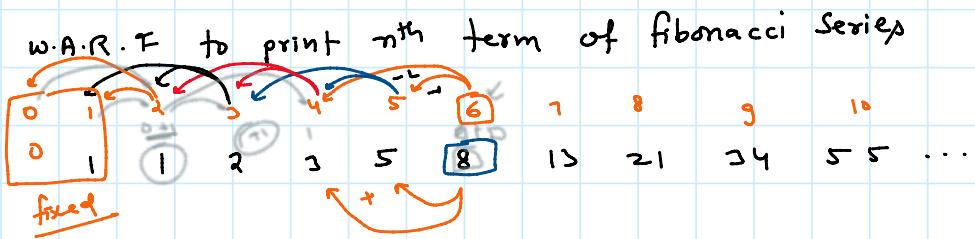
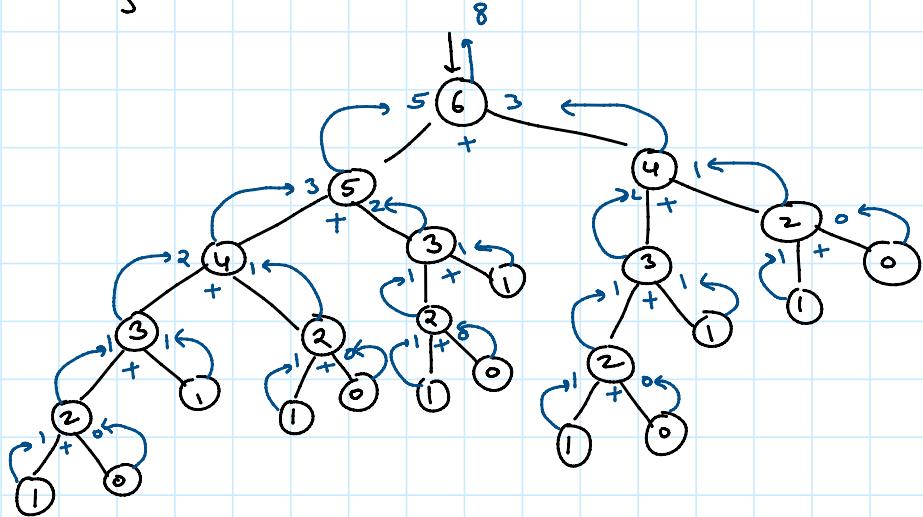


# DAY 13

08 May 2024 01:01 PM



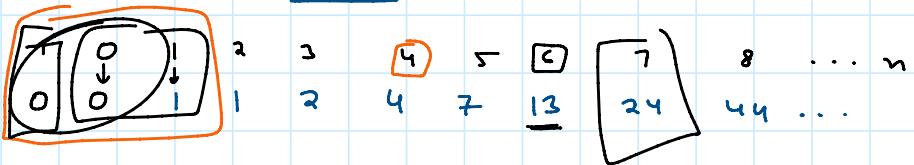
```
int fibo ( int n )
{
    if (n==0 || n==1)
        return n;
    return fibo (n-1) + fibo (n-2);
}
```



```
#include<iostream>
using namespace std;
int fact(int n)
{
    if(n==1 or n==0)
        return n;
    return fact(n-1) + fact(n-2);
}
int main()
{
    cout<<fact(10);
    return 0;
}
```

Tribonacci Series : —

## Tribonacci Series :-



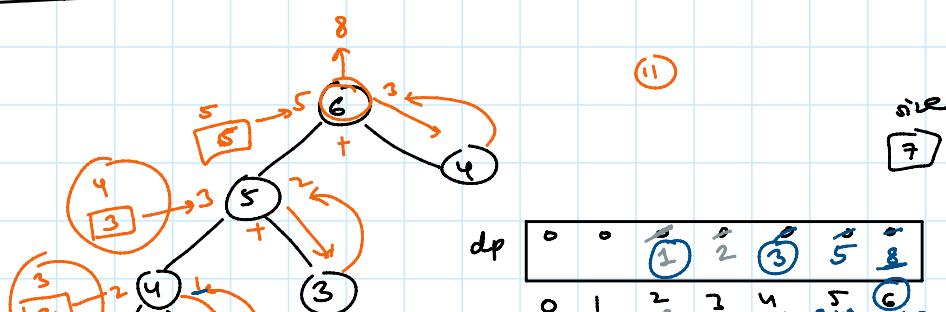
W.A.R.F to print  $n^{\text{th}}$  term of tribonacci' series -

