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Anova

PRACTICAL-1

Topic - Random Variable

Q1] Find the mean & variance for the following

X	-1	0	1	2
P(x)	0.1	0.2	0.3	0.4

Sol -

X	P(X)	X · P(X)	E(X) ²	[E(X)] ²
-1	0.1	-0.1	0.1	0.01
0	0.2	0	0	0
1	0.3	0.3	0.3	0.09
2	0.4	0.8	0.16	0.64
TOTAL	$\sum = 1$	$\sum = 1$	$\sum = 0.20$	$\sum = 0.74$

$$\therefore \text{Mean} = E(X) = \sum x_i \cdot p(x) = 1$$

$$\begin{aligned} \therefore \text{Variance} &= V(X) = \sum E(X)^2 - \sum [E(X)]^2 \\ &= 2 - 0.74 \\ &= 1.24 \end{aligned}$$

ANS Mean is 1 & Variance $\rightarrow 1.24$

b)

X	-1	0	1	2
P(X)	1/8	1/8	1/4	1/2

Soln

X	P(X)	X · P(X)	E(X) ²	[E(X)] ²
-1	1/8	-1/8	1/8	1/64
0	1/8	0	0	0
1	1/4	1/4	1/4	1/16
2	1/2	1	2	1
TOTAL	$\sum = 1$	$\sum = 9/8$	$\sum = 19/8$	$\sum = 69/64$

$$\therefore \text{Mean} = E(X) = \sum_1 X \cdot P(X) = 9/8$$

$$\begin{aligned} \text{Variance} = V(X) &= \sum_1 E(X)^2 - \sum_1 [E(X)]^2 \\ &= \frac{19}{8} - \frac{69}{64} \\ &= \frac{83}{64} \end{aligned}$$

Ans: Mean is $9/8$ & Variance is $83/64$

c]

X	-3	10	15
P(X)	0.4	0.35	0.25

Soln

X	P(X)	X · P(X)	E(X) ²	[E(X)] ²
-3	0.4	-1.2	1.8	1.44
10	0.35	3.5	3.5	12.25
15	0.25	3.75	56.25	14.0625
TOTAL	$\sum_1 = 1$	$\sum_1 = 6.05$	$\sum_1 = 94.85$	$\sum_1 = 27.752$

$$\therefore \text{Mean} = E(X) = \sum_1 X \cdot P(X) = 6.05$$

$$\begin{aligned} \text{Variance} = V(X) &= \sum_1 E(X)^2 - \sum_1 [E(X)]^2 \\ &= 94.85 - 27.752 \\ &= 67.0975 \end{aligned}$$

Ans: Mean $\rightarrow 6.05$ & Variance $\rightarrow 67.0975$

Q3] The pmf of random variable X is given by

X	-3	-1	0	1	2	3	5	8
$P(X)$	0.1	0.2	0.18	0.2	0.1	0.15	0.05	0.05

Obtain cdf. Find ① $P(-1 \leq x \leq 2)$ ② $P(1 \leq x \leq 5)$
 ③ $P(X \leq 2)$ ④ $P(X \geq 0)$

Soln -

x	-3	-1	0	1	2	3	5	8
$P(X)$	0.1	0.2	0.18	0.2	0.1	0.15	0.05	0.05
$F(X)$	0.1	0.3	0.48	0.68	0.78	0.93	0.98	1.0

$$\begin{aligned}
 \textcircled{1} P(-1 \leq x \leq 2) &= P(X \leq 2) - P(X \leq -1) + P(X = -1) \\
 &= F(X_0) - F(X_9) + P(9) \\
 &= F(2) - F(-1) + P(-1) \\
 &= 0.78 - 0.3 + 0.2 \\
 &= 0.68
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{2} P(1 \leq x \leq 5) &= F(X_6) - F(X_9) + P(9) \\
 &= F(5) - F(1) + P(1) \\
 &= 0.98 - 0.68 + 0.2 \\
 &= 0.5
 \end{aligned}$$

Q4] Let f be continuous random variable with pdf

$$f(x) = \frac{x+1}{2} \quad -1 < x < 1$$

$$= 0 \quad \text{otherwise}$$

Obtain cdf of x . Find mean &

Soln - By defn of cdf we have,

$$F(x) = \int_{-\infty}^x f(t) dt$$

$$= \int_{-1}^x \frac{t+1}{2} dt$$

$$= \int_{-1}^x \frac{1}{2} \left(\frac{1}{2} t^2 + t \right) dt \quad \text{for } -1 < x < 1$$

Hence the cdf is

$$F(x) = 0 \quad \text{for } x \leq -1$$

$$= \frac{1}{4} x^2 + \frac{1}{2} x \quad \text{for } -1 < x < 1$$

$$= 0 \quad \text{for } x \geq 1$$

Q5] Let f be continuous random variable with pdf

$$f(x) = \frac{x+2}{18} \quad -2 \leq x \leq 4$$

$$= 0 \quad \text{otherwise}$$

Calculate cdf.

