwargs	-	-	-

### \_minimize\_cg

Minimization of scalar function of one or more variables using the conjugate gradient algorithm. Options ——- disp: bool Set to True to print convergence messages. maxiter: int Maximum number of iterations

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to perform. gtol: float Gradient norm must be less than 'gtol' before successful termination. norm: float Order of norm (Inf is max, -Inf is min). eps: float or ndarray If 'jac is None' the absolute step size used for numerical approximation of the jacobian via forward differences.  $eturn\_all$ : bool, optional Set to True to return a list of the best solution at each of the iterations. finite\\_diff\\_rel\\_step: None or  $eturn\_all$  is optional If 'jac in ['2-point', '3-point', 'cs']' the relative step size to use for numerical approximation of the jacobian. The absolute step size is computed as "eturn = eturn =

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
fun	-	-	-
x0	-	-	-
args	-	-	()
jac	-	-	None
callback	-	-	None
gtol	-	-	1e-5
norm	-	-	Inf
eps	-	-	_epsilon
maxiter	-	-	None
disp	-	-	False
return_all	-	-	False
finite_diff_rel_step	-	-	None
**unknown_options	-	-	-

### 2.19 solver nm

#### nelder\_mead

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
fun	-	-	-
x0	-	-	-
bounds	-	-	np.array([[], []]).T
args	-	-	()
tol_f	-	-	1e-10
tol_x	-	-	1e-10
max_iter	-	-	1000
roh	-	-	1.
chi	-	-	2.
V	-	-	0.5
sigma	-	-	0.5

### \_initialize\_simplex

```
_initialize_simplex(x0, bounds):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
x0	-	-	-
bounds	-	-	-

# \_check\_params

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```
_check_params(rho, chi, v, sigma, bounds, n):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
rho	-	-	-
chi	-	-	-
V	-	-	-
sigma	-	-	-
bounds	-	-	-
n	-	-	-

#### \_check\_bounds

Checks whether 'x' is within 'bounds'. JIT-compiled in 'nopython' mode using Numba. Parameters — -x: ndarray(float, ndim=1) 1-D array with shape (n,) of independent variables. bounds: ndarray(float, ndim=2) Sequence of (min, max) pairs for each element in x. Returns — -bool 'True' if 'x' is within 'bounds', 'False' otherwise.

```
_check_bounds(x, bounds):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	-	-	-
bounds	-	-	-

# **2.20** stats

#### mean

Calculate the arithmetic mean of a vector of numbers x.

```
mean(x: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	float	-	-

### stdev

Calculate the standard deviation of a vector of numbers x.

```
stdev(x: ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	ndarray	-	-

### stderr

Calculate the standard error estimate of a vector of numbers x.

```
stderr(x: ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	ndarray	-	-

#### var

Calculate the variance of a vector of numbers x.

```
var(x: ndarray):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	ndarray	-	-

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### moment

Calculate the m-th moment of a vector of numbers x.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	ndarray	-	-
m	int	-	-

# correlation

Calculate the correlation between two series x1 and x2.

Argument Name	Type	Description	<b>Default Value</b>
x1	ndarray	-	-
x2	ndarray	-	-

# 2.21 \_\_init\_\_

# **Chapter 3**

# financepy.market.curves

### **Discount Curves**

These modules create a family of discount curve types related to the term structures of interest rates. Discount curves that can be used to present value a future cash flow. These differ from best fits curves in that they exactly refit the prices of bonds or CDS. The different discount curves are created by calibrating to different instruments. They also differ in terms of the term structure shapes they can have. Different shapes have different impacts in terms of locality on risk management performed using these different curves. There is often a trade-off between smoothness and locality. These are curves which supply a discount factor that can be used to present-value future payments.

#### **DiscountCurve**

This is a curve made from a Numpy array of times and discount factor values that represents a discount curve. It also requires a specific interpolation scheme. A function is also provided to return a survival probability so that this class can also be used to handle term structures of survival probabilities. Other curves inherit from this in order to share common functionality.

#### **DiscountCurveFlat**

This is a class that takes in a single flat rate.

#### **DiscountCurveNS**

Implementation of the Nelson-Siegel curve parametrisation.

#### **DiscountCurveNSS**

Implementation of the Nelson-Siegel-Svensson curve parametrisation.

#### **DiscountCurveZeros**

This is a discount curve that is made from a vector of times and zero rates.

# Interpolate

This module contains the interpolation function used throughout the discount curves when a discount factor needs to be interpolated. There are three interpolation methods:

- 1. PIECEWISE LINEAR This assumes that a discount factor at a time between two other known discount factors is obtained by linear interpolation. This approach does not guarantee any smoothness but is local. It does not guarantee positive forwards (assuming positive zero rates).
- 2. PIECEWISE LOG LINEAR This assumes that the log of the discount factor is interpolated linearly. The log of a discount factor to time T is T x R(T) where R(T) is the zero rate. So this is not linear interpolation of R(T) but of T x R(T).
- 3. FLAT FORWARDS This interpolation assumes that the forward rate is constant between discount factor points. It is not smooth but is highly local and also ensures positive forward rates if the zero rates are positive.

### 3.1 discount\_curve

### Class: DiscountCurve

class DiscountCurve:

# **DiscountCurve**

Create the discount curve from a vector of times and discount factors with an anchor date and specify an interpolation scheme. As we are explicitly linking dates and discount factors, we do not need to specify any compounding convention or day count calculation since discount factors are pure prices. We do however need to specify a convention for interpolating the discount factors in time.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
df_dts	list	-	-
df_values	np.ndarray	-	-
interp_type	InterpTypes	-	InterpTypes.FLAT_FWD_RATES

### \_zero\_to\_df

Convert a zero with a specified compounding frequency and day count convention to a discount factor for a single maturity date or a list of dates. The day count is used to calculate the elapsed year fraction.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	TODO: why is value_date not used?	-
rates	float or np.ndarray	-	-
times	float or np.ndarray	-	-
freq_type	FrequencyTypes	-	-
dc_type	DayCountTypes	-	-

#### \_df\_to\_zero

Given a dates this first generates the discount factors. It then converts the discount factors to a zero rate with a chosen compounding frequency which may be continuous, simple, or compounded at a specific frequency which are all choices of FrequencyTypes. Returns a list of discount factor.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dfs	float or np.ndarray	-	-
maturity_dts	Date or list	-	-
freq_type	FrequencyTypes	-	-
dc_type	DayCountTypes	-	-

#### zero\_rate

Calculation of zero rates with specified frequency. This function can return a vector of zero rates given a vector of dates so must use Numpy functions. Default frequency is a continuously compounded rate.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
dts	list or Date	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
dc_type	DayCountTypes	-	DayCountTypes.ACT_360

#### cc\_rate

Calculation of zero rates with continuous compounding. This function can return a vector of cc rates given a vector of dates so must use Numpy functions.

<b>Argument Name</b>	Type	Description	Default Value
dts	list or Date	-	-
dc_type	DayCountTypes	-	DayCountTypes.SIMPLE

### swap\_rate

Calculate the swap rate to maturity date. This is the rate paid by a swap that has a price of par today. This is the same as a Libor swap rate except that we do not do any business day adjustments.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
effective_dt	Date	-	-
maturity_dt	list or Date	-	-
freq_type	-	-	FrequencyTypes.ANNUAL
dc_type	DayCountTypes	-	DayCountTypes.THIRTY_E_360

#### df

Function to calculate a discount factor from a date or a vector of dates. The day count determines how dates get converted to years. I allow this to default to ACT\_ACT\_ISDA unless specified.

```
df(dt: (list, Date),
    day_count=DayCountTypes.ACT_ACT_ISDA):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	list or Date	-	-
day_count	-	-	DayCountTypes.ACT_ACT_ISDA

### \_df

Hidden function to calculate a discount factor from a time or a vector of times. Discourage usage in favour of passing in dates.

```
_df(t: (float, np.ndarray)):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
t	float or np.ndarray	-	-

# $survival\_prob$

This returns a survival probability to a specified date based on the assumption that the continuously compounded rate is a default hazard rate in which case the survival probability is directly analogous to a discount factor.

```
survival_prob(dt: Date):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	Date	-	-

#### fwd

Calculate the continuously compounded forward rate at the forward Date provided. This is done by perturbing the time by one day only and measuring the change in the log of the discount factor divided by the time increment dt. I am assuming continuous compounding over the one date.

```
fwd(dts: Date):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
dts	Date	-	-

#### \_fwd

Calculate the continuously compounded forward rate at the forward time provided. This is done by perturbing the time by a small amount and measuring the change in the log of the discount factor divided by the time increment dt.

```
_fwd(times: (np.ndarray, float)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
times	np.ndarray or float	-	-

# bump

Adjust the continuously compounded forward rates by a perturbation upward equal to the bump size and return a curve objet with this bumped curve. This is used for interest rate risk.

```
bump(bump_size: float):
```

Argument Name	Type	Description	Default Value
bump_size	float	-	-

3.1. DISCOUNT\_CURVE

### fwd\_rate

Calculate the forward rate between two forward dates according to the specified day count convention. This defaults to Actual 360. The first date is specified and the second is given as a date or as a tenor which is added to the first date.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
start_dt	list or Date	-	-
date_or_tenor	Date or str	-	-
dc_type	DayCountTypes	-	DayCountTypes.ACT_360

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

### 3.2 discount\_curve\_flat

## Class: DiscountCurveFlat(DiscountCurve)

A very simple discount curve based on a single zero rate with its own specified compounding method. Hence the curve is assumed to be flat. It is used for quick and dirty analysis and when limited information is available. It inherits several methods from FinDiscountCurve.

#### **DiscountCurveFlat**

Create a discount curve which is flat. This is very useful for quick testing and simply requires a curve date a rate and a compound frequency. As we have entered a rate, a corresponding day count convention must be used to specify how time periods are to be measured. As the curve is flat, no interpolation scheme is required.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
flat_rate	float or np.ndarray	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
dc_type	DayCountTypes	-	DayCountTypes.ACT_ACT_ISDA

### bump

Creates a new FinDiscountCurveFlat object with the entire curve bumped up by the bumpsize. All other parameters are preserved.

```
bump(bump_size: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
bump_size	float	-	-

#### df

Return discount factors given a single or vector of dts. The discount factor depends on the rate and this in turn depends on its compounding frequency and it defaults to continuous compounding. It also depends on the day count convention. This was set in the construction of the curve to be ACT\_ACT\_ISDA.

```
df(dts: (Date, list)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dts	Date or list	-	-

# \_\_repr\_\_

### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

\_print():

### 3.3 discount\_curve\_ns

## Class: DiscountCurveNS(DiscountCurve)

Implementation of Nelson-Siegel parametrisation of a discount curve. The internal rate is a continuously compounded rate but you can calculate alternative frequencies by providing a corresponding compounding frequency. A day count convention is needed to ensure that dates are converted to the correct time in years. The class inherits methods from FinDiscountCurve.

#### **DiscountCurveNS**

Creation of a FinDiscountCurveNS object. Parameters are provided individually for beta0, beta1, beta2 and tau. The zero rates produced by this parametrisation have an implicit compounding convention that defaults to continuous but which can be overridden.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
beta0	float	-	-
beta1	float	-	-
beta2	float	-	-
tau	float	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
dc_type	DayCountTypes	-	DayCountTypes.ACT_ACT_ISDA

#### zero\_rate

Calculation of zero rates with specified frequency according to NS parametrisation. This method overrides that in FinDiscountCurve. The parametrisation is not strictly in terms of continuously compounded zero rates, this function allows other compounding and day counts. This function returns a single or vector of zero rates given a vector of dates so must use Numpy functions. The default frequency is a continuously compounded rate and ACT ACT day counting.

Argument Name	Type	Description	Default Value
dates	list or Date	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
dc_type	DayCountTypes	-	DayCountTypes.ACT_360

#### \_zero\_rate

Zero rate for Nelson-Siegel curve parametrisation. This means that the t vector must use the curve day count.

```
_zero_rate(times: (float, np.ndarray)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
times	float or np.ndarray	-	-

#### df

Return discount factors given a single or vector of dates. The discount factor depends on the rate and this in turn depends on its compounding frequency and it defaults to continuous compounding. It also depends on the day count convention. This was set in the construction of the curve to be ACT\_ACT\_ISDA.

```
df(dates: (Date, list)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dates	Date or list	-	-

#### \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# \_print

Simple print function for backward compatibility.

```
_print():
```

### 3.4 discount\_curve\_nss

## Class: DiscountCurveNSS(DiscountCurve)

Implementation of Nelson-Siegel-Svensson parametrisation of the zero rate curve. The zero rate is assumed to be continuously compounded. This can be changed when calling for zero rates. A day count convention is needed to ensure that dates are converted to the correct time in years. The class inherits methods from FinDiscountCurve.

#### **DiscountCurveNSS**

Create a FinDiscountCurveNSS object by passing in curve valuation date plus the 4 different beta values and the 2 tau values. The zero rates produced by this parametrisation have an implicit compounding convention that defaults to continuous but can be overriden.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
beta_0	float	-	-
beta_1	float	-	-
beta_2	float	-	-
beta_3	float	-	-
tau_1	float	-	-
tau_2	float	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
day_count_type	DayCountTypes	-	DayCountTypes.ACT_ACT_ISDA

#### zero\_rate

Calculation of zero rates with specified frequency according to NSS parametrisation. This method overrides that in FinDiscountCurve. The NSS parametrisation is no strictly terms of continuously compounded zero rates, this function allows other compounding and day counts. This function returns a single or vector of zero rates given a vector of dates so must use Numpy functions. The default frequency is a continuously compounded rate and ACT ACT day counting.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dates	list or Date	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
dc_type	DayCountTypes	-	DayCountTypes.ACT_360

#### \_zero\_rate

Calculation of zero rates given a single time or a numpy vector of times. This function can return a single zero rate or a vector of zero rates. The compounding frequency must be provided.

```
_zero_rate(times: (float, np.ndarray)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
times	float or np.ndarray	-	-

#### df

Return discount factors given a single or vector of dates. The discount factor depends on the rate and this in turn depends on its compounding frequency and it defaults to continuous compounding. It also depends on the day count convention. This was set in the construction of the curve to be ACT\_ACT\_ISDA.

```
df(dates: (Date, list)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dates	Date or list	-	-

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## \_print

Simple print function for backward compatibility.

```
_print():
```

# 3.5 discount\_curve\_poly

## Class: DiscountCurvePoly(DiscountCurve)

Zero Rate Curve of a specified frequency parametrised using a cubic polynomial. The zero rate is assumed to be continuously compounded but this can be amended by providing a frequency when extracting zero rates. We also need to specify a Day count convention for time calculations. The class inherits all of the methods from FinDiscountCurve.

## **DiscountCurvePoly**

Create zero rate curve parametrised using a cubic curve from coefficients and specifying a compounding frequency type and day count convention.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
coefficients	list or np.ndarray	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
dc_type	DayCountTypes	-	DayCountTypes.ACT_ACT_ISDA

#### zero\_rate

Calculation of zero rates with specified frequency according to polynomial parametrisation. This method overrides FinDiscountCurve. The parametrisation is not strictly in terms of continuously compounded zero rates, this function allows other compounding and day counts. This function returns a single or vector of zero rates given a vector of dates so must use Numpy functions. The default frequency is a continuously compounded rate and ACT ACT day counting.

Argument Name	Type	Description	Default Value
dts	list or Date	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
dc_type	DayCountTypes	-	DayCountTypes.ACT_360

#### \_zero\_rate

Calculate the zero rate to maturity date but with times as inputs. This function is used internally and should be discouraged for external use. The compounding frequency defaults to that specified in the constructor of the curve object. Which may be annual to continuous.

```
_zero_rate(times: (float, np.ndarray)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
times	float or np.ndarray	-	-

#### df

Calculate the fwd rate to maturity date but with times as inputs. This function is used internally and should be discouraged for external use. The compounding frequency defaults to that specified in the constructor of the curve object.

```
df(dates: (list, Date)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dates	list or Date	-	-

#### \_\_repr\_\_

Display internal parameters of curve.

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Simple print function for backward compatibility.

```
_print():
```

# 3.6 discount\_curve\_pwf

# Class: DiscountCurvePWF(DiscountCurve)

Curve is made up of a series of zero rates sections with each having a piecewise flat zero rate. The default compounding assumption is continuous. The class inherits methods from FinDiscountCurve.

#### **DiscountCurvePWF**

Creates a discount curve using a vector of times and zero rates that assumes that the zero rates are piecewise flat.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
zero_dts	list	-	-
zero_rates	list or np.ndarray	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
day_count_type	DayCountTypes	_	DayCountTypes.ACT_ACT_ISDA

#### \_zero\_rate

The piecewise flat zero rate is selected and returned.

```
_zero_rate(times: (float, np.ndarray, list)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
times	float or np.ndarray,list	-	-

### \_fwd

Calculate the continuously compounded forward rate at the forward time provided. This is done by perturbing the time by a small amount and measuring the change in the log of the discount factor divided by the time increment dt.

```
_fwd(times: (np.ndarray, list)):
```

Argument Name	Type	Description	Default Value
times	np.ndarray or list	-	-

### df

Return discount factors given a single or vector of dates. The discount factor depends on the rate and this in turn depends on its compounding frequency and it defaults to continuous compounding. It also depends on the day count convention. This was set in the construction of the curve to be ACT\_ACT\_ISDA.

```
df(dates: (Date, list)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dates	Date or list	-	-

### \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# \_print

Simple print function for backward compatibility.

```
_print():
```

# 3.7 discount\_curve\_pwl

# Class: DiscountCurvePWL(DiscountCurve)

Curve is made up of a series of sections assumed to each have a piece-wise linear zero rate. The zero rate has a specified frequency which defaults to continuous. This curve inherits all of the extra methods from FinDiscountCurve.

#### DiscountCurvePWL

Curve is defined by a vector of increasing times and zero rates.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
zero_dts	Date or list	-	-
zero_rates	list or np.ndarray	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.CONTINUOUS
dc_type	DayCountTypes	-	DayCountTypes.ACT_ACT_ISDA

#### \_zero\_rate

Calculate the piecewise linear zero rate. This is taken from the initial inputs. A simple linear interpolation scheme is used. If the user supplies a frequency type then a conversion is done.

```
_zero_rate(times: (list, np.ndarray)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
times	list or np.ndarray	-	-

#### df

Return discount factors given a single or vector of dates. The discount factor depends on the rate and this in turn depends on its compounding frequency and it defaults to continuous compounding. It also depends on the day count convention. This was set in the construction of the curve to be ACT\_ACT\_ISDA.

```
df(dates: (Date, list)):
```

Argument Name	Type	Description	<b>Default Value</b>
dates	Date or list	-	-

# \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

The function arguments are described in the following table.

# $\_$ print

Simple print function for backward compatibility.

\_print():

### 3.8 discount\_curve\_zeros

## Class: DiscountCurveZeros(DiscountCurve)

This is a curve calculated from a set of dates and zero rates. As we have rates as inputs, we need to specify the corresponding compounding frequency. Also to go from rates and dates to discount factors we need to compute the year fraction correctly and for this we require a day count convention. Finally, we need to interpolate the zero rate for the times between the zero rates given and for this we must specify an interpolation convention. The class inherits methods from FinDiscountCurve.

### **DiscountCurveZeros**

Create the discount curve from a vector of dates and zero rates factors. The first date is the curve anchor. Then a vector of zero dates and then another same-length vector of rates. The rate is to the corresponding date. We must specify the compounding frequency of the zero rates and also a day count convention for calculating times which we must do to calculate discount factors. Finally we specify the interpolation scheme for off-grid dates.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
zero_dts	list	_	-
zero_rates	list or np.ndarray	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.ANNUAL
dc_type	DayCountTypes	-	DayCountTypes.ACT_ACT_ISDA
interp_type	InterpTypes	-	InterpTypes.FLAT_FWD_RATES

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\mathtt{print}}$

Simple print function for backward compatibility.

```
_print():
```

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# 3.9 interpolator

# Enumerated Type: InterpTypes

This enumerated type has the following values:

- FLAT\_FWD\_RATES
- LINEAR\_FWD\_RATES
- LINEAR\_ZERO\_RATES
- FINCUBIC\_ZERO\_RATES
- NATCUBIC\_LOG\_DISCOUNT
- NATCUBIC\_ZERO\_RATES
- PCHIP\_ZERO\_RATES
- PCHIP\_LOG\_DISCOUNT

# Class: Interpolator()

class Interpolator():

## **Interpolator**

PLEASE ADD A FUNCTION DESCRIPTION

```
Interpolator(interpolatorType: InterpTypes):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
interpolatorType	InterpTypes	-	-

#### fit

# Second derivatives at left is zero and first derivative at # right is clamped to zero.

```
fit(times: np.ndarray,
    dfs: np.ndarray):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
times	np.ndarray	-	-
dfs	np.ndarray	-	-

# interpolate

Interpolation of discount factors at time x given discount factors at times provided using one of the methods in the enum InterpTypes. The value of x can be an array so that the function is vectorised.

```
interpolate(t: float):
```

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t	float	-	-

# interpolate

Fast interpolation of discount factors at time x given discount factors at times provided using one of the methods in the enum InterpTypes. The value of x can be an array so that the function is vectorised.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
t	float or np.ndarray	time or array of times	-
times	np.ndarray	Vector of times on grid	-
dfs	np.ndarray	Vector of discount factors	-
method	int	Interpolation method which is value of enum	-

### \_uinterpolate

Return the interpolated value of y given x and a vector of x and y. The values of x must be monotonic and increasing. The different schemes for interpolation are linear in y (as a function of x), linear in log(y) and piecewise flat in the continuously compounded forward y rate.

```
_uinterpolate(t, times, dfs, method):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
times	-	-	-
dfs	-	-	-
method	-	-	-

# \_vinterpolate

Return the interpolated values of y given x and a vector of x and y. The values of x must be monotonic and increasing. The different schemes for interpolation are linear in y (as a function of x), linear in log(y) and piecewise flat in the continuously compounded forward y rate.

```
_vinterpolate(xValues, xvector, dfs, method):
```

Argument Name	Type	Description	<b>Default Value</b>
xValues	-	-	-
xvector	-	-	-
dfs	-	-	-
method	-	-	-

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3.10 \_\_init\_\_

# **Chapter 4**

# financepy.market.volatility

# **Market Volatility**

These modules create a family of curve types related to the market volatility. There are three types of class:

- 1. Term structures of volatility i.e. volatility as a function of option expiry date.
- 2. Volatility curves which are smile/skews so store volatility as a function of option strike.
- 3. Volatility surfaces which hold volatility as a function of option expiry date AND option strike.

The classes are as follows:

## equity\_vol\_surface

Constructs an equity volatility surface that fits to a grid of market volatilities at a set of strikes and expiry dates. It implements the SVI parametric form for fitting and interpolating volatilities. It also provides plotting of the volatility curve and surfaces.

### **FinFXVolSurface**

FX volatility as a function of option expiry and strike. This class constructs the surface from the ATM volatility plus a choice of 10 and 25 delta strangles and risk reversals or both. This is done for multiple expiry dates. A number of curve fitting choices are possible including polynomial in delta and SABR.

# FinIborCapFloorVol

Libor cap/floor volatility as a function of option expiry (cap/floor start date). Takes in cap (flat) volatility and bootstraps the caplet volatility. This is assumed to be piecewise flat.

# FinlborCapFloorVolFn

Parametric function for storing the cap and caplet volatilities based on form proposed by Rebonato.

# 4.1 equity\_vol\_curve

# Class: EquityVolCurve()

Class to manage a smile or skew in volatility at a single maturity horizon. It fits the volatility using a polynomial. Includes analytics to extract the implied pdf of the underlying at maturity. THIS NEEDS TO BE SUBSTITUTED WITH FINEQUITYVOLSURFACE.

# **EquityVolCurve**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
curve_dt	-	-	-
expiry_dt	-	-	-
strikes	-	-	-
volatilities	-	-	-
polynomial	-	-	3

# volatility

Return the volatility for a strike using a given polynomial interpolation.

```
volatility(strike):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
strike	-	-	-

# $calculate\_pdf$

calculate the probability density function of the underlying using the volatility smile or skew curve following the approach set out in Breedon and Litzenberger.

```
calculate_pdf():
```

# 4.2 equity\_vol\_surface

## Class: EquityVolSurface

Class to perform a calibration of a chosen parametrised surface to the prices of equity options at different strikes and expiry tenors. There is 0 a choice of volatility function from cubic in delta to full SABR and SSVI. Check out VolFuncTypes. Visualising the volatility curve is useful. Also, there is no guarantee that the implied pdf will be positive.

## **EquityVolSurface**

Create the EquitySurface object by passing in market vol data for a list of strikes and expiry dates.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
expiry_dts	list or (list	-	-
strikes	list or np.ndarray	-	-
volatility_grid	list or np.ndarray	-	-
volatility_function_type	VolFuncTypes	-	VolFuncTypes.CLARK
finSolverType	FinSolverTypes	-	NELDER_MEAD

#### vol\_from\_strike\_dt

Interpolates the Black-Scholes volatility from the volatility surface given call option strike and expiry date. Linear interpolation is done in variance space. The smile strikes at bracketed dates are determined by determining the strike that reproduces the provided delta value. This uses the calibration delta convention, but it can be overriden by a provided delta convention. The resulting volatilities are then determined for each bracketing expiry time and linear interpolation is done in variance space and then converted back to a lognormal volatility.

```
vol_from_strike_dt(K, expiry_dt):
```

Argument Name	Type	Description	<b>Default Value</b>
K	-	-	-
expiry_dt	-	-	-

#### vol\_from\_delta\_dt

Interpolates the Black-Scholes volatility from the volatility surface given a call option delta and expiry date. Linear interpolation is done in variance space. The smile strikes at bracketed dates are determined by determining the strike that reproduces the provided delta value. This uses the calibration delta convention, but it can be overriden by a provided delta convention. The resulting volatilities are then determined for each bracketing expiry time and linear interpolation is done in variance space and then converted back to a lognormal volatility.

```
vol_from_delta_dt(call_delta, expiry_dt, delta_method=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
call_delta	-	-	-
expiry_dt	-	-	-
delta_method	-	-	None

### \_build\_vol\_surface

Main function to construct the vol surface.

```
_build_vol_surface(finSolverType=FinSolverTypes.NELDER_MEAD):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
finSolverType	-	-	NELDER_MEAD

#### check calibration

Compare calibrated vol surface with market and output a report which sets out the quality of fit to the ATM and 10 and 25 delta market strangles and risk reversals.

```
check_calibration(verbose: bool, tol: float = 1e-6):
```

Argument Name	Type	Description	<b>Default Value</b>
verbose	bool	-	-
tol	float	-	1e-6

# implied\_dbns

Calculate the pdf for each tenor horizon. Returns a list of FinDistribution objects, one for each tenor horizon.

```
implied_dbns(lowS, highS, numIntervals):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
lowS	-	-	-
highS	-	-	-
numIntervals	-	-	-

# plot\_vol\_curves

Generates a plot of each of the vol discount implied by the market and fitted.

```
plot_vol_curves():
```

The function arguments are described in the following table.

### \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

The function arguments are described in the following table.

# \_obj

Return a value that is minimised when the ATM, MS and RR vols have been best fitted using the parametric volatility curve represented by params and specified by the vol\_type\_value. We fit at one time slice only.

```
_obj(params, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
params	-	-	-
*args	-	-	-

# \_solve\_to\_horizon

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
t	-	-	-
r	-	-	-
q	-	-	-
strikes	-	-	-
time_index	-	-	-
volatility_grid	-	-	-
vol_type_value	-	-	-
x_inits	-	-	-
finSolverType	-	-	-

# vol\_function

Return the volatility for a strike using a given polynomial interpolation following Section 3.9 of Iain Clark book.

```
vol_function(vol_function_type_value, params, f, k, t):
```

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
		Type         Description           -         -           -         -           -         -           -         -           -         -           -         -

# \_delta\_fit

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_delta_fit(k, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
*args	-	-	-

# \_solver\_for\_smile\_strike

Solve for the strike that sets the delta of the option equal to the target value of delta allowing the volatility to be a function of the strike.

<b>Argument Name</b>	Type	Description	Default Value
S	-	-	-
t	-	-	-
r	-	-	-
q	-	-	-
option_type_value	-	-	-
volatilityTypeValue	-	-	-
delta_target	-	-	-
initial_guess	-	-	-
parameters	-	-	-

### 4.3 fx vol surface

## Class: FXVolSurface()

Class to perform a calibration of a chosen parametrised surface to the prices of FX options at different strikes and expiry tenors. The calibration inputs are the ATM and 25 Delta volatilities given in terms of the market strangle amd risk reversals. There is a choice of volatility function ranging from polynomial in delta to a limited version of SABR.

### **FXVolSurface**

Create the FinFXVolSurface object by passing in market vol data for ATM and 25 Delta Market Strangles and Risk Reversals.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
spot_fx_rate	float	-	-
currency_pair	str	-	-
notional_currency	str	-	-
dom_discount_curve	DiscountCurve	-	-
for_discount_curve	DiscountCurve	-	-
tenors	list or (list	-	-
atm_vols	list or np.ndarray	-	-
mktStrangle25DeltaVols	list or np.ndarray	-	-
riskReversal25DeltaVols	list or np.ndarray	-	-
atmMethod	FinFXATMMethod	-	FWD_DELTA_NEUTRAL
delta_method	FinFXDeltaMethod	-	SPOT_DELTA
volatility_function_type	VolFuncTypes	-	VolFuncTypes.CLARK

### volatility

Interpolate the Black-Scholes volatility from the volatility surface given the option strike and expiry date. Linear interpolation is done in variance x time.

4.3. FX\_VOL\_SURFACE

```
volatility(K, expiry_dt):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
K	-	-	-
expiry_dt	-	-	-

## build\_vol\_surface

PLEASE ADD A FUNCTION DESCRIPTION

```
build_vol_surface():
```

The function arguments are described in the following table.

### solver\_for\_smile\_strike

Solve for the strike that sets the delta of the option equal to the target value of delta allowing the volatility to be a function of the strike.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
option_type_value	-	-	-
delta_target	-	-	-
tenor_index	-	-	-
initialValue	-	-	-

## check\_calibration

PLEASE ADD A FUNCTION DESCRIPTION

```
check_calibration(verbose: bool, tol: float = 1e-6):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
verbose	bool	-	-
tol	float	-	1e-6

## implied\_dbns

Calculate the pdf for each tenor horizon. Returns a list of FinDistribution objects, one for each tenor horizon.

```
implied_dbns(lowFX, highFX, numIntervals):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
lowFX	-	-	-
highFX	-	-	-
numIntervals	-	-	-

## plot\_vol\_curves

PLEASE ADD A FUNCTION DESCRIPTION

```
plot_vol_curves():
```

The function arguments are described in the following table.

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

The function arguments are described in the following table.

g

PLEASE ADD A FUNCTION DESCRIPTION

```
g(K, *args):
```

4.3. FX\_VOL\_SURFACE

Argument Name	Type	Description	Default Value
K	-	-	-
*args	-	-	-

## obj\_fast

Return a function that is minimised when the ATM, MS and RR vols have been best fitted using the parametric volatility curve represented by cvec

```
obj_fast(params, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
params	-	-	-
*args	-	-	-

## solve\_to\_horizon\_fast

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
rd	-	-	-
rf	-	-	-
K_ATM	-	-	-
atm_vol	-	-	-
ms25DVol	-	-	-
rr25DVol	-	-	-
delta_method_value	-	-	-
vol_type_value	-	-	-
xopt	-	-	-

## vol\_function

Return the volatility for a strike using a given polynomial interpolation following Section 3.9 of Iain Clark book.

```
vol_function(vol_function_type_value, params, f, k, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
vol_function_type_value	-	-	-
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

### delta\_fit

### PLEASE ADD A FUNCTION DESCRIPTION

```
delta_fit(K, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
K	-	-	-
*args	-	-	-

### solver\_for\_smile\_strike\_fast

Solve for the strike that sets the delta of the option equal to the target value of delta allowing the volatility to be a function of the strike.

<b>Argument Name</b>	Type	Description	Default Value
S	-	-	-
t	-	-	-
rd	-	-	-
rf	-	-	-
option_type_value	-	-	-
volatilityTypeValue	-	-	-
delta_target	-	-	-
delta_method_value	-	-	-
initial_guess	-	-	-
parameters	-	-	-

## solve\_for\_strike

This function determines the implied strike of an FX option given a delta and the other option details. It uses a one-dimensional Newton root search algorithm to determine the strike that matches an input volatility.

Argument Name	Type	Description	Default Value
spot_fx_rate	-	-	-
tdel	-	-	-
rd	-	-	-
rf	-	-	-
option_type_value	-	-	-
delta_target	-	-	-
delta_method_value	-	-	-
volatility	-	-	-

# 4.4 fx\_vol\_surface\_plus

## Class: FXVolSurfacePlus()

Class to perform a calibration of a chosen parametrised surface to the prices of FX options at different strikes and expiry tenors. The calibration inputs are the ATM and 25 and 10 Delta volatilities in terms of the market strangle amd risk reversals. There is a choice of volatility function from cubic in delta to full SABR. Check out VolFuncTypes. Parameter alpha [0,1] is used to interpolate between fitting only 25D when alpha=0 to fitting only 10D when alpha=1.0. Alpha=0.5 assigns equal weights A vol function with more parameters will give a better fit. Of course. But it might also overfit. Visualising the volatility curve is useful. Also, there is no guarantee that the implied pdf will be positive.

### **FXVolSurfacePlus**

Create the FinFXVolSurfacePlus object by passing in market vol data for ATM, 25 Delta and 10 Delta strikes. The alpha weight shifts the fitting between 25D and 10D. Alpha = 0.0 is 100is 100

```
FXVolSurfacePlus(value_dt: Date,
                spot_fx_rate: float,
                 currency_pair: str,
                notional_currency: str,
                 dom_discount_curve: DiscountCurve,
                 for_discount_curve: DiscountCurve,
                 tenors: (list),
                 atm_vols: (list, np.ndarray),
                 mktStrangle25DeltaVols: (list, np.ndarray),
                 riskReversal25DeltaVols: (list, np.ndarray),
                 mktStrangle10DeltaVols: (list, np.ndarray),
                 riskReversal10DeltaVols: (list, np.ndarray),
                 alpha: float,
                 atmMethod: FinFXATMMethod = FinFXATMMethod.FWD_DELTA_NEUTRAL,
                 delta_method: FinFXDeltaMethod = FinFXDeltaMethod.SPOT_DELTA,
                 volatility_function_type: VolFuncTypes = VolFuncTypes.CLARK,
                 finSolverType: FinSolverTypes = FinSolverTypes.NELDER_MEAD,
                 tol: float = 1e-8):
```

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
spot_fx_rate	float	-	-
currency_pair	str	-	-
notional_currency	str	-	-
dom_discount_curve	DiscountCurve	-	-
for_discount_curve	DiscountCurve	-	-
tenors	list or (list	-	-
atm_vols	list or np.ndarray	-	-
mktStrangle25DeltaVols	list or np.ndarray	-	-
riskReversal25DeltaVols	list or np.ndarray	-	-
mktStrangle10DeltaVols	list or np.ndarray	-	-
riskReversal10DeltaVols	list or np.ndarray	-	-
alpha	float	-	-
atmMethod	FinFXATMMethod	-	FWD_DELTA_NEUTRAL
delta_method	FinFXDeltaMethod	-	SPOT_DELTA
volatility_function_type	VolFuncTypes	-	VolFuncTypes.CLARK
finSolverType	FinSolverTypes	-	NELDER_MEAD
tol	float		1e-8

### vol\_from\_strike\_dt

Interpolates the Black-Scholes volatility from the volatility surface given call option strike and expiry date. Linear interpolation is done in variance space. The smile strikes at bracketed dates are determined by determining the strike that reproduces the provided delta value. This uses the calibration delta convention, but it can be overriden by a provided delta convention. The resulting volatilities are then determined for each bracketing expiry time and linear interpolation is done in variance space and then converted back to a lognormal volatility.

```
vol_from_strike_dt(K, expiry_dt):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
K	-	-	-
expiry_dt	-	-	-

### delta\_to\_strike

Interpolates the strike at a delta and expiry date. Linear time to expiry interpolation is used in strike.