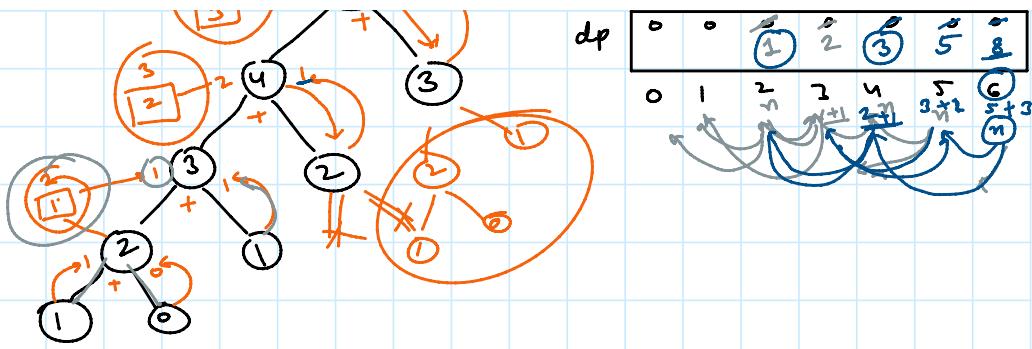
```
int tribo( int n )
{
    if( n==0 || n==1 )
        return n;
    if( n == -1 )
        return 0;
    return tribo(n-1) + tribo(n-2) + tribo(n-3);
}
```

```
#include<iostream>
using namespace std;
int tribo(int n)
{
    if(n==1 or n==0)
        return n;
    if(n== -1)
        return 0;
    return tribo(n-1) + tribo(n-2) + tribo(n-3);
}
int main()
{
    cout<<tribo(10);
    return 0;
}
```

## Dynamic Programming (DP)

### Fibonacci Series      $n^{\text{th}}$ term :-





```
#include<iostream>
using namespace std;
int count=0;
int fact(int n,int dp[])
{
    count++;
    if(n==1 or n==0)
        return n;
    if(dp[n]==0)
        dp[n] = fact(n-1,dp) + fact(n-2,dp);
    return dp[n];
}
int main()
{
    int n;
    cout<<"Enter no of a term:";
    cin>>n;
    int dp[n+1]={0};
    cout<<fact(n,dp)<<endl;
    cout<<count;
    return 0;
}
```

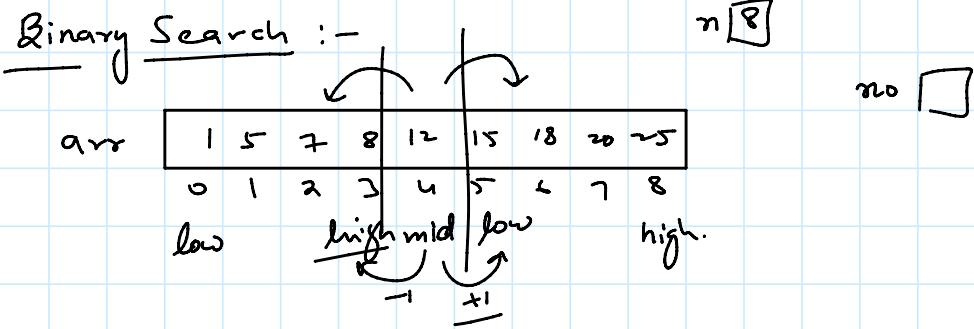
Apply DP on tribonacci series  $n^{\text{th}}$  term

```
#include<iostream>
using namespace std;
int tribo(int n,int dp[])
{
    if(n==1 or n==0)
        return n;
    if(n==1)
        return 0;
    if(dp[n]==0)
        dp[n] = tribo(n-1,dp) + tribo(n-2,dp) + tribo(n-3,dp);
    return dp[n];
}
int main()
{
    int n;
    cout<<"Enter no of a term:";
```