Soln - By defn of cdf we have.

$$F(x) = \int_{-\infty}^x f(t) dt$$

PRACTICAL-2Topic - Binomial Distribution

Q1] An unbiased coin is tossed 4 times, calculate the probability of obtaining no head, at least one head & more than the tail.

a) No head -

$$> \text{dbinom}(0, 4, 0.5)$$

$$\hookrightarrow 0.0625$$

b) At least one head

$$> 1 - \text{dbinom}(0, 4, 0.5)$$

$$\hookrightarrow 0.9375$$

c) More than one tail

$$> \text{pbinom}(1, 4, 0.5, \text{lower.tail} = F)$$

$$\hookrightarrow 0.9375$$

Q2] The probability that student is accepted to a prestigious college is 0.3. If 5 students apply, what's the probability of at most 2 are accepted.

$$> \text{pbinom}(2, 5, 0.3)$$

$$\hookrightarrow 0.83692$$

$$H_0 = P_1 = P_2$$

$$H_1 = P_1 \neq P_2$$

$$> (0.22 * 200$$

$$> 0.185$$

$$> 1 - 0.185$$

$$> 0.815$$

$$> z =$$

$$2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$[1] 0.9969018$$

Accept H_0

Q. EQUALITY OF 2 POPULATION PROPORTION

- 1] In an early election campaign a telephone poll of 800 registered voters shows 460 in second poll opinion 520 of 1000 registered voters favoured the candidate at 5% level of significance is there sufficient evidence that popularity has decreased

$$H_0 = P_1 = P_2$$

$$H_1 = P_1 \neq P_2$$

$$> P = (460 \times 800 + 520 \times 1000) / (520 + 1000)$$

$$> P$$

$$> [1] .544$$

$$> 1 - 0.544$$

$$> Z = \sqrt{P(1-P)} \left(\frac{1}{520} + \frac{1}{1000} \right)$$

$$> Z^* (1 - \text{norm}(\text{abs}(Z)))$$

$$[1] 0.5444$$

Accept H_0

- Q2] From a cement 200 articles are drawn & 44 was found defective from cement. 200 samples are drawn out of which 30 was found defective test whether the proportion of defective items in 2 cement are significantly different

Q4] online score
to fav

graduate
20
40

051

Undergraduate
25
8

Is there any association b/w student's preference
for types of education & method

$\therefore H_0 = \text{Independent}, H_1 = \text{Dependent}$

$\gamma n = (20, 40, 25, 8)$
 $\gamma z = \text{matrix } (n, \text{row} = 2)$
 $\gamma \text{chsq_test}(z)$

Pearson's chi-sq^r test with later continuous
correction

data: z

X-squared = 18.05, df = 1, p-value = 2.75×10^{-6}

\therefore reject null hypothesis
 \therefore Both are dependent

$$= \int_2^4 \frac{n+2}{18} dx = \frac{1}{18} \int_2^4 (x^2 + 2x) dx$$

$$\text{for } -2 \leq x \leq 4$$

Hence cdf is

$$F(x) = 0 \quad \text{for } x < -2$$

$$= \frac{1}{18} \left(\frac{1}{3} x^3 + 2x^2 \right)$$

$$\text{for } -2 < x < 4$$

$$= 0 \quad \text{for } x > 4$$

PRACTICAL - 4 Testing of hypothesis

Q1] Sample mean & deviation given single population
a] Suppose the food level on the cook states
that it has atmost 2g of saturated fat in
a store cookies. In a sample of 35 cookies, it
was found that mean amount of saturated fat
per cookies 2.1g. Assume that sample is 0.3 at
(5% level of conf) can be rejected the claim on
food label

$$H_0 = \mu \leq 2, H_1 = \mu > 2$$

$$Z = (2.1 - 2) / (0.3 / \sqrt{35})$$

$$[1] \quad 972027$$

$$> 1 - \text{pnorm}(Z)$$

$$[1] \quad 0.0243$$

\therefore Reject the null hypothesis.
 \therefore Accept H_1

Q2] A sample of 100 customers was randomly selected
& it was found that avg spending was 275/- The
SD 30. Using 0.05 level of significance would you
conclude that amount spent by customer is more
than 250/-

$$H_0 = \mu \leq 250, H_1 = \mu > 250$$

$$Z = (275 - 250) / (30 / \sqrt{100})$$

$$[1] \quad 8.333$$

$$> 1 - \text{pnorm}(Z, 99) \quad [1] \quad 2.3057$$

\therefore Reject Null hypothesis
 \therefore Accept H_1

Training

H_1 = no change in IQ

H_0 = IQ increased after training

> a = c(120, 118, 125, 136, 121)

> b = c(110, 120, 123, 132, 125)

> z = sum([b-a]^2)/a)

> pchisq(z, df = length[b] - 1)

[1] 0.1135959

∴ Accept null hypothesis

∴ There is change in IQ after training.

next

3] In a big city, 325 men out of 600 men were found to be self employed. conclusion is that maximum men in city are self employed.

$H_0 = \mu = 0.5$, $H_1 = \mu \neq 0.5$

$\rightarrow Z = (0.5 - 0.325) / \sqrt{(0.5 * 0.5) / 600}$

$\rightarrow Z * 1 - \text{pnorm}(\text{abs}(z))$

[] 0.04155239.

Reject H_0
Accept H_1

4] Experience shows that 20% of manufactures products are of top quality. In 1 day production of 400 articles only 50 are top quality. Test hypothesis that experience of 20% of manufactured is wrong.