```
delta_to_strike(call_delta, expiry_dt, delta_method):
```

Argument Name	Type	Description	Default Value
call_delta	-	-	-
expiry_dt	-	-	-
delta_method	-	-	-

### vol\_from\_delta\_dt

Interpolates the Black-Scholes volatility from the volatility surface given a call option delta and expiry date. Linear interpolation is done in variance space. The smile strikes at bracketed dates are determined by determining the strike that reproduces the provided delta value. This uses the calibration delta convention, but it can be overriden by a provided delta convention. The resulting volatilities are then determined for each bracketing expiry time and linear interpolation is done in variance space and then converted back to a lognormal volatility.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
call_delta	-	-	-
expiry_dt	-	-	-
delta_method	-	-	None

### \_build\_vol\_surface

Main function to construct the vol surface.

```
_build_vol_surface(finSolverType=FinSolverTypes.NELDER_MEAD, tol=1e-8):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
finSolverType	-	-	NELDER_MEAD
tol	-	-	1e-8

### check calibration

Compare calibrated vol surface with market and output a report which sets out the quality of fit to the ATM and 10 and 25 delta market strangles and risk reversals.

```
check_calibration(verbose: bool, tol: float = 1e-6):
```

Argument Name	Type	Description	Default Value
verbose	bool	-	-
tol	float	-	1e-6

## implied\_dbns

Calculate the pdf for each tenor horizon. Returns a list of FinDistribution objects, one for each tenor horizon.

```
implied_dbns(lowFX, highFX, numIntervals):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
lowFX	-	-	-
highFX	-	-	-
numIntervals	-	-	-

## plot\_vol\_curves

Generates a plot of each of the vol discount implied by the market and fitted.

```
plot_vol_curves():
```

The function arguments are described in the following table.

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

The function arguments are described in the following table.

 $_{\mathbf{g}}$ 

PLEASE ADD A FUNCTION DESCRIPTION

```
_g(K, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
K	-	-	-
*args	-	-	-

## \_interpolate\_gap

PLEASE ADD A FUNCTION DESCRIPTION

```
_interpolate_gap(k, strikes, gaps):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
strikes	-	-	-
gaps	-	-	-

## \_obj

Return a function that is minimised when the ATM, MS and RR vols have been best fitted using the parametric volatility curve represented by params and specified by the vol\_type\_value

```
_obj(params, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
params	-	-	-
*args	-	-	-

# \_obj\_gap

Return a function that is minimised when the ATM, MS and RR vols have been best fitted using the parametric volatility curve represented by params and specified by the vol\_type\_value

```
_obj_gap(gaps, *args):
```

Argument Name	Type	Description	Default Value
gaps	-	-	-
*args	-	-	-

### \_solve\_to\_horizon

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
rd	-	-	-
rf	-	-	-
K_ATM	-	-	-
atm_vol	-	-	-
ms25DVol	-	-	-
rr25DVol	-	-	-
ms10DVol	-	-	-
rr10DVol	-	-	-
delta_method_value	-	-	-
vol_type_value	-	-	-
alpha	-	-	-
x_inits	-	-	-
ginits	-	-	-
finSolverType	-	-	-
tol	-	-	-

## vol\_function

Return the volatility for a strike using a given polynomial interpolation following Section 3.9 of Iain Clark book.

```
vol_function(vol_function_type_value, params, strikes, gaps, f, k, t):
```

Argument Name	Type	Description	<b>Default Value</b>
vol_function_type_value	-	-	-
params	-	-	-
strikes	-	-	-
gaps	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

## \_delta\_fit

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_delta_fit(k, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
k	-	-	-
*args	-	-	-

### \_solver\_for\_smile\_strike

Solve for the strike that sets the delta of the option equal to the target value of delta allowing the volatility to be a function of the strike.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
rd	-	-	-
rf	-	-	-
option_type_value	-	-	-
volatilityTypeValue	-	-	-
delta_target	-	-	-
delta_method_value	-	-	-
initial_guess	-	-	-
parameters	-	-	-
strikes	-	-	-
gaps	-	-	-

## solve\_for\_strike

This function determines the implied strike of an FX option given a delta and the other option details. It uses a one-dimensional Newton root search algorithm to determine the strike that matches an input volatility.

Argument Name	Type	Description	Default Value
spot_fx_rate	-	-	-
tdel	-	-	-
rd	-	-	-
rf	-	-	-
option_type_value	-	-	-
delta_target	-	-	-
delta_method_value	-	-	-
volatility	-	-	-

# 4.5 ibor\_cap\_vol\_curve

## Class: IborCapVolCurve()

Class to manage a term structure of cap (flat) volatilities and to do the conversion to caplet (spot) volatilities. This does not manage a strike dependency, only a term structure. The cap and caplet volatilies are keyed off the cap and caplet maturity dates. However this volatility only applies to the evolution of the Ibor rate out to the caplet start dates. Note also that this class also handles floor vols.

## **IborCapVolCurve**

Create a cap/floor volatility curve given a curve date, a list of cap maturity dates and a vector of cap volatilities. To avoid confusion first date of the capDates must be equal to the curve date and first cap volatility for this date must equal zero. The internal times are calculated according to the provided day count convention. Note cap and floor volatilities are the same for the same strike and tenor, I just refer to cap volatilities in the code for code simplicity.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
curve_dt	-	Valuation date for cap volatility	-
cap_maturity_dts	-	curve date + maturity dates for caps	-
cap_sigmas	-	Flat cap volatility for cap maturity dates	-
dc_type	-	-	-

# $generate\_caplet\_vols$

Bootstrap caplet volatilities from cap volatilities using similar notation to Hull's book (page 32.11). The first volatility in the vector of caplet vols is zero.

```
generate_caplet_vols():
```

The function arguments are described in the following table.

# caplet\_vol

PLEASE ADD A FUNCTION DESCRIPTION

```
caplet_vol(dt):
```

Argument Name	Type	Description	Default Value
dt	-	-	-

# $cap\_vol$

Return the cap flat volatility for a specific cap maturity date for the last caplet/floorlet in the cap/floor. The volatility interpolation is piecewise flat.

cap\_vol(dt):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

# 4.6 ibor\_cap\_vol\_curve\_fn

# Class: IborCapVolCurveFn()

Class to manage a term structure of caplet volatilities using the parametric form suggested by Rebonato (1999).

# Ibor Cap Vol Curve Fn

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
curve_dt	-	-	-
a	-	-	-
b	-	-	-
С	-	-	-
d	-	-	-

# $cap\_floorlet\_vol$

Return the caplet volatility.

```
cap_floorlet_vol(dt):
```

Argument Name	Type	Description	Default Value
dt	-	-	-

# 4.7 swaption\_vol\_surface

### Class: SwaptionVolSurface()

Class to perform a calibration of a chosen parametrised surface to the prices of swaptions at different expiry dates and swap tenors. There is a choice of volatility function from cubic in delta to full SABR and SSVI. Check out VolFuncTypes. Visualising the volatility curve is useful. Also, there is no guarantee that the implied pdf will be positive.

### **SwaptionVolSurface**

Create the FinSwaptionVolSurface object by passing in market vol data for a list of strikes and expiry dates.

The function arguments are described in the following table.

Type	Description	<b>Default Value</b>
Date	-	-
list or (list	-	-
list or np.ndarray	-	-
np.ndarray or (np.ndarray	-	-
np.ndarray or (np.ndarray	-	-
VolFuncTypes	-	VolFuncTypes.SABR
FinSolverTypes	-	NELDER_MEAD
	Date list or (list list or np.ndarray np.ndarray or (np.ndarray np.ndarray or (np.ndarray VolFuncTypes	Date - list or (list - list or np.ndarray - np.ndarray or (np.ndarray - np.ndarray or (np.ndarray - VolFuncTypes -

### vol\_from\_strike\_dt

Interpolates the Black-Scholes volatility from the volatility surface given call option strike and expiry date. Linear interpolation is done in variance space. The smile strikes at bracketed dates are determined by determining the strike that reproduces the provided delta value. This uses the calibration delta convention, but it can be overriden by a provided delta convention. The resulting volatilities are then determined for each bracketing expiry time and linear interpolation is done in variance space and then converted back to a lognormal volatility.

```
vol_from_strike_dt(K, expiry_dt):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
K	-	-	-
expiry_dt	-	-	-

### \_build\_vol\_surface

Main function to construct the vol surface.

```
_build_vol_surface(finSolverType=FinSolverTypes.NELDER_MEAD):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
finSolverType	-	-	NELDER_MEAD

### check\_calibration

Compare calibrated vol surface with market and output a report which sets out the quality of fit to the ATM and 10 and 25 delta market strangles and risk reversals.

```
check_calibration(verbose: bool, tol: float = 1e-6):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
verbose	bool	-	-
tol	float	-	1e-6

## plot\_vol\_curves

Generates a plot of each of the vol discount implied by the market and fitted.

```
plot_vol_curves():
```

The function arguments are described in the following table.

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

## \_obj

Return a value that is minimised when the ATM, MS and RR vols have been best fitted using the parametric volatility curve represented by params and specified by the vol\_type\_value at a single time slice only.

```
_obj(params, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
params	-	-	-
*args	-	-	-

### \_solve\_to\_horizon

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
f	-	-	-
strikes_grid	-	-	-
time_index	-	-	-
volatility_grid	-	-	-
vol_type_value	-	-	-
x_inits	-	-	-
finSolverType	-	-	-

### vol\_function

Return the volatility for a strike using a given polynomial interpolation following Section 3.9 of Iain Clark book.

```
vol_function(vol_function_type_value, params, f, k, t):
```

Argument Name	Type	Description	<b>Default Value</b>
vol_function_type_value	-	-	-
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

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# 4.8 \_\_init\_\_

# **Chapter 5**

# financepy.products.equity

# **Equity Products**

This folder contains a set of Equity-related products. It includes:

## **EquityVanillaOption**

Handles simple European-style call and put options on a dividend paying stock with analytical and montecarlo valuations.

## **EquityAmericanOption**

Handles America-style call and put options on a dividend paying stock with tree-based valuations.

# **EquityAsianOption**

Handles call and put options where the payoff is determined by the average-stock price over some period before expiry.

# **EquityBasketOption**

Handles call and put options on a basket of assets, with an analytical and Monte-Carlo valuation according to Black-Scholes model.

# **EquityCompoundOption**

Handles options to choose to enter into a call or put option. Has an analytical valuation model for European style options and a tree model if either or both options are American style exercise.

# **EquityDigitalOption**

Handles European-style options to receive cash or nothing, or to receive the asset or nothing. Has an analytical valuation model for European style options.

## **EquityFixedLookbackOption**

Handles European-style options to receive the positive difference between the strike and the minimum (put) or maximum (call) of the stock price over the option life.

## **EquityFloatLookbackOption**

Handles an equity option in which the strike of the option is not fixed but is set at expiry to equal the minimum stock price in the case of a call or the maximum stock price in the case of a put. In other words the buyer of the call gets to buy the asset at the lowest price over the period before expiry while the buyer of the put gets to sell the asset at the highest price before expiry. """

## **EquityBarrierOption**

Handles an option which either knocks-in or knocks-out if a specified barrier is crossed from above or below, resulting in owning or not owning a call or a put option. There are eight variations which are all valued.

## **EquityRainbowOption**

**TBD** 

## **EquityVarianceSwap**

**TBD** 

Products that have not yet been implemented include:

- Power Options
- Ratchet Options
- Forward Start Options
- Log Options

# 5.1 equity\_american\_option

## Class: EquityAmericanOption(EquityOption)

Class for American (and European) style options on simple vanilla calls and puts - a tree valuation model is used that can handle both.

## **EquityAmericanOption**

Class for American style options on simple vanilla calls and puts. Specify the expiry date, strike price, whether the option is a call or put and the number of options.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiry_dt	Date	-	-
strike_price	float	-	-
option_type	OptionTypes	-	-
num_options	float	-	1.0

### value

Valuation of an American option using a CRR tree to take into account the value of early exercise.

```
value(value_dt: Date,
    stock_price: (np.ndarray, float),
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model: Model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	np.ndarray or float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-

#### \_\_repr\_\_

### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $\_$ print

Simple print function for backward compatibility.

\_print():

# 5.2 equity\_asian\_option

### Enumerated Type: AsianOptionValuationMethods

This enumerated type has the following values:

- GEOMETRIC
- TURNBULL\_WAKEMAN
- CURRAN

### Class: EquityAsianOption

Class for an Equity Asian Option. This is an option with a final payoff linked to the averaging of the stock price over some specified period before the option expires. The valuation is done for both an arithmetic and a geometric average but the former can only be done either using an analytical approximation of the arithmetic average distribution or by using Monte-Carlo simulation.

## **EquityAsianOption**

Create an EquityAsian option object which takes a start date for the averaging, an expiry date, a strike price, an option type and a number of observations.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
startAveragingDate	Date	-	-
expiry_dt	Date	-	-
strike_price	float	-	-
option_type	OptionTypes	-	-
numberOfObservations	int	-	100

### value

Calculate the value of an Asian option using one of the specified analytical approximations for an average rate option. These are the three enumerated values in the enum AsianOptionValuationMethods. The choices of approximation are (i) GEOMETRIC - the average is a geometric one as in paper by Kenna and Worst (1990), (ii) TURNBULL\_WAKEMAN - this is a value based on an edgeworth expansion of the moments of the arithmetic average, and (iii) CURRAN - another approximative approach by Curran based on conditioning on the geometric mean price. Just choose the corresponding enumerated value to switch between these different approaches. Note that the accrued average is only required if the value date is inside the averaging period for the option.

```
value(value_dt: Date,
```

```
stock_price: float,
discount_curve: DiscountCurve,
dividend_curve: DiscountCurve,
model,
method: AsianOptionValuationMethods,
accrued_average: float = None):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Туре	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-
method	AsianOptionValuationMethods	-	-
accrued_average	float	-	None

## \_value\_geometric

This option valuation is based on paper by Kemna and Vorst 1990. It calculates the Geometric Asian option price which is a lower bound on the Arithmetic option price. This should not be used as a valuation model for the Arithmetic Average option but can be used as a control variate for other approaches.

```
_value_geometric(value_dt, stock_price, discount_curve, dividend_curve, model, accrued_average):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_price	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-
accrued_average	-	-	-

### \_value\_curran

Valuation of an Asian option using the result by Vorst.

```
_value_curran(value_dt, stock_price, discount_curve, dividend_curve, model, accrued_average):
```

<b>Argument Name</b>	Type	Description	Default Value
value_dt	-	-	-
stock_price	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-
accrued_average	-	-	-

### \_value\_turnbull\_wakeman

Asian option valuation based on paper by Turnbull and Wakeman 1991 which uses the edgeworth expansion to find the first two moments of the arithmetic average.

```
_value_turnbull_wakeman(value_dt, stock_price, discount_curve, dividend_curve, model, accrued_average):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
stock_price	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-
accrued_average	-	-	-

### \_value\_mc

Monte Carlo valuation of the Asian Average option using standard Monte Carlo code enhanced by Numba. I have discontinued the use of this as it is both slow and has limited variance reduction.

```
_value_mc(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model,
    num_paths: int,
    seed: int,
    accrued_average: float):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-
num_paths	int	-	-
seed	int	-	-
accrued_average	float	-	-

### \_value\_mc\_fast

Monte Carlo valuation of the Asian Average option. This method uses a lot of Numpy vectorisation. It is also helped by Numba.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_price	-	-	-
discount_curve	-	-	-
dividend_curve	-	Yield	-
model	-	Model	-
num_paths	-	Numpaths integer	-
seed	-	-	-
accrued_average	-	-	-

### value\_mc

Monte Carlo valuation of the Asian Average option using a control variate method that improves accuracy and reduces the variance of the price. This uses Numpy and Numba. This is the standard MC pricer.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-
num_paths	int	-	-
seed	int	-	-
accrued_average	float	-	-

### \_\_repr\_\_

### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# \_print

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

## \_value\_mc\_numba

### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
t0	-	-	-
t	-	-	-
tau	-	-	-
K	-	-	-
n	-	-	-
option_type	-	-	-
stock_price	-	-	-
interest_rate	-	-	-
dividend_yield	-	-	-
volatility	-	-	-
num_paths	-	-	-
seed	-	-	-
accrued_average	-	-	-

# \_value\_mc\_fast\_numba

### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
t0	float	-	-
t	float	-	-
tau	float	-	-
K	float	-	-
n	int	-	-
option_type	int	-	-
stock_price	float	-	-
interest_rate	float	-	-
dividend_yield	float	-	-
volatility	float	-	-
num_paths	int	-	-
seed	int	-	-
accrued_average	float	-	-

# \_value\_mc\_fast\_cv\_numba

### PLEASE ADD A FUNCTION DESCRIPTION

```
_value_mc_fast_cv_numba(t0, t, tau, K, n, option_type, stock_price, interest_rate, dividend_yield, volatility, num_paths, seed, accrued_average, v_g_exact):
```

Argument Name	Type	Description	<b>Default Value</b>
t0	-	-	-
t	-	-	-
tau	-	-	-
K	-	-	-
n	-	-	-
option_type	-	-	-
stock_price	-	-	-
interest_rate	-	-	-
dividend_yield	-	-	-
volatility	-	-	-
num_paths	-	-	-
seed	-	-	-
accrued_average	-	-	-
v_g_exact	-	-	-

# 5.3 equity\_barrier\_option

## Class: EquityBarrierOption(EquityOption)

Class to hold details of an Equity Barrier Option. It also calculates the option price using Black Scholes for 8 different variants on the Barrier structure in enum EquityBarrierTypes.

# **EquityBarrierOption**

Create the EquityBarrierOption by specifying the expiry date, strike price, option type, barrier level, the number of observations per year and the notional.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiry_dt	Date	-	-
strike_price	float	-	-
option_type	EquityBarrierTypes	-	-
barrier_level	float	-	-
num_obs_per_year	int or float	-	252
notional	float	-	1.0

### value

This prices Equity Barrier option the formulae an using given the Llanos Strickland 1994 per by Clewlow, and December found at https://warwick.ac.uk/fac/soc/wbs/subjects/finance/research/wpaperseries/1994/94-54.pdf

```
value(value_dt: Date,
    stock_price: (float, np.ndarray),
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float or np.ndarray	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

### value\_mc

A Monte-Carlo based valuation of the barrier option which simulates the evolution of the stock price of at a specified number of annual observation times until expiry to examine if the barrier has been crossed and the corresponding value of the final payoff, if any. It assumes a GBM model for the stock price.

```
value_mc(t: float,
    k,
    option_type: int,
    b,
    notional,
    s: float,
    r: float,
    process_type,
    model_params,
    num_ann_obs: int = 252,
    num_paths: int = 10000,
    seed: int = 4242):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
t	float	-	-
k	-	-	-
option_type	int	-	-
b	-	-	-
notional	-	-	-
S	float	-	-
r	float	-	-
process_type	-	-	-
model_params	-	-	-
num_ann_obs	int	-	252
num_paths	int	-	10000
seed	int	-	4242

### \_\_repr\_\_

### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

## 5.4 equity\_basket\_option

## Class: EquityBasketOption

A EquityBasketOption is a contract to buy a put or a call option on an equally weighted portfolio of different stocks, each with its own price, volatility and dividend yield. An analytical and monte-carlo pricing model have been implemented for a European style option.

## **EquityBasketOption**

Define the EquityBasket option by specifying its expiry date, its strike price, whether it is a put or call, and the number of underlying stocks in the basket.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiry_dt	Date	-	-
strike_price	float	-	-
option_type	OptionTypes	-	-
num_assets	int	-	-

### validate

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
stock_prices	-	-	-
dividend_yields	-	-	-
volatilities	-	-	-
correlations	-	-	-

### value

Basket valuation using a moment matching method to approximate the effective variance of the underlying basket value. This approach is able to handle a full rank correlation structure between the individual assets.

```
value(value_dt: Date,
    stock_prices: np.ndarray,
    discount_curve: DiscountCurve,
    dividend_curves: (list),
    volatilities: np.ndarray,
    correlations: np.ndarray):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_prices	np.ndarray	-	-
discount_curve	DiscountCurve	-	-
dividend_curves	list or (list	-	-
volatilities	np.ndarray	-	-
correlations	np.ndarray	-	-

### value mc

Valuation of the EquityBasketOption using a Monte-Carlo simulation of stock prices assuming a GBM distribution. Cholesky decomposition is used to handle a full rank correlation structure between the individual assets. The num\_paths and seed are pre-set to default values but can be overwritten.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
stock_prices	np.ndarray	-	-
discount_curve	DiscountCurve	-	-
dividend_curves	list or (list	-	-
volatilities	np.ndarray	-	-
corr_matrix	np.ndarray	-	-
num_paths	int	-	10000
seed	int	-	4242

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

# $\_print$

Simple print function for backward compatibility.

\_print():

# 5.5 equity\_binomial\_tree

## Enumerated Type: EquityTreePayoffTypes

This enumerated type has the following values:

- FWD\_CONTRACT
- VANILLA\_OPTION
- DIGITAL\_OPTION
- POWER\_CONTRACT
- POWER\_OPTION
- LOG\_CONTRACT
- LOG\_OPTION

### Enumerated Type: EquityTreeExerciseTypes

This enumerated type has the following values:

- EUROPEAN
- AMERICAN

## Class: EquityBinomialTree()

class EquityBinomialTree():

## **EquityBinomialTree**

PLEASE ADD A FUNCTION DESCRIPTION

```
EquityBinomialTree():
```

The function arguments are described in the following table.

### value

#### PLEASE ADD A FUNCTION DESCRIPTION

```
value(stock_price,
    discount_curve,
    dividend_curve,
    volatility,
    num_steps,
    value_dt,
    payoff,
    expiry_dt,
    payoff_type,
    exercise_type,
    payoff_params):
```

<b>Argument Name</b>	Type	Description	Default Value
stock_price	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
volatility	-	-	-
num_steps	-	-	-
value_dt	-	-	-
payoff	-	-	-
expiry_dt	-	-	-
payoff_type	-	-	-
exercise_type	-	-	-
payoff_params	-	-	-

## \_validate\_payoff

### PLEASE ADD A FUNCTION DESCRIPTION

```
_validate_payoff(payoff_type, payoff_params):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
payoff_type	-	-	-
payoff_params	-	-	-

# \_payoff\_value

### PLEASE ADD A FUNCTION DESCRIPTION

```
_payoff_value(s, payoff_type, payoff_params):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
payoff_type	-	-	-
payoff_params	-	-	-

## \_value\_once

### PLEASE ADD A FUNCTION DESCRIPTION

```
time_to_expiry,
payoff_type,
exercise_type,
payoff_params):
```

Argument Name	Type	Description	<b>Default Value</b>
stock_price	-	-	-
r	-	-	-
q	-	-	-
volatility	-	-	-
num_steps	-	-	-
time_to_expiry	-	-	-
payoff_type	-	-	-
exercise_type	-	-	-
payoff_params	-	-	-

## 5.6 equity\_chooser\_option

## Class: EquityChooserOption(EquityOption)

A EquityChooserOption is an option which allows the holder to either enter into a call or a put option on a later expiry date, with both strikes potentially different and both expiry dates potentially different. This is known as a complex chooser. All the option details are set at trade initiation.

## **EquityChooserOption**

Create the EquityChooserOption by passing in the chooser date and then the put and call expiry dates as well as the corresponding put and call strike prices.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
choose_dt	Date	-	-
call_expiry_dt	Date	-	-
put_expiry_dt	Date	-	-
call_strike_price	float	-	-
put_strike_price	float	-	-

#### value

Value the complex chooser option using an approach by Rubinstein (1991). See also Haug page 129 for complex chooser options.

```
value(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

### value\_mc

Value the complex chooser option Monte Carlo.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-
num_paths	int	-	10000
seed	int	-	4242

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

### $\mathbf{f}$

Complex chooser option solve for critical stock price that makes the forward starting call and put options have the same price on the chooser date.

```
_f(ss, *args):
```

Argument Name	Type	Description	Default Value
SS	-	-	-
*args	-	-	-

# 5.7 equity\_cliquet\_option

## Class: EquityCliquetOption(EquityOption)

A EquityCliquetOption is a series of options which start and stop at successive times with each subsequent option resetting its strike to be ATM at the start of its life. This is also known as a reset option.

## **EquityCliquetOption**

Create the EquityCliquetOption by passing in the start date and the end date and whether it is a call or a put. Some additional data is needed in order to calculate the individual payments.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
start_dt	Date	-	-
final_expiry_dt	Date	-	-
option_type	OptionTypes	-	-
freq_type	FrequencyTypes	-	-
day_count_type	DayCountTypes	-	DayCountTypes.THIRTY_E_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

### value

Value the cliquet option as a sequence of options using the Black- Scholes model.

```
value(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model: Model):
```

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-

# $print\_payments$

PLEASE ADD A FUNCTION DESCRIPTION

```
print_payments():
```

The function arguments are described in the following table.

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

The function arguments are described in the following table.

# $\_$ print

Simple print function for backward compatibility.

\_print():

# 5.8 equity\_compound\_option

## Class: EquityCompoundOption(EquityOption)

A EquityCompoundOption is a compound option which allows the holder to either buy or sell another underlying option on a first expiry date that itself expires on a second expiry date. Both strikes are set at trade initiation.

## **EquityCompoundOption**

Create the EquityCompoundOption by passing in the first and second expiry dates as well as the corresponding strike prices and option types.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
cExpiryDate	Date	Compound Option expiry date	-
cOptionType	OptionTypes	Compound option type	-
cStrikePrice	float	Compound option strike	-
uExpiryDate	Date	Underlying option expiry date	-
uOptionType	OptionTypes	Underlying option type	-
uStrikePrice	float	Underlying option strike price	-

#### value

Value the compound option using an analytical approach if it is entirely European style. Otherwise use a Tree approach to handle the early exercise. Solution by Geske (1977), Hodges and Selby (1987) and Rubinstein (1991). See also Haug page 132.

```
value(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model,
    num_steps: int = 200):
```

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-
num_steps	int	-	200

### \_value\_tree

This function is called if the option has American features.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_price	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-
num_steps	-	-	200

# \_implied\_stock\_price

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
stock_price	-	-	-
expiry_dt1	-	-	-
expiry_dt2	-	-	-
strike_price1	-	-	-
strike_price2	-	-	-
option_type2	-	-	-
interest_rate	-	-	-
dividend_yield	-	-	-
model	-	-	-

## \_\_repr\_\_

### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

### $\mathbf{f}$

### PLEASE ADD A FUNCTION DESCRIPTION

```
_f(s0, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
s0	-	-	-
*args	-	-	-

## \_value\_once

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_value_once(s, r, q,
```

```
volatility,
t1, t2,
option_type1, option_type2,
k1, k2,
num_steps):
```

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
r	-	-	-
q	-	-	-
volatility	-	-	-
t1	-	-	-
t2	-	-	-
option_type1	-	-	-
option_type2	-	-	-
k1	-	-	-
k2	-	-	-
num_steps	-	-	-

## 5.9 equity\_digital\_option

## Enumerated Type: FinDigitalOptionTypes

This enumerated type has the following values:

- CASH\_OR\_NOTHING
- ASSET\_OR\_NOTHING

## Class: EquityDigitalOption(EquityOption)

A EquityDigitalOption is an option in which the buyer receives some payment if the stock price has crossed a barrier ONLY at expiry and zero otherwise. There are two types: cash-or-nothing and the asset-or-nothing option. We do not care whether the stock price has crossed the barrier today, we only care about the barrier at option expiry. For a continuously- monitored barrier, use the EquityOneTouchOption class.

## **EquityDigitalOption**

Create the digital option by specifying the expiry date, the barrier price and the type of option which is either a EUROPEAN\_CALL or a EUROPEAN\_PUT or an AMERICAN\_CALL or AMERICAN\_PUT. There are two types of underlying - cash or nothing and asset or nothing.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiry_dt	Date	-	-
barrier	float	-	-
call_put_type	OptionTypes	-	-
digital_type	FinDigitalOptionTypes	-	-

### value

Digital Option valuation using the Black-Scholes model assuming a barrier at expiry. Handles both cash-or-nothing and asset-or-nothing options.

```
value(value_dt: Date,
    s: (float, np.ndarray),
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
S	float or np.ndarray	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

### value\_mc

Digital Option valuation using the Black-Scholes model and Monte Carlo simulation. Product assumes a barrier only at expiry. Monte Carlo handles both a cash-or-nothing and an asset-or-nothing option.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-
num_paths	int	-	10000
seed	int	-	4242

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## \_print

Simple print function for backward compatibility.

```
_print():
```

# 5.10 equity\_fixed\_lookback\_option

## Class: EquityFixedLookbackOption(EquityOption)

This is an equity option in which the strike of the option is fixed but the value of the stock price used to determine the payoff is the maximum in the case of a call option, and a minimum in the case of a put option.

## EquityFixedLookbackOption

Create the FixedLookbackOption by specifying the expiry date, the option type and the option strike.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
option_type	OptionTypes	-	-
strike_price	float	-	-

#### value

Valuation of the Fixed Lookback option using Black-Scholes using the formulae derived by Conze and Viswanathan (1991). One of the inputs is the minimum of maximum of the stock price since the start of the option depending on whether the option is a call or a put.

```
value(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    volatility: float,
    stock_min_max: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
volatility	float	-	-
stock_min_max	float	-	-

#### value\_mc

Monte Carlo valuation of a fixed strike lookback option using a Black-Scholes model that assumes the stock follows a GBM process.

```
value_mc(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    volatility: float,
    stock_min_max: float,
    num_paths: int = 10000,
    num_steps_per_year: int = 252,
    seed: int = 4242):
```

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
volatility	float	-	-
stock_min_max	float	-	-
num_paths	int	-	10000
num_steps_per_year	int	-	252
seed	int	-	4242

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $\_print$

Simple print function for backward compatibility.

```
_print():
```

# 5.11 equity\_float\_lookback\_option

## Class: EquityFloatLookbackOption(EquityOption)

This is an equity option in which the strike of the option is not fixed but is set at expiry to equal the minimum stock price in the case of a call or the maximum stock price in the case of a put. In other words the buyer of the call gets to buy the asset at the lowest price over the period before expiry while the buyer of the put gets to sell the asset at the highest price before expiry.

## **EquityFloatLookbackOption**

Create the FloatLookbackOption by specifying the expiry date and the option type. The strike is determined internally as the maximum or minimum of the stock price depending on whether it is a put or a call option.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
option_type	OptionTypes	-	-

### value

Valuation of the Floating Lookback option using Black-Scholes using the formulae derived by Goldman, Sosin and Gatto (1979).

```
value(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    volatility: float,
    stock_min_max: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
volatility	float	-	-
stock_min_max	float	-	-

#### value\_mc

Monte Carlo valuation of a floating strike lookback option using a Black-Scholes model that assumes the stock follows a GBM process.

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
volatility	float	-	-
stock_min_max	float	-	-
num_paths	int	-	10000
num_steps_per_year	int	-	252
seed	int	-	4242

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

# 5.12 equity\_forward

## Class: EquityForward()

## **EquityForward**

Creates a EquityForward which allows the owner to buy the stock at a price agreed today. Need to specify if LONG or SHORT.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
forward_price	float	PRICE OF 1 UNIT OF FOREIGN IN DOM CCY	-
notional	float	-	-
long_short	FinLongShort	-	LONG

### value

Calculate the value of an equity forward contract from the stock price and discount and dividend discount.

```
value(value_dt,
    stock_price, # Current stock price
    discount_curve,
    dividend_curve):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_price	-	Current stock price	-
discount_curve	-	-	-
dividend_curve	-	-	-

### forward

Calculate the forward price of the equity forward contract.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_price	-	Current stock price	-
discount_curve	-	-	-
dividend_curve	-	-	-

\_\_repr\_\_

### PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

The function arguments are described in the following table.

## \_print

Simple print function for backward compatibility.

\_print():

# 5.13 equity\_index\_option

## Class: EquityIndexOption

Class for managing plain vanilla European/American calls and puts on equity indices.

## **EquityIndexOption**

Create the Equity Index option object by specifying the expiry date, the option strike, the option type and the number of options.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiry_dt	Date or list	-	-
strike_price	float or np.ndarray	-	-
option_type	OptionTypes	-	-
num_options	Optional[float]	-	1.0

### value

Equity Index Option valuation using Black model.

```
value(value_dt: Union[Date, list],
    forward_price: float,
    discount_curve: DiscountCurve,
    model: Model,
    ):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date or list	-	-
forward_price	float	-	-
discount_curve	DiscountCurve	-	-
model	Model	-	-

### delta

Calculate delta of a European/American Index option.

```
discount_curve: DiscountCurve,
model):
```

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
forward_price	float	-	-
discount_curve	DiscountCurve	-	-
model	-	-	-

### gamma

Calculate gamma of a European/American Index option.

```
gamma(value_dt: Date,
    forward_price: float,
    discount_curve: DiscountCurve,
    model: Model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
forward_price	float	-	-
discount_curve	DiscountCurve	-	-
model	Model	-	-

### vega

Calculate vega of a European/American Index option.

```
vega(value_dt: Date,
    forward_price: float,
    discount_curve: DiscountCurve,
    model: Model):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
forward_price	float	-	-
discount_curve	DiscountCurve	-	-
model	Model	-	-

### theta

Calculate theta of a European/American Index option.

```
theta(value_dt: Date,
    forward_price: float,
    discount_curve: DiscountCurve,
    model: Model):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
forward_price	float	-	-
discount_curve	DiscountCurve	-	-
model	Model	-	-

## implied\_volatility

Calculate the Black implied volatility of a European/American Index option.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
forward_price	float or list,np.ndarray	-	-
discount_curve	DiscountCurve	-	-
model	Model	-	-
price	float	-	-

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $\_print$

Simple print function for backward compatibility.

```
_print():
```

# 5.14 equity\_model\_types

Class: EquityModel

## **EquityModel**

PLEASE ADD A FUNCTION DESCRIPTION

EquityModel():

The function arguments are described in the following table.

## Class: EquityModelHeston(EquityModel)

 $class\ Equity Model Heston (Equity Model):$ 

## **EquityModelHeston**

PLEASE ADD A FUNCTION DESCRIPTION

EquityModelHeston(volatility, mean\_reversion):

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
volatility	-	-	-
mean_reversion	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

# 5.15 equity\_one\_touch\_option

## Class: EquityOneTouchOption(EquityOption)

A EquityOneTouchOption is an option in which the buyer receives one unit of cash OR stock if the stock price touches a barrier at any time before the option expiry date and zero otherwise. The choice of cash or stock is made at trade initiation. The single barrier payoff must define whether the option pays or cancels if the barrier is touched and also when the payment is made (at hit time or option expiry). All of these variants are all members of the FinTouchOptionTypes enumerated type.

## **EquityOneTouchOption**

Create the one touch option by defining its expiry date and the barrier level and a payment size if it is a cash

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
option_type	TouchOptionTypes	-	-
barrier_price	float	-	-
payment_size	float	-	1.0

#### value

Equity One-Touch Option valuation using the Black-Scholes model assuming a continuous (American) barrier from value date to expiry. Handles both cash-or-nothing and asset-or-nothing options.

```
value(value_dt: Date,
    stock_price: (float, np.ndarray),
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float or np.ndarray	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

### value\_mc

Touch Option valuation using the Black-Scholes model and Monte Carlo simulation. Accuracy is not great when compared to the analytical result as we only observe the barrier a finite number of times. The convergence is slow.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-
num_paths	int	-	10000
num_steps_per_year	int	-	252
seed	int	-	4242

### \_\_repr\_\_

### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## \_print

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

# \_barrier\_pay\_one\_at\_hit\_pv\_down

Pay \$1 if the stock crosses the barrier H from above. PV payment.

```
_barrier_pay_one_at_hit_pv_down(s, H, r, dt):
```

<b>Argument Name</b>	Type	Description	Default Value
S	-	-	-
Н	-	-	-
r	-	-	-
dt	-	-	-

# \_barrier\_pay\_one\_at\_hit\_pv\_up

Pay \$1 if the stock crosses the barrier H from below. PV payment.

```
_barrier_pay_one_at_hit_pv_up(s, H, r, dt):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
S	-	-	-
Н	-	-	-
r	-	-	-
dt	-	-	-

## \_barrier\_pay\_asset\_at\_expiry\_down\_out

Pay \$1 if the stock crosses the barrier H from above. PV payment.

