

Tutorial - 26.

Linear Regression, In-depth Maths Contribution

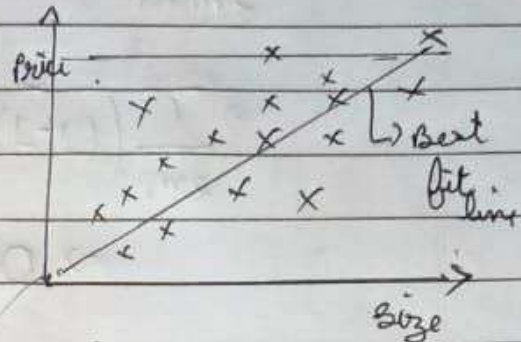
$$y = mx + c$$

Best fit line

m = slope

c = Intercept.

.



In the Best fit line for some limit say n try. the error is summed up to give the least error on the minimal error. gives value of m or c

when \rightarrow size = 0 i.e. $x = 0$
 $y = mx + c$
 $y = m \cdot 0 + c \rightarrow c$
 $\boxed{y = c}$

Cost function is made:

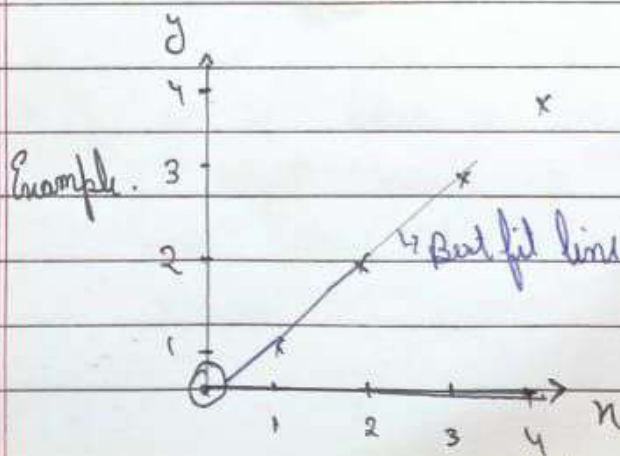
$$\frac{1}{2m} \sum_{i=1}^m (\hat{y}_i - y_i)^2$$

$\frac{1}{2m}$ number of pts

$$\hat{y} \rightarrow y = mx + c$$

the points on best fit line (predicted)

$y \rightarrow$ Preexisting points. actual line



For BFL

$$\rightarrow y = mx + c = 0$$

must pass through origin

$$n=1$$

$$y = mx$$

$$\text{if } m=1 \rightarrow \hat{y} = 1 \cdot 1$$

$$n=2$$

$$m=1$$

$$\rightarrow \hat{y} = 2$$

$$\Rightarrow 1$$

$$0 \leq 0$$

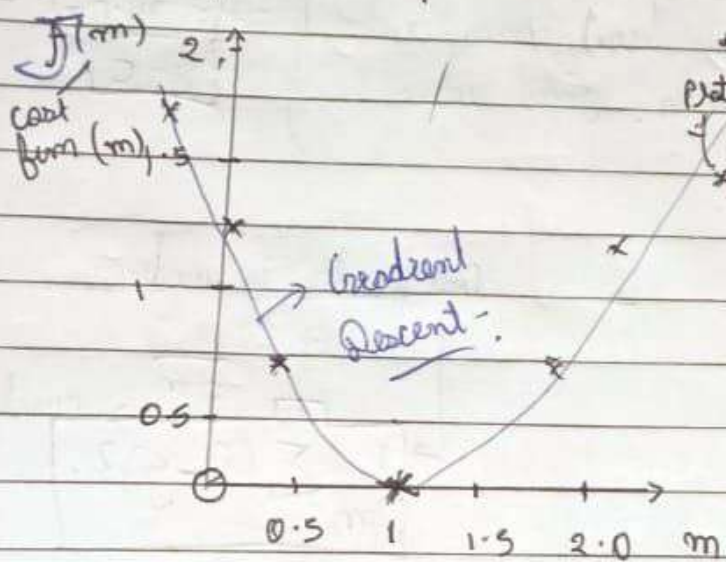
Cost function,

$$= \frac{1}{2m} \sum_{i=1}^m (\hat{y} - y)^2$$

$$\Rightarrow \frac{1}{2m} ((1-1)^2 + (2-2)^2 + (3-3)^2)$$

$$\Rightarrow 0 \text{ cost.}$$

Q2. Cost function slope.