$H_0 = \mu = 0.2$

$H_1 = \mu \neq 0.2$

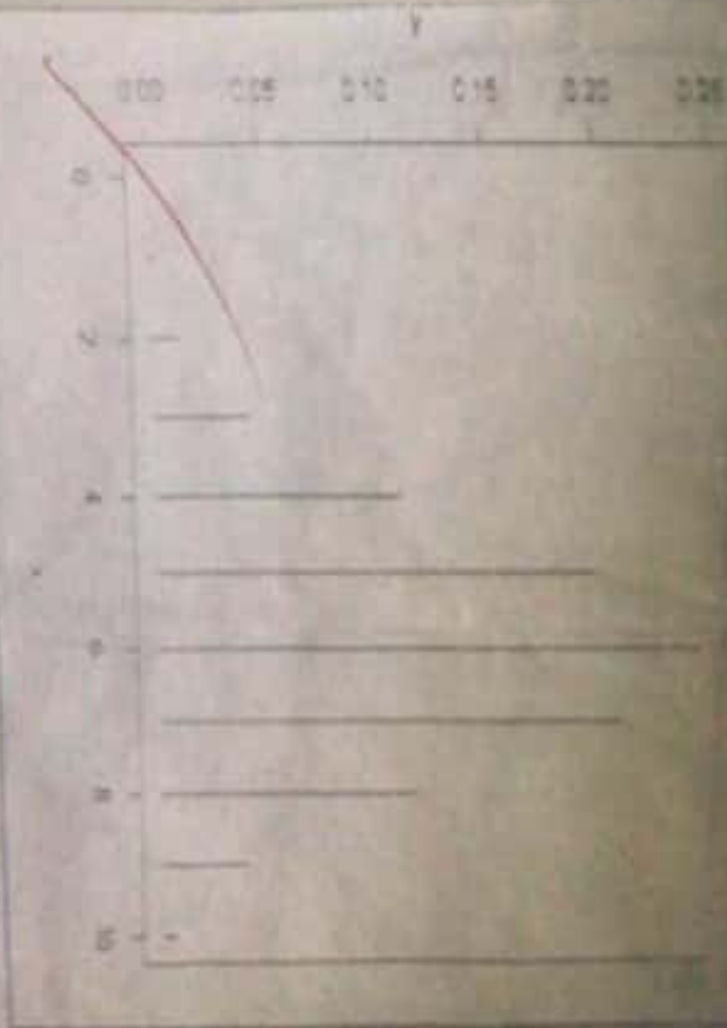
$\rightarrow Z = (0.125 - 0.20) / \sqrt{(0.2 * 0.8) / 400}$

$\rightarrow Z * 1 - \text{pnorm}(\text{abs}(z))$

[] 0.001768346

Reject H_0 , Accept H_1

lenovo



Q3) A fair coin is tossed 6 times the probability of
 head at any toss = 0.5. let x be no. of heads that
 comes up. calculate $P(X=2)$, $P(X=3)$, $P(1 \leq X \leq 5)$

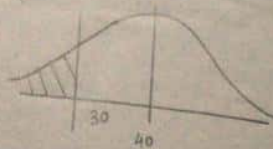
$$\begin{aligned} &> \text{dbinom}(2, 6, 0.5) \\ &\hookrightarrow 0.324135 \\ &> \text{dbinom}(3, 6, 0.5) \\ &\hookrightarrow 0.18522 \\ &> \text{dbinom}(2, 6, 0.5) + \text{dbinom}(3, 6, 0.5) + \text{dbinom}(4, 6, 0.5) \\ &\hookrightarrow 0.7437 \end{aligned}$$

Q4) For $n=10$, $p=0.6$, evaluate binomial probabilities and
 plot the graphs of pmf & cdf

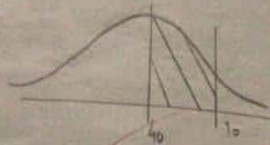
$$\begin{aligned} &> x = \text{seq}(0, 10) \\ &> y = \text{dbinom}(x, 10, 0.6) \\ &> y \\ &[1] \quad 0.0001048576 \quad 0.0015728640 \quad 0.0106168320 \quad 0.20065812 \\ &\quad 0.0424673280 \quad 0.1114767360 \quad 0.2508226560 \quad 0.2149908480 \quad 0.120932950 \end{aligned}$$

~~$> \text{plot}(n, y, \text{lab} = "sequence", \text{ylab} = "probabilities", "0", \text{pch} = 16)$~~
 ~~$> \text{rseq}(0, 10)$~~
 ~~$> y = \text{pbinom}(n, 10, 0.6)$~~
 ~~$> \text{plot}(n, y, \text{lab} = "sequence", \text{ylab} = "probabilities", "0", \text{pch} = 16)$~~

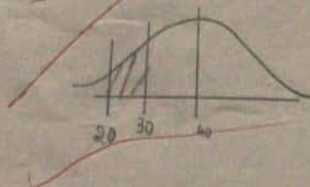
a)



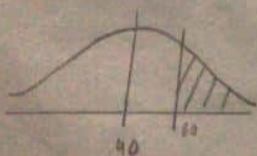
b)



c)



d)



PRACTICAL-03

Title - Normal Distribution

Q] A normal distribution of 100 students with mean = 40, SD = 15
Find no. of students whose marks are
(1) $P(X < 30)$ (2) $P(40 < X < 50)$ (3) $P(25 < X < 35)$
(4) $P(X > 60)$

$> \text{pnorm}(30, 40, 15)$
 $\hookrightarrow 0.2524925$

$> \text{pnorm}(50, 40, 15) - \text{pnorm}(40, 40, 15)$
 $\hookrightarrow 0.477499$

$> \text{pnorm}(38, 40, 15) - \text{pnorm}(25, 40, 15)$
 $\hookrightarrow 0.2107861$

$> 1 - \text{pnorm}(60, 40, 15)$
 $\hookrightarrow 0.09121122$

83] A quality control of engines finds that sample of 100 light have avg life of 470 hours. Assuming population SD = 25. Test whether the population mean is 480 hours. $\alpha = 0.05$.

$$H_0 = \mu \leq 480 \quad H_1 = \mu > 480$$

$$Z = \frac{470 - 480}{(25 / \sqrt{100})} = -4$$

$$P(Z, 99, \text{lower tail} = 7)$$

$$[1] 6.11257$$

Reject Null hypothesis

Accept H_1 .