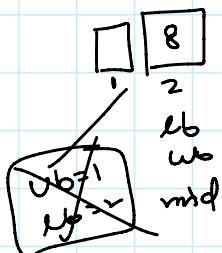
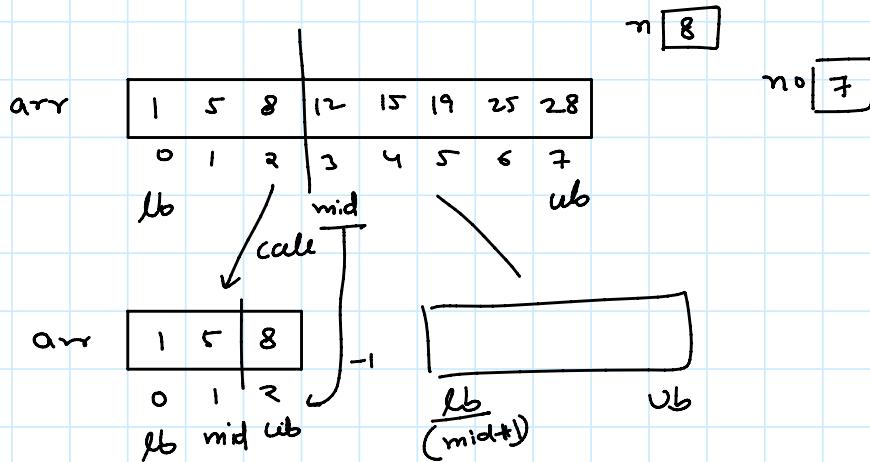
```

    cin>>n;
    int dp[n+1]={0};
    cout<<tribo(n,dp)<<endl;
    return 0;
}

```



Binary Searching using recursion



bool BinarySearch (int arr[], int lb, int ub, int no)

```

{
    if (lb > ub)
        return false;
    int mid = (lb+ub)/2;
}

```

```

        return false;
    int mid = (lb+ub)/2;
    if (arr[mid] == no)
        return true;
    if (no < arr[mid])
        return BinarySearch (arr, lb, mid-1, no);
    else
        return BinarySearch (arr, mid+1, ub, no);
}

```

```

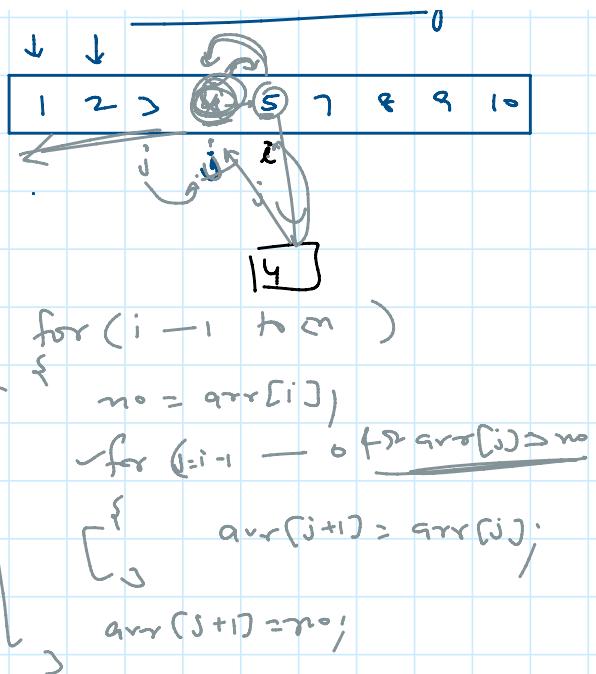
#include<iostream>
using namespace std;
bool binarySearch(int arr[], int lb, int ub, int no)
{
    if(lb>ub)
        return false;
    int mid=(lb+ub)/2;
    if(arr[mid]==no)
        return true;
    if(no < arr[mid])
        return binarySearch(arr,lb,mid-1,no);
    else
        return binarySearch(arr,mid+1,ub,no);
}
int main()
{
    int arr[]={1,5,9,10,15,17,19,22,25};
    int n=sizeof(arr)/sizeof(int);
    if(binarySearch(arr,0,n-1,190))
        cout<<"Found";
    else
        cout<<"Not found";
    return 0;
}

