Day52_K-Nearest_Neighbors_(KNN)_Classifier

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Introduction

K-Nearest Neighbors (KNN) is a simple and powerful machine learning algorithm used for **classification** and **regression**. It works by finding the 'k' closest data points to a new input and making predictions based on them.

There are two types of KNN:

- KNN Classifier: Assigns the class that most of the nearest neighbors belong to (majority voting).
- KNN Regressor: Predicts a value by averaging the values of the nearest neighbors.

Distance Metrics in KNN

• Euclidean Distance (p=2): Straight-line distance between two points in space, calculated as:

$$\text{Euclidean} = \sqrt{\sum (x_i - y_i)^2}$$

• Manhattan Distance (p=1): Distance measured along axes at right angles (like a grid):

$$\text{Manhattan} = \sum |x_i - y_i|$$

Both methods measure "closeness," and the best choice depends on your data's shape and scale.

Scaling is Important: Always apply scaling (like StandardScaler) to ensure all features are treated equally in distance calculations.

Balancing Imbalanced Data If your dataset has 99% of one class and 1% of another, your model may become biased.

- Case 1 (Model 1): Downsample the majority class to 70%, increase minority samples → Accuracy: a1
- Case 2 (Model 2): 75% downsample + 25% upsample \rightarrow Accuracy: a2
- Case 3 (Model 3): 80% downsample + 20% upsample \rightarrow Accuracy: a3
- Final balanced model = (a1 + a2 + a3) / 3

This process is known as ${\bf SMOTE}$ – Synthetic Minority Over-sampling Technique.

How KNN Works

- 1. Choose the number of neighbors k.
- 2. Calculate the distance between the new data point and every other point in the dataset.
- 3. Sort the distances and choose the top \mathbf{k} nearest neighbors.
- 4. For **classification**, return the most common class.

5. For **regression**, return the average of their values.

Manual Example (Math + CS Marks)

We want to predict the result (pass/fail) of a student with: - Math = 6, CS = 8 using K = 3

Math	CS	Result
4	3	F
6	7	P
7	8	P
5	5	\mathbf{F}
8	8	Р

We'll use Euclidean distance:

```
[2]: import numpy as np
from collections import Counter

samples = np.array([[4,3],[6,7],[7,8],[5,5],[8,8]])
labels = np.array(['f','p','p','f','p'])
new_point = np.array([6,8])
```

```
[3]: # Step 1: Compute distances
distances = [np.sqrt(((new_point - pt)**2).sum()) for pt in samples]
```

```
[4]: # Step 2: Show distances
for i, d in enumerate(distances):
    print(f"Distance to {samples[i]} (label={labels[i]}): {d:.2f}")
```

```
Distance to [4 3] (label=f): 5.39
Distance to [6 7] (label=p): 1.00
Distance to [7 8] (label=p): 1.00
Distance to [5 5] (label=f): 3.16
Distance to [8 8] (label=p): 2.00
```

```
[5]: # Step 3: Top 3 Neighbors
sorted_idx = np.argsort(distances)[:3]
nearest_labels = labels[sorted_idx]
print("\nTop 3 Nearest Labels:", nearest_labels)
```

Top 3 Nearest Labels: ['p' 'p' 'p']

```
[6]: # Step 4: Predict by majority
print("Predicted class:", Counter(nearest_labels).most_common(1)[0][0])
```

Predicted class: p

1 Import Required Libraries

```
[7]: import pandas as pd
import numpy as np
from sklearn.neighbors import KNeighborsClassifier
from sklearn.linear_model import LogisticRegression
from sklearn.preprocessing import StandardScaler
from sklearn.model_selection import train_test_split
from sklearn.metrics import accuracy_score, confusion_matrix
import warnings
warnings.filterwarnings('ignore')
```

2 Load Dataset

```
[8]:
        User ID Gender Age EstimatedSalary Purchased
    0 15624510
                  Male
                                       19000
                         19
    1 15810944
                  Male
                                       20000
                                                     0
                         35
    2 15668575 Female
                        26
                                       43000
                                                     0
    3 15603246 Female
                         27
                                       57000
                                                     0
    4 15804002
                  Male
                                       76000
                                                     0
                         19
```