curve - $m=1$, $cf=0$

stationary. $\hat{y} = 0.5$

say $m = 0.5$

\hat{y} for $n=1$

$\hat{y} \rightarrow 0.5$

for $n=2$

$\hat{y} = 1$

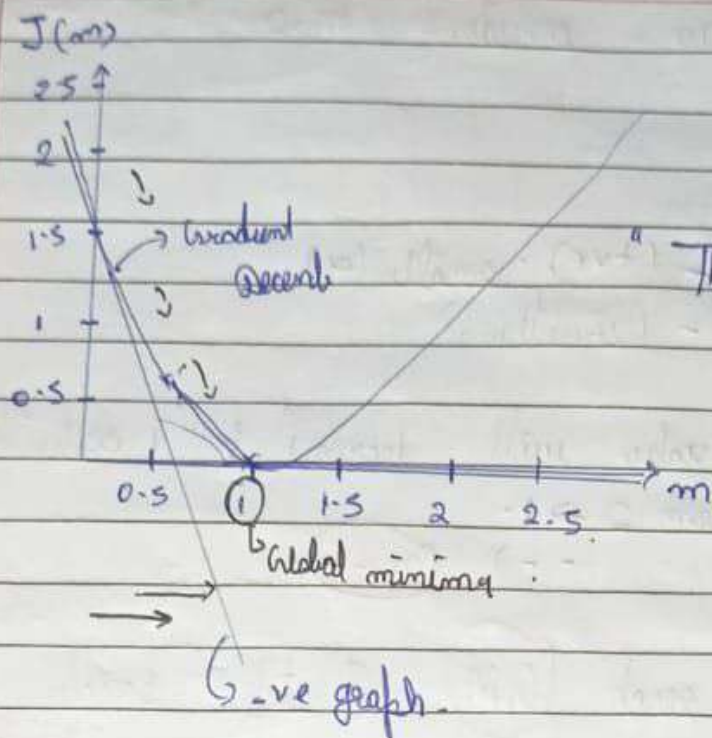
for $n=3$

$\hat{y} = 1.5$

$$\frac{1}{2m} \sum_{i=1}^m ((0.5-1)^2 + (1-2)^2 + (1.5-3)^2)$$

$$\Rightarrow 0.58$$

P.T.O.



To reach Global minimum we have to follow a theorem to go down from LLL "The Convergence Theorem" -

$$m = m - \left(\frac{\partial J}{\partial m} \right) \times \alpha$$

$\frac{\partial J}{\partial m}$ $\xrightarrow{\text{func.}}$ α
 slope. $\xrightarrow{\text{learning rate}}$

Applying Convergence theorem -

$$m = m - \left(\frac{\partial J}{\partial m} \right) * \alpha \rightarrow \approx 0.001$$

$$m = m - (-ve) * (\text{small})$$

$$m = m + (+ve) * \text{smaller}$$

\hookrightarrow This suggests that value of m will be +ve & tend to come nearer to 1 or Global minimum.

* If α is taken as larger value say, 1, it might jump up the result of m & never allow it to reach the Global minimum.

Similarly, if we consider $m=2$.

$$m = +ve$$

$$m = m - (+ve) \cdot \text{smaller}(\alpha)$$

$$m = m - (\text{something})$$

m value will decrease to 1 certainly
from $2 \rightarrow 1$.

$$(- -) \quad (m - -)$$

The time I reach (GM) I stop searching
or training.

say we have more than one feature in model.
our Gradient descent would be a B-P figure.
Thus we get a complex answer.