84] A principal at school claims that the IQ is 100 of the students. A random sample of 30 students whose IQ was found to be 112. The SD of population = 15. Test the claim of principal.

$$H_0 = \mu = 100$$

$$H_1 = \mu > 100$$

$$Z = \frac{112 - 100}{(15 / \sqrt{30})} = 4.38178$$

$$[1] 4.38178$$

$$P(Z, 99, \text{lower tail} = F)$$

$$[1] 5.8856 \quad \alpha = 0.05$$

Reject Null Hypothesis.

PRACTICAL-5

Chi-Square Test

Q1) Use the following data to test whether the alternative conditions of home & child are independent

		Condition of home	
Condition of a child	clean	Dirty	
	clean	Dirty	
clean	70	50	
dirty	80	20	
	85	45	

$H_0 = \text{Both are independent}$, $H_1 = \text{Both are dependent}$

$\chi^2 = 6(70, 80, 35)$

$y = 6(50, 20, 45)$

$z = \text{data.frame}(x, y)$

[1]

#	x	y
1	70	50
2	80	20
3	85	45

$> \text{chsq.test}(z)$

Pearson's chi-squared test
data: z

$\chi^2\text{-squared} = 25.646$, $df = 2$, $p\text{-value} = 2.098 \times 10^{-5}$

Reject null hypothesis
Both are dependent

Q2] If $P(x)$ is pmf of a random variable X . If $P(x)$ represents pmf for random variable X . Find value of k . Then evaluate mean & variance.

Soln- As $P(x)$ is a pmf, it should satisfy the properties of pmf which are

- $P(x_i) > 0$ for all sample space
- $\sum P(x_i) = 1$

X	-1	0	1	2
$P(x)$	$\frac{k+1}{13}$	$\frac{k}{13}$	$\frac{1}{13}$	$\frac{k-4}{13}$

$$\sum P(x) = 1 = \frac{k+1}{13} + \frac{k}{13} + \frac{1}{13} + \frac{k-4}{13}$$

$$1 = \frac{k+1+k+1+k-4}{13}$$

$$13 = 3k - 2$$

$$15 = 3k$$

$$k = 5$$

X	$P(x)$	$X \cdot P(x)$	$E(X)^2$	$[E(X)]^2$
-1	$\frac{6}{13}$	$-\frac{6}{13}$	$\frac{6}{13}$	$\frac{36}{169}$
0	$\frac{5}{13}$	0	0	0
1	$\frac{1}{13}$	$\frac{1}{13}$	$\frac{1}{13}$	$\frac{1}{169}$
2	$\frac{1}{13}$	$\frac{2}{13}$	$\frac{4}{13}$	$\frac{4}{169}$
TOTAL	$\sum = 1$	$\sum = -\frac{3}{13}$	$\sum = \frac{11}{13}$	$\sum = \frac{41}{169}$

$$\therefore \text{Mean} = \sum X \cdot P(x) = \frac{-3}{13}$$

$$\therefore \text{Variance} = \sum E(X)^2 - \sum [E(X)]^2$$

$$= \frac{11}{13} - \frac{41}{169} = \frac{102}{169}$$

Q4] A random variable X follows normal distribution with $\mu = 10$, $\sigma = 2$. generate 100 obs & syntax & evaluate its mean, median & variance.

```
> x = rnorm(100, 10, 2)
> summary(x)
  Min      1st Q      Median      Mean      3rd Q      Max
  5.713      8.444      9.723      9.914     11.325     14.238

> var(x)
[1] 3.648924
```

Q5] Write a command to generate 10 s.n for normally distribution with $\mu = 50$, $\sigma = 4$. Find the sample mean & median.

```
> x = rnorm(10, 50, 4)
> summary(x)
  Min      1st Q      Median      Mean      3rd Q      Max
  44.73     50.46     52.01     52.35     54.39     58.95
```

Mean

SINGLE POPULATION PROPORTION

- 01) It is believed that coin is fair. The coin is tossed 40 times; 28 times head occurs. Indicate, whether the coin is fair or not at 95% $p_0 = 0.5$, $q_0 = 1 - p_0 = 0.5$

$$p = 28/40 = 0.7, n = 40, H_0 = \mu = 0.5$$

$$H_1 = \mu \neq 0.5$$

$$Z = (0.7 - 0.5) / \sqrt{(0.5 * 0.5) / 40}$$

$> Z$

$$> 2 * (1 - \text{pnorm}(\text{abs}(Z)))$$

$$[1] 0.01141204$$

Reject null hypothesis

Accept H_1

- 2] In a hospital 400 females & 520 males are born in a week. Do this confirm male & female are born equal in number.