```

Sorting :-

insertion Sorting :-





## Bubble Sorting:-

Pass-1		arr							n	5	
i=1		2	3	4	5	6	7	8	9	10	5
		0	1	2	3	4	5	6	7	8	9
		↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
j=0 to j+1							j+1				

Pass-2		arr							n	5	
i=2		2	3	4	5	6	7	8	9	10	5
		0	1	2	3	4	5	6	7	8	9
		↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
j=0 to j+1							j+1				

Pass-3		arr							n	5	
i=3		2	3	4	5	6	7	8	9	10	5
		0	1	2	3	4	5	6	7	8	9
		↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
j=0 to j+1							j+1				

Pass-4		arr							n	5	
i=4		2	3	4	5	6	7	8	9	10	5
		0	1	2	3	4	5	6	7	8	9
		↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
j=0 to j+1							j+1				

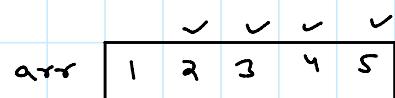


if ( $\text{arr}[i] > \text{arr}[i+1]$ )

swap( $\text{arr}[i], \text{arr}[i+1]$ )

$i = 1 \text{ to } n-1 \quad ++$

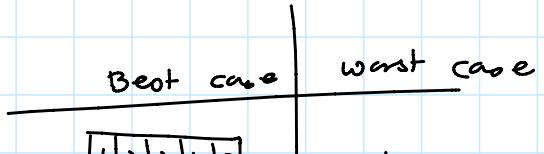
$j = 0 \text{ to } n-i-1 \quad ++$



↑  
sorted Array

## I. method

```
#include<iostream>
using namespace std;
void BubbleSort(int arr[], int n)
{
    for(int i=1; i<n; i++)
    {
```



```

{
    for(int i=1; i<n; i++)
    {
        for(int j=0; j<n-i; j++)
        {
            if(arr[j] > arr[j+1])
                swap(arr[j], arr[j+1]);
        }
    }
}

int main()
{
    int arr[] = {5, 1, 3, 2, 4};
    int n = sizeof(arr)/sizeof(int);
    BubbleSort(arr, n);
    for(int i:arr)
        cout << i << " ";
    return 0;
}

```

Best case	worst case
$O(n)$	$O(n^2)$
$\boxed{1 \ 2 \ 3 \ 4 \ 5}$	$\boxed{5 \ 4 \ 3 \ 2 \ 1}$

## If method

```

#include<iostream>
using namespace std;
void BubbleSort(int arr[], int n)
{
    bool flag=true;
    for(int i=1; i<n and flag; i++)
    {
        flag=false;
        for(int j=0; j<n-i; j++)
        {
            if(arr[j] > arr[j+1])
            {
                swap(arr[j], arr[j+1]);
                flag=true;
            }
        }
    }
}

int main()
{
    int arr[] = {5, 1, 3, 2, 4};
    int n = sizeof(arr)/sizeof(int);
    BubbleSort(arr, n);
    for(int i:arr)
        cout << i << " ";
    return 0;
}

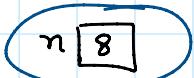
```

