MATH-505A: Homework # 4

Due on Friday, September 19, 2014

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Exercise # 2.1

(1)

Given: X is a random variable \Longrightarrow

$$\{\omega \in \Omega : X(\omega) \le x\} \forall x \in R \tag{1}$$

Part A) To Prove: aX is a random variable

Consider Y = aX, then since 1 holds:

Case1: $a \ge 0$

Then $\{\omega \in \Omega : aX(\omega) \leq x'\} \forall x' \in R \text{ where } x' = ax$

Case2: $a \leq 0$

Then $\{\omega \in \Omega : aX(\omega) \ge x'\} \forall x' \in R \text{ where } x' = ax \implies \bigcup \{\{\omega \in \Omega : aX(\omega) \le x''\}\}^c \text{ where } x'' = x'$

Case 3: $ais \ 0$ Then, aX = 0**Case 1:** x < 0

 $\{\omega \in \Omega : aX(\omega) = \phi\}$

Case 2: $x \ge 0$ $\{\omega \in \Omega : aX(\omega) = \Omega\}$

(2)

For part 1, Y' = aX is also a random variable: **To Prove:** Y = Y' + b is a random variable where Y' is a random variable and b is a constant.

Since Y' is a random variable: $\{\omega \in \Omega : Y(\omega) \le y\} \forall y \in R \text{ and so, } \{\omega \in \Omega : Y(\omega) + b \le y'\} \forall y' \in R \text{ where } y' = y + b$

Hence Y' + b is a random variable $\implies aX + b$ is a random variable

(3)

p(H) = p; p(T) = 1 - p

Tossing a coin n times is a binomial process(each individual toss is a bernoulli process) and let A be the event such that k out of n tosses are heads:

 $p(A) = \binom{n}{k} p^k * (1-p)$

(4)

(5)

(4)

Exercise	# 2.3			
(1)				
(2)				
(3)				

(5)