$$H_0 = \mu = 0.5, H_1 = \mu \neq 0.5$$

$$Z = (0.52 - 0.5) / \sqrt{(0.5 * 0.5) / 1000}$$

$$[1] 1.2645$$

$$> 2 * (1 - \text{pnorm}(\text{abs}(Z)))$$

$$[1] 0.2060506$$

Reject H_0

Accept H_1

Q2) A die is tossed 120 times & following results are obtained

049

No. of turns

Frequency

1	30
2	25
3	18
4	10
5	22
6	15

Test the hypothesis that die is unbiased

H_0 = die is unbiased

H_1 = die is biased

> obs = c(30, 25, 18, 10, 22, 15)

> exp = sum(obs) / length(obs)

> exp

[1] 20

> z = sum((obs - exp) ^ 2 / exp)

> pchisq(z, df = length[obs] - 1)

[1] 0.9566

∴ Accept null hypothesis

∴ Die is unbiased

PRACTICAL-6

053

Topic - t-test

Q Let $n = 33.66, 33.87, 33.61, 34.14, 33.16, 33.57, 33.56, 33.76, 33.82, 33.55, 34.08, 34.01, 33.98, 34.29, 33.88, 33.74, 33.84, 33.74$
Write the R command for following test hypothesis

① $H_0: \mu = 3400, H_1: \mu \neq 3400$

② $H_0: \mu = 3400, H_1: \mu > 3400$

③ $H_0: \mu = 3400, H_1: \mu < 3400$

at 95% level of confidence. Also check at 95% level of confidence.

→ ① $H_0: \mu = 3400$

$H_1: \mu \neq 3400$

→ $n = c(33.66, 33.87, 33.61, 34.14, 33.16, 33.57, 33.56, 33.76, 33.82, 33.55, 34.08, 34.01, 33.98, 34.29, 33.88, 33.74, 33.84, 33.74)$

→ t-test ($n, mu = 3400, alter = "two.sided", confidence.level = 0.95$)
one sample t-test.

data: n

$t = -4.4885, df = 10, p\text{-value} = 0.002528$
95 percent level of confidence level.

3361.797 3386.03.

∴ Reject H_0

∴ Accept H_1

→ t-test (μ , $m = 3400$, alt. "two-sided", conf. level = 0.05)

t = -4.4865, $df = 19$, p-value = 0.0002528

alt. hypothesis: two mean is not equal to 3400

336.33 3387.57

sample estimates:

mean of x :

3373.95

∴ Reject H_0 ∴ Accept H_1

↳ ② $H_0 = \mu = 3400$

$H_1 = \mu > 3400$

t-test = -4.4865, $df = 19$, p-value = 0.995

alternative hypothesis: true mean is greater than 3400

3363.91 Inf

sample estimates:

Mean of x :

3373.95

Accept H_0

Q8] A die is tossed 180 times

No. of times	frequency
1	20
2	30
3	35
4	40
5	12
6	43

Test the hypothesis that die is unbiased
 $H_0 \rightarrow$ die is biased
 $H_1 \rightarrow$ die is unbiased

$\chi = (20, 30, 35, 40, 12, 43)$

χ^2 test (χ)

data: χ

χ^2 = 23.933, $df = 5$, p -value = 0.000

\therefore reject null hypothesis

\therefore Die is biased

Keshu

95 percent level of confidence.

Try 3855 563

Sample estimates

Mean of n

337 83.95

Rej H_0 Accept H_1

82) Below all the data of gain in weights on a different data A and B

Diet A: 26, 25, 32, 30, 43, 24, 14, 32, 24, 31, 31, 35, 25

Diet B: 44, 34, 22, 10, 47, 31, 40, 30, 32, 35, 18, 21

$$H_0: \mu_a - \mu_b = 0$$

$$H_1: \mu_a - \mu_b \neq 0$$

$a = (25, 32, 30, 43, 24, 14, 32, 24, 31, 31, 25, 35)$

$b = (44, 34, 22, 10, 47, 31, 40, 30, 32, 35, 18, 21)$

t-test (a, b, paired = T, alter = "two sided", conf.level = 0.95)

Paired test

data: a and b

$t = -0.62187$, $df = 11$, $p\text{-value} = 0.5429$

alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval

-14.2673 30 7.933447

sample estimate
mean of difference = 3.166667

Accept H_0
There is no difference in weights.

Q3] Eleven students gained the test after 1 month, they again gave the test after the tutions, do the marks gives confidence that students have benefited by coaching.

E_1 : 23, 20, 19, 21, 18, 20, 18, 17, 23, 16, 19

E_2 : 24, 19, 22, 18, 20, 22, 20, 20, 23, 20, 15
test at 99% level of confidence.