Best case	worst case
$O(n)$	$O(n^2)$
$\boxed{1 \ 2 \ 3 \ 4 \ 5}$	$\boxed{5 \ 4 \ 3 \ 2 \ 1}$

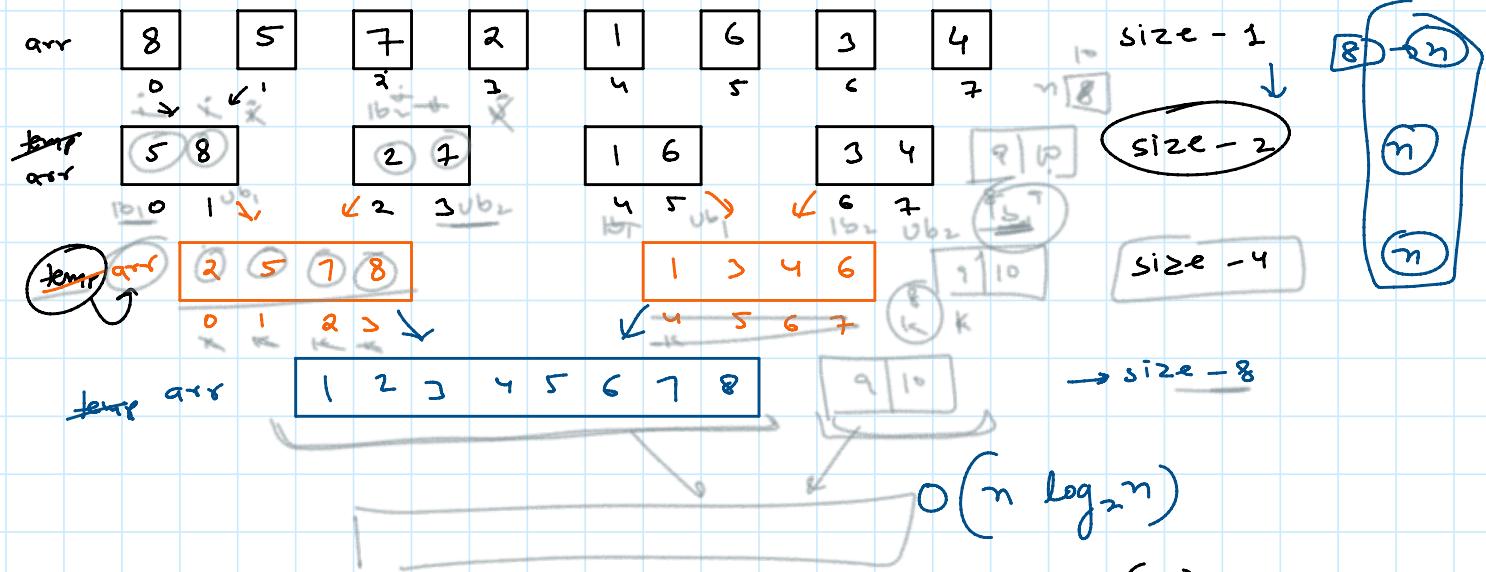
## Merge Sorting :-

$n \boxed{8}$

$\leftarrow 0 \rightarrow \dots j$



arr	8	5	7	2	1	6	3	4
	0	1	2	3	4	5	6	7



① Copy from temp to arr

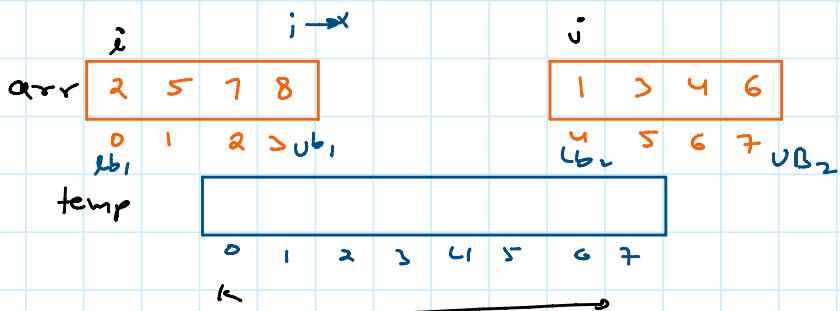
```
for (i=0; i < n; i++)
    arr[i] = temp[i];
```