```
_barrier_pay_asset_at_expiry_down_out(s, H):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
Н	-	-	-

## \_barrier\_pay\_asset\_at\_expiry\_up\_out

Pay \$1 if the stock crosses the barrier H from below. PV payment.

```
_barrier_pay_asset_at_expiry_up_out(s, H):
```

Type	Description	Default Value
-	-	-
-	-	-
	Type - -	Type Description

# 5.16 equity\_option

## Enumerated Type: EquityOptionModelTypes

This enumerated type has the following values:

- BLACKSCHOLES
- ANOTHER

## Class: EquityOption

This class is a parent class for all option classes that require any perturbatory risk.

### value

#### PLEASE ADD A FUNCTION DESCRIPTION

```
value(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_yield: float,
    model):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_yield	float	-	-
model	-	-	-

### delta

Calculation of option delta by perturbation of stock price and revaluation.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

### gamma

Calculation of option gamma by perturbation of stock price and revaluation.

```
gamma(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

### vega

Calculation of option vega by perturbing vol and revaluation.

```
vega(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

#### vanna

Calculation of option vanna by perturbing delta with respect to the stock price volatility.

```
vanna(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

### theta

Calculation of option theta by perturbing value date by one calendar date (not a business date) and then doing revaluation and calculating the difference divided by dt = 1 / gDaysInYear.

```
theta(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

## rho

Calculation of option rho by perturbing interest rate and revaluation.

```
rho(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

# 5.17 equity\_rainbow\_option

## Enumerated Type: EquityRainbowOptionTypes

This enumerated type has the following values:

- CALL\_ON\_MAXIMUM
- PUT\_ON\_MAXIMUM
- CALL\_ON\_MINIMUM
- PUT\_ON\_MINIMUM
- CALL\_ON\_NTH
- PUT\_ON\_NTH

## Class: EquityRainbowOption(EquityOption)

class EquityRainbowOption(EquityOption):

# **EquityRainbowOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Туре	Description	Default Value
expiry_dt	Date	-	-
payoff_type	EquityRainbowOptionTypes	-	-
payoff_params	List[float]	-	-
num_assets	int	-	-

### \_validate

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
stock_prices	-	-	-
dividend_curves	-	-	-
volatilities	-	-	-
betas	-	-	-

## \_validate\_payoff

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_validate_payoff(payoff_type, payoff_params, num_assets):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
payoff_type	-	-	-
payoff_params	-	-	-
num_assets	-	-	-

### value

#### PLEASE ADD A FUNCTION DESCRIPTION

```
value(value_dt: Date,
    stock_prices: np.ndarray,
    discount_curve: DiscountCurve,
    dividend_curves: (list),
    volatilities: np.ndarray,
    corr_matrix: np.ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_prices	np.ndarray	-	-
discount_curve	DiscountCurve	-	-
dividend_curves	list or (list	-	-
volatilities	np.ndarray	-	-
corr_matrix	np.ndarray	-	-

### value\_mc

#### PLEASE ADD A FUNCTION DESCRIPTION

```
value_mc(value_dt,
    stock_prices,
    discount_curve,
    dividend_curves,
    volatilities,
    corr_matrix,
    num_paths=10000,
    seed=4242):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_prices	-	-	-
discount_curve	-	-	-
dividend_curves	-	-	-
volatilities	-	-	-
corr_matrix	-	-	-
num_paths	-	-	10000
seed	-	-	4242

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

# payoff\_value

#### PLEASE ADD A FUNCTION DESCRIPTION

```
payoff_value(s, payoff_typeValue, payoff_params):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
payoff_typeValue	-	-	-
payoff_params	-	-	-

### value\_mc\_fast

```
dividend_curves,
  volatilities,
  betas,
  num_assets,
  payoff_type,
  payoff_params,
  num_paths=10000,
  seed=4242):
```

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
stock_prices	-	-	-
discount_curve	-	-	-
dividend_curves	-	-	-
volatilities	-	-	-
betas	-	-	-
num_assets	-	-	-
payoff_type	-	-	-
payoff_params	-	-	-
num_paths	-	-	10000
seed	-	-	4242

# 5.18 equity\_swap

### Class: EquitySwap

Class for managing a standard Equity vs Float leg swap. This is a contract in which an equity payment leg is exchanged for a series of floating rates payments. There is no exchange of principal. The contract is entered into at zero initial cost when spreads are zero. The contract lasts from an effective date to a specified maturity date.

The equity payments are not known fully until the end of the payment period.

The floating rate is not known fully until the end of the preceding payment period. It is set in advance and paid in arrears.

The value of the contract is the NPV of the two coupon streams. Discounting is done on a supplied discount curve which is separate from the curve from which the implied index rates are extracted.

### **EquitySwap**

Create an equity swap contract given the contract effective date, its maturity, underlying price and quantity, day count convention and return type and other details. The equity leg parameters have default values that can be overwritten if needed. The start date is contractual and is the same as the settlement date for a new swap. It is the date on which interest starts to accrue. The end of the contract is the termination date. This is not adjusted for business days. The adjusted termination date is called the maturity date. This is calculated.

```
EquitySwap(effective_dt: Date,  # Date contract starts or last Equity Reset
          term_dt_or_tenor: (Date, str), # Date contract ends
           eq_leg_type: SwapTypes,
           eq_freq_type: FrequencyTypes,
           eq_dc_type: DayCountTypes,
          strike: float, # Price at effective date
           quantity: float = 1.0, # Quantity at effective date
           eq_payment_lag: int = 0,
           eq_return_type: ReturnTypes = ReturnTypes.TOTAL_RETURN,
           rate_freq_type: FrequencyTypes = FrequencyTypes.MONTHLY,
           rate_dc_type: DayCountTypes = DayCountTypes.ACT_360,
           rate_spread: float = 0.0,
           rate_payment_lag: int = 0,
           cal_type: CalendarTypes = CalendarTypes.WEEKEND,
          bd_type: BusDayAdjustTypes = BusDayAdjustTypes.FOLLOWING,
           dg_type: DateGenRuleTypes = DateGenRuleTypes.BACKWARD,
           end_of_month: bool = False):
```

Argument Name	Type	Description	Default Value
effective_dt	Date	Date contract starts or last Equity Reset	-
term_dt_or_tenor	Date or str	Date contract ends	_
eq_leg_type	SwapTypes		-
eq_freq_type	FrequencyTypes		
eq_dc_type	DayCountTypes	-	
strike	float	Price at effective date	-
quantity	float	Quantity at effective date	1.0
eq_payment_lag	int	<u>-</u>	0
eq_return_type	ReturnTypes	-	ReturnTypes.TOTAL_RETURN
rate_freq_type	FrequencyTypes	-	FrequencyTypes.MONTHLY
rate_dc_type	DayCountTypes	-	DayCountTypes.ACT_360
rate_spread	float		0.0
rate_payment_lag	int	-	0
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
end_of_month	bool	-	False

### value

Value the Equity swap on a valuation date.

```
value(value_dt: Date,
    discount_curve: DiscountCurve,
    index_curve: DiscountCurve = None,
    dividend_curve: DiscountCurve = None,
    current_price: float = None,
    firstFixingRate=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
index_curve	DiscountCurve	-	None
dividend_curve	DiscountCurve	-	None
current_price	float	-	None
firstFixingRate	-	-	None

# $\underline{\ \ } \underline{\ \ \ } \underline{\ \ \ \ } \underline{\ \ } \underline{\$

In an equity swap, at every equity reset, the notional of the contract is updated to reflect the new underlying price. This is a helper function that takes the Equity Notional list from Equity Leg and convert it to a Notional array that fits the payment schedule defined for the rate leg.

```
_fill_rate_notional_array():
```

### PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

# 5.19 equity\_swap\_leg

### Class: EquitySwapLeg

Class for managing the equity leg of an equity swap. An equity leg is a leg with a sequence of flows calculated according to an ISDA schedule and follows the economics of a collection of equity forward contracts.

# **EquitySwapLeg**

Create the equity leg of a swap contract giving the contract start date, its maturity, underlying strike price and quantity, payment frequency, day count convention, return type, and other details

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
effective_dt	Date	Contract starts or last equity reset	-
term_dt_or_tenor	Date or str	Date contract ends	-
leg_type	SwapTypes	-	-
freq_type	FrequencyTypes	-	-
dc_type	DayCountTypes	-	-
strike	float	Price at effective date	-
quantity	float	Quantity at effective date	1.0
payment_lag	int	-	0
return_type	ReturnTypes	-	ReturnTypes.TOTAL_RETURN
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
end_of_month	bool	-	False

## $generate\_payment\_dts$

Generate the Equity leg payment dates and accrual factors. Similar to swap float leg, payment values can't be generated, as we do not have index curve, dividend curve and equity price.

```
generate_payment_dts():
```

#### value

Value the equity leg with payments from an equity price, quantity, an index curve and an [optional] dividend curve. Discounting is based on a supplied discount curve as of the valuation date supplied.

```
value(value_dt: Date,
    discount_curve: DiscountCurve,
    index_curve: DiscountCurve,
    dividend_curve: DiscountCurve = None,
    current_price: float = None):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
index_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	None
current_price	float	-	None

### print\_payments

Prints the payment dates, accrual factors, discount factors, cash amounts, their present value and their cumulative PV using the last valuation performed.

```
print_payments():
```

The function arguments are described in the following table.

## print\_valuation

Prints the valuation dates, accrual factors, discount factors, cash amounts, their present value and their cumulative PV using the last valuation performed.

```
print_valuation():
```

The function arguments are described in the following table.

```
__repr__
```

\_\_repr\_\_():

# 5.20 equity\_vanilla\_option

### Class: EquityVanillaOption()

Class for managing plain vanilla European calls and puts on equities. For American calls and puts see the EquityAmericanOption class.

# **EquityVanillaOption**

Create the Equity Vanilla option object by specifying the expiry date, the option strike, the option type and the number of options.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
expiry_dt	Date or list	-	-
strike_price	float or np.ndarray	-	-
option_type	OptionTypes or list	-	-
num_options	float	-	1.0

#### intrinsic

Equity Vanilla Option valuation using Black-Scholes model.

```
intrinsic(value_dt: (Date, list),
    stock_price: (np.ndarray, float),
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve):
```

The function arguments are described in the following table.

Type	Description	<b>Default Value</b>
Date or list	-	-
np.ndarray or float	-	-
DiscountCurve	-	-
DiscountCurve	-	-
	Date or list np.ndarray or float DiscountCurve	Date or list - np.ndarray or float - DiscountCurve -

#### value

Equity Vanilla Option valuation using Black-Scholes model.

```
value(value_dt: (Date, list),
    stock_price: (np.ndarray, float),
    discount_curve: DiscountCurve,
```

```
dividend_curve: DiscountCurve,
model: Model):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date or list	-	-
stock_price	np.ndarray or float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-

### delta

Calculate the analytical delta of a European vanilla option.

```
delta(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	-	-	-

#### gamma

Calculate the analytical gamma of a European vanilla option.

```
gamma(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model: Model):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-

#### vega

Calculate the analytical vega of a European vanilla option.

```
vega(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model: Model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-

#### theta

Calculate the analytical theta of a European vanilla option.

```
theta(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model: Model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-

#### rho

Calculate the analytical rho of a European vanilla option.

```
rho(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model: Model):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-

#### vanna

Calculate the analytical vanna of a European vanilla option.

```
vanna(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model: Model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-

# $implied\_volatility$

Calculate the Black-Scholes implied volatility of a European vanilla option.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float or list,np.ndarray	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
price	-	-	-

# value\_mc\_numpy\_only

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-
num_paths	int	-	10000
seed	int	-	4242
use_sobol	int	-	0

### value\_mc\_numba\_only

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-
num_paths	int	-	10000
seed	int	-	4242
use_sobol	int	-	0

# $value\_mc\_numba\_parallel$

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-
num_paths	int	-	10000
seed	int	-	4242
use_sobol	int	-	0

# value\_mc\_numpy\_numba

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-
num_paths	int	-	10000
seed	int	-	4242
use_sobol	int	-	0

# $value\_mc\_nonumba\_nonumpy$

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-
num_paths	int	-	10000
seed	int	-	4242
use_sobol	int	-	0

### value\_mc

Value European style call or put option using Monte Carlo. This is mainly for educational purposes. Sobol numbers can be used.

```
value_mc(value_dt: Date,
    stock_price: float,
    discount_curve: DiscountCurve,
    dividend_curve: DiscountCurve,
    model: Model,
    num_paths: int = 10000,
    seed: int = 4242,
    use_sobol: int = 0):
```

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
discount_curve	DiscountCurve	-	-
dividend_curve	DiscountCurve	-	-
model	Model	-	-
num_paths	int	-	10000
seed	int	-	4242
use_sobol	int	-	0

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

### \_**f**

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_f(v, args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
V	-	-	-
args	-	-	-

# \_fvega

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_fvega(v, *args):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
V	-	-	-
*args	-	-	-

# 5.21 equity\_variance\_swap

## Class: EquityVarianceSwap

### **EquityVarianceSwap**

Create variance swap contract.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
start_dt	Date	-	-
maturity_dt_or_tenor	Date or str	-	-
strike_variance	float	-	-
notional	float	-	ONE_MILLION
pay_strike_flag	bool	-	True

#### value

Calculate the value of the variance swap based on the realised volatility to the valuation date, the forward looking implied volatility to the maturity date using the libor discount curve.

```
value(value_dt,
    realisedVar,
    fair_strikeVar,
    libor_curve):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
realisedVar	-	-	-
fair_strikeVar	-	-	-
libor_curve	-	-	-

## $fair\_strike\_approx$

This is an approximation of the fair strike variance by Demeterfi et al. (1999) which assumes that sigma(K) = sigma(F) - b(K-F)/F where F is the forward stock price and sigma(F) is the ATM forward vol.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
fwdStockPrice	-	-	-
strikes	-	-	-
volatilities	-	-	-

### fair\_strike

Calculate the implied variance according to the volatility surface using a static replication methodology with a specially weighted portfolio of put and call options across a range of strikes using the approximate method set out by Demeterfi et al. 1999.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
stock_price	-	-	-
dividend_curve	-	-	-
volatility_curve	-	-	-
num_call_options	-	-	-
num_put_options	-	-	-
strike_spacing	-	-	-
discount_curve	-	-	-
use_forward	-	-	True

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
f(x): return (2.0/tmat)*((x-sstar)/sstar-np.log(x/sstar))
```

Argument Name	Type	Description	<b>Default Value</b>
x return (2.0/tmat)*((x-sstar)/sstar-np.log(x/sstar))	-	-	-

### realised\_variance

Calculate the realised variance according to market standard calculations which can either use log or percentage returns.

```
realised_variance(closePrices, useLogs=True):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
closePrices	-	-	-
useLogs	-	-	True

# print\_weights

Print the list of puts and calls used to replicate the static replication component of the variance swap hedge.

```
print_weights():
```

The function arguments are described in the following table.

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Simple print function for backward compatibility.

```
_print():
```

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# Chapter 6

# financepy.products.credit

This folder contains a set of credit-related assets ranging from CDS to CDS options, to CDS indices, CDS index options and then to CDS tranches. They are as follows:

- CDS is a credit default swap contract. It includes schedule generation, contract valuation and risk-management functionality.
- CDSBasket is a credit default basket such as a first-to-default basket. The class includes valuation according to the Gaussian copula.
- CDSCurve is a discount curve and survival curve constructed from discount rates and CDS spreads.
- CDSIndexOption is an option on an index of CDS such as CDX or iTraxx. A full valuation model is included.
- CDSIndexPortfolio is a portfolio of CDS contracts.
- CDSOption is an option on a single CDS. The strike is expressed in spread terms and the option is European style. It is different from an option on a CDS index option. A suitable pricing model is provided which adjusts for the risk that the reference credit defaults before the option expiry date.
- CDSTranche is a synthetic CDO tranche. This is a financial derivative which takes a loss if the total loss on the portfolio exceeds a lower threshold K1 and which is wiped out if it exceeds a higher threshold K2. The value depends on the default correlation between the assets in the portfolio of credits. This also includes a valuation model based on the Gaussian copula model.

#### **FinCDSCurve**

This is a curve that has been calibrated to fit the market term structure of CDS contracts given a recovery rate assumption and a IborSingleCurve discount curve. It also contains a IborCurve object for discounting. It has methods for fitting the curve and also for extracting survival probabilities.

### 6.1 cds

### Class: CDS

A class which manages a Credit Default Swap. It performs schedule generation and the valuation and risk management of CDS.

#### **CDS**

Create a CDS from the step-in date, maturity date and coupon

```
CDS(step_in_dt: Date, # Date protection starts
    maturity_dt_or_tenor: (Date, str), # Date or tenor
    running_coupon: float, # Annualised coupon on premium fee leg
    notional: float = ONE_MILLION,
    long_protection: bool = True,
    freq_type: FrequencyTypes = FrequencyTypes.QUARTERLY,
    dc_type: DayCountTypes = DayCountTypes.ACT_360,
    cal_type: CalendarTypes = CalendarTypes.WEEKEND,
    bd_type: BusDayAdjustTypes = BusDayAdjustTypes.FOLLOWING,
    dg_type: DateGenRuleTypes = DateGenRuleTypes.BACKWARD):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
step_in_dt	Date	Date protection starts	-
maturity_dt_or_tenor	Date or str	Date or tenor	-
running_coupon	float	Annualised coupon on premium fee leg	-
notional	float	-	ONE_MILLION
long_protection	bool	-	True
freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
dc_type	DayCountTypes	-	DayCountTypes.ACT_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWIN
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARI

## \_generate\_adjusted\_cds\_payment\_dts

Generate CDS payment dates which have been holiday adjusted.

```
_generate_adjusted_cds_payment_dts():
```

The function arguments are described in the following table.

#### \_calc\_flows

Calculate cash flow amounts on premium leg.

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```
_calc_flows():
```

The function arguments are described in the following table.

### value

Valuation of a CDS contract on a specific valuation date given an issuer curve and a contract recovery rate.

```
value(value_dt,
    issuer_curve,
    contract_recovery_rate,
    pv01_method=0,
    prot_method=0,
    num_steps_per_year=glob_num_steps_per_year):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curve	-	-	-
contract_recovery_rate	-	-	-
pv01_method	-	-	0
prot_method	-	-	0
num_steps_per_year	-	-	glob_num_steps_per_year

### credit\_dv01

Calculation of the change in the value of the CDS contract for a one basis point change in the level of the CDS curve.

```
credit_dv01(value_dt,
    issuer_curve,
    contract_recovery_rate,
    pv01_method=0,
    prot_method=0,
    num_steps_per_year=glob_num_steps_per_year):
```

Argument Name	Type	Description	Default Value
value_dt	-	-	-
issuer_curve	-	-	-
contract_recovery_rate	-	-	-
pv01_method	-	-	0
prot_method	-	-	0
num_steps_per_year	-	-	glob_num_steps_per_year

### interest\_dv01

Calculation of the interest DV01 based on a simple bump of the discount factors and reconstruction of the CDS curve.

```
interest_dv01(value_dt: Date,
    issuer_curve,
    contract_recovery_rate,
    pv01_method: int = 0,
    prot_method: int = 0,
    num_steps_per_year=glob_num_steps_per_year):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
issuer_curve	-	-	-
contract_recovery_rate	-	-	-
pv01_method	int	-	0
prot_method	int	-	0
num_steps_per_year	-	-	glob_num_steps_per_year

#### cash\_settlement\_amount

Value of the contract on the settlement date including accrued interest.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
settle_dt	-	-	-
issuer_curve	-	-	-
contract_recovery_rate	-	-	-
pv01_method	-	-	0
prot_method	-	-	0
num_steps_per_year	-	-	glob_num_steps_per_year

# $clean\_price$

Value of the CDS contract excluding accrued interest.

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```
clean_price(value_dt,
    issuer_curve,
    contract_recovery_rate,
    pv01_method=0,
    prot_method=0,
    num_steps_per_year=glob_num_steps_per_year):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curve	-	-	-
contract_recovery_rate	-	-	-
pv01_method	-	-	0
prot_method	-	-	0
num_steps_per_year	-	-	glob_num_steps_per_year

### accrued\_days

Number of days between the previous coupon and the currrent step in date.

```
accrued_days():
```

The function arguments are described in the following table.

#### accrued\_interest

Calculate the amount of accrued interest that has accrued from the previous coupon date (PCD) to the step\_in\_dt of the CDS contract.

```
accrued_interest():
```

The function arguments are described in the following table.

## protection\_leg\_pv

Calculates the protection leg PV of the CDS by calling into the fast NUMBA code that has been defined above.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curve	-	-	-
contract_recovery_rate	-	-	standard_recovery_rate
num_steps_per_year	-	-	glob_num_steps_per_year
protMethod	-	-	0

# $risky_pv01$

The risky\_pv01 is the present value of a risky one dollar paid on the premium leg of a CDS contract.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curve	-	-	-
pv01_method	-	-	0

### premium\_leg\_pv

Value of the premium leg of a CDS.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curve	-	-	-
pv01_method	-	-	0

## par\_spread

Breakeven CDS coupon that would make the value of the CDS contract equal to zero.

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
issuer_curve	-	-	-
contract_recovery_rate	-	_	standard_recovery_rate
num_steps_per_year	-	-	glob_num_steps_per_year
pv01_method	-	-	0
protMethod	-	-	0

# value\_fast\_approx

Implementation of fast valuation of the CDS contract using an accurate approximation that avoids curve building.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
flatContinuousInterestRate	-	-	-
flatCDSCurveSpread	-	-	-
curveRecovery	-	-	standard_recovery_rate
contract_recovery_rate	-	-	standard_recovery_rate

# $print\_payments$

We only print payments after the current valuation date

```
print_payments(value_dt, issuer_curve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curve	-	-	-

```
__repr__
```

print out details of the CDS contract and all of the calculated cash flows

```
__repr__():
```

### \_print

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

### \_risky\_pv01\_numba

Fast calculation of the risky PV01 of a CDS using NUMBA. The output is a numpy array of the full and clean risky PV01.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
teff	-	-	-
accrual_factorPCDToNow	-	-	-
paymentTimes	-	-	-
year_fracs	-	-	-
npIborTimes	-	-	-
npIborValues	-	-	-
npSurvTimes	-	-	-
npSurvValues	-	-	-
pv01_method	-	-	-

# \_protection\_leg\_pv\_numba

Fast calculation of the CDS protection leg PV using NUMBA to speed up the numerical integration over time.

npSurvValues,
contract\_recovery\_rate,
num\_steps\_per\_year,
protMethod):

Argument Name	Type	Description	<b>Default Value</b>
teff	-	-	-
tmat	-	-	-
npIborTimes	-	-	-
npIborValues	-	-	-
npSurvTimes	-	-	-
npSurvValues	-	-	-
contract_recovery_rate	-	-	-
num_steps_per_year	-	-	-
protMethod	-	-	-

### 6.2 cds\_basket

Class: CDSBasket

#### **CDSBasket**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
step_in_dt	Date	-	-
maturity_dt	Date	-	-
notional	float	-	ONE_MILLION
running_cpn	float	-	0.0
long_protection	bool	-	True
freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
dc_type	DayCountTypes	-	DayCountTypes.ACT_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

# value\_legs\_mc

Value the legs of the default basket using Monte Carlo. The default times are an input so this valuation is not model dependent.

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Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
n_to_default	-	-	-
default_times	-	-	-
issuer_curves	-	-	-
libor_curve	-	-	-

# value\_gaussian\_mc

Value the default basket using a Gaussian copula model. This depends on the issuer discount and correlation matrix.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
n_to_default	-	-	-
issuer_curves	-	-	-
correlation_matrix	-	-	-
libor_curve	-	-	-
num_trials	-	-	-
seed	-	-	-

### value\_student\_t\_mc

Value the default basket using the Student-T copula.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
n_to_default	-	-	-
issuer_curves	-	-	-
correlation_matrix	-	-	-
degrees_of_freedom	-	-	-
libor_curve	-	-	-
num_trials	-	-	-
seed	-	-	-

# value\_1f\_gaussian\_homo

Value default basket using 1 factor Gaussian copula and analytical approach which is only exact when all recovery rates are the same.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
n_to_default	-	-	-
issuer_curves	-	-	-
beta_vector	-	-	-
libor_curve	-	-	-
num_points	-	-	50

\_\_repr\_\_

print out details of the CDS contract and all of the calculated cash flows

```
__repr__():
```

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### 6.3 cds\_curve

### Class: CDSCurve

Generate a survival probability curve implied by the value of CDS contracts given a Ibor curve and an assumed recovery rate. The recovery rate corresponds to the seniority of the debt for these CDS. A scheme for the interpolation of the survival probabilities is also required.

### **CDSCurve**

Construct a credit curve from a sequence of maturity-ordered CDS contracts and a Ibor curve using the same recovery rate and the same interpolation method.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
cds_contracts	list	-	-
libor_curve	-	-	-
recovery_rate	-	-	-
use_cache	bool	-	False
interp_method	InterpTypes	-	InterpTypes.FLAT_FWD_RATES

#### \_validate

Ensure that contracts are in increasing maturity.

```
_validate(cds_contracts):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
cds_contracts	-	-	-

### survival\_prob

Extract the survival probability to date dt. This function supports vectorisation.

```
survival_prob(dt):
```

<b>Argument Name</b>	Type	Description	Default Value
dt	-	-	-

#### df

Extract the discount factor from the underlying Ibor curve. This function supports vectorisation.

df(dt):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	-	-	-

### build curve

Construct the CDS survival curve from a set of CDS contracts

\_build\_curve():

The function arguments are described in the following table.

### fwd

Calculate the instantaneous forward rate at the forward date dt using the numerical derivative.

fwd(dt):

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
dt	-	-	-

### fwd\_rate

Calculate the forward rate according between dates date1 and date2 according to the specified day count convention.

fwd\_rate(date1, date2, day\_count\_type):

Argument Name	Type	Description	<b>Default Value</b>
date1	-	-	-
date2	-	-	-
day_count_type	-	-	-

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#### zero\_rate

Calculate the zero rate to date dt in the chosen compounding frequency where -1 is continuous is the default.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	-	-	-
freq_type	-	-	FrequencyTypes.CONTINUOUS

### \_\_repr\_\_

Print out the details of the survival probability curve.

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

### f

Function that returns zero when the survival probability that gives a zero value of the CDS has been determined.

```
f(q, *args):
```

Ar	gument Name	Type	Description	Default Value
	q	-	-	-
	*args	-	-	-

## 6.4 cds\_index\_option

### Class: CDSIndexOption

Class to manage the pricing and risk management of an option to enter into a CDS index. Different pricing algorithms are presented.

## **CDSIndexOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
expiry_dt	Date	-	-
maturity_dt	Date	-	-
index_coupon	float	-	-
strike_coupon	float	-	-
notional	float	-	ONE_MILLION
long_protection	bool	-	True
freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
dc_type	DayCountTypes	-	DayCountTypes.ACT_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

## value\_adjusted\_black

This approach uses two adjustments to Black's option pricing model to value an option on a CDS index.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
index_curve	-	-	-
indexRecovery	-	-	-
libor_curve	-	-	-
sigma	-	-	-

#### value\_anderson

This function values a CDS index option following approach by Anderson (2006). This ensures that a noarbitrage relationship between the constituent CDS contract and the CDS index is enforced. It models the forward spread as a log-normally distributed quantity and uses the credit triangle to compute the forward RPV01.

```
value_anderson(value_dt,
    issuer_curves,
    index_recovery,
    sigma):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
issuer_curves	-	-	-
index_recovery	-	-	-
sigma	-	-	-

#### \_solve\_for\_x

Function to solve for the arbitrage free

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
sigma	-	-	-
index_coupon	-	-	-
indexRecovery	-	-	-
libor_curve	-	-	-
expH	-	-	-

## \_calc\_obj\_func

An internal function used in the Anderson valuation.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	-	-	-
value_dt	-	-	-
sigma	-	-	-
index_coupon	-	-	-
indexRecovery	-	-	-
libor_curve	-	-	-

## \_calc\_index\_payer\_option\_price

Calculates the intrinsic value of the index payer swap and the value of the index payer option which are both returned in an array.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
X	-	-	-
sigma	-	-	-
index_coupon	-	-	-
strike_value	-	-	-
libor_curve	-	-	-
indexRecovery	-	-	-

#### \_\_repr\_\_

print out details of the CDS contract and all of the calculated cash flows

\_\_repr\_\_():

The function arguments are described in the following table.

## $\_print$

Simple print function for backward compatibility.

\_print():

## 6.5 cds\_index\_portfolio

### Class: cds\_indexPortfolio

This class manages the calculations associated with an equally weighted portfolio of CDS contracts with the same maturity date.

#### cds indexPortfolio

Create Fincds\_indexPortfolio object. Note that all of the inputs have a default value which reflects the CDS market standard.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
day_count_type	DayCountTypes	-	DayCountTypes.ACT_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

## intrinsic\_rpv01

Calculation of the risky PV01 of the CDS portfolio by taking the average of the risky PV01s of each contract.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
step_in_dt	-	-	-
maturity_dt	-	-	-
issuer_curves	-	-	-

## intrinsic\_protection\_leg\_pv

Calculation of intrinsic protection leg value of the CDS portfolio by taking the average sum the protection legs of each contract.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
step_in_dt	-	-	-
maturity_dt	-	-	-
issuer_curves	-	-	-

### intrinsic\_spread

Calculation of the intrinsic spread of the CDS portfolio as the one which would make the value of the protection legs equal to the value of the premium legs if all premium legs paid the same spread.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
step_in_dt	-	-	-
maturity_dt	-	-	-
issuer_curves	-	-	-

## average\_spread

Calculates the average par CDS spread of the CDS portfolio.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
step_in_dt	-	-	-
maturity_dt	-	-	-
issuer_curves	-	-	-

### total\_spread

Calculates the total CDS spread of the CDS portfolio by summing over all of the issuers and adding the spread with no weights.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
step_in_dt	-	-	-
maturity_dt	-	-	-
issuer_curves	-	-	-

### min\_spread

Calculates the minimum par CDS spread across all of the issuers in the CDS portfolio.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
step_in_dt	-	-	-
maturity_dt	-	-	-
issuer_curves	-	-	-

### max\_spread

Calculates the maximum par CDS spread across all of the issuers in the CDS portfolio.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
step_in_dt	-	-	-
maturity_dt	-	-	-
issuer_curves	-	-	-

### spread\_adjust\_intrinsic

Adjust individual CDS discount to reprice CDS index prices. This approach uses an iterative scheme but is slow as it has to use a CDS curve bootstrap required when each trial spread adjustment is made

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
issuer_curves	-	-	-
index_cpns	-	-	-
index_upfronts	-	-	-
index_maturity_dts	-	-	-
index_recovery_rate	-	-	_
tolerance	-	-	1e-6

## hazard\_rate\_adjust\_intrinsic

Adjust individual CDS discount to reprice CDS index prices. This approach adjusts the hazard rates and so avoids the slowish CDS curve bootstrap required when a spread adjustment is made.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curves	-	-	-
index_cpns	-	-	-
index_up_fronts	-	-	-
index_maturity_dts	-	-	-
index_recovery_rate	-	-	-
tolerance	-	-	1e-6
max_iterations	-	-	200

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## $\_$ print

Simple print function for backward compatibility.

\_print():

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## 6.6 cds\_option

### Class: CDSOption

Class to manage the pricing and risk-management of an option on a single-name CDS. This is a contract in which the option buyer pays for an option to either buy or sell protection on the underlying CDS at a fixed spread agreed today and to be exercised in the future on a specified expiry date. The option may or may not cancel if there is a credit event before option expiry. This needs to be specified.

### **CDSOption**

Create a FinCDSOption object with the option expiry date, the maturity date of the underlying CDS, the option strike coupon, notional, whether the option knocks out or not in the event of a credit event before expiry and the payment details of the underlying CDS.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiry_dt	Date	-	-
maturity_dt	Date	-	-
strike_coupon	float	-	-
notional	float	-	ONE_MILLION
long_protection	bool	-	True
knockout_flag	bool	-	True
freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
dc_type	DayCountTypes	-	DayCountTypes.ACT_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

#### value

Value the CDS option using Black's model with an adjustment for any Front End Protection. TODO - Should the CDS be created in the init method?

```
value(value_dt,
    issuer_curve,
```

volatility):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
issuer_curve	-	-	-
volatility	-	-	-

## $implied\_volatility$

Calculate the implied CDS option volatility from a price.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curve	-	-	-
option_value	-	-	-

### fvol

Root searching function in the calculation of the CDS implied volatility.

```
fvol(volatility, *args):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
volatility	-	-	-
*args	-	-	-

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## 6.7 cds\_tranche

### Enumerated Type: FinLossDistributionBuilder

This enumerated type has the following values:

- RECURSION
- ADJUSTED\_BINOMIAL
- GAUSSIAN
- LHP

#### Class: CDSTranche

class CDSTranche:

### **CDSTranche**

PLEASE ADD A FUNCTION DESCRIPTION

Type	Description	Default Value
Date	-	-
Date	-	-
float	-	-
float	-	-
float	-	ONE_MILLION
float	-	0.0
bool	-	True
FrequencyTypes	-	FrequencyTypes.QUARTERLY
DayCountTypes	-	DayCountTypes.ACT_360
CalendarTypes	-	CalendarTypes.WEEKEND
BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
	Date Date Date float float float float bool FrequencyTypes DayCountTypes CalendarTypes BusDayAdjustTypes	Date - Date - In the control of the

## value\_bc

#### PLEASE ADD A FUNCTION DESCRIPTION

```
value_bc(value_dt,
    issuer_curves,
    upfront,
    running_coupon,
    corr1,
    corr2,
    num_points=50,
    model=FinLossDistributionBuilder.RECURSION):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
issuer_curves	-	-	-
upfront	-	-	-
running_coupon	-	-	-
corr1	-	-	-
corr2	-	-	-
num_points	-	-	50
model	-	-	RECURSION

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6.8 \_\_init\_\_

# **Chapter 7**

# financepy.products.bonds

This folder contains a suite of bond-related functionality across a set of files and classes. They are as follows:

- Bond is a basic fixed coupon bond with all of the associated duration and convexity measures. It also includes some common spread measures such as the asset swap spread and the option adjusted spread.
- BondZero is a zero coupon bond. This is a bond issued at a deep discount that matures at par. Accrued interest is calculated by interpolating the price growth.
- BondAnnuity is a stream of cash flows that is generated and can be priced.
- BondCallable is a bond that has embedded call and put options. A number of rate models pricing functions have been included to allow such bonds to be priced and risk-managed.
- BondConvertible enables the pricing and risk-management of convertible bonds. The model is a binomial tree implementation of Black-Scholes which allows for discrete dividends, embedded puts and calls, and a delayed start of the conversion option.
- BondFRN enables the pricing and risk-management of a bond with floating rate coupons. Discount margin calculations are provided.
- BondFuture is a bond future that has functionality around determination of the conversion factor and calculation of the invoice price and determination of the cheapest to deliver.
- BondMarket is a database of country-specific bond market conventions that can be referenced. These include settlement days and accrued interest conventions.
- BondMortgage generates the periodic cash flows for an interest-only and a repayment mortgage.
- BondOption is a bond option class that includes a number of valuation models for pricing both European and American style bond options. Models for European options include a Lognormal Price, Hull-White (HW) and Black-Karasinski (BK). The HW valuation is fast as it uses Jamshidians decomposition trick. American options can also be priced using a HW and BK trinomial tree. The details are abstracted away making it easy to use.
- BondPortfolio is a portfolio of bonds.
- Yield Curve is a class to handle bond yield curves. It uses a variety of shapes to best-fit a set of bond yields.
- Zero curve is a class to perform an exact fit to a set of provided bonds using a piece-wise flat zero rate.