$E_1 = (23, 20, 19, 21, 18, 20, 18, 17, 23, 16, 19)$

$E_2 = (24, 19, 22, 18, 20, 22, 20, 20, 23, 20, 15)$

$H_0: \mu_1 = \mu_2$

$H_1: \mu_1 < \mu_2$

> t-test (μ_1, μ_2 , paired = T, alter = "less", conf. level = 0.99)
paired t-test

> data: μ_1 and μ_2

$t = -1.4832$, $df = 10$, $p\text{-value} = 0.0844$

alternative hypothesis: true difference in mean is less than 0

99 percent confidence Interval:

-1.0863333

sample estimate

mean of difference

-1

Accept H_0

2nd test $\mu = 3400$ 0.97
 alt. = "greater" $\mu > 3400$ [$\alpha = 0.03$]
 data: x

$t = 4.4865$, $df = 19$, $p\text{-value} = 0.0001864$ after data
 3 343.95 μ mean is greater than 3400
 3 373.95

sample size
 data of n :
 3 373.95
 Accept H_0

1st test: $\mu_1 = 3400$

$H_1: \mu_1 < 3400$

\rightarrow t-test (μ , $\mu_0 = 3400$, alt. = "less", conf. level = 0.03,
 one sided t-test)

data: n

t-test = 4.4865 $df = 19$, $p\text{-value} = 0.0001864$

95 percent level of confidence \rightarrow 338.394

sample of n :

Mean of n :

3 373.95

Reject H_0 Accept H_0

1st test (μ , $\mu_{\text{mean}} = 3400$, alt. = "less", conf. level = 0.03)

data: x

$t = 4.4865$, $df = 19$, $p\text{-value} = 0.0001864$

alternative hypothesis μ is less than 3400

Q4] Two drugs for BP was given & data was collected
 $d_1 = 0.3, 1.6, 0.2, -1.2, 0.1, 3.4, 8.9, 0.8, 0.2$

$d_2 = 1.4, 0.8, 1.1, 0.1, 0.1, 4.4, 5.5, 1.6, 4.8, 3.4$

The two drugs have same effect, check whether two drugs have same effect on patient or not

$$H_0 = d_1 = d_2$$

$$H_1 = d_1 \neq d_2$$

$$> d_1 = c(0.3, 1.6, 0.2, -1.2, -0.1, 3.4, 8.9, 0.8, 0.2)$$

$$> d_2 = c(1.4, 0.8, 1.1, 0.1, 0.1, 4.4, 5.5, 1.6, 4.8, 3.4)$$

> t.test(d1, d2, alt = "two.sided", paired = T, conf.level = 0.95)

Paired t-test

data: d1 and d2

95 percent confidence interval

mean of the difference
-1.58

Reject H_0

Accept H_1

Q5 If there is difference in salaries for the same job in 2 different countries.

$L_A = c(5300, 4995, 4936, 40470, 36963)$

$L_B = c(62990, 58850, 4995, 55263, 47674, 43532)$

$$H_1 = \sigma_1 = \sigma_2$$

$$H_0 = \sigma_1 \neq \sigma_2$$

\rightarrow t-test (C.A.Cb) paired = T, alter = "two-sided"
 conf. level = 0.95

paired t test

data: Ca and Cb

$$t = -4.4569, df = 5$$

alternative hypothesis

$$p\text{-value} = 0.00666$$

t-test differ of difference
 investments

not equal to 0

95 percent confidence interval

$$-10404.821$$

$$-2792.848$$

Sample estimates

mean of the difference : -6698.863

Reject H_0

Accept H_1

Mem

PRACTICAL-7

F-test

- Q1 Life expectancy in 10 regions of India in 1990 & 2000 are given below. Test whether variance at the 2-times are the same
- 1990: 37, 39, 36, 42, 45, 44, 46, 49, 50, 51
- 2000: 44, 45, 47, 43, 42, 49, 50, 41, 48, 58, 42

$$x = (37, 39, 42, 45, 46, 49, 50, 51)$$

$$y = (44, 45, 47, 43, 42, 49, 50, 41, 48, 58, 42)$$

var.test(x, y)

F test to compare two variances:
data: x and y.

$$F = 1.1449, \text{ num df} = 9, \text{ denom df} = 11$$

$$p\text{-value} = 0.81845$$

alternative hypothesis: true ratio of variances not equal to 1

95% confidence interval:

$$0.3141005$$

$$0.4780350$$

sample estimates:

Ratio of variances:

$$1.1449$$

	25	28	26	22	29	31	31	26	31
I	30	25	31	32	23	25	36	26	31
II				32	32	27	31		

for following data. test hypothesis for
 (1) equality of two population mean (t-test)
 (2) equality of two population variance (F-test)

Let $x = C C 175, 168, 145, 190, 81, 135, 175, 200$
 $y = C C 180, 170, 153, 130, 179, 183, 187, 200$
 \Rightarrow Var. test (x, y)

F test to compare two variances.
 data: x and y .

$F = 1.25$, num of 7 , denom of 7 ,
 p-value alternative hypothesis: the
 ratio of variances is not equal to 1
 0.250289 0.2437398

Sample estimates
 of ratio of variances:
 1.250021

t-test (n)

one sample t-test.
 data: 0

Sample estimates

Mean of x :

177.375

Q3] The following are the prices of commodities in the sample of shop selected at random from different cities.

C.A = C.C. 74.10, 77.70, 75.35, 74, 73.80, 79.30,
75.80, 76.80, 77.10, 76.40
C.B = C.C. 70.80, 74.90, 76.20, 77.80, 78.10,
74.20, 69.80, 81.20.

4 var. test (C.A, C.B).

F-test to compare two variances
data a and b.