space  $\rightarrow \underline{o(n)}$

II<sup>nd</sup>

$O(n \log_2 n)$

② Merge to parts :-



for ( $i = lb_1, j = lb_2 ; i \leq ub_1$  and  $j \leq ub_2 ; k++$ )

{ if ( $arr[i] < arr[j]$ )

[ temp[k] = arr[i];
 i++;
}

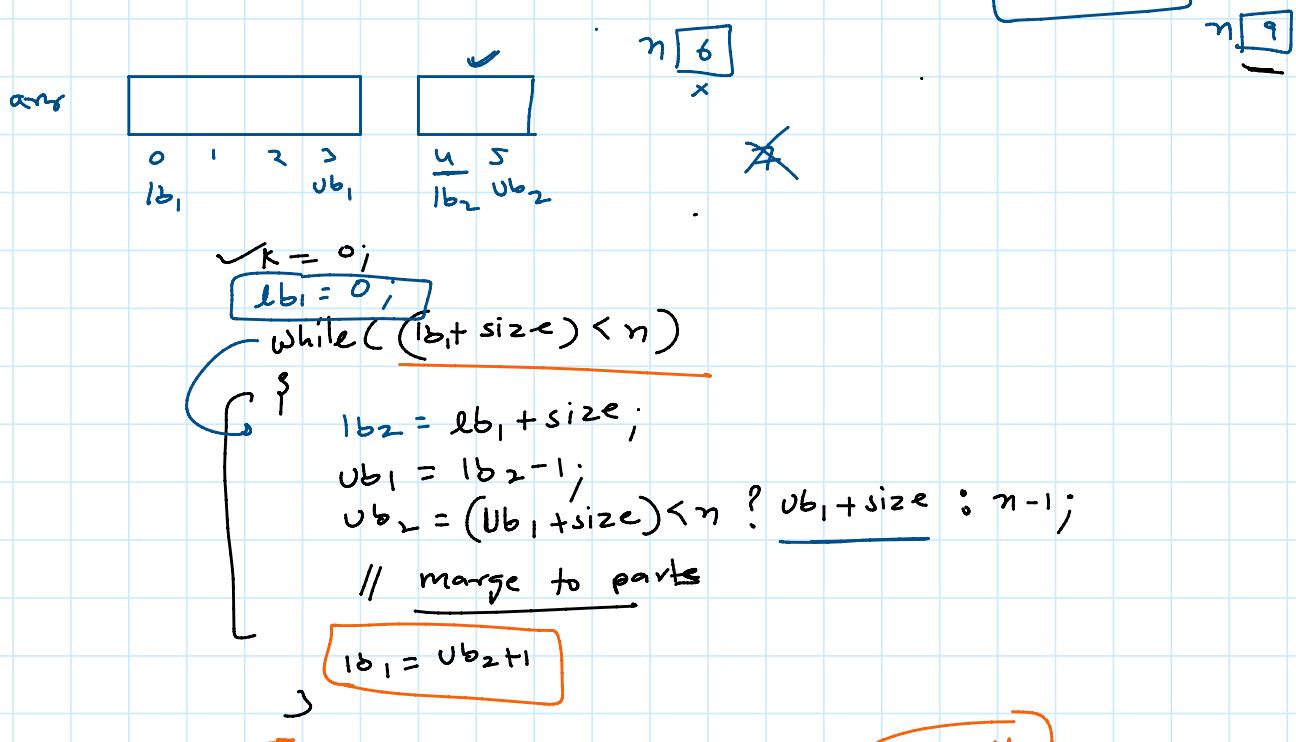
{ else
 [ temp[k] = arr[j];
 j++;
}

$\left[ \begin{array}{c} \\ \end{array} \right]_0 \quad \left[ \begin{array}{c} \\ \end{array} \right]_k \quad \text{temp}[k] = \text{arr}[i];$   
 $i++;$