#### **Conventions**

- All interest rates are expressed as a fraction of 1. So 3
- All notionals of bond positions are given in terms of a notional amount.
- All bond prices are based on a notional of 100.0.
- The face of a derivatives position is the size of the underlying position.

#### **Bond Curves**

These modules create a family of curve types related to the term structures of interest rates. These are best fit yield curves fitting to bond prices which are used for interpolation. A range of curve shapes from polynomials to B-Splines is available. This module describes a curve that is fitted to bond yields calculated from bond market prices supplied by the user. The curve is not guaranteed to fit all of the bond prices exactly and a least squares approach is used. A number of fitting forms are provided which consist of

- Polynomial
- Nelson-Siegel
- Nelson-Siegel-Svensson
- Cubic B-Splines

This fitted curve cannot be used for pricing as yields assume a flat term structure. It can be used for fitting and interpolating yields off a nicely constructed yield curve interpolation curve.

#### FinCurveFitMethod

This module sets out a range of curve forms that can be fitted to the bond yields. These includes a number of parametric curves that can be used to fit yield curves. These include:

- · Polynomials of any degree
- Nelson-Siegel functional form.
- Nelson-Siegel-Svensson functional form.
- B-Splines

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#### **7.1** bond

### Enumerated Type: YTMCalcType

This enumerated type has the following values:

- ZERO
- UK\_DMO
- US\_STREET
- US\_TREASURY
- CFETS

#### Class: Bond

Class for fixed coupon bonds and performing related analytics. These are bullet bonds which means they have regular coupon payments of a known size that are paid on known dates plus a payment of par at maturity.

#### **Bond**

Create Bond object by providing the issue date, maturity Date, coupon frequency, annualised coupon, the accrual convention type, face amount and the number of ex-dividend days. A calendar type is used to determine holidays from which coupon dates might be shifted.

```
Bond(issue_dt: Date,
    maturity_dt: Date,
    coupon: float, # Annualised bond coupon
    freq_type: FrequencyTypes,
    dc_type: DayCountTypes,
    ex_div_days: int = 0,
    cal_type: CalendarTypes = CalendarTypes.WEEKEND,
    bd_type=BusDayAdjustTypes.FOLLOWING,
    dg_type=DateGenRuleTypes.BACKWARD):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
issue_dt	Date	-	-
maturity_dt	Date	-	-
coupon	float	Annualised bond coupon	-
freq_type	FrequencyTypes	-	-
dc_type	DayCountTypes	-	-
ex_div_days	int	-	0
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	-	-	BusDayAdjustTypes.FOLLOWING
dg_type	-	-	DateGenRuleTypes.BACKWARD

### \_calculate\_cpn\_dts

Determine the bond coupon dates. Note that for analytical calculations these are not usually adjusted and so may fall on a weekend or holiday.

```
_calculate_cpn_dts():
```

The function arguments are described in the following table.

### \_calculate\_payment\_dts

For the actual payment dates, they are adjusted and so we then use the calendar payment dates. Although payments are calculated as though coupon periods are the same length, payments that fall on a Saturday or Sunday can only be made on the next business day

```
_calculate_payment_dts():
```

The function arguments are described in the following table.

#### calculate flows

Determine the bond cash flow payment amounts without principal. There is no adjustment based on the adjusted payment dates.

```
_calculate_flows():
```

The function arguments are described in the following table.

## dirty\_price\_from\_ytm

Calculate the dirty price of bond from its yield to maturity. This function is vectorised with respect to the yield input. It implements a number of standard conventions for calculating the YTM.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

## principal

Calculate the principal value of the bond based on the face amount from its discount margin and making assumptions about the future Ibor rates.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
ytm	float	-	-
face	float or (float	-	-
convention	YTMCalcType	-	-

#### dollar\_duration

Calculate the risk or dP/dy of the bond by bumping. This is also known as the DV01 in Bloomberg.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	_	YTMCalcType.UK_DMO

## macauley\_duration

Calculate the Macauley duration of the bond on a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

#### modified\_duration

Calculate the modified duration of the bond on a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

### key\_rate\_durations

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
bond	-	-	-
settle_dt	Date	-	-
ytm	float	-	-
key_rate_tenors	list	-	None
shift	float	-	None
rates	list	-	None

## convexity\_from\_ytm

Calculate the bond convexity from the yield to maturity. This function is vectorised with respect to the yield input.

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Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

### clean\_price\_from\_ytm

Calculate the bond clean price from the yield to maturity. This function is vectorised with respect to the yield input.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

### clean\_price\_from\_discount\_curve

Calculate the clean bond value using some discount curve to present-value the bond's cash flows back to the curve anchor date and not to the settlement date.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-

## $dirty\_price\_from\_discount\_curve$

Calculate the bond price using a provided discount curve to PV the bond's cash flows to the settlement date. As such it is effectively a forward bond price if the settlement date is after the valuation date.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-

### current\_yield

Calculate the current yield of the bond which is the coupon divided by the clean price (not the full price)

```
current_yield(clean_price):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
clean_price	-	-	-

### yield\_to\_maturity

Calculate the bond's yield to maturity by solving the price yield relationship using a one-dimensional root solver.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
clean_price	float	-	-
convention	YTMCalcType	-	YTMCalcType.US_TREASURY

## \_calc\_pcd\_ncd

PLEASE ADD A FUNCTION DESCRIPTION

```
_calc_pcd_ncd(settle_dt: Date):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-

#### accrued\_interest

Calculate the amount of coupon that has accrued between the previous coupon date and the settlement date. Note that for some day count schemes (such as 30E/360) this is not actually the number of days between the previous coupon payment date and settlement date. If the bond trades with ex-coupon dates then you need to use the number of days before the coupon date the ex-coupon date is. You can specify the calendar to be used in the bond constructor - NONE means only calendar days, WEEKEND is only weekends or you can specify a country calendar for business days.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float	-	100.0

### asset\_swap\_spread

Calculate the par asset swap spread of the bond. The discount curve is a Ibor curve that is passed in. This function is vectorised with respect to the clean price.

```
asset_swap_spread(settle_dt: Date,
    clean_price: float,
    discount_curve: DiscountCurve,
    swapFloatDayCountConventionType=DayCountTypes.ACT_360,
    swapFloatFrequencyType=FrequencyTypes.SEMI_ANNUAL,
    swapFloatCalendarType=CalendarTypes.WEEKEND,
    swapFloatBusDayAdjustRuleType=BusDayAdjustTypes.FOLLOWING,
    swapFloatDateGenRuleType=DateGenRuleTypes.BACKWARD):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
clean_price	float	-	-
discount_curve	DiscountCurve	-	-
swapFloatDayCountConventionType	-	-	DayCountTypes.ACT_360
swapFloatFrequencyType	-	-	FrequencyTypes.SEMI_ANNUAL
swapFloatCalendarType	-	-	CalendarTypes.WEEKEND
swapFloatBusDayAdjustRuleType	-	-	BusDayAdjustTypes.FOLLOWING
swapFloatDateGenRuleType	-	-	DateGenRuleTypes.BACKWARD

## dirty\_price\_from\_oas

Calculate the full price of the bond from its OAS given the bond settlement date, a discount curve and the oas as a number.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
oas	float	-	-

### option\_adjusted\_spread

Return OAS for bullet bond given settlement date, clean bond price and the discount relative to which the spread is to be computed.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
clean_price	float	-	-
discount_curve	DiscountCurve	-	-

## bond\_payments

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
bond_payments(settle_dt: Date, face: (float)):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float or (float	-	-

## print\_payments

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float or (float	-	100.0

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### dirty\_price\_from\_survival\_curve

Calculate discounted present value of flows assuming default model. The survival curve treats the coupons as zero recovery payments while the recovery fraction of the par amount is paid at default. For the defaulting principal we discretize the time steps using the coupon payment times. A finer discretization may handle the time value with more accuracy. I reduce any error by averaging period start and period end payment present values.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
survival_curve	DiscountCurve	-	-
recovery_rate	float	-	-

### clean\_price\_from\_survival\_curve

Calculate clean price value of flows assuming default model. The survival curve treats the coupons as zero recovery payments while the recovery fraction of the par amount is paid at default.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
survival_curve	DiscountCurve	-	-
recovery_rate	float	-	-

#### calc\_ror

Calculate the rate of total return(capital return and interest) given a BUY YTM and a SELL YTM of this bond. This function computes the full prices at buying and selling, plus the coupon payments during the period. It returns a tuple which includes a simple rate of return, a compounded IRR and the PnL.

```
convention: YTMCalcType = YTMCalcType.US_STREET):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
begin_dt	Date	-	-
end_dt	Date	-	-
begin_ytm	float	-	-
end_ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.US_STREET

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### $_{\rm print}$

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

The function arguments are described in the following table.

### $_{\mathbf{f}}$

Function used to do root search in price to yield calculation.

```
_f(ytm, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
ytm	-	-	-
*args	-	-	-

#### \_**g**

Function used to do root search in price to OAS calculation.

```
_g(oas, *args):
```

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Argument Name	Type	Description	Default Value
oas	-	-	-
*args	-	-	-

## 7.2 bond\_annuity

### Class: BondAnnuity

An annuity is a vector of dates and flows generated according to ISDA standard rules which starts on the next date after the start date (effective date) and runs up to an end date with no principal repayment. Dates are then adjusted according to a specified calendar.

### **BondAnnuity**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
maturity_dt	Date	-	-
cpn	float	-	-
freq_type	FrequencyTypes	-	-
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
dc_type	DayCountTypes	-	DayCountTypes.ACT_360

## clean\_price\_from\_discount\_curve

Calculate the bond price using some discount curve to present-value the bond's cash flows.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-

## dirty\_price\_from\_discount\_curve

Calculate the bond price using some discount curve to present-value the bond's cash flows.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-

## $calculate\_payments$

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float or (float	-	-

#### accrued\_interest

Calculate the amount of coupon that has accrued between the previous coupon date and the settlement date.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
face	float or (float	-	-

### print\_payments

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float or (float	-	-

### \_\_repr\_\_

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

The function arguments are described in the following table.

## $_{\rm print}$

Simple print function for backward compatibility.

\_print():

7.3. BOND\_CALLABLE 243

## 7.3 bond\_callable

## Enumerated Type: BondModelTypes

This enumerated type has the following values:

- BLACK
- HO\_LEE
- HULL\_WHITE
- BLACK\_KARASINSKI

### Enumerated Type: BondOptionTypes

This enumerated type has the following values:

- EUROPEAN\_CALL
- EUROPEAN\_PUT
- AMERICAN\_CALL
- AMERICAN\_PUT

### Class: BondEmbeddedOption

### **BondEmbeddedOption**

Create a BondEmbeddedOption object with a maturity date, coupon and all of the bond inputs.

Argument Name	Type	Description	<b>Default Value</b>
issue_dt	Date	-	-
maturity_dt	Date	Date	-
coupon	float	Annualised coupon - $0.03 = 3.00\%$	-
freq_type	FrequencyTypes	-	-
dc_type	DayCountTypes	-	-
call_dts	List[Date]	-	-
call_prices	List[float]	-	-
put_dts	List[Date]	-	-
put_prices	List[float]	-	-

### value

Value the bond that settles on the specified date that can have both embedded call and put options. This is done using the specified model and a discount curve.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
model	-	-	-

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### $_{\rm print}$

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_print():
```

#### 7.4 bond\_convertible

#### Class: BondConvertible

Class for convertible bonds. These bonds embed rights to call and put the bond in return for equity. Until then they are bullet bonds which means they have regular coupon payments of a known size that are paid on known dates plus a payment of par at maturity. As the options are price based, the decision to convert to equity depends on the stock price, the credit quality of the issuer and the level of interest rates.

#### **BondConvertible**

Create BondConvertible object by providing the bond Maturity date, coupon, frequency type, accrual convention type and then all of the details regarding the conversion option including the list of the call and put dates and the corresponding list of call and put prices.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
maturity_dt	Date	bond maturity date	-
coupon	float	annual coupon	-
freq_type	FrequencyTypes	coupon frequency type	-
start_convert_dt	Date	conversion starts on this date	-
conversion_ratio	float	num shares per face of notional	-
call_dts	List[Date]	list of call dates	-
call_prices	List[float]	list of call prices	-
put_dts	List[Date]	list of put dates	-
put_prices	List[float]	list of put prices	-
dc_type	DayCountTypes	day count type for accrued	<del>-</del>
cal_type	CalendarTypes	<del>-</del>	CalendarTypes.WEEKEND

### \_calculate\_cpn\_dts

Determine the convertible bond cash flow payment dates.

```
_calculate_cpn_dts(settle_dt: Date):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-

#### value

A binomial tree valuation model for a convertible bond that captures the embedded equity option due to the existence of a conversion option which can be invoked after a specific date. The model allows the user to enter a schedule of dividend payment dates but the size of the payments must be in yield terms i.e. a known percentage of currently unknown future stock price is paid. Not a fixed amount. A fixed yield. Following this payment the stock is assumed to drop by the size of the dividend payment. The model also captures the stock dependent credit risk of the cash flows in which the bond price can default at any time with a hazard rate implied by the credit spread and an associated recovery rate. This is the model proposed by Hull (OFODS 6th edition, page 522). The model captures both the issuer's call schedule which is assumed to apply on a list of dates provided by the user, along with a call price. It also captures the embedded owner's put schedule of prices.

```
value(settle_dt: Date,
    stock_price: float,
    stock_volatility: float,
    dividend_dts: List[Date],
    dividend_yields: List[float],
    discount_curve: DiscountCurve,
    credit_spread: float,
    recovery_rate: float = 0.40,
    num_steps_per_year: int = 100):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
stock_price	float	-	-
stock_volatility	float	-	-
dividend_dts	List[Date]	-	-
dividend_yields	List[float]	-	-
discount_curve	DiscountCurve	-	-
credit_spread	float	-	-
recovery_rate	float	-	0.40
num_steps_per_year	int	-	100

### accrued\_days

Calculate number days from previous coupon date to settlement.

```
accrued_days(settle_dt: Date):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-

#### accrued\_interest

Calculate the amount of coupon that has accrued between the previous coupon date and the settlement date.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
face	float or (float	-	-

### current\_yield

Calculate the current yield of the bond which is the coupon divided by the clean price (not the full price)

```
current_yield(clean_price: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
clean_price	float	-	-

#### \_\_repr\_\_

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
__repr__():
```

The function arguments are described in the following table.

## \_print

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

### \_value\_convertible

PLEASE ADD A FUNCTION DESCRIPTION

```
_value_convertible(tmat,
                  face_amount,
                   cpn_times,
                   cpn_flows,
                   call_times,
                  call_prices,
                  put_times,
                  put_prices,
                  conv_ratio,
                   start_convert_time,
                   # Market inputs
                   stock_price,
                   df_times,
                   df_values,
                   dividend_times,
                   dividend_yields,
                   stock_volatility,
                   credit_spread,
                   recovery_rate,
                   # Tree details
                   num_steps_per_year):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
tmat	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
call_times	-	-	-
call_prices	-	-	-
put_times	-	-	-
put_prices	-	-	-
conv_ratio	-	-	-
start_convert_time	-	-	-
stock_price	-	-	-
df_times	-	-	-
df_values	-	-	-
dividend_times	-	-	-
dividend_yields	-	-	-
stock_volatility	-	-	-
credit_spread	-	-	-
recovery_rate	-	-	-
num_steps_per_year	-	-	-

# print\_tree

PLEASE ADD A FUNCTION DESCRIPTION

print\_tree(array):

<b>Argument Name</b>	Type	Description	Default Value
array	-	-	-

### 7.5 bond frn

#### Class: BondFRN

Class for managing floating rate notes that pay a floating index plus a quoted margin.

#### **BondFRN**

Create FinFloatingRateNote object given its maturity date, its quoted margin, coupon frequency, DAY COUNT TYPE. Face is the size of the position and par is the notional on which price is quoted.

```
BondFRN(issue_dt: Date,
    maturity_dt: Date,
    quoted_margin: float, # Fixed spread paid on top of index
    freq_type: FrequencyTypes,
    dc_type: DayCountTypes,
    cal_type: CalendarTypes = CalendarTypes.WEEKEND):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
issue_dt	Date	-	-
maturity_dt	Date	-	-
quoted_margin	float	Fixed spread paid on top of index	-
freq_type	FrequencyTypes	-	-
dc_type	DayCountTypes	-	-
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND

### \_calculate\_cpn\_dts

Determine the bond cashflow payment dates.

```
_calculate_cpn_dts():
```

The function arguments are described in the following table.

# dirty\_price\_from\_dm

Calculate the full price of the bond from its discount margin (DM) using standard model based on assumptions about future Ibor rates. The next Ibor payment which has reset is entered, so to is the current Ibor rate from settlement to the next coupon date (NCD). Finally there is the level of subsequent future Ibor payments and the discount margin.

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The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
next_cpn	float	The total reset coupon on NCD	-
current_ibor	float	Ibor discount to NCD	-
future_ibor	float	Future constant Ibor rates	-
dm	float	Discount margin	-

### principal

Calculate the clean trade price of the bond based on the face amount from its discount margin and making assumptions about the future Ibor rates.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
dm	float	-	-
face	float	-	100.0

### dollar\_duration

Calculate the risk or dP/dy of the bond by bumping. This is also known as the DV01 in Bloomberg.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
dm	float	-	-

#### dollar\_credit\_duration

Calculate the risk or dP/dy of the bond by bumping.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
dm	float	-	-

### macauley\_duration

Calculate the Macauley duration of the FRN on a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
dm	float	-	-

#### modified\_duration

Calculate the modified duration of the bond on a settlement date using standard model based on assumptions about future Ibor rates. The next Ibor payment which has reset is entered, so to is the current Ibor rate from settlement to the next coupon date (NCD). Finally there is the level of subsequent future Ibor payments and the discount margin.

7.5. BOND\_FRN 253

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
dm	float	-	-

### modified\_credit\_duration

Calculate the modified duration of the bond on a settlement date using standard model based on assumptions about future Ibor rates. The next Ibor payment which has reset is entered, so to is the current Ibor rate from settlement to the next coupon date (NCD). Finally there is the level of subsequent future Ibor payments and the discount margin.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
dm	float	-	-

### convexity\_from\_dm

Calculate the bond convexity from the discount margin (DM) using a standard model based on assumptions about future Ibor rates. The next Ibor payment which has reset is entered, so to is the current Ibor rate from settlement to the next coupon date (NCD). Finally there is the level of subsequent future Ibor payments and the discount margin.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
dm	float	-	-

### clean\_price\_from\_dm

Calculate the bond clean price from the discount margin using standard model based on assumptions about future Ibor rates. The next Ibor payment which has reset is entered, so to is the current Ibor rate from settlement to the next coupon date (NCD). Finally there is the level of subsequent future Ibor payments and the discount margin.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
dm	float	-	-

## discount\_margin

Calculate the bond's yield to maturity by solving the price yield relationship using a one-dimensional root solver.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
next_cpn	float	-	-
current_ibor	float	-	-
future_ibor	float	-	-
clean_price	float	-	-

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#### accrued\_interest

Calculate the amount of coupon that has accrued between the previous coupon date and the settlement date. *Ex-dividend dates are not handled. Contact me if you need this functionality.* 

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
next_cpn	float	-	-
face	float or (float	-	-

### print\_payments

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
print_payments(settle_dt: Date):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-

#### \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

#### $_{\mathbf{f}}$

Function used to do solve root search in DM calculation

\_f(dm, \*args):

Argument Name	Type	Description	Default Value
dm	-	-	-
*args	-	-	-

7.6. BOND\_FUTURE 257

## 7.6 bond\_future

#### Class: BondFuture

Class for managing futures contracts on government bonds that follows CME conventions and related analytics.

#### **BondFuture**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
ticker_name	str	-	-
first_delivery_dt	Date	-	-
last_delivery_dt	Date	-	-
contract_size	int	-	-
cpn	float	-	-

#### conversion\_factor

Determine the conversion factor for a specific bond using CME convention. To do this we need to know the contract standard coupon and must round the bond maturity (starting its life on the first delivery date) to the nearest 3 month multiple and then calculate the bond clean price.

```
conversion_factor(bond: Bond):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
bond	Bond	-	-

## principal\_invoice\_price

The principal invoice price as defined by the CME.

Argument Name	Type	Description	<b>Default Value</b>
bond	Bond	-	-
futures_price	float	-	-

#### total\_invoice\_amount

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
bond	Bond	-	-
futures_price	float	-	-

### cheapest\_to\_deliver

Determination of CTD as deliverable bond with lowest cost to buy versus what is received when the bond is delivered.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
bonds	list	-	-
bond_clean_prices	list	-	-
futures_price	float	-	-

### delivery\_gain\_loss

Determination of what is received when the bond is delivered.

Argument Name	Type	Description	Default Value
bond	Bond	-	-
bond_clean_price	float	-	-
futures_price	float	-	-

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## \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_\_():

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

\_print():

### 7.7 bond\_market

### Enumerated Type: BondMarkets

This enumerated type has the following values:

- AUSTRIA
- BELGIUM
- CYPRUS
- ESTONIA
- FINLAND
- FRANCE
- GERMANY
- GREECE
- IRELAND
- ITALY
- LATVIA
- LITHUANIA
- LUXEMBOURG
- MALTA
- NETHERLANDS
- PORTUGAL
- SLOVAKIA
- SLOVENIA
- SPAIN
- ESM
- EFSF
- BULGARIA
- CROATIA
- CZECH\_REPUBLIC
- DENMARK
- HUNGARY
- POLAND
- ROMANIA
- SWEDEN
- JAPAN
- SWITZERLAND
- UNITED\_KINGDOM
- UNITED\_STATES
- AUSTRALIA
- NEW\_ZEALAND
- NORWAY
- SOUTH\_AFRICA

### get\_bond\_market\_conventions

Returns the day count convention for accrued interest, the frequency and the number of days from trade date to settlement date. This is for Treasury markets. And for secondary bond markets.

7.7. BOND\_MARKET 261

get\_bond\_market\_conventions(country):

<b>Argument Name</b>	Type	Description	Default Value
country	-	-	-

# 7.8 bond\_mortgage

### Enumerated Type: BondMortgageTypes

This enumerated type has the following values:

- REPAYMENT
- INTEREST\_ONLY

### Class: BondMortgage

A mortgage is a vector of dates and flows generated in order to repay a fixed amount given a known interest rate. Payments are all the same amount but with a varying mixture of interest and repayment of principal.

## **BondMortgage**

Create the mortgage using start and end dates and principal.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
start_dt	Date	-	-
end_dt	Date	-	-
principal	float	-	-
freq_type	FrequencyTypes	-	FrequencyTypes.MONTHLY
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
dc_type	DayCountTypes	-	DayCountTypes.ACT_360

### repayment\_amount

Determine monthly repayment amount based on current zero rate.

```
repayment_amount(zero_rate: float):
```

Argument Name	Type	Description	<b>Default Value</b>
zero_rate	float	-	-

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### generate\_flows

Generate the bond flow amounts.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
zero_rate	float	-	-
mortgage_type	BondMortgageTypes	-	-

## print\_leg

PLEASE ADD A FUNCTION DESCRIPTION

```
print_leg():
```

The function arguments are described in the following table.

```
__repr__
```

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $\_$ print

Simple print function for backward compatibility.

```
_print():
```

# 7.9 bond\_option

### Enumerated Type: BondModelTypes

This enumerated type has the following values:

- BLACK
- HO\_LEE
- HULL\_WHITE
- BLACK\_KARASINSKI

### Class: BondOption()

Class for options on fixed coupon bonds. These are options to either buy or sell a bond on or before a specific future expiry date at a strike price that is set on trade date. A European option only allows the bond to be exercised into on a specific expiry date. An American option allows the option holder to exercise early, potentially allowing earlier coupons to be received.

### **BondOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
bond	Bond	-	-
expiry_dt	Date	_	-
strike_price	float	-	-
option_type	OptionTypes	-	-

#### value

Value a bond option (option on a bond) using a specified model which include the Hull-White, Black-Karasinski and Black-Derman-Toy model which are all implemented as short rate tree models.

```
value(value_dt: Date,
    discount_curve: DiscountCurve,
    model):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
model	-	-	-

7.9. BOND\_OPTION 265

## \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_\_():

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

\_print():

# 7.10 bond\_portfolio

Class: BondPortfolio

#### **BondPortfolio**

XXX

```
BondPortfolio(bonds: (list),
bondWeights: (list, np.ndarray)):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
bonds	list or (list	-	-
bondWeights	list or np.ndarray	-	-

#### \_calculate\_flows

Determine the bond cashflow payment amounts without principal

```
_calculate_flows():
```

The function arguments are described in the following table.

#### dollar\_duration

Calculate the risk or dP/dy of the bond by bumping. This is also known as the DV01 in Bloomberg.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

### macauley\_duration

Calculate the Macauley duration of the bond on a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

#### modified\_duration

Calculate the modified duration of the bondon a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

### convexity\_from\_ytm

Calculate the bond convexity from the yield to maturity. This function is vectorised with respect to the yield input.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

# $clean\_price\_from\_ytm$

Calculate the bond clean price from the yield to maturity. This function is vectorised with respect to the yield input.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.UK_DMO

### clean\_price\_from\_discount\_curve

Calculate the clean bond value using some discount curve to present-value the bond's cash flows back to the curve anchor date and not to the settlement date.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-

### dirty\_price\_from\_discount\_curve

Calculate the bond price using a provided discount curve to PV the bond's cash flows to the settlement date. As such it is effectively a forward bond price if the settlement date is after the valuation date.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-

### current\_yield

Calculate the current yield of the bond which is the coupon divided by the clean price (not the full price)

```
current_yield(clean_price):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
clean_price	-	-	-

# $yield\_to\_maturity$

Calculate the bond's yield to maturity by solving the price yield relationship using a one-dimensional root solver.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
clean_price	float	-	-
convention	YTMCalcType	-	YTMCalcType.US_TREASURY

#### accrued\_interest

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
num_ex_dividend_days	int	-	0
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND

## print\_payments

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float or (float	-	-

# $dirty\_price\_from\_survival\_curve$

Calculate discounted present value of flows assuming default model. The survival curve treats the coupons as zero recovery payments while the recovery fraction of the par amount is paid at default. For the defaulting principal we discretise the time steps using the coupon payment times. A finer discretisation may handle the time value with more accuracy. I reduce any error by averaging period start and period end payment present values.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
survival_curve	DiscountCurve	-	-
recovery_rate	float	-	-

### clean\_price\_from\_survival\_curve

Calculate clean price value of flows assuming default model. The survival curve treats the coupons as zero recovery payments while the recovery fraction of the par amount is paid at default.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
survival_curve	DiscountCurve	-	-
recovery_rate	float	-	-

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

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### 7.11 bond zero

#### Class: BondZero

A zero coupon bond is a bond which doesnt pay any periodic payments. Instead, it is issued at a discount. The entire face value of the bond is paid out at maturity. It is issued as a deep discount bond.

There is a special convention for accrued interest in which

```
Accrued_interest = (par - issue price) * D where D = (settle_dt - issue_dt)/(maturity_dt - issue_dt).
```

#### **BondZero**

Create BondZero object by providing the issue date, maturity Date, face amount and issue price.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
issue_dt	Date	-	-
maturity_dt	Date	-	-
issue_price	float	Issue price usually discounted	-

### dirty\_price\_from\_ytm

Calculate the full price of bond from its yield to maturity. This function is vectorised with respect to the yield input. It implements a number of standard conventions for calculating the YTM.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

### principal

Calculate the principal value of the bond based on the face amount from its discount margin and making assumptions about the future Ibor rates.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
face	float or (float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

#### dollar\_duration

Calculate the risk or dP/dy of the bond by bumping. This is also known as the DV01 in Bloomberg.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

## macauley\_duration

Calculate the Macauley duration of the bond on a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

#### modified\_duration

Calculate the modified duration of the bondon a settlement date given its yield to maturity.

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

## $convexity\_from\_ytm$

Calculate the bond convexity from the yield to maturity. This function is vectorised with respect to the yield input.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

# $clean\_price\_from\_ytm$

Calculate the bond clean price from the yield to maturity. This function is vectorised with respect to the yield input.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

# $clean\_price\_from\_discount\_curve$

Calculate the clean bond value using some discount curve to present-value the bond's cash flows back to the curve anchor date and not to the settlement date.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-

## dirty\_price\_from\_discount\_curve

Calculate the bond price using a provided discount curve to PV the bond's cash flows to the settlement date. As such it is effectively a forward bond price if the settlement date is after the valuation date.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-

# current\_yield

Calculate the current yield of the bond which is the coupon divided by the clean price (not the full price). The coupon of a zero coupon bond is defined as: (par - issue\_price) / tenor

```
current_yield(clean_price):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
clean_price	-	-	-

# yield\_to\_maturity

Calculate the bond's yield to maturity by solving the price yield relationship using a one-dimensional root solver.

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Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
clean_price	float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

#### accrued\_interest

Calculate the amount of coupon that has accrued between the previous coupon date and the settlement date. Note that for some day count schemes (such as 30E/360) this is not actually the number of days between the previous coupon payment date and settlement date. If the bond trades with ex-coupon dates then you need to supply the number of days before the coupon date the ex-coupon date is. You can specify the calendar to be used - NONE means only calendar days, WEEKEND is only weekends or you can specify a country calendar for business days.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float or (float	-	-

### asset\_swap\_spread

Calculate the par asset swap spread of the bond. The discount curve is a Ibor curve that is passed in. This function is vectorised with respect to the clean price.

```
asset_swap_spread(settle_dt: Date,
    clean_price: float,
    discount_curve: DiscountCurve,
    swapFloatDayCountConventionType=DayCountTypes.ACT_360,
    swapFloatFrequencyType=FrequencyTypes.SEMI_ANNUAL,
    swapFloatCalendarType=CalendarTypes.WEEKEND,
    swapFloatBusDayAdjustRuleType=BusDayAdjustTypes.FOLLOWING,
    swapFloatDateGenRuleType=DateGenRuleTypes.BACKWARD):
```

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
clean_price	float	-	-
discount_curve	DiscountCurve	-	-
swapFloatDayCountConventionType	-	-	DayCountTypes.ACT_360
swapFloatFrequencyType	-	-	FrequencyTypes.SEMI_ANNUAL
swapFloatCalendarType	-	-	CalendarTypes.WEEKEND
swapFloatBusDayAdjustRuleType	-	-	BusDayAdjustTypes.FOLLOWING
swapFloatDateGenRuleType	-	-	DateGenRuleTypes.BACKWARD

## dirty\_price\_from\_oas

Calculate the full price of the bond from its OAS given the bond settlement date, a discount curve and the oas as a number.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
oas	float	-	-

### option\_adjusted\_spread

Return OAS for bullet bond given settlement date, clean bond price and the discount relative to which the spread is to be computed.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
clean_price	float	-	-
discount_curve	DiscountCurve	-	-

# bond\_payments

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float or (float	-	-

# $print\_bond\_payments$

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settle_dt	Date	-	-
face	float or (float	-	100.0

### dirty\_price\_from\_survival\_curve

Calculate discounted present value of flows assuming default model. The survival curve treats the coupons as zero recovery payments while the recovery fraction of the par amount is paid at default. For the defaulting principal we discretize the time steps using the coupon payment times. A finer discretization may handle the time value with more accuracy. I reduce any error by averaging period start and period end payment present values.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
survival_curve	DiscountCurve	-	-
recovery_rate	float	-	-

### clean\_price\_from\_survival\_curve

Calculate clean price value of flows assuming default model. The survival curve treats the coupons as zero recovery payments while the recovery fraction of the par amount is paid at default.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
discount_curve	DiscountCurve	-	-
survival_curve	DiscountCurve	-	-
recovery_rate	float	-	-

#### calc\_ror

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
begin_dt	Date	-	-
end_dt	Date	-	-
begin_ytm	float	-	-
end_ytm	float	-	-
convention	YTMCalcType	-	YTMCalcType.ZERO

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

The function arguments are described in the following table.

#### $_{\mathbf{f}}$

Function used to do root search in price to yield calculation.

```
_f(ytm, *args):
```

7.11. BOND\_ZERO 279

<b>Argument Name</b>	Type	Description	Default Value
ytm	-	-	-
*args	-	-	-

# \_**g**

Function used to do root search in price to OAS calculation.

```
_g(oas, *args):
```

Argument Name	Type	Description	Default Value
oas	-	-	-
*args	-	-	-

## 7.12 yield\_curve

### Class: BondYieldCurve()

Class to do fitting of the yield curve and to enable interpolation of yields. Because yields assume a flat term structure for each bond, this class does not allow discounting to be done and so does not inherit from FinDiscountCurve. It should only be used for visualisation and simple interpolation but not for full term-structure-consistent pricing.

#### **BondYieldCurve**

Fit the curve to a set of bond yields using the type of curve specified. Bounds can be provided if you wish to enforce lower and upper limits on the respective model parameters.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settle_dt	Date	-	-
bonds	list	-	-
ylds	np.ndarray or list	-	-
curveFit	-	-	-

## $interpolated\_yield$

PLEASE ADD A FUNCTION DESCRIPTION

```
interpolated_yield(maturity_dt: Date):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
maturity_dt	Date	-	-

### plot

Display yield curve.

```
plot(title):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
title	-	-	-

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## \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_\_():

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

\_print():

# 7.13 yield\_curve\_model

Class: FinCurveFitMethod()

class FinCurveFitMethod():

Class: CurveFitPolynomial()

class CurveFitPolynomial():

### CurveFitPolynomial

PLEASE ADD A FUNCTION DESCRIPTION

CurveFitPolynomial(power=3):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
power	-	-	3

### \_interpolated\_yield

PLEASE ADD A FUNCTION DESCRIPTION

\_interpolated\_yield(t):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

The function arguments are described in the following table.

#### \_print

Simple print function for backward compatibility.

\_print():

### Class: CurveFitNelsonSiegel()

class CurveFitNelsonSiegel():

### CurveFitNelsonSiegel

Fairly permissive bounds. Only tau1 is 1-100

```
CurveFitNelsonSiegel(tau=None, bounds=[(-1, -1, -1, 0.5), (1, 1, 1, 100)]):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
tau	-	-	None
bounds	-	-	[(-1, -1, -1, 0.5), (1, 1, 1, 100)]

## \_interpolated\_yield

PLEASE ADD A FUNCTION DESCRIPTION

```
_interpolated_yield(t, beta1=None, beta2=None, beta3=None, tau=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
beta1	-	-	None
beta2	-	-	None
beta3	-	-	None
tau	-	-	None

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## $_{-}$ print

Simple print function for backward compatibility.

```
_print():
```

### Class: CurveFitNelsonSiegelSvensson()

class CurveFitNelsonSiegelSvensson():

### CurveFitNelsonSiegelSvensson

Create object to store calibration and functional form of NSS parametric fit.

```
CurveFitNelsonSiegelSvensson(tau1=None, tau2=None, bounds=[(0, -1, -1, -1, 0, 1), (1, 1, 1, 1, 10, 100)]):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value	
tau1	-	-	None	
tau2	-	-	None	
bounds	-	-	[(0, -1, -1, -1, 0, 1), (1, 1, 1, 1, 10, 100)]	

# \_interpolated\_yield

PLEASE ADD A FUNCTION DESCRIPTION

```
_interpolated_yield(t, beta1=None, beta2=None, beta3=None, beta4=None, tau1=None, tau2=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
beta1	-	-	None
beta2	-	-	None
beta3	-	-	None
beta4	-	-	None
tau1	-	-	None
tau2	-	-	None

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

\_print():

The function arguments are described in the following table.

# Class: CurveFitBSpline()

class CurveFitBSpline():

# CurveFitBSpline

PLEASE ADD A FUNCTION DESCRIPTION

```
CurveFitBSpline(power=3, knots=[1, 3, 5, 10]):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
power	-	-	3
knots	-	-	[1, 3, 5, 10]

# \_interpolated\_yield

PLEASE ADD A FUNCTION DESCRIPTION

```
_interpolated_yield(t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# \_print

Simple print function for backward compatibility.