$F = 0.22579$, num df = 9, denom df = 7,
pvalue = 0.04249

alternative hypothesis: true ratio of variance
is not equal to 1

95% confidence level:

Sample estimate

Ratio of variance:

0.22579,

Import CSV file in excel - import file in R & apply the test to check equality of variance of 2 data

obs1 \rightarrow 10, 15, 17, 11, 16, 20
 obs2 \rightarrow 15, 14, 10, 11, 12, 19

> data = read.csv (file.choose (), header = TRUE)
 > Data

	obs 1	obs 2
1	10	15
2	15	14
3	17	16
4	11	11
5	16	12
6	20	19

> attach (Data)

> var.test (obs1, obs2)

data: obs1 and obs2

F = 1.7068, num df = 5, denom df = 5,

p-value = 0.5717

alternative hypothesis: true ratio of variances is not equal to 1

95% confidence interval

0.233838

12.192660

sample estimates

Q5] I: 25, 28, 26, 28, 22, 29, 31, 31, 26, 31
 II: 30, 25, 31, 32, 32, 23, 25, 31, 31, 32,
 32, 32, 27, 31, 38, 24

at 95% of confidence level, check the ratio of population variation.

$$H_0 = \sigma_1^2 = \sigma_2^2$$

$$H_1 = \sigma_1^2 \neq \sigma_2^2$$

$$n = 10 \text{ (25, 28, 26, 28, 22, 29, 31, 31, 26, 31)}$$

$$y = 10 \text{ (30, 25, 31, 32, 32, 23, 25, 31, 31, 32, 32, 32, 27, 31, 38, 24)}$$

$$\text{Var Test } (n, y)$$

F test

to compare two variance

$$p\text{-value} = 0.4535$$

Accept H_0 .

\therefore Variance of I & II are same.

Ans

The time of (in hrs) of 10 randomly selected 9 volt battery of a certain company is as follows
 28.9, 15.2, 28.7, 72.5, 48.0, 52.4,
 37.6, 49.5, 62.1, 54.1. Test the hypothesis that the population median is 63 against the alternative hypothesis less than 63 at 5% level of significance.

↳ $a = \{28.9, 15.2, 28.7, 72.5, 48.0, 52.4, 37.6, 49.5, 62.1, 54.1\}$

↳ which ($a > 63$)
 [4]

↳ $y = \text{which } (a > 63)$

↳ length (y)

↳ [1]

↳ $d = \text{which } (a < 63)$

↳ length (d)

↳ [9]

↳ $q_{\text{binom}}(0.05, 10, 0.5)$
 [12]

If q_{binom} value greater than d then accept the null hypothesis.

Q2 Following data gives weight of 40 students in random sample.

46, 49, 57, 64, 46, 67, 54, 48, 69, 61, 57, 54, 50,
48, 65, 61, 66, 54, 50, 48, 49, 62, 67, 49,
47, 55, 59, 63, 53, 56, 67, 49, 60, 64,
53, 50, 48, 51, 52, 54.

Use sign test to test whether mean weight of the population is 50 kg against alternative that it is greater than 50 kg.

$\hookrightarrow \pi = 0$ (46, 49, 57, 64, 46, 67, 54, 48, 69, 61, 57, 54, 50, 48, 65, 61, 66, 54, 50, 48, 49, 62, 67, 49, 47, 55, 59, 63, 53, 56, 67, 49, 60, 64, 53, 50, 48, 51, 52, 54)

$\hookrightarrow S_p = \text{which } (\pi > 50)$

$\hookrightarrow \text{length}(S_p)$
[12] [12]

$\hookrightarrow S_n = \text{which } (\pi < 50)$

$\hookrightarrow \text{length}(S_n)$
[12]

$\hookrightarrow \text{qbinom}(0.05, 40, 0.5)$
[15]

So, S_p is greater than binom then Reject Null Hypothesis.

Median age of tourists in visiting a certain place is claimed to be 41 years. A random sample of 17 tourists have age

48, 52, 25, 29, 57, 39, 45, 36, 30, 49, 28, 31, 44, 63, 32, 65, 42.

Use sign test to check the claim

H_0 :- age = 41

H_1 :- age \neq 41

$y = c$ (48, 52, 25, 29, 57, 39, 45, 36, 30, 49, 28, 39, 44, 63, 32, 65, 42)

$z = \text{which}(y > 41)$

$\rightarrow \text{length}(z)$

[1] 9

$j = \text{which}(y < 41)$

$\rightarrow \text{length}(j)$

[1] 8

$\text{qbinom}(0.05, 17, 0.5)$

[1] 5

Accept null hypothesis.

09. The time in minutes that a patient has to wait for consultation is recorded as follow.
 $y = (15, 12, 22, 25, 20, 21, 32, 28, 12, 25, 29, 26)$
 Use wilcox test to check whether the median in town is greater than 5% level of median
 $H_0: - \text{mean } \cancel{25} \geq 20$ significant
 $H_1: - \text{mean } \cancel{25} < 20$

$y = \text{which}(x \geq 50)$

$z = \text{which}(y \leq 20)$

$\text{length}(z)$

[1] 3

$\text{wilcox.test}(y, \text{alternative} = "greater")$

[1] Wilcoxon signed rank test with continuity correction.
 data: x

$V = 78$, $p\text{-value} = 0.001253$

Accept null hypothesis.

> aov (values ~ wind, e)

071

Terms:

Sum of Squares 203.333 ind

Deg. of Freedom 2

Residuals
54.000
12

Adjusted Standard error: 2.12132

> oneway.test (values ~ wind, e)

data: values and ind

F = 21.537, num df = 2.000, denom df = 7.9314

p-value = 0.0006232

Reject the null hypothesis.