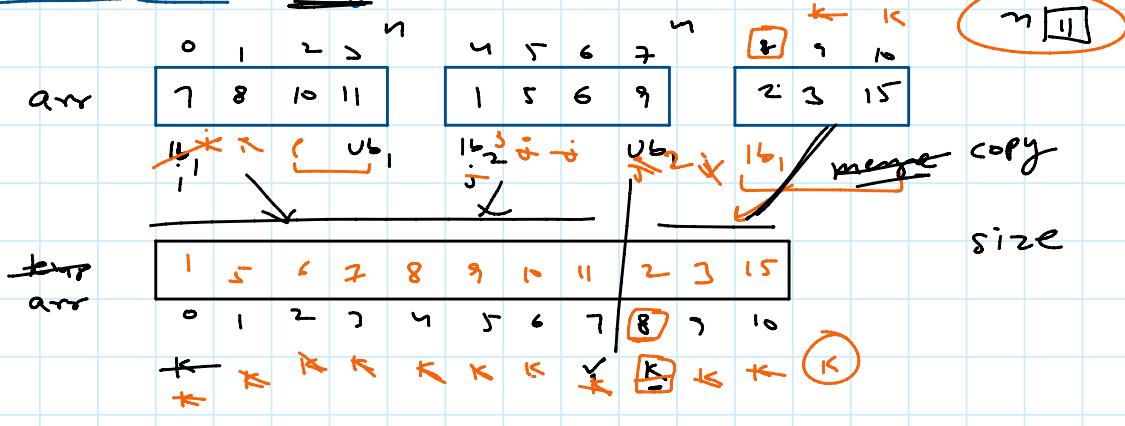
$\text{while } (i \leq \text{ub}_1)$   
 $\left[ \begin{array}{c} \\ \end{array} \right]_i \quad \text{temp}[k++] = \text{arr}[i++];$

$\text{while } (j \leq \text{ub}_2)$   
 $\left[ \begin{array}{c} \\ \end{array} \right]_j \quad \text{temp}[k++] = \text{arr}[j++];$

### ③ Partition :-



### ④ unpaired part $\rightarrow$ copy arr to temp



```

while (k < n)
{
    temp[k] = arr[k]
    k++
}

```

## 5 size

```
int size = 1;
```

```

while (size < n)
{
    {
        ③
        ②
        ④
    ①
    size *= 2;
}

```

```

#include<iostream>
using namespace std;
void mergeSort(int arr[], int n)
{
    int size=1, i, j, k, lb1, ub1, lb2, ub2;
    int temp[n];
    while(size < n)
    {
        k=0;
        lb1=0;
        while((lb1+size) < n)
        {
            lb2=lb1+size;
            ub1=lb2-1;
            ub2=(ub1+size) < n ? ub1+size : n-1;
            for(i=lb1, j=lb2; i <= ub1 and j <= ub2; k++)
            {
                if(arr[i] < arr[j])
                    temp[k]=arr[i++];
                else
                    temp[k]=arr[j++];
            }
            while(i <= ub1)
                temp[k++]=arr[i++];
            while(j <= ub2)
                temp[k++]=arr[j++];
            lb1=ub2+1;
        }
        while(k < n)
    }
}

```

```
{  
    temp[k]=arr[k];  
    k++;  
}  
for(i=0;i<n;i++)  
    arr[i]=temp[i];  
size *= 2;  
}  
}  
int main()  
{  
    int arr[]={5,1,3,2,4,8,7,6,9};  
    int n=sizeof(arr)/sizeof(int);  
    mergeSort(arr,n);  
    for(int i:arr)  
        cout<<i<<" ";  
    return 0;  
}
```