```
_print():
```

### 7.14 zero\_curve

# Class: BondZeroCurve(DiscountCurve)

#### **BondZeroCurve**

Fit a discount curve to a set of bond yields using the type of curve specified.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
value_dt	Date	-	-
bonds	list	-	-
clean_prices	list	-	-
interp_type	InterpTypes	-	InterpTypes.FLAT_FWD_RATES

### \_bootstrap\_zero\_rates

PLEASE ADD A FUNCTION DESCRIPTION

```
_bootstrap_zero_rates():
```

The function arguments are described in the following table.

#### zero\_rate

Calculate the zero rate to maturity date.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	Date	-	-
frequencyType	FrequencyTypes	-	FrequencyTypes.CONTINUOUS

#### df

PLEASE ADD A FUNCTION DESCRIPTION

```
df(dt: Date):
```

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	Date	-	-

# $survival\_prob$

PLEASE ADD A FUNCTION DESCRIPTION

```
survival_prob(dt: Date):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	Date	-	-

#### fwd

Calculate the continuous forward rate at the forward date.

```
fwd(dt: Date):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
dt	Date	-	-

### fwd\_rate

Calculate the forward rate according to the specified day count convention.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
date1	Date	-	-
date2	Date	-	-
day_count_type	DayCountTypes	-	-

# plot

Display yield curve.

```
plot(title: str):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
title	str	-	-

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

\_print():

The function arguments are described in the following table.

### $_{\mathbf{f}}$

#### PLEASE ADD A FUNCTION DESCRIPTION

\_f(df, \*args):

Argument Name	Type	Description	Default Value
df	-	-	-
*args	-	-	-

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# 7.15 \_\_init\_\_

# **Chapter 8**

# financepy.products.rates

# **Funding**

This folder contains a set of funding-related products. These reflect contracts linked to funding indices such as Ibors and Overnight index rate swaps (OIS). It includes:

### **IborDeposit**

This is the basic Ibor instrument in which a party borrows an amount for a specified term and rate unsecured.

#### FinInterestRateFuture

This is a class to handle interest rate futures contracts. This is an exchange-traded contract to receive or pay Ibor on a specified future date. It can be used to build the Liboir term structure.

#### **IborFRA**

This is a class to manage Forward Rate Agreements (FRAs) in which one party agrees to lock in a forward Ibor rate.

### **Swaps**

# FinFixedIborSwap

This is a contract to exchange fixed rate coupons for floating Ibor rates. This class has functionality to value the swap contract and to calculate its risk.

# FinFixedIborSwap - IN PROGRESS

This is a contract to exchange fixed rate coupons for floating Ibor rates. This class has functionality to value the swap contract and to calculate its risk.

### IborlborSwap - IN PROGRESS

This is a contract to exchange IBOR rates with different terms, also known as a basis swap. This class has functionality to value the swap contract and to calculate its risk.

### FinFixedOISwap - IN PROGRESS

This is an OIS, a contract to exchange fixed rate coupons for the overnight index rate. This class has functionality to value the swap contract and to calculate its risk.

### IborOISwap - IN PROGRESS

This is a contract to exchange overnight index rates for Ibor rates. This class has functionality to value the swap contract and to calculate its risk.

### Currency Swaps

### FinFixedFixedCcySwap - IN PROGRESS

This is a contract to exchange fixed rate coupons in two different currencies. This class has functionality to value the swap contract and to calculate its risk.

# IborlborCcySwap - IN PROGRESS

This is a contract to exchange IBOR coupons in two different currencies. This class has functionality to value the swap contract and to calculate its risk.

#### **FinOIS**

This is a contract to exchange the daily compounded Overnight index swap rate for a fixed rate agreed at contract initiation.

#### **FinOISCurve**

This is a discount curve that is extracted by bootstrapping a set of OIS rates. The internal representation of the curve are discount factors on each of the OIS dates. Between these dates, discount factors are interpolated according to a specified scheme.

# IborSingleCurve

This is a discount curve that is extracted by bootstrapping a set of Ibor deposits, Ibor FRAs and Ibor swap prices. The internal representation of the curve are discount factors on each of the deposit, FRA and swap maturity dates. Between these dates, discount factors are interpolated according to a specified scheme - see below.

### **Options**

### *IborCapFloor*

### **IborSwaption**

This is a contract to buy or sell an option to enter into a swap to either pay or receive a fixed swap rate at a specific future expiry date. The model includes code that prices a payer or receiver swaption with the following models:

- Black's Model - Shifted Black Model - SABR - Shifted SABR - Hull-White Tree Model - Black-Karasinski Tree Model - Black-Derman-Toy Tree Model

### **IborBermudanSwaption**

This is a contract to buy or sell an option to enter into a swap to either pay or receive a fixed swap rate at a specific future expiry date on specific coupon dates starting on a designated expiry date. The model includes code that prices a payer or receiver swaption with the following models:

- Hull-White Tree Model - Black-Karasinski Tree Model - Black-Derman-Toy Tree Model

It is also possible to price this using a Ibor Market Model. However for the moment this must be done directly via the Monte-Carlo implementation of the LMM found in FinModelRatesLMM.

# 8.1 bermudan\_swaption

### Class: IborBermudanSwaption

This is the class for the Bermudan-style swaption, an option to enter into a swap (payer or receiver of the fixed coupon), that starts in the future and with a fixed maturity, at a swap rate fixed today. This swaption can be exercised on any of the fixed coupon payment dates after the first exercise date.

### **IborBermudanSwaption**

Create a Bermudan swaption contract. This is an option to enter into a payer or receiver swap at a fixed coupon on all of the fixed # leg coupon dates until the exercise date inclusive.

The function arguments are described in the following table.

Type	Description	Default Value
Date	-	-
Date	-	-
Date	-	-
SwapTypes	-	-
FinExerciseTypes	-	-
float	-	-
FrequencyTypes	-	-
DayCountTypes	-	-
-	-	ONE_MILLION
-	-	FrequencyTypes.QUARTERLY
-	-	DayCountTypes.THIRTY_E_360
-	-	CalendarTypes.WEEKEND
-	-	BusDayAdjustTypes.FOLLOWING
-	-	DateGenRuleTypes.BACKWARD
	Date Date SwapTypes FinExerciseTypes float FrequencyTypes	Date - Date - SwapTypes - FinExerciseTypes - float - FrequencyTypes -

#### value

Value the Bermudan swaption using the specified model and a discount curve. The choices of model are the

Hull-White model, the Black-Karasinski model and the Black-Derman-Toy model.

```
value(value_dt,
    discount_curve,
    model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
discount_curve	-	-	-
model	-	-	-

# print\_swaption\_value

PLEASE ADD A FUNCTION DESCRIPTION

```
print_swaption_value():
```

The function arguments are described in the following table.

```
__repr__
```

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# \_print

PLEASE ADD A FUNCTION DESCRIPTION

```
_print():
```

# 8.2 callable\_swap

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### 8.3 dual curve

### Class: IborDualCurve(DiscountCurve)

Constructs an index curve as implied by the prices of Ibor deposits, FRAs and IRS. Discounting is assumed to be at a discount rate that is an input and usually derived from OIS rates.

#### **IborDualCurve**

Create an instance of a Ibor curve given a valuation date and a set of ibor deposits, ibor FRAs and ibor\_swaps. Some of these may be left None and the algorithm will just use what is provided. An interpolation method has also to be provided. The default is to use a linear interpolation for swap rates on coupon dates and to then assume flat forwards between these coupon dates. The curve will assign a discount factor of 1.0 to the valuation date.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
ibor_deposits	list	-	-
ibor_fras	list	-	-
ibor_swaps	list	-	-
interp_type	InterpTypes	-	InterpTypes.FLAT_FWD_RATES
check_refit	bool	Set to True to test it works	False

#### \_build\_curve

Build curve based on interpolation.

```
_build_curve():
```

The function arguments are described in the following table.

# $_{\rm validate\_inputs}$

Validate the inputs for each of the Ibor products.

```
_validate_inputs(ibor_deposits, ibor_fras,
```

```
ibor_swaps):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
ibor_deposits	-	-	-
ibor_fras	-	-	-
ibor_swaps	-	-	-

# \_build\_curve\_using\_1d\_solver

Construct the discount curve using a bootstrap approach. This is the non-linear slower method that allows the user to choose a number of interpolation approaches between the swap rates and other rates. It involves the use of a solver.

```
_build_curve_using_1d_solver():
```

The function arguments are described in the following table.

#### \_check\_refits

Ensure that the Ibor curve refits the calibration instruments.

```
_check_refits(depoTol, fraTol, swapTol):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
depoTol	-	-	-
fraTol	-	-	-
swapTol	-	-	-

#### \_\_repr\_\_

Print out the details of the Ibor curve.

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Simple print function for backward compatibility.

```
_print():
```

8.3. DUAL\_CURVE

### $\mathbf{f}$

Root search objective function for swaps

```
_f(df, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
df	-	-	-
*args	-	-	-

# \_**g**

Root search objective function for swaps

```
_g(df, *args):
```

Argument Name	Type	Description	<b>Default Value</b>
df	-	-	-
*args	-	-	-

# 8.4 ibor\_basis\_swap

### Class: IborBasisSwap

Class for managing an Ibor-Ibor basis swap contract. This is a contract in which a floating leg with one LIBOR tenor is exchanged for a floating leg payment in a different LIBOR tenor. There is no exchange of par. The contract is entered into at zero initial cost. The contract lasts from an effective date to a specified maturity date.

The value of the contract is the NPV of the two coupon streams. Discounting is done on a supplied discount curve which can be different from the two index discount from which the implied index rates are extracted.

### **IborBasisSwap**

Create a Ibor basis swap contract giving the contract start date, its maturity, frequency and day counts on the two floating legs and notional. The floating leg parameters have default values that can be overwritten if needed. The start date is contractual and is the same as the settlement date for a new swap. It is the date on which interest starts to accrue. The end of the contract is the termination date. This is not adjusted for business days. The adjusted termination date is called the maturity date. This is calculated.

Type	Description	Default Value
Date	Date interest starts to accrue	-
Date or str	Date contract ends	-
SwapTypes	-	-
FrequencyTypes	-	FrequencyTypes.QUARTERLY
DayCountTypes	-	DayCountTypes.THIRTY_E_360
float	-	0.0
FrequencyTypes	-	FrequencyTypes.QUARTERLY
DayCountTypes	-	DayCountTypes.THIRTY_E_360
float	-	0.0
float	-	ONE_MILLION
CalendarTypes	-	CalendarTypes.WEEKEND
BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
	Date Date or str SwapTypes FrequencyTypes DayCountTypes float FrequencyTypes DayCountTypes CalendarTypes BusDayAdjustTypes	Date or str Date contract ends SwapTypes - FrequencyTypes - DayCountTypes - float - FrequencyTypes - DayCountTypes - CalendarTypes - BusDayAdjustTypes -

#### value

Value the interest rate swap on a value date given a single Ibor discount curve and an index curve for the Ibors on each swap leg.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
index_curveLeg1	DiscountCurve	-	None
index_curveLeg2	DiscountCurve	-	None
firstFixingRateLeg1	-	-	None
firstFixingRateLeg2	-	-	None

# print\_float\_leg\_1\_pv

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_float_leg_1_pv():
```

# print\_float\_leg\_2\_pv

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_float_leg_2_pv():
```

The function arguments are described in the following table.

# print\_payments

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_payments():
```

The function arguments are described in the following table.

```
__repr__
```

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### \_print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

8.5. IBOR\_CAP\_FLOOR 303

# 8.5 ibor\_cap\_floor

# Enumerated Type: IborCapFloorModelTypes

This enumerated type has the following values:

- BLACK
- SHIFTED\_BLACK
- SABR

### Class: IborCapFloor()

Class for Caps and Floors. These are contracts which observe a Ibor reset L on a future start date and then make a payoff at the end of the Ibor period which is Max[L-K,0] for a cap and Max[K-L,0] for a floor. This is then day count adjusted for the Ibor period and then scaled by the contract notional to produce a valuation. A number of models can be selected from.

### **IborCapFloor**

Initialise IborCapFloor object.

Argument Name	Type	Description	Default Value
start_dt	Date	-	-
maturity_dt_or_tenor	Date or str	-	-
option_type	FinCapFloorTypes	-	-
strike_rate	float	-	-
last_fixing	Optional[float]	-	None
freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
dc_type	DayCountTypes	-	DayCountTypes.THIRTY_E_360_ISDA
notional	float	-	ONE_MILLION
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

### \_generate\_dts

PLEASE ADD A FUNCTION DESCRIPTION

```
_generate_dts():
```

The function arguments are described in the following table.

#### value

Value the cap or floor using the chosen model which specifies the volatility of the Ibor rate to the cap start date.

```
value(value_dt, libor_curve, model):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
libor_curve	-	-	-
model	-	-	-

# value\_caplet\_floor\_let

Value the caplet or floorlet using a specific model.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
caplet_start_dt	-	-	-
caplet_end_dt	-	-	-
libor_curve	-	-	-
model	-	-	-

# print\_leg

Prints the cap floor payment amounts.

```
print_leg():
```

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# \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_repr\_\_():

The function arguments are described in the following table.

# $\_$ print

PLEASE ADD A FUNCTION DESCRIPTION

\_print():

# 8.6 ibor\_conventions

Class: IborConventions()

class IborConventions():

# **IborConventions**

PLEASE ADD A FUNCTION DESCRIPTION

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
currencyName	str	-	-
indexName	str	-	"LIBOR"

8.7. IBOR\_DEPOSIT 307

# 8.7 ibor\_deposit

#### Class: IborDeposit

An Ibor deposit is an agreement to borrow money interbank at the Ibor fixing rate starting on the start date and repaid on the maturity date with the interest amount calculated according to a day count convention and dates calculated according to a calendar and business day adjustment rule.

Care must be taken to calculate the correct start (settlement) date. Start with the trade (value) date which is typically today, we may need to add on a number of business days (spot days) to get to the settlement date. The maturity date is then calculated by adding on the deposit tenor/term to the settlement date and adjusting for weekends and holidays according to the calendar and adjustment type.

Note that for over-night (ON) depos the settlement date is today with maturity in one business day. For tomorrow-next (TN) depos the settlement is in one business day with maturity on the following business day. For later maturity deposits, settlement is usually in 1-3 business days. The number of days depends on the currency and jurisdiction of the deposit contract.

### **IborDeposit**

Create a Libor deposit object which takes the start date when the amount of notional is borrowed, a maturity date or a tenor and the deposit rate. If a tenor is used then this is added to the start date and the calendar and business day adjustment method are applied if the maturity date fall on a holiday. Note that in order to calculate the start date you add the spot business days to the trade date which usually today.

```
IborDeposit(start_dt: Date, # When the interest starts to accrue
    maturity_dt_or_tenor: (Date, str), # Repayment of interest
    deposit_rate: float, # MM rate using simple interest
    dc_type: DayCountTypes, # How year fraction is calculated
    notional: float = 100.0, # Amount borrowed
    cal_type: CalendarTypes=CalendarTypes.WEEKEND, # Maturity date
    bd_type: BusDayAdjustTypes=BusDayAdjustTypes.MODIFIED_FOLLOWING):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
start_dt	Date	When the interest starts to accrue	-
maturity_dt_or_tenor	Date or str	Repayment of interest	-
deposit_rate	float	MM rate using simple interest	-
dc_type	DayCountTypes	How year fraction is calculated	-
notional	float	Amount borrowed	100.0
cal_type	CalendarTypes	Maturity date	Calendar Types. WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.MODIFIED_FOLL

# \_maturity\_df

Returns the maturity date discount factor that would allow the Libor curve to reprice the contractual market deposit rate. Note that this is a forward discount factor that starts on settlement date.

```
_maturity_df():
```

The function arguments are described in the following table.

#### value

Determine the value of an existing Libor Deposit contract given a valuation date and a Libor curve. This is simply the PV of the future repayment plus interest discounted on the current Libor curve.

```
value(value_dt: Date,
    libor_curve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
libor_curve	-	-	-

# print\_payments

Print the date and size of the future repayment.

```
print_payments(value_dt: Date):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-

#### \_\_repr\_\_

Print the contractual details of the Libor deposit.

```
__repr__():
```

The function arguments are described in the following table.

### $_{\rm print}$

PLEASE ADD A FUNCTION DESCRIPTION

```
_print():
```

8.8. IBOR\_FRA 309

#### 8.8 ibor fra

#### Class: IborFRA

Class for managing LIBOR forward rate agreements. A forward rate agreement is an agreement to exchange a fixed pre-agreed rate for a floating rate linked to LIBOR that is not known until some specified future fixing date. The FRA payment occurs on or soon after this date on the FRA settlement date. Typically the timing gap is two days.

A FRA is used to hedge a Ibor quality loan or lend of some agreed notional amount. This period starts on the settlement date of the FRA and ends on the maturity date of the FRA. For example a 1x4 FRA relates to a Ibor starting in 1 month for a loan period ending in 4 months. Hence it links to 3-month Ibor rate. The amount received by a payer of fixed rate at settlement is:

```
acc(1,2) * (Ibor(1,2) - FRA RATE) / (1 + acc(0,1) x Ibor(0,1))
So the value at time 0 is acc(1,2) * (FWD Ibor(1,2) - FRA RATE) x df(0,2)
```

If the base date of the curve is before the value date then we forward adjust this amount to that value date. For simplicity I have assumed that the fixing date and the settlement date are the same date. This should be amended later.

The valuation below incorporates a dual curve approach.

#### **IborFRA**

Create a Forward Rate Agreement object.

```
IborFRA(start_dt: Date, # The date the FRA starts to accrue
    # End of the Ibor rate period
    maturity_dt_or_tenor: (Date, str),
    fraRate: float, # The fixed contractual FRA rate
    dc_type: DayCountTypes, # For interest period
    notional: float = 100.0,
    payFixedRate: bool = True, # True if the FRA rate is being paid
    cal_type: CalendarTypes = CalendarTypes.WEEKEND,
    bd_type: BusDayAdjustTypes = BusDayAdjustTypes.MODIFIED_FOLLOWING):
```

Type	Description	Default Value
Date	The date the FRA starts to accrue	-
Date or str	-	-
float	The fixed contractual FRA rate	-
DayCountTypes	For interest period	-
float	-	100.0
bool	True if the FRA rate is being paid	True
CalendarTypes	-	CalendarTypes.WEEKEND
BusDayAdjustTypes	-	BusDayAdjustTypes.MODIFIED_FOLI
	Date Date or str float DayCountTypes float bool CalendarTypes	Date The date the FRA starts to accrue  Date or str -  float The fixed contractual FRA rate  DayCountTypes For interest period  float -  bool True if the FRA rate is being paid  CalendarTypes -

#### value

Determine mark to market value of a FRA contract based on the market FRA rate. We allow the pricing to have a different curve for the Libor index and the discounting of promised cash flows.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
index_curve	DiscountCurve	-	None

# maturity\_df

Determine the maturity date index discount factor needed to refit the market FRA rate. In a dual-curve world, this is not the discount rate discount factor but the index curve discount factor.

```
maturity_df(index_curve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
index_curve	-	-	-

# print\_payments

Determine the value of the Deposit given a Ibor curve.

```
print_payments(value_dt):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
value_dt	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

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# \_print

### PLEASE ADD A FUNCTION DESCRIPTION

\_print():

### 8.9 ibor\_future

Class: IborFuture

#### **IborFuture**

Create an interest rate futures contract which has the same conventions as those traded on the CME. The current \_dt, the tenor of the future, the number of the future and the accrual convention and the contract size should be provided.

```
IborFuture(today_dt: Date,
    future_number: int, # The number of the future after today_dt
    futureTenor: str = "3M", # '1M', '2M', '3M'
    dc_type: DayCountTypes = DayCountTypes.ACT_360,
    contract_size: float = ONE_MILLION):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
today_dt	Date	-	-
future_number	int	The number of the future after today_dt	-
futureTenor	str	'1M', '2M', '3M'	"3M"
dc_type	DayCountTypes	-	DayCountTypes.ACT_360
contract_size	float	-	ONE_MILLION

#### to\_fra

Convert the futures contract to a IborFRA object so it can be used to boostrap a Ibor curve. For this we need to adjust the futures rate using the convexity correction.

```
to_fra(futures_price, convexity):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
futures_price	-	-	-
convexity	-	-	-

#### futures\_rate

Calculate implied futures rate from the futures price.

```
futures_rate(futures_price):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
futures_price	-	-	-

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#### fra\_rate

Convert futures price and convexity to a FRA rate using the BBG negative convexity (in percent). This is then divided by 100 before being added to the futures rate.

```
fra_rate(futures_price, convexity):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
futures_price	-	-	-
convexity	-	-	-

# convexity

Calculation of the convexity adjustment between FRAs and interest rate futures using the Hull-White model as described in technical note in link below: http://www-2.rotman.utoronto.ca/ hull/TechnicalNotes/TechnicalNote1.pdf NOTE THIS DOES NOT APPEAR TO AGREE WITH BLOOMBERG!! INVESTIGATE.

```
convexity(value__dt, volatility, mean_reversion):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
valuedt	-	-	-
volatility	-	-	-
mean_reversion	-	-	-

#### \_\_repr\_\_

Print a list of the unadjusted coupon payment \_dts used in analytic calculations for the bond.

```
__repr__():
```

# 8.10 ibor\_Imm\_products

Class: IborLMMProducts()

#### **IborLMMProducts**

Create a European-style swaption by defining the exercise date of the swaption, and all of the details of the underlying interest rate swap including the fixed coupon and the details of the fixed and the floating leg payment schedules.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
settle_dt	Date	-	-
maturity_dt	Date	-	-
float_freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
float_dc_type	DayCountTypes	-	DayCountTypes.THIRTY_E_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

#### simulate\_1f

Run the one-factor simulation of the evolution of the forward Ibors to generate and store all of the Ibor forward rate paths.

Argument Name	Type	Description	<b>Default Value</b>
discount_curve	-	-	-
vol_curve	IborCapVolCurve	-	-
num_paths	int	-	1000
numeraireIndex	int	-	0
use_sobol	bool	-	True
seed	int	-	42

#### simulate\_mf

Run the simulation to generate and store all of the Ibor forward rate paths. This is a multi-factorial version so the user must input a numpy array consisting of a column for each factor and the number of rows must equal the number of grid times on the underlying simulation grid. CHECK THIS.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
discount_curve	-	-	-
numFactors	int	-	-
lambdas	np.ndarray	-	-
num_paths	int	-	10000
numeraireIndex	int	-	0
use_sobol	bool	-	True
seed	int	-	42

#### simulate\_nf

Run the simulation to generate and store all of the Ibor forward rate paths using a full factor reduction of the fwd-fwd correlation matrix using Cholesky decomposition.

Argument Name	Type	Description	Default Value
discount_curve	-	-	-
vol_curve	IborCapVolCurve	-	-
corr_matrix	np.ndarray	-	-
model_type	ModelLMMModelTypes	-	-
num_paths	int	-	1000
numeraire_index	int	-	0
use_sobol	bool	-	True
seed	int	-	42

# value\_swaption

Value a swaption in the LMM model using simulated paths of the forward curve. This relies on pricing the fixed leg of the swap and assuming that the floating leg will be worth par. As a result we only need simulate Ibors with the frequency of the fixed leg.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
settle_dt	Date	-	-
exercise_dt	Date	-	-
maturity_dt	Date	-	-
swaptionType	SwapTypes	-	-
fixed_coupon	float	-	-
fixed_freq_type	FrequencyTypes	-	-
fixed_dc_type	DayCountTypes	-	-
notional	float	-	ONE_MILLION
float_freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
float_dc_type	DayCountTypes	-	DayCountTypes.THIRTY_E_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

# value\_cap\_floor

Value a cap or floor in the LMM.

The function arguments are described in the following table.

Type	Description	Default Value
Date	-	-
Date	-	-
FinCapFloorTypes	-	-
float	-	-
FrequencyTypes	-	FrequencyTypes.QUARTERLY
DayCountTypes	-	DayCountTypes.ACT_360
float	-	ONE_MILLION
CalendarTypes	-	CalendarTypes.WEEKEND
BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
	Date Date Date FinCapFloorTypes float FrequencyTypes DayCountTypes float CalendarTypes BusDayAdjustTypes	Date - Date - FinCapFloorTypes - float - FrequencyTypes - DayCountTypes - float - CalendarTypes - BusDayAdjustTypes -

# \_\_repr\_\_

Function to allow us to print the LMM Products details.

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Alternative print method.

\_print():

# 8.11 ibor\_single\_curve

### Class: IborSingleCurve(DiscountCurve)

Constructs one discount and index curve as implied by prices of Ibor deposits, FRAs and IRS. Discounting is assumed to be at Libor and the value of the floating leg (including a notional) is assumed to be par. This approach has been overtaken since 2008 as OIS discounting has become the agreed discounting approach for ISDA derivatives. This curve method is therefore intended for those happy to assume simple Libor discounting.

The curve date is the date on which we are performing the valuation based on the information available on the curve date. Typically it is the date on which an amount of 1 unit paid has a present value of 1. This class inherits from FinDiscountCurve and so it has all of the methods that that class has.

There are two main curve-building approaches:

- 1) The first uses a bootstrap that interpolates swap rates linearly for coupon dates that fall between the swap maturity dates. With this, we can solve for the discount factors iteratively without need of a solver. This will give us a set of discount factors on the grid dates that refit the market exactly. However, when extracting discount factors, we will then assume flat forward rates between these coupon dates. There is no contradiction as it is as though we had been quoted a swap curve with all of the market swap rates, and with an additional set as though the market quoted swap rates at a higher frequency than the market.
- 2) The second uses a bootstrap that uses only the swap rates provided but which also assumes that forwards are flat between these swap maturity dates. This approach is non-linear and so requires a solver. Consequently it is slower. Its advantage is that we can switch interpolation schemes to provide a smoother or other functional curve shape which may have a more economically justifiable shape. However the root search makes it slower.

# **IborSingleCurve**

Create an instance of a FinIbor curve given a valuation date and a set of ibor deposits, ibor FRAs and ibor\_swaps. Some of these may be left None and the algorithm will just use what is provided. An interpolation method has also to be provided. The default is to use a linear interpolation for swap rates on coupon dates and to then assume flat forwards between these coupon dates. The curve will assign a discount factor of 1.0 to the valuation date. If no instrument is starting on the valuation date, the curve is then assumed to be flat out to the first instrument using its zero rate.

Argument Name	Type	Description	Default Value
value_dt	Date	This is the trade date (not T+2)	-
ibor_deposits	list	-	-
ibor_fras	list	-	-
ibor_swaps	list	-	-
interp_type	InterpTypes	-	InterpTypes.FLAT_FWD_RATES
check_refit	bool	Set to True to test it works	False

#### \_build\_curve

Build curve based on interpolation.

```
_build_curve():
```

The function arguments are described in the following table.

### \_validate\_inputs

Validate the inputs for each of the Ibor products.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
ibor_deposits	-	-	-
ibor_fras	-	-	-
ibor_swaps	-	-	-

# \_build\_curve\_using\_1d\_solver

Construct the discount curve using a bootstrap approach. This is the non-linear slower method that allows the user to choose a number of interpolation approaches between the swap rates and other rates. It involves the use of a solver.

```
_build_curve_using_1d_solver():
```

The function arguments are described in the following table.

# \_build\_curve\_using\_quadratic\_minimiser

Construct the discount curve using a minimisation approach. This is the This enables a more complex interpolation scheme.

```
_build_curve_using_quadratic_minimiser():
```

The function arguments are described in the following table.

## \_build\_curve\_linear\_swap\_rate\_interpolation

Construct the discount curve using a bootstrap approach. This is the linear swap rate method that is fast and exact as it does not require the use of a solver. It is also market standard.

```
_build_curve_linear_swap_rate_interpolation():
```

The function arguments are described in the following table.

#### \_check\_refits

Ensure that the Ibor curve refits the calibration instruments.

```
_check_refits(depoTol, fraTol, swapTol):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
depoTol	-	-	-
fraTol	-	-	-
swapTol	-	-	-

#### \_\_repr\_\_

Print out the details of the Ibor curve.

```
__repr__():
```

The function arguments are described in the following table.

## \_print

Simple print function for backward compatibility.

```
_print():
```

 $\mathbf{f}$ 

Root search objective function for IRS

```
_f(df, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
df	-	-	-
*args	-	-	-

\_**g** 

Root search objective function for FRAs

```
_g(df, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
df	-	-	-
*args	-	-	-

## \_cost\_function

Root search objective function for swaps

```
_cost_function(dfs, *args):
```

<b>Argument Name</b>	Type	Description	Default Value
dfs	-	-	-
*args	-	-	-

## 8.12 ibor\_swap

### Class: IborSwap

Class for managing a standard Fixed vs IBOR swap. This is a contract in which a fixed payment leg is exchanged for a series of floating rates payments linked to some IBOR index rate. There is no exchange of principal. The contract is entered into at zero initial cost. The contract lasts from a start date to a specified maturity date.

The floating rate is not known fully until the end of the preceding payment period. It is set in advance and paid in arrears.

The value of the contract is the NPV of the two coupon streams. Discounting is done on a supplied discount curve which is separate from the curve from which the implied index rates are extracted.

### **IborSwap**

Create an interest rate swap contract giving the contract start date, its maturity, fixed coupon, fixed leg frequency, fixed leg day count convention and notional. The floating leg parameters have default values that can be overwritten if needed. The start date is contractual and is the same as the settlement date for a new swap. It is the date on which interest starts to accrue. The end of the contract is the termination date. This is not adjusted for business days. The adjusted termination date is called the maturity date. This is calculated.

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Argument Name	Type	Description	Default Value
effective_dt	Date	Date interest starts to accrue	-
term_dt_or_tenor	Date or str	Date contract ends	-
fixed_leg_type	SwapTypes	-	-
fixed_coupon	float	Fixed coupon (annualised)	-
fixed_freq_type	FrequencyTypes	-	-
fixed_dc_type	DayCountTypes	-	-
notional	float	-	ONE_MILLION
float_spread	float	-	0.0
float_freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
float_dc_type	DayCountTypes	-	DayCountTypes.THIRTY_E_360
cal_type	CalendarTypes	-	Calendar Types. WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

#### value

Value the interest rate swap on a value date given a single Ibor discount curve.

```
value(value_dt: Date,
    discount_curve: DiscountCurve,
    index_curve: DiscountCurve = None,
    firstFixingRate=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
index_curve	DiscountCurve	-	None
firstFixingRate	-	-	None

## pv01

Calculate the value of 1 basis point coupon on the fixed leg.

```
pv01(value_dt, discount_curve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
discount_curve	-	-	-

### swap\_rate

Calculate the fixed leg coupon that makes the swap worth zero. If the valuation date is before the swap payments start then this is the forward swap rate as it starts in the future. The swap rate is then a forward

swap rate and so we use a forward discount factor. If the swap fixed leg has begun then we have a spot starting swap. The swap rate can also be calculated in a dual curve approach but in this case the first fixing on the floating leg is needed.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
index_curve	DiscountCurve	-	None
first_fixing	float	-	None

## $cash\_settled\_pv01$

Calculate the forward value of an annuity of a forward starting swap using a single flat discount rate equal to the swap rate. This is used in the pricing of a cash-settled swaption in the IborSwaption class. This method does not affect the standard valuation methods.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
flat_swap_rate	-	-	-
freq_type	-	-	-

## $print\_fixed\_leg\_pv$

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_fixed_leg_pv():
```

The function arguments are described in the following table.

## print\_float\_leg\_pv

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

8.12. IBOR\_SWAP 325

```
print_float_leg_pv():
```

The function arguments are described in the following table.

## print\_payments

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_payments():
```

The function arguments are described in the following table.

```
__repr__
```

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## \_print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
_print():
```

## 8.13 ibor\_swaption

## Class: IborSwaption()

This is the class for the European-style swaption, an option to enter into a swap (payer or receiver of the fixed coupon), that starts in the future and with a fixed maturity, at a swap rate fixed today.

## **IborSwaption**

Create a European-style swaption by defining the exercise date of the swaption, and all of the details of the underlying interest rate swap including the fixed coupon and the details of the fixed and the floating leg payment schedules. Bermudan style swaption should be priced using the IborBermudanSwaption class.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
settle_dt	Date	-	-
exercise_dt	Date	-	-
maturity_dt	Date	-	-
fixed_leg_type	SwapTypes	-	-
fixed_coupon	float	-	-
fixed_freq_type	FrequencyTypes	-	-
fixed_dc_type	DayCountTypes	-	-
notional	float	-	ONE_MILLION
float_freq_type	FrequencyTypes	-	FrequencyTypes.QUARTERLY
float_dc_type	DayCountTypes	-	DayCountTypes.THIRTY_E_360
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

#### value

Valuation of a Ibor European-style swaption using a choice of models on a specified valuation date. Models include FinModelBlack, FinModelBlackShifted, SABR, SABRShifted, FinModelHW, FinModelBK and Fin-ModelBDT. The last two involved a tree-based valuation.

8.13. IBOR\_SWAPTION 327

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
discount_curve	-	-	-
model	-	-	-

#### cash\_settled\_value

Valuation of a Ibor European-style swaption using a cash settled approach which is a market convention that used Black's model and that discounts all of the future payments at a flat swap rate. Note that the Black volatility for this valuation should in general not equal the Black volatility for the standard arbitrage-free valuation.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
discount_curve	-	-	-
swap_rate	float	-	-
model	-	-	-

## print\_swap\_fixed\_leg

PLEASE ADD A FUNCTION DESCRIPTION

```
print_swap_fixed_leg():
```

The function arguments are described in the following table.

## print\_swap\_float\_leg

PLEASE ADD A FUNCTION DESCRIPTION

```
print_swap_float_leg():
```

## \_\_repr\_\_

Function to allow us to print the swaption details.

The function arguments are described in the following table.

## $\_$ print

Alternative print method.

\_print():

8.14. OIS 329

#### 8.14 ois

#### Enumerated Type: FinCompoundingTypes

This enumerated type has the following values:

- COMPOUNDED
- OVERNIGHT COMPOUNDED ANNUAL RATE
- AVERAGED
- AVERAGED\_DAILY

#### Class: OIS

Class for managing overnight index rate swaps (OIS) and Fed Fund swaps. This is a contract in which a fixed payment leg is exchanged for a payment which pays the rolled-up overnight index rate (OIR). There is no exchange of par. The contract is entered into at zero initial cost.

NOTE: This class is almost identical to IborSwap but will possibly deviate as distinctions between the two become clear to me. If not they will be converged (or inherited) to avoid duplication.

The contract lasts from a start date to a specified maturity date. The fixed coupon is the OIS fixed rate for the corresponding tenor which is set at contract initiation.

The floating rate is not known fully until the end of each payment period. Its calculated at the contract maturity and is based on daily observations of the overnight index rate which are compounded according to a specific convention. Hence the OIS floating rate is determined by the history of the OIS rates.

In its simplest form, there is just one fixed rate payment and one floating rate payment at contract maturity. However when the contract becomes longer than one year the floating and fixed payments become periodic, usually with annual exchanges of cash.

The value of the contract is the NPV of the two coupon streams. Discounting is done on the OIS curve which is itself implied by the term structure of market OIS rates.