The following gives the life of tyres of brand

A	B	C	D
20	18	21	15
23	15	19	14
18	17	22	16
17	20	17	18
22	16	20	14
24	17		16

Test the hypothesis.

> a = c (A)

> b = c (B)

> c = c (C)

> d = c (D)

> L = list(a1=a, b1=b, c1=c, d1=d)

> L

\$ a1

[1] 20 23 18 17 22 24

\$ b1

[1] 18 15 17 20 16 17


```

> d = c (data of no-exercise)
> p = c (data of 20min)
> q = c (data of 60min)
> L = list(a1 = d, b1 = p, c1 = q)
> L

```

```
$[a1]
```

23 26 31 48 58 37 29 44

```
$[b1]
```

22 27 29 39 46 48 49 65

```
$[c1]
```

59 66 38 49 56 60 56 62

```
> e = stack(L)
```

```
> e
```

Data is arranged

```
> oneway.test(values = ind, e)
```

data values and ind

F = 5.9169, num df = 2.000, denom df = 18.333

p-value = 0.01633

Reject Null hypothesis

reject

```

> a = c (data of A)
> b = c (data of B)
> c = c (data of C)
> L = list (a1=a, b1=b, c1=c)
> L

```

```

# a1
[1] 44 45 46 47 48 49

```

```

# b1
[1] 40 42 50 52 55

```

```

# c1
[1] 50 53 58 59

```

```

> e = stack(L)

```

```

> e

```

The data is arranged in continuous form.

```

> oneway.test (values = ind, e)

```

data: values and ind

$F = 6.325$, num df = 2.000, denom df = 5.413,
 $p\text{-value} = 0.03824$

Reject the null hypothesis.

The experiment was conducted on 8 person & the observation noted are.

NO exercise - 23, 26, 51, 48, 58, 37, 29, 44

20 min - 22, 27, 29, 39, 46, 48, 49, 65

60 min - 59, 66, 38, 49, 56, 60, 56, 62

Test the hypothesis are equal.

$\# c1$
 $c1 = 19 \quad 2 = 14 \quad 20$

$\# d1$
 $d1 = 15 \quad 14 \quad 16 \quad 18 \quad 14 \quad 16$
 $> e = \text{stack}(L)$
 $> e$

The data is formed in the way of data.

$> \text{oneway.test}(\text{values} \sim \text{ind}, e)$
 data: $\# \text{ Values and ind}$
 $F = 6.6498$, num df = 3.000, denom df = 10.093
 $p\text{-value} = 0.009346$
 Reject the null hypothesis.

3) This type of way is applied for the protection of cars & no of days of protection were needed. Test them are equally effective

A	B	C
44	40	50
45	42	53
46	51	58
47	52	59
48	55	
49		

Test whether 3 are equally effective.

PRACTICAL-9
data gives the effect of 3

a) The following
treatments

T1	T2	T3
2	10	10
3	8	13
7	7	14
2	5	13
6	10	15

Test the hypothesis that all treatment
are equally affected

```
> t1 = c(2, 3, 7, 2, 6)
> t2 = c(10, 8, 7, 5, 10)
> t3 = c(10, 13, 14, 13, 15)
> data = data.frame(t1, t2, t3)
> data
```

	t1	t2	t3
1	2	10	10
2	3	8	13
3	7	7	14
4	2	5	13
5	6	10	15

```
> e = stack(data)
> e
```

The numbers are arranged in the form of
data

The weight in kgs of the person before and after stop smoking is

Before: 65, 75, 75, 72, 62 | After: 72, 72, 72, 66, 82
 Use wilcoxon test to check weight of a person is less after smoking at 5% level of significance.

$$X = C(65, 75, 75, 72, 62)$$

$$Y = C(72, 72, 72, 66, 82)$$

$$Z = X - Y$$

Z

[1] -7 0 3 -7 -4

wilcoxon test (Z, $\mu_0 = 0$, alternative = "less")
 correction

data: Z

$$V = 1, \text{ p-value} = 0.09873$$

alternative hypothesis true location
 is less than 0

Reject null hypothesis

Result

Q2] If the random variable x follows the normal distribution with mean $= 50$, $V = 10.0$
 find ① $P(X \leq 40)$ ② $P(X > 65)$ ③ $P(X \leq 32)$
 ④ $P(35 \leq x \leq 60)$ ⑤ $P(20 \leq x \leq 30)$

a) $> \text{pnorm}(40, 50, 10)$
 $\hookrightarrow 0.9772499$

b) $> 1 - \text{pnorm}(65, 50, 10)$
 $\hookrightarrow 0.03593032$

c) $> \text{pnorm}(32, 50, 10)$
 $\hookrightarrow 0.0668072$

d) $> \text{pnorm}(60, 50, 10) - \text{pnorm}(35, 50, 10)$
 $\hookrightarrow 0.7745375$

e) $> \text{pnorm}(30, 50, 10) - \text{pnorm}(20, 50, 10)$
 $\hookrightarrow 0.02140023$

Q3] Let $X \sim N(30, 50, 160, 400)$ find k_1 & k_2 such that $P(X < k_1) = 0.8$ & $P(X > k_2) = 0.8$

$> \text{qnorm}(0.8, 160, 20)$
 $\hookrightarrow 165.0669$

$> \text{qnorm}(0.8, 160, 20)$
 $\hookrightarrow 176.8324$

Q2]