#### OIS

Create an overnight index swap contract giving the contract start date, its maturity, fixed coupon, fixed leg frequency, fixed leg day count convention and notional. The floating leg parameters have default values that can be overwritten if needed. The start date is contractual and is the same as the settlement date for a new swap. It is the date on which interest starts to accrue. The end of the contract is the termination date. This is not adjusted for business days. The adjusted termination date is called the maturity date. This is calculated.

```
OIS(effective_dt: Date, # Date interest starts to accrue
    term_dt_or_tenor: (Date, str), # Date contract ends
    fixed_leg_type: SwapTypes,
    fixed_coupon: float, # Fixed coupon (annualised)
    fixed_freq_type: FrequencyTypes,
    fixed_dc_type: DayCountTypes,
    notional: float = ONE_MILLION,
    payment_lag: int = 0, # Number of days after period payment occurs
    float_spread: float = 0.0,
    float_freq_type: FrequencyTypes = FrequencyTypes.ANNUAL,
    float_dc_type: DayCountTypes = DayCountTypes.THIRTY_E_360,
    cal_type: CalendarTypes = CalendarTypes.WEEKEND,
```

```
bd_type: BusDayAdjustTypes = BusDayAdjustTypes.FOLLOWING,
dg_type: DateGenRuleTypes = DateGenRuleTypes.BACKWARD):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
effective_dt	Date	Date interest starts to accrue	-
term_dt_or_tenor	Date or str	Date contract ends	-
fixed_leg_type	SwapTypes	-	-
fixed_coupon	float	Fixed coupon (annualised)	-
fixed_freq_type	FrequencyTypes	-	-
fixed_dc_type	DayCountTypes	-	-
notional	float	-	ONE_MILLION
payment_lag	int	Number of days after period payment occurs	0
float_spread	float	-	0.0
float_freq_type	FrequencyTypes	-	FrequencyTypes.ANNUAl
float_dc_type	DayCountTypes	-	DayCountTypes.THIRTY_E_
cal_type	CalendarTypes	-	CalendarTypes.WEEKENI
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOV
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWA

#### value

Value the interest rate swap on a value date given a single Ibor discount curve.

```
value(value_dt: Date,
    ois_curve: DiscountCurve,
    first_fixing_rate=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
ois_curve	DiscountCurve	-	-
first_fixing_rate	-	-	None

## pv01

Calculate the value of 1 basis point coupon on the fixed leg.

```
pv01(value_dt, discount_curve):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
discount_curve	-	-	-

8.14. OIS 331

#### swap\_rate

Calculate the fixed leg coupon that makes the swap worth zero. If the valuation date is before the swap payments start then this is the forward swap rate as it starts in the future. The swap rate is then a forward swap rate and so we use a forward discount factor. If the swap fixed leg has begun then we have a spot starting swap.

```
swap_rate(value_dt, ois_curve, first_fixing_rate=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
ois_curve	-	-	-
first_fixing_rate	-	-	None

## print\_fixed\_leg\_pv

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_fixed_leg_pv():
```

The function arguments are described in the following table.

## print\_float\_leg\_pv

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_float_leg_pv():
```

The function arguments are described in the following table.

## print\_payments

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_payments():
```

The function arguments are described in the following table.

```
__repr__
```

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

The function arguments are described in the following table.

## $\_print$

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

\_print():

8.15. OIS\_BASIS\_SWAP 333

## 8.15 ois\_basis\_swap

### Class: OISBasisSwap

Class for managing an Ibor-OIS basis swap contract. This is a contract in which a floating leg with one LIBOR tenor is exchanged for a floating leg payment of an overnight index swap. There is no exchange of par. The contract is entered into at zero initial cost. The contract lasts from a start date to a specified maturity date.

The value of the contract is the NPV of the two coupon streams. Discounting is done on a supplied discount curve which is separate from the discount from which the implied index rates are extracted.

## **OISBasisSwap**

Create a Ibor basis swap contract giving the contract start date, its maturity, frequency and day counts on the two floating legs and notional. The floating leg parameters have default values that can be overwritten if needed. The start date is contractual and is the same as the settlement date for a new swap. It is the date on which interest starts to accrue. The end of the contract is the termination date. This is not adjusted for business days. The adjusted termination date is called the maturity date. This is calculated.

```
OISBasisSwap(effective_dt: Date,  # Date interest starts to accrue
    term_dt_or_tenor: (Date, str),  # Date contract ends
    iborType: SwapTypes,
    iborFreqType: FrequencyTypes = FrequencyTypes.QUARTERLY,
    iborDayCountType: DayCountTypes = DayCountTypes.THIRTY_E_360,
    iborSpread: float = 0.0,
    oisFreqType: FrequencyTypes = FrequencyTypes.QUARTERLY,
    oisDayCountType: DayCountTypes = DayCountTypes.THIRTY_E_360,
    oisSpread: float = 0.0,
    oisPaymentLag: int = 0,
    notional: float = ONE_MILLION,
    cal_type: CalendarTypes = CalendarTypes.WEEKEND,
    bd_type: BusDayAdjustTypes = BusDayAdjustTypes.FOLLOWING,
    dg_type: DateGenRuleTypes = DateGenRuleTypes.BACKWARD):
```

Argument Name	Type	Description	Default Value
effective_dt	Date	Date interest starts to accrue	-
term_dt_or_tenor	Date or str	Date contract ends	-
iborType	SwapTypes	-	-
iborFreqType	FrequencyTypes	-	FrequencyTypes.QUARTERLY
iborDayCountType	DayCountTypes	-	DayCountTypes.THIRTY_E_360
iborSpread	float	-	0.0
oisFreqType	FrequencyTypes	-	FrequencyTypes.QUARTERLY
oisDayCountType	DayCountTypes	-	DayCountTypes.THIRTY_E_360
oisSpread	float	-	0.0
oisPaymentLag	int	-	0
notional	float	-	ONE_MILLION
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD

#### value

Value the interest rate swap on a value date given a single Ibor discount curve and an index curve for the Ibors on each swap leg.

```
value(value_dt: Date,
    discount_curve: DiscountCurve,
    indexIborCurve: DiscountCurve = None,
    indexOISCurve: DiscountCurve = None,
    firstFixingRateLeg1=None,
    firstFixingRateLeg2=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-
indexIborCurve	DiscountCurve	-	None
indexOISCurve	DiscountCurve	-	None
firstFixingRateLeg1	-	-	None
firstFixingRateLeg2	-	-	None

## print\_payments

Prints the fixed leg amounts without any valuation details. Shows the dates and sizes of the promised fixed leg flows.

```
print_payments():
```

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## \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_repr\_\_():

The function arguments are described in the following table.

## $\_$ print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

\_print():

### 8.16 ois\_curve

### Class: OISCurve(DiscountCurve)

Constructs a discount curve as implied by the prices of Overnight Index Rate swaps. The curve date is the date on which we are performing the valuation based on the information available on the curve date. Typically it is the date on which an amount of 1 unit paid has a present value of 1. This class inherits from FinDiscountCurve and so it has all of the methods that that class has.

The construction of the curve is assumed to depend on just the OIS curve, i.e. it does not include information from Ibor-OIS basis swaps. For this reason I call it a one-curve.

#### **OISCurve**

Create an instance of an overnight index rate swap curve given a valuation date and a set of OIS rates. Some of these may be left None and the algorithm will just use what is provided. An interpolation method has also to be provided. The default is to use a linear interpolation for swap rates on coupon dates and to then assume flat forwards between these coupon dates. The curve will assign a discount factor of 1.0 to the valuation date.

The function arguments are described in the following table.

Argument Name	Туре	Description	Default Value
value_dt	Date	-	-
ois_deposits	list	-	-
ois_fras	list	-	-
ois_swaps	list	-	-
interp_type	InterpTypes	-	InterpTypes.FLAT_FWD_RATES
check_refit	bool	Set to True to test it works	False

#### \_build\_curve

Build curve based on interpolation.

```
_build_curve():
```

The function arguments are described in the following table.

## \_validate\_inputs

Validate the inputs for each of the Libor products.

8.16. OIS\_CURVE 337

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
oisDeposits	-	-	-
oisFRAs	-	-	-
oisSwaps	-	-	-

## \_build\_curve\_using\_1d\_solver

Construct the discount curve using a bootstrap approach. This is the non-linear slower method that allows the user to choose a number of interpolation approaches between the swap rates and other rates. It involves the use of a solver.

```
_build_curve_using_1d_solver():
```

The function arguments are described in the following table.

## \_build\_curve\_linear\_swap\_rate\_interpolation

Construct the discount curve using a bootstrap approach. This is the linear swap rate method that is fast and exact as it does not require the use of a solver. It is also market standard.

```
_build_curve_linear_swap_rate_interpolation():
```

The function arguments are described in the following table.

#### \_check\_refits

Ensure that the Libor curve refits the calibration instruments.

```
_check_refits(depoTol, fraTol, swapTol):
```

<b>Argument Name</b>	Type	Description	Default Value
depoTol	-	-	-
fraTol	-	-	-
swapTol	-	-	-

#### \_\_repr\_\_

Print out the details of the Libor curve.

```
__repr__():
```

The function arguments are described in the following table.

## $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

#### \_fois

Extract the implied overnight index rate assuming it is flat over period in question.

```
_fois(oir, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
oir	-	-	-
*args	-	-	-

#### $_{\mathbf{f}}$

Root search objective function for OIS

```
_f(df, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
df	-	-	-
*args	-	-	-

#### $_{\mathbf{g}}$

Root search objective function for swaps

```
_g(df, *args):
```

8.16. OIS\_CURVE 339

Argument Name	Type	Description	<b>Default Value</b>
df	-	-	-
*args	-	-	-

## 8.17 swap\_fixed\_leg

## Class: SwapFixedLeg

Class for managing the fixed leg of a swap. A fixed leg is a leg with a sequence of flows calculated according to an ISDA schedule and with a coupon that is fixed over the life of the swap.

## **SwapFixedLeg**

Create the fixed leg of a swap contract giving the contract start date, its maturity, fixed coupon, fixed leg frequency, fixed leg day count convention and notional.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
effective_dt	Date	Date interest starts to accrue	-
end_dt	Date or str	Date contract ends	-
leg_type	SwapTypes	-	-
coupon	float or (float	-	-
freq_type	FrequencyTypes	-	-
dc_type	DayCountTypes	-	-
notional	float	-	ONE_MILLION
principal	float	-	0.0
payment_lag	int	-	0
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
end_of_month	bool	-	False

#### generate\_payments

These are generated immediately as they are for the entire life of the swap. Given a valuation date we can determine which cash flows are in the future and value the swap The schedule allows for a specified lag in

8.17. SWAP\_FIXED\_LEG 341

the payment date Nothing is paid on the swap effective date and so the first payment date is the first actual payment date.

```
generate_payments():
```

The function arguments are described in the following table.

#### value

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
discount_curve	DiscountCurve	-	-

## print\_payments

Prints the fixed leg dates, accrual factors, discount factors, cash amounts, their present value and their cumulative PV using the last valuation performed.

```
print_payments():
```

The function arguments are described in the following table.

## $print\_valuation$

Prints the fixed leg dates, accrual factors, discount factors, cash amounts, their present value and their cumulative PV using the last valuation performed.

```
print_valuation():
```

The function arguments are described in the following table.

```
__repr__
```

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

## $_{\rm print}$

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

\_print():

## 8.18 swap\_float\_leg

## Class: SwapFloatLeg

Class for managing the floating leg of a swap. A float leg consists of a sequence of flows calculated according to an ISDA schedule and with a coupon determined by an index curve which changes over life of the swap.

## **SwapFloatLeg**

Create the fixed leg of a swap contract giving the contract start date, its maturity, fixed coupon, fixed leg frequency, fixed leg day count convention and notional.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
effective_dt	Date	Date interest starts to accrue	-
end_dt	Date or str	Date contract ends	-
leg_type	SwapTypes	-	-
spread	float or (float	-	-
freq_type	FrequencyTypes	-	-
dc_type	DayCountTypes	-	-
notional	float	-	ONE_MILLION
principal	float	-	0.0
payment_lag	int	-	0
cal_type	CalendarTypes	-	CalendarTypes.WEEKEND
bd_type	BusDayAdjustTypes	-	BusDayAdjustTypes.FOLLOWING
dg_type	DateGenRuleTypes	-	DateGenRuleTypes.BACKWARD
end_of_month	bool	-	False

## generate\_payment\_dts

Generate the floating leg payment dates and accrual factors. The coupons cannot be generated yet as we do not have the index curve.

```
generate_payment_dts():
```

The function arguments are described in the following table.

#### value

Value the floating leg with payments from an index curve and discounting based on a supplied discount curve as of the valuation date supplied. For an existing swap, the user must enter the next fixing coupon.

```
value(value_dt: Date, # This should be the settlement date
    discount_curve: DiscountCurve,
    index_curve: DiscountCurve,
    firstFixingRate: float = None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	This should be the settlement date	-
discount_curve	DiscountCurve	-	-
index_curve	DiscountCurve	-	-
firstFixingRate	float	-	None

## print\_payments

Prints the fixed leg dates, accrual factors, discount factors, cash amounts, their present value and their cumulative PV using the last valuation performed.

```
print_payments():
```

The function arguments are described in the following table.

## print\_valuation

Prints the fixed leg dates, accrual factors, discount factors, cash amounts, their present value and their cumulative PV using the last valuation performed.

```
print_valuation():
```

The function arguments are described in the following table.

```
\_repr\_
```

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

8.18. SWAP\_FLOAT\_LEG 345

The function arguments are described in the following table.

## $\_print$

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

\_print():

8.19 \_\_init\_\_

# **Chapter 9**

# financepy.products.fx

## **FX** Derivatives

#### **Overview**

These modules price and produce the sensitivity measures needed to hedge a range of FX Options and other derivatives with an FX underlying.

#### **FX Forwards**

Calculate the price and breakeven forward FX Rate of an FX Forward contract.

## FX Vanilla Option

## **FX** Option

This is a class from which other classes inherit and is used to perform simple perturbatory calculation of option Greeks.

FX Barrier Options

FX Basket Options

FX Digital Options

FX Fixed Lookback Option

FX Float Lookback Option

FX Rainbow Option

FX Variance Swap

## 9.1 fx\_barrier\_option

## Enumerated Type: FinFXBarrierTypes

This enumerated type has the following values:

- DOWN\_AND\_OUT\_CALL
- DOWN\_AND\_IN\_CALL
- UP\_AND\_OUT\_CALL
- UP\_AND\_IN\_CALL
- UP\_AND\_OUT\_PUT
- UP\_AND\_IN\_PUT
- DOWN\_AND\_OUT\_PUT
- DOWN\_AND\_IN\_PUT

## Class: FXBarrierOption(FXOption)

class FXBarrierOption(FXOption):

## **FXBarrierOption**

Create FX Barrier option product. This is an option that cancels if the FX rate crosses a barrier during the life of the option.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
strike_fx_rate	float	1 unit of foreign in domestic	-
currency_pair	str	FORDOM	-
option_type	FinFXBarrierTypes	-	-
barrier_level	float	-	-
num_obs_per_year	int	-	-
notional	float	-	-
notional_currency	str	-	-

#### value

Value FX Barrier Option using Black-Scholes model with closed-form analytical models.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
spot_fx_rate	-	-	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-

## value\_mc

Value the FX Barrier Option using Monte Carlo.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	-	-
dom_interest_rate	-	-	-
process_type	-	-	-
model_params	-	-	-
num_ann_steps	-	-	552
num_paths	-	-	5000
seed	-	-	4242

#### \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

## \_print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

\_print():

## 9.2 fx\_digital\_option

## Class: FXDigitalOption

class FXDigitalOption:

## **FXDigitalOption**

Create the FX Digital Option object. Inputs include expiry date, strike, currency pair, option type (call or put), notional and the currency of the notional. And adjustment for spot days is enabled. All currency rates must be entered in the price in domestic currency of one unit of foreign. And the currency pair should be in the form FORDOM where FOR is the foreign currency pair currency code and DOM is the same for the domestic currency.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
strike_fx_rate	float or np.ndarray	-	-
currency_pair	str	FORDOM	-
option_type	OptionTypes or list	-	-
notional	float	-	-
prem_currency	str	-	-
spot_days	int	-	0

#### value

Valuation of a digital option using Black-Scholes model. This allows for 4 cases - first upper barriers that when crossed pay out cash (calls) and lower barriers than when crossed from above cause a cash payout (puts) PLUS the fact that the cash payment can be in domestic or foreign currency.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	1 unit of foreign in domestic	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-

## 9.3 fx\_double\_digital\_option

### Class: FXDoubleDigitalOption

class FXDoubleDigitalOption:

## **FXDoubleDigitalOption**

Create the FX Double Digital Option object. Inputs include expiry date, upper strike, lower strike, currency pair, option type notional and the currency of the notional. An adjustment for spot days is enabled. All currency rates must be entered in the price in domestic currency of one unit of foreign. And the currency pair should be in the form FORDOM where FOR is the foreign currency pair currency code and DOM is the same for the domestic currency.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
upper_strike	float or np.ndarray	_	-
lower_strike	float or np.ndarray	-	-
currency_pair	str	FORDOM	-
notional	float	-	-
prem_currency	str	-	-
spot_days	int	-	0

#### value

Valuation of a double digital option using Black-Scholes model. The option pays out the notional in the premium currency if the fx rate is between the upper and lower strike at maturity. The valuation is equivalent to the valuation of the difference of the value of two digital puts, one with the upper and the other with the lower strike

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	1 unit of foreign in domestic	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-

## 9.4 fx\_fixed\_lookback\_option

## Class: FXFixedLookbackOption

## **FXFixedLookbackOption**

Create option with expiry date, option type and the option strike

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiry_dt	Date	-	-
option_type	OptionTypes	-	-
optionStrike	float	-	-

#### value

Value FX Fixed Lookback Option using Black Scholes model and analytical formulae.

```
value(value_dt: Date,
    stock_price: float,
    dom_discount_curve: DiscountCurve,
    for_discount_curve: DiscountCurve,
    volatility: float,
    stock_min_max: float):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
dom_discount_curve	DiscountCurve	-	-
for_discount_curve	DiscountCurve	-	-
volatility	float	-	-
stock_min_max	float	-	-

#### value\_mc

Value FX Fixed Lookback option using Monte Carlo.

```
spot_fx_rateMinMax: float,
num_paths: int = 10000,
num_steps_per_year: int = 252,
seed: int = 4242):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
spot_fx_rate	float	FORDOM	-
domestic_curve	DiscountCurve	-	-
foreign_curve	DiscountCurve	-	-
volatility	float	-	-
spot_fx_rateMinMax	float	-	-
num_paths	int	-	10000
num_steps_per_year	int	-	252
seed	int	-	4242

# 9.5 fx\_float\_lookback\_option

## Class: FXFloatLookbackOption(FXOption)

This is an FX option in which the strike of the option is not fixed but is set at expiry to equal the minimum fx rate in the case of a call or the maximum fx rate in the case of a put.

# FXF loat Look back Option

Create the FX Float Look Back Option by specifying the expiry date and the option type.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
option_type	OptionTypes	-	-

#### value

Valuation of the Floating Lookback option using Black-Scholes using the formulae derived by Goldman, Sosin and Gatto (1979).

```
value(value_dt: Date,
    stock_price: float,
    domestic_curve: DiscountCurve,
    foreign_curve: DiscountCurve,
    volatility: float,
    stock_min_max: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	Date	-	-
stock_price	float	-	-
domestic_curve	DiscountCurve	-	-
foreign_curve	DiscountCurve	-	-
volatility	float	-	-
stock_min_max	float	-	-

#### value mc

#### PLEASE ADD A FUNCTION DESCRIPTION

```
foreign_curve,
volatility,
stock_min_max,
num_paths=10000,
num_steps_per_year=252,
seed=4242):
```

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	10000
-	-	252
-	-	4242
		Type Description

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## 9.6 fx\_forward

#### Class: FXForward

#### **FXForward**

Creates a FinFXForward which allows the owner to buy the FOR against the DOM currency at the strike\_fx\_rate and to pay it in the notional currency.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
strike_fx_rate	float	PRICE OF 1 UNIT OF FOREIGN IN DOM CCY	-
currency_pair	str	FOR DOM	-
notional	float	-	-
notional_currency	str	must be FOR or DOM	-
spot_days	int	-	0

#### value

Calculate the value of an FX forward contract where the current FX rate is the spot\_fx\_rate.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	1 unit of foreign in domestic	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-

#### forward

Calculate the FX Forward rate that makes the value of the FX contract equal to zero.

```
dom_discount_curve,
for_discount_curve):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	1 unit of foreign in domestic	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-

## \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\rm print}$

Simple print function for backward compatibility.

```
_print():
```

## 9.7 fx\_mkt\_conventions

## Enumerated Type: FinFXATMMethod

This enumerated type has the following values:

- SPOT
- FWD
- FWD\_DELTA\_NEUTRAL
- FWD\_DELTA\_NEUTRAL\_PREM\_ADJ

# Enumerated Type: FinFXDeltaMethod

This enumerated type has the following values:

- SPOT\_DELTA
- FORWARD\_DELTA
- SPOT\_DELTA\_PREM\_ADJ
- FORWARD\_DELTA\_PREM\_ADJ

## Class: FinFXRate()

class FinFXRate():

## **FinFXRate**

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
ccy1	-	-	-
ccy2	-	-	-
rate	-	-	-

# 9.8 fx\_one\_touch\_option

## Class: FXOneTouchOption(FXOption)

A FinFXOneTouchOption is an option in which the buyer receives one unit of currency if the FX rate touches a barrier at any time before the option expiry date and zero otherwise. The single barrier payoff must define whether the option pays or cancels if the barrier is touched and also when the payment is made (at hit time or option expiry). All of these variants are members of the FinTouchOptionTypes type.

# **FXOneTouchOption**

Create the one touch option by defining its expiry date and the barrier level and a payment size if it is a cash

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiry_dt	Date	-	-
option_type	TouchOptionTypes	-	-
barrier_rate	float	-	-
payment_size	float	-	1.0

#### value

FX One-Touch Option valuation using the Black-Scholes model assuming a continuous (American) barrier from value date to expiry. Handles both cash-or-nothing and asset-or-nothing options.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
spot_fx_rate	float or np.ndarray	-	-
dom_discount_curve	DiscountCurve	-	-
for_discount_curve	DiscountCurve	-	-
model	-	-	-

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## \_print

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

#### value\_mc

Touch Option valuation using the Black-Scholes model and Monte Carlo simulation. Accuracy is not great when compared to the analytical result as we only observe the barrier a finite number of times. The convergence is slow.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	Date	-	-
stock_price	float	-	-
domCurve	DiscountCurve	-	-
forCurve	DiscountCurve	-	-
model	-	-	-
num_paths	int	-	10000
num_steps_per_year	int	-	252
seed	int	-	4242

# \_barrier\_pay\_one\_at\_hit\_pv\_down

Pay \$1 if the stock crosses the barrier H from above. PV payment.

```
_barrier_pay_one_at_hit_pv_down(s, H, r, dt):
```

<b>Argument Name</b>	Type	Description	Default Value
S	-	-	-
Н	-	-	-
r	-	-	-
dt	-	-	-

## \_barrier\_pay\_one\_at\_hit\_pv\_up

Pay \$1 if the stock crosses the barrier H from below. PV payment.

```
_barrier_pay_one_at_hit_pv_up(s, H, r, dt):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
Н	-	-	-
r	-	-	-
dt	-	-	-

## \_barrier\_pay\_asset\_at\_expiry\_down\_out

Pay \$1 if the stock crosses the barrier H from above. PV payment.

```
_barrier_pay_asset_at_expiry_down_out(s, H):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
Н	-	-	-

# \_barrier\_pay\_asset\_at\_expiry\_up\_out

Pay \$1 if the stock crosses the barrier H from below. PV payment.

```
_barrier_pay_asset_at_expiry_up_out(s, H):
```

Argument Name	Type	Description	Default Value
S	-	-	-
Н	-	-	-

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# 9.9 fx\_option

Class: FXOption

#### delta

Calculate the option delta (FX rate sensitivity) by adding on a small bump and calculating the change in the option price.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
spot_fx_rate	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-

### gamma

Calculate the option gamma (delta sensitivity) by adding on a small bump and calculating the change in the option delta.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
spot_fx_rate	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-

#### vega

Calculate the option vega (volatility sensitivity) by adding on a small bump and calculating the change in the option price.

```
vega(value_dt, spot_fx_rate, discount_curve, dividend_curve, model):
```

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-

#### theta

Calculate the option theta (calendar time sensitivity) by moving forward one day and calculating the change in the option price.

```
theta(value_dt, spot_fx_rate, discount_curve, dividend_curve, model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
spot_fx_rate	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-

#### rho

Calculate the option rho (interest rate sensitivity) by perturbing the discount curve and revaluing.

```
rho(value_dt, spot_fx_rate, discount_curve, dividend_curve, model):
```

Argument Name	Type	Description	Default Value
value_dt	-	-	-
spot_fx_rate	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
model	-	-	-

# 9.10 fx\_rainbow\_option

## Enumerated Type: FXRainbowOptionTypes

This enumerated type has the following values:

- CALL\_ON\_MAXIMUM
- PUT\_ON\_MAXIMUM
- CALL\_ON\_MINIMUM
- PUT\_ON\_MINIMUM
- CALL\_ON\_NTH
- PUT\_ON\_NTH

## Class: FXRainbowOption(EquityOption)

class FXRainbowOption(EquityOption):

## **FXRainbowOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
expiry_dt	Date	-	-
payoff_type	FXRainbowOptionTypes	-	-
payoff_params	List[float]	-	-
num_assets	int	-	-

#### validate

#### PLEASE ADD A FUNCTION DESCRIPTION

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
stock_prices	-	-	-
dividend_yields	-	-	-
volatilities	-	-	-
betas	-	-	-

# $validate\_payoff$

#### PLEASE ADD A FUNCTION DESCRIPTION

```
validate_payoff(payoff_type, payoff_params, num_assets):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
payoff_type	-	-	-
payoff_params	-	-	-
num_assets	-	-	-

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

```
value(value_dt,
    stock_prices,
    dom_discount_curve,
    for_discount_curve,
    volatilities,
    betas):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_prices	-	-	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
volatilities	-	-	-
betas	-	-	-

#### value\_mc

#### PLEASE ADD A FUNCTION DESCRIPTION

Type	Description	Default Value
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	10000
-	-	4242
	Type	Type         Description           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -

# payoff\_value

#### PLEASE ADD A FUNCTION DESCRIPTION

```
payoff_value(s, payoff_typeValue, payoff_params):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
payoff_typeValue	-	-	-
payoff_params	-	-	-

## value\_mc\_fast

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
stock_prices	-	-	-
discount_curve	-	-	-
dividend_yields	-	-	-
volatilities	-	-	-
betas	-	-	-
num_assets	-	-	-
payoff_type	-	-	-
payoff_params	-	-	-
num_paths	-	-	10000
seed	-	-	4242

# 9.11 fx\_vanilla\_option

## Class: FXVanillaOption()

This is a class for an FX Option trade. It permits the user to calculate the price of an FX Option trade which can be expressed in a number of ways depending on the investor or hedgers currency. It aslo allows the calculation of the options delta in a number of forms as well as the various Greek risk sensitivies.

## **FXVanillaOption**

Create the FX Vanilla Option object. Inputs include expiry date, strike, currency pair, option type (call or put), notional and the currency of the notional. And adjustment for spot days is enabled. All currency rates must be entered in the price in domestic currency of one unit of foreign. And the currency pair should be in the form FORDOM where FOR is the foreign currency pair currency code and DOM is the same for the domestic currency.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
expiry_dt	Date	-	-
strike_fx_rate	float or np.ndarray	-	-
currency_pair	str	FORDOM	-
option_type	OptionTypes or list	-	-
notional	float	-	-
prem_currency	str	_	-
spot_days	int	-	0

#### value

This function calculates the value of the option using a specified model with the resulting value being in domestic i.e. ccy2 terms. Recall that Domestic = CCY2 and Foreign = CCY1 and FX rate is in price in domestic of one unit of foreign currency.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	1 unit of foreign in domestic	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-

# delta\_bump

Calculation of the FX option delta by bumping the spot FX rate by 1 cent of its value. This gives the FX spot delta. For speed we prefer to use the analytical calculation of the derivative given below.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
spot_fx_rate	-	-	-
ccy1DiscountCurve	-	-	-
ccy2DiscountCurve	-	-	-
model	-	-	-

## delta

Calculation of the FX Option delta. There are several definitions of delta and so we are required to return a dictionary of values. The definitions can be found on Page 44 of Foreign Exchange Option Pricing by Iain Clark, published by Wiley Finance.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	-	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-

#### fast\_delta

Calculation of the FX Option delta. Used in the determination of the volatility surface. Avoids discount curve interpolation so it should be slightly faster than the full calculation of delta.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
S	-	-	-
rd	-	-	-
rf	-	-	-
vol	-	-	-

### gamma

This function calculates the FX Option Gamma using the spot delta.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	value of a unit of foreign in domestic currency	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-

#### vega

This function calculates the FX Option Vega using the spot delta.

```
vega(value_dt,
     spot_fx_rate, # value of a unit of foreign in domestic currency
     dom_discount_curve,
     for_discount_curve,
     model):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	value of a unit of foreign in domestic currency	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-

#### theta

This function calculates the time decay of the FX option.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
spot_fx_rate	-	value of a unit of foreign in domestic currency	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-

# implied\_volatility

This function determines the implied volatility of an FX option given a price and the other option details. It uses a one-dimensional Newton root search algorith to determine the implied volatility.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_price	-	-	-
discount_curve	-	-	-
dividend_curve	-	-	-
price	-	-	-

#### value\_mc

Calculate the value of an FX Option using Monte Carlo methods. This function can be used to validate the risk measures calculated above or used as the starting code for a model exotic FX product that cannot be priced analytically. This function uses Numpy vectorisation for speed of execution.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
spot_fx_rate	-	-	-
dom_discount_curve	-	-	-
for_discount_curve	-	-	-
model	-	-	-
num_paths	-	-	10000
seed	-	-	4242

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## \_print

Simple print function for backward compatibility.

```
_print():
```

The function arguments are described in the following table.

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
f(volatility, *args):
```

Argument Name	Type	Description	<b>Default Value</b>
volatility	-	-	-
*args	-	-	-

## fvega

#### PLEASE ADD A FUNCTION DESCRIPTION

```
fvega(volatility, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	-	-	-
*args	-	-	-

## fast\_delta

Calculation of the FX Option delta. Used in the determination of the volatility surface. Avoids discount curve interpolation so it should be slightly faster than the full calculation of delta.

```
fast_delta(s, t, k, rd, rf, vol, deltaTypeValue, option_type_value):
```

Argument Name	Type	Description	Default Value
S	-	-	-
t	-	-	-
k	-	-	-
rd	-	-	-
rf	-	-	-
vol	-	-	-
deltaTypeValue	-	-	-
option_type_value	-	-	-

# 9.12 fx\_variance\_swap

# Class: FinFXVarianceSwap

## **FinFXVarianceSwap**

Create variance swap contract.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
effective_dt	Date	-	-
maturity_dt_or_tenor	[Date,str]	-	-
strike_variance	float	-	-
notional	float	-	ONE_MILLION
pay_strike_flag	bool	-	True

#### value

Calculate the value of the variance swap based on the realised volatility to the valuation date, the forward looking implied volatility to the maturity date using the libor discount curve.

```
value(value_dt,
    realisedVar,
    fair_strikeVar,
    libor_curve):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
realisedVar	-	-	-
fair_strikeVar	-	-	-
libor_curve	-	-	-

# $fair\_strike\_approx$

This is an approximation of the fair strike variance by Demeterfi et al. (1999) which assumes that sigma(K) = sigma(F) - b(K-F)/F where F is the forward stock price and sigma(F) is the ATM forward vol.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
fwdStockPrice	-	-	-
strikes	-	-	-
volatilities	-	-	-

### fair\_strike

Calculate the implied variance according to the volatility surface using a static replication methodology with a specially weighted portfolio of put and call options across a range of strikes using the approximate method set out by Demeterfi et al. 1999.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
stock_price	-	-	-
dividend_curve	-	-	-
volatility_curve	-	-	-
num_call_options	-	-	-
num_put_options	-	-	-
strike_spacing	-	-	-
discount_curve	-	-	-
use_forward	-	-	True

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
f(x): return (2.0/tmat)*((x-sstar)/sstar-np.log(x/sstar))
```

Argument Name	Type	Description	<b>Default Value</b>
x return (2.0/tmat)*((x-sstar)/sstar-np.log(x/sstar))	-	-	-

## realised\_variance

Calculate the realised variance according to market standard calculations which can either use log or percentage returns.

```
realised_variance(closePrices, useLogs=True):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
closePrices	-	-	-
useLogs	-	-	True

# print\_strikes

PLEASE ADD A FUNCTION DESCRIPTION

```
print_strikes():
```

9.13 \_\_init\_\_

# Chapter 10

# financepy.models

#### **Models**

#### Overview

This folder contains a range of models used in the various derivative pricing models implemented in the product folder. These include credit models for valuing portfolio credit products such as CDS Tranches, Monte-Carlo based models of stochastics processes used to value equity, FX and interest rate derivatives, and some generic implementations of models such as a tree-based Hull White model. Because the models are useful across a range of products, it is better to factor them out of the product/asset class categorisation as it avoids any unnecessary duplication.

In addition we seek to make the interface to these models rely only on fast types such as floats and integers and Numpy arrays.

These modules hold all of the models used by FinancePy across asset classes.

The general philosophy is to separate where possible product and models so that these models have as little product knowledge as possible.

Also, Numba is used extensively, resulting in code speedups of between x 10 and x 100.

# **Generic Arbitrage-Free Models**

There are the following arbitrage-free models:

- black is Black's model for pricing forward starting contracts (in the forward measure) assuming the forward is lognormally distributed.
- black\_shifted is Black's model for pricing forward starting contracts (in the forward measure) assuming the forward plus a shift is lognormally distributed. CHECK
- bachelier prices options assuming the underlying evolves according to a Gaussian (normal) process.
- sabr is a stochastic volatility model for forward values with a closed form approximate solution for the
  implied volatility. It is widely used for pricing European style interest rate options, specifically caps
  and floors and also swaptions.
- sabr\_shifted is a stochastic volatility model for forward value with a closed form approximate solution
  for the implied volatility. It is widely used for pricing European style interest rate options, specifically
  caps and floors and also swaptions.

The following asset-specific models have been implemented:

# **Equity Models**

- · heston\_model
- process\_simulator

#### **Interest Rate Models**

## **Equilibrium Rate Models**

There are two main short rate models.

- CIR is a short rate model where the randomness component is proportional to the square root of the short rate. This model implementation is not arbitrage-free across the term structure.
- Vasicek is a short rate model that assumes mean-reversion and normal volatility. It has a closed form solution for bond prices. It does not have the flexibility to fit a term structure of interest rates. For that you need to use the more flexible Hull-White model.

## Arbitrage Free Rate Models

- BKTree is a short rate model in which the log of the short rate follows a mean-reverting normal process. It refits the interest rate term structure. It is implemented as a trinomial tree and allows valuation of European and American-style rate-based options.
- HWTree is a short rate model in which the short rate follows a mean-reverting normal process. It fits the interest rate term structure. It is implemented as a trinomial tree and allows valuation of European and American-style rate-based options. It also implements Jamshidian's decomposition of the bond option for European options.

## **Credit Models**

- GaussianCopula1F is a Gaussian copula one-factor model. This class includes functions that calculate the portfolio loss distribution. This is numerical but deterministic.
- GaussianCopulaLHP is a Gaussian copula one-factor model in the limit that the number of credits tends to infinity. This is an asymptotic analytical solution.
- GaussianCopula is a Gaussian copula model which is multifactor model. It has a Monte-Carlo implementation.
- LossDbnBuilder calculates the loss distribution.
- MertonFirm is a model of the firm as proposed by Merton (1974).

#### **FX Models**

10.1. BACHELIER 383

## 10.1 bachelier

## Class: Bachelier()

Bacheliers Model which prices call and put options in the forward measure assuming the underlying rate follows a normal process.

#### **Bachelier**

Create FinModel black using parameters.

```
Bachelier(volatility):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
volatility	-	-	-

#### value

Price a call or put option using Bachelier's model.

```
value(forward_rate,  # Forward rate F
    strike_rate,  # Strike Rate K
    time_to_expiry,  # Time to Expiry (years)
    df,  # Discount Factor to expiry date
    call_or_put):  # Call or put
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
forward_rate	-	Forward rate F	-
strike_rate	-	Strike Rate K	-
time_to_expiry	-	Time to Expiry (years)	-
df	-	Discount Factor to expiry date	-
call_or_put	-	Call or put	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

## 10.2 bdt\_tree

Class: BDTTree()

class BDTTree():

## **BDTTree**

Constructs the Black-Derman-Toy rate model in the case when the volatility is assumed to be constant. The short rate process simplifies and is given by  $d(\log(r)) = theta(t) * dt + sigma * dW$ . Although

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
sigma	float	-	-
num_time_steps	int	-	100

## build\_tree

#### PLEASE ADD A FUNCTION DESCRIPTION

```
build_tree(treeMat, df_times, df_values):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
treeMat	-	-	-
df_times	-	-	-
df_values	-	-	-

## bond\_option

Value a bond option that can have European or American exercise using the Black-Derman-Toy model. The model uses a binomial tree.

10.2. BDT\_TREE 385

<b>Argument Name</b>	Type	Description	Default Value
t_exp	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_type	-	-	-

# $bermudan\_swaption$

Swaption that can be exercised on specific dates over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

```
bermudan_swaption(t_exp, tmat, strike, face_amount, cpn_times, cpn_flows, exercise_type):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t_exp	-	-	-
tmat	-	-	-
strike	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_type	-	-	-

# $callable\_puttable\_bond\_tree$

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
cpn_times	-	-	-
cpn_flows	-	-	-
call_times	-	-	-
call_prices	-	-	-
put_times	-	-	-
put_prices	-	-	-
face_amount	-	-	-

\_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# option\_exercise\_types\_to\_int

PLEASE ADD A FUNCTION DESCRIPTION

```
option_exercise_types_to_int(option_exercise_type):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
option_exercise_type	-	-	-

f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
f(x0, m, q_matrix, rt, df_end, dt, sigma):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
x0	-	-	-
m	-	-	-
q_matrix	-	-	-
rt	-	-	-
df_end	-	-	-
dt	-	-	-
sigma	-	-	-

#### search\_root

#### PLEASE ADD A FUNCTION DESCRIPTION

```
search_root(x0, m, q_matrix, rt, df_end, dt, sigma):
```

10.2. BDT\_TREE 387

Argument Name	Type	Description	<b>Default Value</b>
x0	-	-	-
m	-	-	-
q_matrix	-	-	-
rt	-	-	-
df_end	-	-	-
dt	-	-	-
sigma	-	-	-

# $bermudan\_swaption\_tree\_fast$

Option to enter into a swap that can be exercised on coupon payment dates after the start of the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
t_exp	-	-	-
tmat	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_type_int	-	-	-
_df_times	-	-	-
_df_values	-	-	-
_tree_times	-	-	-
_Q	-	-	-
_rt	-	-	-
_dt	-	-	-

# $american\_bond\_option\_tree\_fast$

Option to buy or sell bond at a specified strike price that can be exercised over the exercise period depending on choice of exercise type. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
t_exp	-	-	-
tmat	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_type_int	-	-	-
_df_times	-	-	-
_df_values	-	-	-
_tree_times	-	-	-
Q	-	-	-
rt	-	-	-
_dt	-	-	-

# $callable\_puttable\_bond\_tree\_fast$

Value a bond with embedded put and call options that can be exercised at any time over the specified list of put and call dates. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

10.2. BDT\_TREE 389

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
cpn_times	-	-	-
cpn_flows	-	-	-
call_times	-	-	-
call_prices	-	-	-
put_times	-	-	-
put_prices	-	-	-
face_amount	-	-	-
₋sigma	-	IS SIGMA USED ?	-
_a	-	IS SIGMA USED ?	-
_q_matrix	-	IS SIGMA USED ?	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
_rt	-	-	-
_dt	-	-	-
_tree_times	-	-	-
_df_times	-	-	-
_df_values	-	-	-

# build\_tree\_fast

#### PLEASE ADD A FUNCTION DESCRIPTION

```
build_tree_fast(sigma, tree_times, num_time_steps, discount_factors):
```

Argument Name	Type	Description	<b>Default Value</b>
sigma	-	-	-
tree_times	-	-	-
num_time_steps	-	-	-
discount_factors	-	-	-

## 10.3 bk\_tree

Class: BKTree()

class BKTree():

#### **BKTree**

Constructs the Black Karasinski rate model. The speed of mean reversion a and volatility are passed in. The short rate process is given by  $d(\log(r)) = (theta(t) - a*log(r))*dt + sigma*dW$ 

```
BKTree(sigma: float,
    a: float,
    num_time_steps: int = 100):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
sigma	float	-	-
a	float	-	-
num_time_steps	int	-	100

#### build\_tree

PLEASE ADD A FUNCTION DESCRIPTION

```
build_tree(tmat, df_times, df_values):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
tmat	-	-	-
df_times	-	-	-
df_values	-	-	-

# $bond\_option$

Value a bond option that has European or American exercise using the Black-Karasinski model. The model uses a trinomial tree.

10.3. BK\_TREE 391

Argument Name	Type	Description	<b>Default Value</b>
t_exp	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_type	-	-	-

## bermudan\_swaption

Swaption that can be exercised on specific dates over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

```
bermudan_swaption(t_exp, tmat, strike_price, face_amount, cpn_times, cpn_flows, exercise_type):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t_exp	-	-	-
tmat	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_type	-	-	-

# $callable\_puttable\_bond\_tree$

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
cpn_times	-	-	-
cpn_flows	-	-	-
call_times	-	-	-
call_prices	-	-	-
put_times	-	-	-
put_prices	-	-	-
face	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

The function arguments are described in the following table.

# option\_exercise\_types\_to\_int

PLEASE ADD A FUNCTION DESCRIPTION

option\_exercise\_types\_to\_int(optionExerciseType):

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
optionExerciseType	-	-	-

f

PLEASE ADD A FUNCTION DESCRIPTION

f(alpha, nm, Q, P, dX, dt, N):

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
nm	-	-	-
Q	-	-	-
P	-	-	-
dX	-	-	-
dt	-	-	-
N	-	-	-

# **fprime**

PLEASE ADD A FUNCTION DESCRIPTION

fprime(alpha, nm, Q, P, dX, dt, N):

10.3. BK\_TREE 393

Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
nm	-	-	-
Q	-	-	-
P	-	-	-
dX	-	-	-
dt	-	-	-
N	-	-	-

### search\_root

PLEASE ADD A FUNCTION DESCRIPTION

```
search_root(x0, nm, Q, P, dX, dt, N):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
x0	-	-	-
nm	-	-	-
Q	-	-	-
P	-	-	-
dX	-	-	-
dt	-	-	-
N	-	-	-

### search\_root\_deriv

PLEASE ADD A FUNCTION DESCRIPTION

```
search_root_deriv(x0, nm, Q, P, dX, dt, N):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
x0	-	-	-
nm	-	-	-
Q	-	-	-
P	-	-	-
dX	-	-	-
dt	-	-	-
N	-	-	-

# $bermudan\_swaption\_tree\_fast$

Option to enter into a swap that can be exercised on coupon payment dates after the start of the exercise

period. Due to multiple exercise times we need to extend tree out to bond maturity and take into account cash flows through time.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
t_exp	-	-	-
tmat	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_typeInt	-	-	-
_df_times	-	-	-
_df_values	-	-	-
_tree_times	-	-	-
_Q	-	-	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
_rt	-	-	-
_dt	-	-	-
_a	-	-	-

# american\_bond\_option\_tree\_fast

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

10.3. BK\_TREE 395

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-	-	-
-	-	-
	- - - - - - - - - - - -	

# $callable\_puttable\_bond\_tree\_fast$

Value a bond with embedded put and call options that can be exercised at any time over the specified list of put and call dates. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
cpn_times	-	-	-
cpn_flows	-	-	-
call_times	-	-	-
call_prices	-	-	-
put_times	-	-	-
put_prices	-	-	-
face_amount	-	-	-
₋sigma	-	IS SIGMA USED ?	-
_a	-	IS SIGMA USED ?	-
_Q	-	IS SIGMA USED ?	-
₋pu	-	-	-
_pm	-	-	-
_pd	-	-	-
_rt	-	-	-
_dt	-	-	-
_tree_times	-	-	-
_df_times	-	-	-
_df_values	_	-	-

# build\_tree\_fast

Calibrate the tree to a term structure of interest rates.

```
build_tree_fast(a, sigma, tree_times, num_time_steps, discount_factors):
```

Argument Name	Type	Description	Default Value
a	-	-	-
sigma	-	-	-
tree_times	-	-	-
num_time_steps	-	-	-
discount_factors	-	-	-

10.4. BLACK 397

### 10.4 black

### Enumerated Type: BlackTypes

This enumerated type has the following values:

- ANALYTICAL
- CRR\_TREE

### Class: Black()

Blacks Model which prices call and put options in the forward measure according to the Black-Scholes equation.

#### **Black**

Create FinModel black using parameters.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	-	-	-
implementation_type	-	-	BlackTypes.ANALYTICAL
num_steps	-	-	0

#### value

Price a derivative using Black's model which values in the forward measure following a change of measure.

```
value(forward_rate,  # Forward rate F
    strike_rate,  # Strike Rate K
    time_to_expiry,  # Time to Expiry (years)
    df,  # df RFR to expiry date
    option_type):  # Call or put
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
forward_rate	-	Forward rate F	-
strike_rate	-	Strike Rate K	-
time_to_expiry	-	Time to Expiry (years)	-
df	-	df RFR to expiry date	-
option_type	-	Call or put	-

#### delta

Calculate delta using Black's model which values in the forward measure following a change of measure.

```
delta(forward_rate,  # Forward rate F
    strike_rate,  # Strike Rate K
    time_to_expiry,  # Time to Expiry (years)
    df,  # RFR to expiry date
    option_type):  # Call or put
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
forward_rate	-	Forward rate F	-
strike_rate	-	Strike Rate K	-
time_to_expiry	-	Time to Expiry (years)	-
df	-	RFR to expiry date	-
option_type	-	Call or put	-

#### gamma

Calculate gamma using Black's model which values in the forward measure following a change of measure.

```
gamma(forward_rate, # Forward rate F
    strike_rate, # Strike Rate K
    time_to_expiry, # Time to Expiry (years)
    df, # RFR to expiry date
    option_type): # Call or put
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
forward_rate	-	Forward rate F	-
strike_rate	-	Strike Rate K	-
time_to_expiry	-	Time to Expiry (years)	-
df	-	RFR to expiry date	-
option_type	-	Call or put	-

#### theta

Calculate theta using Black's model which values in the forward measure following a change of measure.

```
theta(forward_rate,  # Forward rate F
    strike_rate,  # Strike Rate K
    time_to_expiry,  # Time to Expiry (years)
    df,  # Discount Factor to expiry date
    option_type):  # Call or put
```

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
forward_rate	-	Forward rate F	-
strike_rate	-	Strike Rate K	-
time_to_expiry	-	Time to Expiry (years)	-
df	-	Discount Factor to expiry date	-
option_type	-	Call or put	-

### vega

Calculate vega using Black's model which values in the forward measure following a change of measure.

```
vega(forward_rate,  # Forward rate F
    strike_rate,  # Strike Rate K
    time_to_expiry,  # Time to Expiry (years)
    df,  # df RFR to expiry date
    option_type):  # Call or put
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
forward_rate	-	Forward rate F	-
strike_rate	-	Strike Rate K	-
time_to_expiry	-	Time to Expiry (years)	-
df	-	df RFR to expiry date	-
option_type	-	Call or put	-

### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

# $_{\mathbf{f}}$ european

Function to determine ststar for pricing European options on future contracts.

```
_f_european(sigma, args):
```

Argument Name	Type	Description	<b>Default Value</b>
sigma	-	-	-
args	-	-	-

# \_f\_european\_vega

Function to calculate the Vega of European options on future contracts.

```
_f_european_vega(sigma, args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
sigma	-	-	-
args	-	-	-

### \_f\_american

Function to determine ststar for pricing American options on future contracts.

```
_f_american(sigma, args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
sigma	-	-	-
args	-	-	-

# \_f\_american\_vega

 $Function \ to \ calculate \ the \ Vega \ of \ American \ options \ on \ future \ contracts.$ 

```
_f_american_vega(sigma, args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
sigma	-	-	-
args	-	-	-

# $\_estimate\_vol\_from\_price$

PLEASE ADD A FUNCTION DESCRIPTION

```
_estimate_vol_from_price(fwd, t, k, european_option_type, european_price):
```

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Argument Name	Type	Description	<b>Default Value</b>
fwd	-	-	-
t	-	-	-
k	-	-	-
european_option_type	-	-	-
european_price	-	-	-

### black\_value

Price a derivative using Black model.

```
black_value(fwd, t, k, r, v, option_type):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
fwd	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
V	-	-	-
option_type	-	-	-

### black\_delta

Return delta of a derivative using Black model.

```
black_delta(fwd, t, k, r, v, option_type):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
fwd	-	-	-
t	-	-	-
k	-	_	-
r	-	-	-
v	-	-	-
option_type	-	-	-

# black\_gamma

Return gamma of a derivative using Black model.

```
black_gamma(fwd, t, k, r, v, option_type):
```

Argument Name	Type	Description	<b>Default Value</b>
fwd	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
V	-	-	-
option_type	-	-	-

# $black\_vega$

Return vega of a derivative using Black model.

```
black_vega(fwd, t, k, r, v, option_type):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
fwd	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
V	-	-	-
option_type	-	-	-

### black\_theta

Return theta of a derivative using Black model.

```
black_theta(fwd, t, k, r, v, option_type):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
fwd	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
V	-	-	-
option_type	-	-	-

### calculate\_d1\_d2

PLEASE ADD A FUNCTION DESCRIPTION

```
calculate_d1_d2(f, t, k, v):
```

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
f	-	-	-
t	-	-	-
k	-	-	-
V	-	-	-

# $implied\_volatility$

Calculate the Black implied volatility of a European/American options on futures contracts using Newton with a fallback to bisection.

```
implied_volatility(fwd, t, r, k, price, option_type, debug_print=True):
```

Argument Name	Type	Description	Default Value
fwd	-	-	-
t	-	-	-
r	-	-	-
k	-	-	-
price	-	-	-
option_type	-	-	-
debug_print	-	-	True

# 10.5 black\_scholes

# Enumerated Type: BlackScholesTypes

This enumerated type has the following values:

- DEFAULT
- ANALYTICAL
- CRR\_TREE
- BARONE\_ADESI
- LSMC
- Bjerksund\_Stensland
- FINITE\_DIFFERENCE
- PSOR

# Class: BlackScholes(Model)

class BlackScholes(Model):

### **BlackScholes**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	float or np.ndarray	-	-
bs_type	BlackScholesTypes	-	BlackScholesTypes.DEFAULT
num_steps_per_year	-	-	52
num_paths	-	-	10000
seed	-	-	42
use_sobol	-	-	False
params	-	-	None

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

```
dividend_rate: float,
option_type: OptionTypes):
```

Argument Name	Type	Description	Default Value
spot_price	float	-	-
time_to_expiry	float	-	-
strike_price	float	-	-
risk_free_rate	float	-	-
dividend_rate	float	-	-
option_type	OptionTypes	-	-

# 10.6 black\_scholes\_analytic

### bs\_value

Price a derivative using Black-Scholes model.

```
bs_value(s, t, k, r, q, v, option_type_value):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
v	-	-	-
option_type_value	-	-	-

### bs\_delta

Price a derivative using Black-Scholes model.

```
bs_delta(s, t, k, r, q, v, option_type_value):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
option_type_value	-	-	-

# bs\_gamma

Price a derivative using Black-Scholes model.

```
bs_gamma(s, t, k, r, q, v, option_type_value):
```

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
option_type_value	-	-	-

# $bs\_vega$

Price a derivative using Black-Scholes model.

```
bs_vega(s, t, k, r, q, v, option_type_value):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
option_type_value	-	-	-

### bs\_theta

Price a derivative using Black-Scholes model.

```
bs_theta(s, t, k, r, q, v, option_type_value):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
option_type_value	-	-	-

# bs\_rho

Price a derivative using Black-Scholes model.

```
bs_rho(s, t, k, r, q, v, option_type_value):
```

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
option_type_value	-	-	-

### bs\_vanna

Price a derivative using Black-Scholes model.

```
bs_vanna(s, t, k, r, q, v, option_type_value):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
option_type_value	-	-	-

### $\mathbf{f}$

### PLEASE ADD A FUNCTION DESCRIPTION

```
_f(sigma, args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
sigma	-	-	-
args	-	-	-

# \_fvega

PLEASE ADD A FUNCTION DESCRIPTION

```
_fvega(sigma, args):
```

Argument Name	Type	Description	Default Value
sigma	-	-	-
args	-	-	-

#### bs\_intrinsic

Calculate the Black-Scholes implied volatility of a European vanilla option using Newton with a fallback to bisection.

```
bs_intrinsic(s, t, k, r, q, option_type_value):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
option_type_value	-	-	-

# $bs\_implied\_volatility$

Calculate the Black-Scholes implied volatility of a European vanilla option using Newton with a fallback to bisection.

```
bs_implied_volatility(s, t, k, r, q, price, option_type_value):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
price	-	-	-
option_type_value	-	-	-

### \_fcall

Function to determine ststar for pricing American call options.

```
_fcall(si, *args):
```

Argument Name	Type	Description	Default Value
si	-	-	-
*args	-	-	-

# \_fput

Function to determine sstar for pricing American put options.

```
_fput(si, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
si	-	-	-
*args	-	-	-

#### baw\_value

American Option Pricing Approximation using the Barone-Adesi-Whaley approximation for the Black Scholes Model

```
baw_value(s, t, k, r, q, v, phi):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
phi	-	-	-

# $bjerksund\_stensland\_value$

Price American Option using the Bjerksund-Stensland approximation (1993) for the Black Scholes Model

```
bjerksund_stensland_value(s, t, k, r, q, v, option_type_value):
```

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
option_type_value	-	-	-

# 10.7 black\_scholes\_mc

# \_value\_mc\_nonumba\_nonumpy

PLEASE ADD A FUNCTION DESCRIPTION

```
_value_mc_nonumba_nonumpy(s, t, K, option_type, r, q, v, num_paths, seed, use_sobol):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
K	-	-	-
option_type	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-
use_sobol	-	-	-

# \_value\_mc\_numpy\_only

PLEASE ADD A FUNCTION DESCRIPTION

```
_value_mc_numpy_only(s, t, K, option_type, r, q, v, num_paths, seed, use_sobol):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
t	-	-	-
K	-	-	-
option_type	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-
use_sobol	-	-	-

# \_value\_mc\_numpy\_numba

PLEASE ADD A FUNCTION DESCRIPTION

```
_value_mc_numpy_numba(s, t, K, option_type, r, q, v, num_paths, seed, use_sobol):
```

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
K	-	-	-
option_type	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-
use_sobol	-	-	-

# \_value\_mc\_numba\_only

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_value_mc_numba_only(s, t, K, option_type, r, q, v, num_paths, seed, use_sobol):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
K	-	-	-
option_type	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-
use_sobol	-	-	-

# \_value\_mc\_numba\_parallel

#### PLEASE ADD A FUNCTION DESCRIPTION

```
_value_mc_numba_parallel(s, t, K, option_type, r, q, v, num_paths, seed, use_sobol):
```

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
K	-	-	-
option_type	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-
use_sobol	-	-	-

# 10.8 black\_scholes\_mc\_tests

### value\_mc1

PLEASE ADD A FUNCTION DESCRIPTION

```
value_mc1(s0, t, k, r, q, v, num_paths, seed):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
s0	-	-	-
t	-	-	-
k	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-

# value\_mc2

PLEASE ADD A FUNCTION DESCRIPTION

```
value_mc2(s0, t, K, r, q, v, num_paths, seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
s0	-	-	-
t	-	-	-
K	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-

### value\_mc3

PLEASE ADD A FUNCTION DESCRIPTION

```
value_mc3(s0, t, K, r, q, v, num_paths, seed):
```

Argument Name	Type	Description	<b>Default Value</b>
s0	-	-	-
t	-	-	-
K	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-

### value\_mc4

#### PLEASE ADD A FUNCTION DESCRIPTION

```
value_mc4(s0, t, K, r, q, v, num_paths, seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
s0	-	-	-
t	-	-	-
K	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
num_paths	-	-	-
seed	-	-	-

### value\_mc5

### PLEASE ADD A FUNCTION DESCRIPTION

```
value_mc5(s0, t, K, r, q, v, num_paths, seed):
```

Type	Description	Default Value
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-

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### 10.9 black\_shifted

### Class: BlackShifted()

Blacks Model which prices call and put options in the forward measure according to the Black-Scholes equation. This model also allows the distribution to be shifted to the negative in order to allow for negative interest rates.

#### **BlackShifted**

Create FinModel black using parameters.

```
BlackShifted(volatility, shift, implementation=0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	-	-	-
shift	-	-	-
implementation	-	-	0

#### value

Price a derivative using Black's model which values in the forward measure following a change of measure. The sign of the shift is the same as Matlab.

```
value(forward_rate,  # Forward rate
    strike_rate,  # Strike Rate
    time_to_expiry,  # time to expiry in years
    df,  # Discount Factor to expiry date
    call_or_put):  # Call or put
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
forward_rate	-	Forward rate	-
strike_rate	-	Strike Rate	-
time_to_expiry	-	time to expiry in years	-
df	-	Discount Factor to expiry date	-
call_or_put	-	Call or put	-

### \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

# 10.10 bond\_analytics

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### 10.11 cir\_mc

# Enumerated Type: CIRNumericalScheme

This enumerated type has the following values:

- EULER
- LOGNORMAL
- MILSTEIN
- KAHLJACKEL
- EXACT

Class: CIR\_MC()

class CIR\_MC():

#### **CIR\_MC**

PLEASE ADD A FUNCTION DESCRIPTION

```
CIR_MC(a, b, sigma):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
a	-	-	-
b	-	-	-
sigma	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

#### meanr

Mean value of a CIR process after time t

```
meanr(r0, a, b, t):
```

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
t	-	-	-

### variancer

Variance of a CIR process after time t

```
variancer(r0, a, b, sigma, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-

# zero\_price

Price of a zero coupon bond in CIR model.

```
zero_price(r0, a, b, sigma, t):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-

### draw

Draw a next rate from the CIR model in Monte Carlo.

```
draw(rt, a, b, sigma, dt):
```

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Argument Name	Type	Description	Default Value
rt	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
dt	-	-	-

# $rate\_path\_mc$

Generate a path of CIR rates using a number of numerical schemes.

```
rate_path_mc(r0, a, b, sigma, t, dt, seed, scheme):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-
dt	-	-	-
seed	-	-	-
scheme	-	-	-

# zero\_price\_mc

Determine the CIR zero price using Monte Carlo.

```
zero_price_mc(r0, a, b, sigma, t, dt, num_paths, seed, scheme):
```

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-
dt	-	-	-
num_paths	-	-	-
seed	-	-	-
scheme	-	-	-

# 10.12 equity\_barrier\_models

### value\_bs

This values a single option. Because of its structure it cannot easily be vectorised which is why it has been wrapped. # number of observations per year

```
value_bs(t, k, h, s, r, q, v, option_type, nobs):
```

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
k	-	-	-
h	-	-	-
S	-	-	-
r	-	-	-
q	-	-	-
V	-	-	-
option_type	-	-	-
nobs	-	-	-

# 10.13 equity\_crr\_tree

#### crr\_tree\_val

Value an American option using a Binomial Treee

```
crr_tree_val(stock_price,
    interest_rate, # continuously compounded
    dividend_rate, # continuously compounded
    volatility, # Black scholes volatility
    num_steps_per_year,
    time_to_expiry,
    option_type,
    strike_price,
    isEven):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
stock_price	-	-	-
interest_rate	-	continuously compounded	-
dividend_rate	-	continuously compounded	-
volatility	-	Black scholes volatility	-
num_steps_per_year	-	-	-
time_to_expiry	-	-	-
option_type	-	-	-
strike_price	-	-	-
isEven	-	-	-

# crr\_tree\_val\_avg

Calculate the average values off the tree using an even and an odd number of time steps.

Argument Name	Type	Description	<b>Default Value</b>
stock_price	-	-	-
interest_rate	-	continuously compounded	-
dividend_rate	-	continuously compounded	-
volatility	-	Black scholes volatility	-
num_steps_per_year	-	-	-
time_to_expiry	-	-	-
option_type	-	-	-
strike_price	-	-	-

# 10.14 equity\_lsmc

# Enumerated Type: FIT\_TYPES

This enumerated type has the following values:

- HERMITE\_E
- LAGUERRE
- HERMITE
- LEGENDRE
- CHEBYCHEV
- POLYNOMIAL

# equity\_lsmc

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
spot_price	-	-	-
risk_free_rate	-	-	-
dividend_yield	-	-	-
sigma	-	-	-
num_paths	-	-	-
num_steps_per_year	-	-	-
time_to_expiry	-	-	-
option_type_value	-	-	-
strike_price	-	-	-
poly_degree	-	-	-
fit_type_value	-	-	-
use_sobol	-	-	-
seed	-	-	-

# 10.15 finite\_difference

#### dx

PLEASE ADD A FUNCTION DESCRIPTION

dx(x, wind=0):

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	-	-	-
wind	-	-	0

### dxx

PLEASE ADD A FUNCTION DESCRIPTION

dxx(x):

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	-	-	-

#### calculate fd matrix

1d finite difference solution for pdes of the form  $0 = dV/dt + AVA = -risk\_free\_rate + mu d/dx + 1/2 var d2/dx2 using the theta scheme [1-theta dt A] <math>V(t) = [1 + (1-theta) dt A] V(t+dt)$ 

calculate\_fd\_matrix(x, r, mu, var, dt, theta, wind=0):

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	-	-	-
r	-	-	-
mu	-	-	-
var	-	-	-
dt	-	-	-
theta	-	-	-
wind	-	-	0

### fd\_roll\_backwards

PLEASE ADD A FUNCTION DESCRIPTION

```
fd_roll_backwards(res, theta, Ai=None, Ae=None):
```

Argument Name	Type	Description	<b>Default Value</b>
res	-	-	-
theta	-	-	-
Ai	-	-	None
Ae	-	-	None

# fd\_roll\_forwards

### PLEASE ADD A FUNCTION DESCRIPTION

```
fd_roll_forwards(res, theta, Ai=None, Ae=None):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
res	-	-	-
theta	-	-	-
Ai	-	-	None
Ae	-	-	None

# $smooth\_digital$

#### PLEASE ADD A FUNCTION DESCRIPTION

```
smooth_digital(xl, xu, strike):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
xl	-	-	-
xu	-	-	-
strike	-	-	-

# digital

#### PLEASE ADD A FUNCTION DESCRIPTION

```
digital(x, strike):
```

Argument Name	Type	Description	Default Value
X	-	-	-
strike	-	-	-

## smooth\_call

#### PLEASE ADD A FUNCTION DESCRIPTION

```
smooth_call(xl, xu, strike):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
xl	-	-	-
xu	-	-	-
strike	-	-	-

# option\_payoff

#### PLEASE ADD A FUNCTION DESCRIPTION

```
option_payoff(s, strike, smooth, dig, option_type):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
strike	-	-	-
smooth	-	-	-
dig	-	-	-
option_type	-	-	-

#### black\_scholes\_fd

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
spot_price	-	-	-
volatility	-	-	-
time_to_expiry	-	-	-
strike_price	-	-	-
risk_free_rate	-	-	-
dividend_yield	-	-	-
option_type	-	-	-
num_time_steps	-	-	None
num_samples	-	-	2000
num_std	-	-	5
theta	-	-	0.5
wind	-	-	0
digital	-	-	False
smooth	-	-	False
update	-	-	False

### 10.16 finite\_difference\_PSOR

#### black\_scholes\_fd\_PSOR

Solve Black-Scholes equation using projected successive over-relaxtion. Parameters: acc: Keep iterating until this accuracy is achieved d\_omega: Larger numbers lead to bigger changes in omega with each iteration max\_iter: Maximum number of iterations in PSOR step. Set to 0 to allow any number of iterations.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
spot_price	-	-	-
volatility	-	-	-
time_to_expiry	-	-	-
strike_price	-	-	-
risk_free_rate	-	-	-
dividend_yield	-	-	-
option_type	-	-	-
num_time_steps	-	-	None
num_samples	-	-	2000
num_std	-	-	5
theta	-	-	0.5
wind	-	-	0
digital	-	-	False
smooth	-	-	False
acc	-	-	1e-13
d_omega	-	-	5e-5
max_iter	-	-	0

#### PSOR\_roll\_backwards

PLEASE ADD A FUNCTION DESCRIPTION

```
PSOR_roll_backwards(Ae, Ai, res_k, omega, acc=1e-13, max_iter=0):
```

Argument Name	Type	Description	<b>Default Value</b>
Ae	-	-	-
Ai	-	-	-
res_k	-	-	-
omega	-	-	-
acc	-	-	1e-13
max_iter	-	-	0

#### **PSOR**

Projected Successive Over Relaxation - Parameters: Ai (np.array): Implicit finite difference matrix omega (float): Number between 1 and 2 weighted average of previous and current iteration initial\_value (np.array): Vector produced by previous iteration z\_ip1 (matrix): Matrix for updating to next timestep max\_iter (int): Maximum number of iterations before raising an error # (max\_iter=0 means no maximum) acc (float): Accuracy. The maximum acceptable square difference # between two iterations Returns: res\_k (np.array): Vector for next time step nloops: Number of iterations required to achieve required accuracy

```
PSOR(Ai, omega, initial_value, z_ip1, max_iter=0, acc=1e-13):
```

Argument Name	Type	Description	<b>Default Value</b>
Ai	-	-	-
omega	-	-	-
initial_value	-	-	-
z_ip1	-	-	-
max_iter	-	-	0
acc	-	-	1e-13

# 10.17 gauss\_copula

# $default\_times\_gc$

Generate a matrix of default times by credit and trial using a Gaussian copula model using a full rank correlation matrix.

Argument Name	Type	Description	Default Value
issuer_curves	-	-	-
correlation_matrix	-	-	-
num_trials	-	-	-
seed	-	-	-

# 10.18 gauss\_copula\_lhp

## tr\_surv\_prob\_lhp

Get the approximated tranche survival probability of a portfolio of credits in the one-factor GC model using the large portfolio limit which assumes a homogenous portfolio with an infinite number of credits. This approach is very fast but not so as accurate as the adjusted binomial.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
num_credits	-	-	-
survival_probs	-	-	-
recovery_rates	-	-	-
beta	-	-	-

# portfolio\_cdf\_lhp

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
num_credits	-	-	-
qvector	-	-	-
recovery_rates	-	-	-
beta	-	-	-
num_points	-	-	-

## exp\_min\_lk

PLEASE ADD A FUNCTION DESCRIPTION

```
exp_min_lk(k, p, r, n, beta):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
р	-	-	-
r	-	-	-
n	-	-	-
beta	-	-	-

# lhp\_density

PLEASE ADD A FUNCTION DESCRIPTION

```
lhp_density(k, p, r, beta):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
p	-	-	-
r	-	-	-
beta	-	-	-

# $lhp\_analytical\_density\_base\_corr$

PLEASE ADD A FUNCTION DESCRIPTION

```
lhp_analytical_density_base_corr(k, p, r, beta, dbeta_dk):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
k	-	-	-
р	-	-	-
r	-	-	-
beta	-	-	-
dbeta_dk	-	-	-

# lhp\_analytical\_density

PLEASE ADD A FUNCTION DESCRIPTION

```
lhp_analytical_density(k, p, r, beta):
```

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
p	-	-	-
r	-	-	-
beta	-	-	-

# $exp\_min\_lk$

PLEASE ADD A FUNCTION DESCRIPTION

```
exp_min_lk(k, p, r, n, beta):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
p	-	-	-
r	-	-	-
n	-	-	-
beta	-	-	-

# prob\_l\_greater\_than\_k

PLEASE ADD A FUNCTION DESCRIPTION

```
prob_l_greater_than_k(K, P, R, beta):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
K	-	-	-
P	-	-	-
R	-	-	-
beta	-	-	-

# 10.19 gauss\_copula\_lhplus

## Class: LHPlusModel()

Large Homogenous Portfolio model with extra asset. Used for approximating full Gaussian copula.

## LHPlusModel

PLEASE ADD A FUNCTION DESCRIPTION

```
LHPlusModel(P, R, H, beta, P0, R0, H0, beta0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
P	-	-	-
R	-	-	-
Н	-	-	-
beta	-	-	-
P0	-	-	-
R0	-	-	-
Н0	-	-	-
beta0	-	-	-

## prob\_loss\_gt\_k

Returns  $P(L_{\zeta}K)$  where L is the portfolio loss given by model.

```
prob_loss_gt_k(K):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
K	-	-	-

# exp\_min\_lk\_integral

PLEASE ADD A FUNCTION DESCRIPTION

```
exp_min_lk_integral(K, dK):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
K	-	-	-
dK	-	-	-

# exp\_min\_lk

PLEASE ADD A FUNCTION DESCRIPTION

exp\_min\_lk(K):

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
K	-	-	-

# $exp\_min\_lk2$

PLEASE ADD A FUNCTION DESCRIPTION

exp\_min\_lk2(K):

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
K	-	-	-

# $tranche\_survival\_prob$

PLEASE ADD A FUNCTION DESCRIPTION

tranche\_survival\_prob(k1, k2):

Argument Name	Type	Description	Default Value
k1	-	-	-
k2	-	-	-

# 10.20 gauss\_copula\_onefactor

## loss\_dbn\_recursion\_gcd

Full construction of the loss distribution of a portfolio of credits where losses have been calculate as number of units based on the GCD.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
num_credits	-	-	-
default_probs	-	-	-
loss_units	-	-	-
beta_vector	-	-	-
num_integration_steps	-	-	-

### homog\_basket\_loss\_dbn

Calculate the loss distribution of a CDS default basket where the portfolio is equally weighted and the losses in the portfolio are homo-geneous i.e. the credits have the same recovery rates.

```
homog_basket_loss_dbn(survival_probs,
recovery_rates,
beta_vector,
num_integration_steps):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
survival_probs	-	-	-
recovery_rates	-	-	-
beta_vector	-	-	-
num_integration_steps	-	-	-

# $tranche\_surv\_prob\_recursion$

Get the tranche survival probability of a portfolio of credits in the one-factor GC model using a full recursion calculation of the loss distribution and survival probabilities to some time horizon.

```
recovery_rates,
beta_vector,
num_integration_steps):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
num_credits	-	-	-
survival_probs	-	-	-
recovery_rates	-	-	-
beta_vector	-	-	-
num_integration_steps	-	-	-

## gauss\_approx\_tranche\_loss

PLEASE ADD A FUNCTION DESCRIPTION

```
gauss_approx_tranche_loss(k1, k2, mu, sigma):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
mu	-	-	-
sigma	-	-	-

# $tranch\_surv\_prob\_gaussian$

Get the approximated tranche survival probability of a portfolio of credits in the one-factor GC model using a Gaussian fit of the conditional loss distribution and survival probabilities to some time horizon. Note that the losses in this fit are allowed to be negative.

Argument Name	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
num_credits	-	-	-
survival_probs	-	-	-
recovery_rates	-	-	-
beta_vector	-	-	-
num_integration_steps	-	-	-

## loss\_dbn\_hetero\_adj\_binomial

Get the portfolio loss distribution using the adjusted binomial approximation to the conditional loss distribution.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
num_credits	-	-	-
default_probs	-	-	-
loss_ratio	-	-	-
beta_vector	-	-	-
num_integration_steps	-	-	-

# $tranche\_surv\_prob\_adj\_binomial$

Get the approximated tranche survival probability of a portfolio of credits in the one-factor GC model using the adjusted binomial fit of the conditional loss distribution and survival probabilities to some time horizon. This approach is both fast and highly accurate.

Argument Name	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
num_credits	-	-	-
survival_probs	-	-	-
recovery_rates	-	-	-
beta_vector	-	-	-
num_integration_steps	-	-	-

# 10.21 gbm\_process\_simulator

### Class: FinGBMProcess()

class FinGBMProcess():

### get\_paths

Get a matrix of simulated GBM asset values by path and time step. Inputs are the number of paths and time steps, the time horizon and the initial asset value, volatility and random number seed.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
num_paths	int	-	-
num_time_steps	int	-	-
t	float	-	-
mu	float	-	-
stock_price	float	-	-
volatility	float	-	-
seed	int	-	-

# $get\_paths\_assets$

Get a matrix of simulated GBM asset values by asset, path and time step. Inputs are the number of assets, paths and time steps, the time-horizon and the initial asset values, volatilities and betas.

Argument Name	Type	Description	Default Value
num_assets	-	-	-
num_paths	-	-	-
num_time_steps	-	-	-
t	-	-	-
mus	-	-	-
stock_prices	-	-	-
volatilities	-	-	-
corr_matrix	-	-	-
seed	-	-	-

## get\_paths

Get the simulated GBM process for a single asset with many paths and time steps. Inputs include the number of time steps, paths, the drift mu, stock price, volatility and a seed.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
num_paths	-	-	-
num_time_steps	-	-	-
t	-	-	-
mu	-	-	-
stock_price	-	-	-
volatility	-	-	-
seed	-	-	-

# $get\_paths\_assets$

Get the simulated GBM process for a number of assets and paths and num time steps. Inputs include the number of assets, paths, the vector of mus, stock prices, volatilities, a correlation matrix and a seed.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
num_assets	-	-	-
num_paths	-	-	-
num_time_steps	-	-	-
t	-	-	-
mus	-	-	-
stock_prices	-	-	-
volatilities	-	-	-
corr_matrix	-	-	-
seed	-	-	-

# $get\_assets$

Get the simulated GBM process for a number of assets and paths for one time step. Inputs include the number of assets, paths, the vector of mus, stock prices, volatilities, a correlation matrix and a seed.

Argument Name	Type	Description	Default Value
num_assets	-	-	-
num_paths	-	-	-
t	-	-	-
mus	-	-	-
stock_prices	-	-	-
volatilities	-	-	-
corr_matrix	-	-	-
seed	-	-	-

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## 10.22 heston

## Enumerated Type: HestonNumericalScheme

This enumerated type has the following values:

- EULER
- EULERLOG
- QUADEXP

## Class: Heston()

class Heston():

### Heston

#### PLEASE ADD A FUNCTION DESCRIPTION

```
Heston(v0, kappa, theta, sigma, rho):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
v0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
rho	-	-	-

#### value\_mc

#### PLEASE ADD A FUNCTION DESCRIPTION

<b>Argument Name</b>	Type	Description	Default Value
value_dt	-	-	-
option	-	-	-
stock_price	-	-	-
interest_rate	-	-	-
dividend_yield	-	-	-
num_paths	-	-	-
num_steps_per_year	-	-	-
seed	-	-	-
scheme	-	-	HestonNumericalScheme.EULERLOG

## value\_lewis

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
option	-	-	-
stock_price	-	-	-
interest_rate	-	-	-
dividend_yield	-	-	-

### phi

#### PLEASE ADD A FUNCTION DESCRIPTION

```
phi(k_in,):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k_in	-	-	-

# phi\_transform

#### PLEASE ADD A FUNCTION DESCRIPTION

```
phi_transform(x):
```

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The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	-	-	-

# integrand

PLEASE ADD A FUNCTION DESCRIPTION

```
integrand(k): return 2.0 * np.real(np.exp(-1j * k * x)
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
---------------	------	-------------	----------------------

#### value\_lewis\_rouah

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
value_dt	-	-	-
option	-	-	-
stock_price	-	-	-
interest_rate	-	-	-
dividend_yield	-	-	-

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
f(k_in):
```

<b>Argument Name</b>	Type	Description	Default Value
k_in	-	-	-

## value\_weber

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
value_dt	-	-	-
option	-	-	-
stock_price	-	_	-
interest_rate	-	-	-
dividend_yield	-	-	-

### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
f(s, b):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
S	-	-	-
b	-	-	-

## integrand

#### PLEASE ADD A FUNCTION DESCRIPTION

```
integrand(u):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
u	-	-	-

# value\_gatheral

#### PLEASE ADD A FUNCTION DESCRIPTION

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```
stock_price,
interest_rate,
dividend_yield):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
value_dt	-	-	-
option	-	-	-
stock_price	-	-	-
interest_rate	-	-	-
dividend_yield	-	-	-

## ff

#### PLEASE ADD A FUNCTION DESCRIPTION

```
ff(j):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
j	-	-	-

# integrand

#### PLEASE ADD A FUNCTION DESCRIPTION

```
integrand(u):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
u	-	-	-

# get\_paths

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
s0	-	-	-
r	-	-	-
q	-	-	-
v0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-
dt	-	-	-
num_paths	-	-	-
seed	-	-	-
scheme	-	-	-

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#### 10.23 hw tree

### Enumerated Type: FinHWEuropeanCalcType

This enumerated type has the following values:

- JAMSHIDIAN
- EXPIRY\_ONLY
- EXPIRY\_TREE

### Class: HWTree()

class HWTree():

#### **HWTree**

Constructs the Hull-White rate model. The speed of mean reversion a and volatility are passed in. The short rate process is given by dr = (theta(t) - ar) \* dt + sigma \* dW. The model will switch to use Jamshidian's approach where possible unless the useJamshidian flag is set to false in which case it uses the trinomial Tree.

```
HWTree(sigma,
    a,
    num_time_steps=100,
    europeanCalcType=FinHWEuropeanCalcType.EXPIRY_TREE):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
sigma	-	-	-
a	-	-	-
num_time_steps	-	-	100
europeanCalcType	-	-	EXPIRY_TREE

### option\_on\_zcb

Price an option on a zero coupon bond using analytical solution of Hull-White model. User provides bond face and option strike and expiry date and maturity date.

Argument Name	Type	Description	Default Value
t_exp	-	-	-
tmat	-	-	-
strike	-	-	-
face_amount	-	-	-
df_times	-	-	-
df_values	-	-	-

## european\_bond\_option\_jamshidian

Valuation of a European bond option using the Jamshidian deconstruction of the bond into a strip of zero coupon bonds with the short rate that would make the bond option be at the money forward.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t_exp	-	-	-
strike_price	-	-	-
face	-	-	-
cpn_times	-	-	-
cpn_amounts	-	-	-
df_times	-	-	-
df_values	-	-	-

## european\_bond\_option\_expiry\_only

Price a European option on a coupon-paying bond using a tree to generate short rates at the expiry date and then to use the analytical solution of zero coupon bond prices in the HW model to calculate the corresponding bond price. User provides bond object and option details.

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<b>Argument Name</b>	Type	Description	Default Value
t_exp	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_amounts	-	-	-

# option\_on\_zero\_coupon\_bond\_tree

Price an option on a zero coupon bond using a HW trinomial tree. The discount curve was already supplied to the tree build.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
t_exp	-	-	-
tmat	-	-	-
strike_price	-	-	-
face_amount	-	-	-

## bermudan\_swaption

Swaption that can be exercised on specific dates over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

```
bermudan_swaption(t_exp, tmat, strike, face, cpn_times, cpn_flows, exercise_type):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t_exp	-	-	-
tmat	-	-	-
strike	-	-	-
face	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_type	-	-	-

# $bond\_option$

Value a bond option that can have European or American exercise. This is done using a trinomial tree that

we extend out to bond maturity. For European bond options, Jamshidian's model is faster and is used instead i.e. not this function.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
t_exp	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_type	-	-	-

## $callable\_puttable\_bond\_tree$

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
cpn_times	-	-	-
cpn_flows	-	-	-
call_times	-	-	-
call_prices	-	-	-
put_times	-	-	-
put_prices	-	-	-
face_amount	-	-	-

#### df\_tree

Discount factor as seen from now to time tmat as long as the time is on the tree grid.

```
df_tree(tmat):
```

Argument Name	Type	Description	Default Value
tmat	-	-	-

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#### build\_tree

Build the trinomial tree.

```
build_tree(treeMat, df_times, df_values):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
treeMat	-	-	-
df_times	-	-	-
df_values	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

## option\_exercise\_types\_to\_int

PLEASE ADD A FUNCTION DESCRIPTION

```
option_exercise_types_to_int(optionExerciseType):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
optionExerciseType	-	-	-

## p\_fast

Forward discount factor as seen at some time t which may be in the future for payment at time T where Rt is the delta-period short rate seen at time t and pt is the discount factor to time t, ptd is the one period discount factor to time t+dt and pT is the discount factor from now until the payment of the 1 dollar of the discount factor.

```
p_fast(t, T, Rt, delta, pt, ptd, pT, _sigma, _a):
```

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
T	-	-	-
Rt	-	-	-
delta	-	-	-
pt	-	-	-
ptd	-	-	-
pT	-	-	-
_sigma	-	-	-
_a	-	-	-

### build\_tree\_fast

Fast tree construction using Numba.

```
build_tree_fast(a, sigma, tree_times, num_time_steps, discount_factors):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
a	-	-	-
sigma	-	-	-
tree_times	-	-	-
num_time_steps	-	-	-
discount_factors	-	-	-

# american\_bond\_option\_tree\_fast

Value an option on a bond with coupons that can have European or American exercise. Some minor issues to do with handling coupons on the option expiry date need to be solved.

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Argument Name	Type	Description	<b>Default Value</b>
t_exp	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_amounts	-	-	-
exercise_typeInt	-	-	-
_sigma	-	-	-
_a	-	-	-
_Q	-	-	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
_rt	-	-	-
_dt	-	-	-
_tree_times	-	-	-
_df_times	-	_	-
_df_values	-	-	-

# $bermudan\_swaption\_tree\_fast$

Option to enter into a swap that can be exercised on coupon payment dates after the start of the exercise period. Due to multiple exercise times we need to extend tree out to bond maturity and take into account cash flows through time.

```
bermudan_swaption_tree_fast(t_exp, tmat, strike_price, face_amount, cpn_times, cpn_flows, exercise_typeInt, __df_times, __df_values, __tree_times, _Q, _pu, _pm, _pd, _rt, _dt, _a):
```

Argument Name	Type	Description	<b>Default Value</b>
t_exp	-	-	-
tmat	-	-	-
strike_price	-	-	-
face_amount	-	-	-
cpn_times	-	-	-
cpn_flows	-	-	-
exercise_typeInt	-	-	-
_df_times	-	-	-
_df_values	-	-	-
_tree_times	-	-	-
Q	-	-	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
rt	-	-	-
_dt	-	-	-
_a	-	-	-

# $callable\_puttable\_bond\_tree\_fast$

Value an option on a bond with coupons that can have European or American exercise. Some minor issues to do with handling coupons on the option expiry date need to be solved.

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# $fwd\_dirty\_bond\_price$

Price a coupon bearing bond on the option expiry date and return the difference from a strike price. This is used in a root search to find the future expiry time short rate that makes the bond price equal to the option strike price. It is a key step in the Jamshidian bond decomposition approach. The strike is a clean price.

```
fwd_dirty_bond_price(rt, *args):
```

Argument Name	Type	Description	Default Value
rt	-	-	-
*args	-	-	-

### 10.24 Imm mc

### Enumerated Type: ModelLMMModelTypes

This enumerated type has the following values:

- LMM\_ONE\_FACTOR
- LMM\_HW\_M\_FACTOR
- LMM\_FULL\_N\_FACTOR

## lmm\_print\_forwards

Helper function to display the simulated Ibor rates.

```
lmm_print_forwards(fwds):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
fwds	-	-	-

## $lmm\_swaption\_vol\_approx$

Implements Rebonato's approximation for the swap rate volatility to be used when pricing a swaption that expires in period a for a swap maturing at the end of period b taking into account the forward volatility term structure (zetas) and the forward-forward correlation matrix rho..

```
lmm_swaption_vol_approx(a, b, fwd0, taus, zetas, rho):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
fwd0	-	-	-
taus	-	-	-
zetas	-	-	-
rho	-	-	-

## lmm\_sim\_swaption\_vol

Calculates the swap rate volatility using the forwards generated in the simulation to see how it compares to Rebonatto estimate.

```
lmm_sim_swaption_vol(a, b, fwd0, fwds, taus):
```

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Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

#### lmm\_fwd\_fwd\_correlation

Extract forward forward correlation matrix at some future time index from the simulated forward rates and return the matrix.

```
lmm_fwd_fwd_correlation(numForwards, num_paths, i_time, fwds):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numForwards	-	-	-
num_paths	-	-	-
i_time	-	-	-
fwds	-	-	-

## lmm\_price\_caps\_black

Price a strip of capfloorlets using Black's model using the time grid of the LMM model. The prices can be compared with the LMM model prices.

```
lmm_price_caps_black(fwd0, volCaplet, p, K, taus):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
fwd0	-	-	-
volCaplet	-	-	-
p	-	-	-
K	-	-	-
taus	-	-	-

#### sub\_matrix

Returns a submatrix of correlation matrix at later time step in the LMM simulation which is then used to generate correlated Gaussian RVs.

```
sub_matrix(t, N):
```

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
N	-	-	-

### cholesky\_np

Numba-compliant wrapper around Numpy cholesky function.

```
cholesky_np(rho):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
rho	-	-	-

### lmm\_simulate\_fwds\_nf

Full N-Factor Arbitrage-free simulation of forward Ibor discount in the spot measure given an initial forward curve, volatility term structure and full rank correlation structure. Cholesky decomposition is used to extract the factor weights. The number of forwards at time 0 is given. The 3D matrix of forward rates by path, time and forward point is returned. WARNING: NEED TO CHECK THAT CORRECT VOLATILITY IS BEING USED (OFF BY ONE BUG NEEDS TO BE RULED OUT)

```
lmm_simulate_fwds_nf(num_fwds, num_paths, fwd0, zetas, correl, taus, seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
num_fwds	-	-	-
num_paths	-	-	-
fwd0	-	-	-
zetas	-	-	-
correl	-	-	-
taus	-	-	-
seed	-	<u>-</u>	<del>-</del>

#### lmm\_simulate\_fwds\_1f

One factor Arbitrage-free simulation of forward Ibor discount in the spot measure following Hull Page 768. Given an initial forward curve, volatility term structure. The 3D matrix of forward rates by path, time and forward point is returned. This function is kept mainly for its simplicity and speed. NB: The Gamma volatility has an initial entry of zero. This differs from Hull's indexing by one and so is why I do not subtract 1 from the index as Hull does in his equation 32.14. The Number of Forwards is the number of points on the initial curve to the trade maturity date. But be careful: a cap that matures in 10 years with quarterly caplets has 40 forwards BUT the last forward to reset occurs at 9.75 years. You should not simulate beyond this time. If you give the model 10 years as in the Hull examples, you need to simulate 41 (or in this case 11) forwards as the final cap or ratchet has its reset in 10 years.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
num_fwds	-	-	-
num_paths	-	-	-
numeraireIndex	-	-	-
fwd0	-	-	-
gammas	-	-	-
taus	-	-	-
use_sobol	-	-	-
seed	-	-	-

#### lmm simulate fwds mf

Multi-Factor Arbitrage-free simulation of forward Ibor discount in the spot measure following Hull Page 768. Given an initial forward curve, volatility factor term structure. The 3D matrix of forward rates by path, time and forward point is returned.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
num_fwds	-	-	-
numFactors	-	-	-
num_paths	-	-	-
numeraireIndex	-	-	-
fwd0	-	-	-
lambdas	-	-	-
taus	-	-	-
use_sobol	-	-	-
seed	-	-	-

## lmm\_cap\_flr\_pricer

Function to price a strip of cap or floorlets in accordance with the simulated forward curve dynamics.

```
lmm_cap_flr_pricer(num_fwds, num_paths, K, fwd0, fwds, taus, isCap):
```

Argument Name	Type	Description	<b>Default Value</b>
num_fwds	-	-	-
num_paths	-	-	-
K	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-
isCap	-	-	-

### lmm\_swap\_pricer

Function to reprice a basic swap using the simulated forward Ibors.

```
lmm_swap_pricer(cpn, num_periods, num_paths, fwd0, fwds, taus):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
cpn	-	-	-
num_periods	-	-	-
num_paths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

### lmm\_swaption\_pricer

Function to price a European swaption using the simulated forward discount.

```
lmm_swaption_pricer(strike, a, b, num_paths, fwd0, fwds, taus, isPayer):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
strike	-	-	-
a	-	-	-
b	-	-	-
num_paths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-
isPayer	-	-	-

# $lmm\_ratchet\_caplet\_pricer$

Price a ratchet using the simulated Ibor rates.

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```
lmm_ratchet_caplet_pricer(spd, num_periods, num_paths, fwd0, fwds, taus):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
spd	-	-	-
num_periods	-	-	-
num_paths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

### lmm\_flexi\_cap\_pricer

Price a flexicap using the simulated Ibor rates.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
maxCaplets	-	-	-
K	-	-	-
num_periods	-	-	-
num_paths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

## lmm\_sticky\_caplet\_pricer

Price a sticky cap using the simulated Ibor rates.

```
lmm_sticky_caplet_pricer(spread, num_periods, num_paths, fwd0, fwds, taus):
```

Argument Name	Type	Description	Default Value
spread	-	-	-
num_periods	-	-	-
num_paths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

## 10.25 loss\_dbn\_builder

### indep\_loss\_dbn\_heterogeneous\_adj\_binomial

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
num_credits	-	-	-
cond_probs	-	-	-
loss_ratio	-	-	-

### portfolio\_gcd

PLEASE ADD A FUNCTION DESCRIPTION

```
portfolio_gcd(actual_losses):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
actual_losses	-	-	-

## $indep\_loss\_dbn\_recursion\_gcd$

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
num_credits	-	-	-
cond_default_probs	-	-	-
loss_units	-	-	-

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#### 10.26 merton\_firm

### Class: MertonFirm()

Implementation of the Merton Firm Value Model according to the original formulation by Merton with the inputs being the asset value of the firm, the liabilities (bond face), the time to maturity in years, the risk-free rate, the asset growth rate and the asset value volatility.

#### MertonFirm

Create an object that holds all of the model parameters. These parameters may be vectorised.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
assetValue	float or list,np.ndarray	-	-
bondFace	float or list,np.ndarray	-	-
timeToMaturity	float or list,np.ndarray	-	-
risk_free_rate	float or list,np.ndarray	-	-
assetGrowthRate	float or list,np.ndarray	-	-
assetVolatility	float or list,np.ndarray	-	-

### leverage

Calculate the leverage.

```
leverage():
```

The function arguments are described in the following table.

#### asset value

Calculate the asset value.

```
asset_value():
```

#### debt\_face\_value

Calculate the asset value.

```
debt_face_value():
```

The function arguments are described in the following table.

### equity\_vol

Calculate the equity volatility.

```
equity_vol():
```

The function arguments are described in the following table.

# $equity\_value$

Calculate the equity value.

```
equity_value():
```

The function arguments are described in the following table.

#### debt\_value

Calculate the debt value

```
debt_value():
```

The function arguments are described in the following table.

### credit\_spread

Calculate the credit spread from the debt value.

```
credit_spread():
```

The function arguments are described in the following table.

### prob\_default

Calculate the default probability. This is not risk-neutral so it uses the real world drift rather than the risk-free rate.

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```
prob_default():
```

The function arguments are described in the following table.

### dist\_default

Calculate the distance to default. This is not risk-neutral so it uses the real world drift rather than the risk-free rate.

```
dist_default():
```

The function arguments are described in the following table.

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

\_\_repr\_\_():

### 10.27 merton\_firm\_mkt

#### Class: MertonFirmMkt(MertonFirm)

Market Extension of the Merton Firm Model according to the original formulation by Merton with the inputs being the equity value of the firm, the liabilities (bond face), the time to maturity in years, the risk-free rate, the asset growth rate and the equity volatility. The asset value and asset volatility are computed internally by solving two non-linear simultaneous equations.

#### MertonFirmMkt

Create an object that holds all of the model parameters. These parameters may be vectorised.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
equity_value	float or list,np.ndarray	-	-
bondFace	float or list,np.ndarray	-	-
timeToMaturity	float or list,np.ndarray	-	-
risk_free_rate	float or list,np.ndarray	-	-
assetGrowthRate	float or list,np.ndarray	-	-
equity_volatility	float or list,np.ndarray	-	-

#### \_solve\_for\_asset\_value\_and\_vol

PLEASE ADD A FUNCTION DESCRIPTION

```
_solve_for_asset_value_and_vol():
```

The function arguments are described in the following table.

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

# \_fobj

Find value of asset value and vol that fit equity value and vol

```
_fobj(x, *args):
```

Argument Name	Type	Description	Default Value
X	-	-	-
*args	-	-	-

# 10.28 model

Class: Model()

class Model():

# Model

PLEASE ADD A FUNCTION DESCRIPTION

Model():

# 10.29 option\_implied\_dbn

# $option\_implied\_dbn$

This function calculates the option smile/skew-implied probability density function times the interval width.

```
option_implied_dbn(s, t, r, q, strikes, sigmas):
```

Argument Name	Type	Description	<b>Default Value</b>
S	-	-	-
t	-	-	-
r	-	-	-
q	-	_	-
strikes	-	-	-
sigmas	-	-	-

## 10.30 process\_simulator

### Enumerated Type: ProcessTypes

This enumerated type has the following values:

- GBM
- CIR
- HESTON
- VASICEK
- CEV
- JUMP\_DIFFUSION

### Enumerated Type: FinHestonNumericalScheme

This enumerated type has the following values:

- EULER
- EULERLOG
- QUADEXP

### Enumerated Type: FinGBMNumericalScheme

This enumerated type has the following values:

- NORMAL
- ANTITHETIC

### Enumerated Type: FinVasicekNumericalScheme

This enumerated type has the following values:

- NORMAL
- ANTITHETIC

# Enumerated Type: CIRNumericalScheme

This enumerated type has the following values:

- EULER
- LOGNORMAL
- MILSTEIN
- KAHLJACKEL
- EXACT

# Class: FinProcessSimulator()

class FinProcessSimulator():

#### **FinProcessSimulator**

PLEASE ADD A FUNCTION DESCRIPTION

```
FinProcessSimulator():
```

The function arguments are described in the following table.

### $get\_process$

#### PLEASE ADD A FUNCTION DESCRIPTION

```
get_process(process_type,
    t,
    model_params,
    numAnnSteps,
    num_paths,
    seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
process_type	-	-	-
t	-	-	-
model_params	-	-	-
numAnnSteps	-	-	-
num_paths	-	-	-
seed	-	-	-

## get\_heston\_paths

#### PLEASE ADD A FUNCTION DESCRIPTION

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
	Type	Type Description

# $get\_gbm\_paths$

#### PLEASE ADD A FUNCTION DESCRIPTION

```
get_gbm_paths(num_paths, numAnnSteps, t, mu, stock_price, sigma, scheme, seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
num_paths	-	-	-
numAnnSteps	-	-	-
t	-	-	-
mu	-	-	-
stock_price	-	-	-
sigma	-	-	-
scheme	-	-	-
seed	-	-	-

# $get\_vasicek\_paths$

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
num_paths	-	-	-
numAnnSteps	-	-	-
t	-	-	-
r0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
scheme	-	-	-
seed	-	-	-

# get\_cir\_paths

#### PLEASE ADD A FUNCTION DESCRIPTION

<b>Argument Name</b>	Type	Description	Default Value
num_paths	-	-	-
numAnnSteps	-	-	-
t	-	-	-
r0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
scheme	-	-	-
seed	-	-	-
-			

### 10.31 rates\_ho\_lee

#### Class: ModelRatesHoLee

class ModelRatesHoLee:

#### **ModelRatesHoLee**

Construct Ho-Lee model using single parameter of volatility. The dynamical equation is dr = theta(t) dt + sigma \* dW. Any no-arbitrage fitting is done within functions below.

```
ModelRatesHoLee(sigma):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
sigma	-	-	-

#### zcb

#### PLEASE ADD A FUNCTION DESCRIPTION

```
zcb(rt1, t1, t2, discount_curve):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
rt1	-	-	-
t1	-	-	-
t2	-	-	-
discount_curve	-	-	-

## $option\_on\_zcb$

Price an option on a zero coupon bond using analytical solution of Hull-White model. User provides bond face and option strike and expiry date and maturity date.

Argument Name	Type	Description	<b>Default Value</b>
t_exp	-	-	-
tmat	-	-	-
strike_price	-	-	-
face_amount	-	-	-
df_times	-	-	-
df_values	-	-	-

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#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

### p\_fast

Forward discount factor as seen at some time t which may be in the future for payment at time T where Rt is the delta-period short rate seen at time t and pt is the discount factor to time t, ptd is the one period discount factor to time t+dt and pT is the discount factor from now until the payment of the 1 dollar of the discount factor.

```
p_fast(t, T, Rt, delta, pt, ptd, pT, _sigma):
```

Argument Name	Type	Description	Default Value
t	-	-	-
T	-	-	-
Rt	-	-	-
delta	-	-	-
pt	-	-	-
ptd	-	-	-
pT	-	-	-
_sigma	-	-	-
<u>F</u>	-	-	-

### 10.32 sabr

### Class: SABR()

SABR - Stochastic alpha beta rho model by Hagan et al. which is a stochastic volatility model where alpha controls the implied volatility, beta is the exponent on the the underlying assets process so beta = 0 is normal and beta = 1 is lognormal, rho is the correlation between the underlying and the volatility process.

#### **SABR**

Create SABR with all of the model parameters. We will also provide functions below to assist with the calibration of the value of alpha.

```
SABR(alpha, beta, rho, nu):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
alpha	-	-	-
beta	-	-	-
rho	-	-	-
nu	-	-	-

#### black\_vol

Black volatility from SABR model using Hagan et al. approx.

```
black_vol(f, k, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
f	-	-	-
k	-	-	-
t	-	-	-

### black\_vol\_with\_alpha

PLEASE ADD A FUNCTION DESCRIPTION

```
black_vol_with_alpha(alpha, f, k, t):
```

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Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

#### value

Price an option using Black's model which values in the forward measure following a change of measure.

```
value(forward_rate,  # Forward rate
    strike_rate,  # Strike Rate
    time_to_expiry,  # time to expiry in years
    df,  # Discount Factor to expiry date
    call_or_put):  # Call or put
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
forward_rate	-	Forward rate	-
strike_rate	-	Strike Rate	-
time_to_expiry	-	time to expiry in years	-
df	-	Discount Factor to expiry date	-
call_or_put	-	Call or put	-

## $set\_alpha\_from\_black\_vol$

Estimate the value of the alpha coefficient of the SABR model by solving for the value of alpha that makes the SABR black vol equal to the input black vol. This uses a numerical 1D solver.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
blackVol	-	-	-
forward	-	-	-
strike	-	-	-
time_to_expiry	-	-	-

#### fn

#### PLEASE ADD A FUNCTION DESCRIPTION

```
fn(x): return np.sqrt(
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>

### set\_alpha\_from\_atm\_black\_vol

We solve cubic equation for the unknown variable alpha for the special ATM case of the strike equalling the forward following Hagan and al. equation (3.3). We take the smallest real root as the preferred solution. This is useful for calibrating the model when beta has been chosen.

```
set_alpha_from_atm_black_vol(blackVol, atmStrike, time_to_expiry):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
blackVol	-	-	-
atmStrike	-	-	-
time_to_expiry	-	-	-

#### \_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

\_X

Return function x used in Hagan's 2002 SABR lognormal vol expansion.

```
_x(rho, z):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
rho	-	-	-
Z	-	-	-

#### vol\_function\_sabr

Black volatility implied by SABR model.

```
vol_function_sabr(params, f, k, t):
```

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Argument Name	Type	Description	<b>Default Value</b>
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

### vol\_function\_sabr\_beta\_one

This is the SABR function with the exponent beta set equal to 1 so only 3 parameters are free. The first parameter is alpha, then nu and the third parameter is rho. Check the order as it is not the same as main SABR fn

```
vol_function_sabr_beta_one(params, f, k, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

### vol\_function\_sabr\_beta\_half

Black volatility implied by SABR model.

```
vol_function_sabr_beta_half(params, f, k, t):
```

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	-
		Type Description

### 10.33 sabr\_shifted

### Class: SABRShifted()

SABR - Shifted Stochastic alpha beta rho model by Hagan et al. is a stochastic volatility model where alpha controls the implied volatility, beta is the exponent on the the underlying assets process so beta = 0 is normal and beta = 1 is lognormal, rho is the correlation between the underlying and the volatility process. The shift allows negative rates.

#### **SABRShifted**

Create SABRShifted with all of the model parameters. We also provide functions below to assist with the calibration of the value of alpha.

```
SABRShifted(alpha, beta, rho, nu, shift):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
alpha	-	-	-
beta	-	-	-
rho	-	-	-
nu	-	-	-
shift	-	-	-

#### black\_vol

Black volatility from SABR model using Hagan et al. approx.

```
black_vol(f, k, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
f	-	-	-
k	-	-	-
t	-	-	-

## black\_vol\_with\_alpha

PLEASE ADD A FUNCTION DESCRIPTION

```
black_vol_with_alpha(alpha, f, k, t):
```

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Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

#### value

Price an option using Black's model which values in the forward measure following a change of measure.

```
value(forward_rate,  # Forward rate F
    strike_rate,  # Strike Rate K
    time_to_expiry,  # Time to Expiry (years)
    df,  # Discount Factor to expiry date
    call_or_put):  # Call or put
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
forward_rate	-	Forward rate F	-
strike_rate	-	Strike Rate K	-
time_to_expiry	-	Time to Expiry (years)	-
df	-	Discount Factor to expiry date	-
call_or_put	-	Call or put	-

## $set\_alpha\_from\_black\_vol$

Estimate the value of the alpha coefficient of the SABR model by solving for the value of alpha that makes the SABR black vol equal to the input black vol. This uses a numerical 1D solver.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
blackVol	-	-	-
forward	-	-	-
strike	-	-	-
time_to_expiry	-	-	-

#### fn

#### PLEASE ADD A FUNCTION DESCRIPTION

```
fn(x): return np.sqrt(
```

The function arguments are described in the following table.

Argument Name Type	Description	<b>Default Value</b>
--------------------	-------------	----------------------

## $set\_alpha\_from\_atm\_black\_vol$

We solve cubic equation for the unknown variable alpha for the special ATM case of the strike equalling the forward following Hagan and al. equation (3.3). We take the smallest real root as the preferred solution. This is useful for calibrating the model when beta has been chosen.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
blackVol	-	-	-
atmStrike	-	-	-
time_to_expiry	-	-	-

#### \_\_repr\_\_

#### PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

#### $\mathbf{X}$

Return function x used in Hagan's 2002 SABR lognormal vol expansion.

```
_x(rho, z):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
rho	-	-	-
Z	-	-	-

### vol\_function\_shifted\_sabr

Black volatility implied by SABR model.

```
vol_function_shifted_sabr(params, f, k, t):
```

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Argument Name	Type	Description	Default Value
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

### 10.34 sobol

### get\_gaussian\_sobol

Sobol Gaussian quasi random points generator based on graycode order. The generated points follow a normal distribution.

```
get_gaussian_sobol(num_points, dimension):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
num_points	-	-	-
dimension	-	-	-

### get\_uniform\_sobol

Sobol uniform quasi random points generator based on graycode order. This function returns a 2D Numpy array of values where the number of rows is the number of draws and the number of columns is the number of dimensions of the random values. Each dimension has the same number of random draws. Each column of random numbers is ordered so as not to correlate, i.e be independent from any other column.

```
get_uniform_sobol(num_points, dimension):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
num_points	-	-	-
dimension	-	-	-

# 10.35 student\_t\_copula

# Class: StudentTCopula()

class StudentTCopula():

## default\_times

#### PLEASE ADD A FUNCTION DESCRIPTION

<b>Argument Name</b>	Type	Description	Default Value
issuer_curves	-	-	-
correlation_matrix	-	-	-
degreesOfFreedom	-	-	-
num_trials	-	-	-
seed	-	-	-

## 10.36 vasicek\_mc

## Class: ModelRatesVasicek()

class ModelRatesVasicek():

## **ModelRatesVasicek**

PLEASE ADD A FUNCTION DESCRIPTION

```
ModelRatesVasicek(a, b, sigma):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
sigma	-	-	-

\_\_repr\_\_

PLEASE ADD A FUNCTION DESCRIPTION

```
__repr__():
```

The function arguments are described in the following table.

#### meanr

PLEASE ADD A FUNCTION DESCRIPTION

```
meanr(r0, a, b, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
t	-	-	-

#### variancer

PLEASE ADD A FUNCTION DESCRIPTION

```
variancer(a, b, sigma, t):
```

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-

## zero\_price

PLEASE ADD A FUNCTION DESCRIPTION

```
zero_price(r0, a, b, sigma, t):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-

## rate\_path\_mc

PLEASE ADD A FUNCTION DESCRIPTION

```
rate_path_mc(r0, a, b, sigma, t, dt, seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-
dt	-	-	-
seed	-	-	-

## zero\_price\_mc

PLEASE ADD A FUNCTION DESCRIPTION

```
zero_price_mc(r0, a, b, sigma, t, dt, num_paths, seed):
```

<b>Argument Name</b>	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-
dt	-	-	-
num_paths	-	-	-
seed	-	-	-

## 10.37 volatility\_fns

### Enumerated Type: VolFuncTypes

This enumerated type has the following values:

- CLARK
- SABR
- SABR\_BETA\_ONE
- SABR\_BETA\_HALF
- BBG
- CLARK5
- SVI
- SSVI

#### vol\_function\_clark

Volatility Function in book by Iain Clark generalised to allow for higher than quadratic power. Care needs to be taken to avoid overfitting. The exact reference is Clark Page 59.

```
vol_function_clark(params, f, k, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

## vol\_function\_bloomberg

Volatility Function similar to the one used by Bloomberg. It is a quadratic function in the spot delta of the option. It can therefore go negative so it requires a good initial guess when performing the fitting to avoid this happening. The first parameter is the quadratic coefficient i.e. sigma(K) = a \* D \* D + b \* D + c where a = params[0], b = params[1], c = params[2] and D is the spot delta.

```
vol_function_bloomberg(params, f, k, t):
```

Argument Name	Type	Description	Default Value
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

#### vol\_function\_svi

Volatility Function proposed by Gatheral in 2004. Increasing a results in a vertical translation of the smile in the positive direction. Increasing b decreases the angle between the put and call wing, i.e. tightens the smile. Increasing rho results in a counter-clockwise rotation of the smile. Increasing m results in a horizontal translation of the smile in the positive direction. Increasing sigma reduces the at-the-money curvature of the smile.

```
vol_function_svi(params, f, k, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

### phi\_ssvi

#### PLEASE ADD A FUNCTION DESCRIPTION

```
phi_ssvi(theta, gamma):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
theta	-	-	-
gamma	-	-	-

#### ssvi

This is the total variance w = sigma(t) x sigma(t) (0,t) x t

```
ssvi(x, gamma, sigma, rho, t):
```

Argument Name	Type	Description	<b>Default Value</b>
X	-	-	-
gamma	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-

### ssvi1

#### PLEASE ADD A FUNCTION DESCRIPTION

```
ssvil(x, gamma, sigma, rho, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	-	-	-
gamma	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-

### ssvi2

#### PLEASE ADD A FUNCTION DESCRIPTION

```
ssvi2(x, gamma, sigma, rho, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	-	-	-
gamma	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-

### ssvit

#### PLEASE ADD A FUNCTION DESCRIPTION

```
ssvit(x, gamma, sigma, rho, t):
```

Argument Name	Type	Description	<b>Default Value</b>
X	-	-	-
gamma	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-

g

#### PLEASE ADD A FUNCTION DESCRIPTION

```
g(x, gamma, sigma, rho, t):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	-	-	-
gamma	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-

### dminus

#### PLEASE ADD A FUNCTION DESCRIPTION

```
dminus(x, gamma, sigma, rho, t):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	-	-	-
gamma	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-

# density\_ssvi

#### PLEASE ADD A FUNCTION DESCRIPTION

```
density_ssvi(x, gamma, sigma, rho, t):
```

Argument Name	Type	Description	<b>Default Value</b>
X	-	-	-
gamma	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-

# ssvi\_local\_varg

#### PLEASE ADD A FUNCTION DESCRIPTION

```
ssvi_local_varg(x, gamma, sigma, rho, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	-	-	-
gamma	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-

### vol\_function\_ssvi

Volatility Function proposed by Gatheral in 2004.

```
vol_function_ssvi(params, f, k, t):
```

Argument Name	Type	Description	Default Value
params	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

10.38 \_\_init\_\_