3 Feature Selection

```
[9]: X = dataset[["Age", "EstimatedSalary"]].values
y = dataset["Purchased"].values
```

4 Train-Test Split

```
[10]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.25, u arandom_state=0)
```

5 Apply StandardScaler

```
[11]: scaler = StandardScaler()
    X_train_scaled = scaler.fit_transform(X_train)
    X_test_scaled = scaler.transform(X_test)
```

6 Try KNN with different parameters (one by one for beginners)

6.1 Model A: k=3, p=1 (Manhattan)

```
[12]: # Model A: k=3, p=1 (Manhattan)
model_a = KNeighborsClassifier(n_neighbors=3, p=1)
model_a.fit(X_train_scaled, y_train)
y_pred_a = model_a.predict(X_test_scaled)
print("Model A - k=3, p=1 (Manhattan):", accuracy_score(y_test, y_pred_a))
```

Model A - k=3, p=1 (Manhattan): 0.93

6.2 Model B: k=3, p=2 (Euclidean)

```
[13]: # Model B: k=3, p=2 (Euclidean)
model_b = KNeighborsClassifier(n_neighbors=3, p=2)
model_b.fit(X_train_scaled, y_train)
y_pred_b = model_b.predict(X_test_scaled)
print("Model B - k=3, p=2 (Euclidean):", accuracy_score(y_test, y_pred_b))
```

Model B - k=3, p=2 (Euclidean): 0.93

6.3 Model C: k=4, p=1 (Manhattan)

```
[14]: # Model C: k=4, p=1 (Manhattan)
model_c = KNeighborsClassifier(n_neighbors=4, p=1)
model_c.fit(X_train_scaled, y_train)
y_pred_c = model_c.predict(X_test_scaled)
print("Model C - k=4, p=1 (Manhattan):", accuracy_score(y_test, y_pred_c))
```

Model C - k=4, p=1 (Manhattan): 0.93

6.4 Model D: k=4, p=2 (Euclidean)

```
[15]: # Model D: k=4, p=2 (Euclidean)
model_d = KNeighborsClassifier(n_neighbors=4, p=2)
model_d.fit(X_train_scaled, y_train)
y_pred_d = model_d.predict(X_test_scaled)
print("Model D - k=4, p=2 (Euclidean):", accuracy_score(y_test, y_pred_d))
```

Model D - k=4, p=2 (Euclidean): 0.92

6.5 Model E: k=5, p=1 (Manhattan)

```
[16]: # Model E: k=5, p=1 (Manhattan)
model_e = KNeighborsClassifier(n_neighbors=5, p=1)
model_e.fit(X_train_scaled, y_train)
y_pred_e = model_e.predict(X_test_scaled)
print("Model E - k=5, p=1 (Manhattan):", accuracy_score(y_test, y_pred_e))
```

```
Model E - k=5, p=1 (Manhattan): 0.93
```

6.6 Model F: k=5, p=2 (Euclidean)

```
[17]: # Model F: k=5, p=2 (Euclidean)
model_f = KNeighborsClassifier(n_neighbors=5, p=2)
model_f.fit(X_train_scaled, y_train)
y_pred_f = model_f.predict(X_test_scaled)
print("Model F - k=5, p=2 (Euclidean):", accuracy_score(y_test, y_pred_f))
```

Model F - k=5, p=2 (Euclidean): 0.93

7 Without scaling

```
[18]: # Without scaling
model_raw = KNeighborsClassifier(n_neighbors=4, p=1)
model_raw.fit(X_train, y_train)
y_pred_raw = model_raw.predict(X_test)
acc_raw = accuracy_score(y_test, y_pred_raw)
print("\nAccuracy without scaling:", acc_raw)
```

Accuracy without scaling: 0.81

8 Results Comparison Table

```
[20]: results_df = pd.DataFrame({
          "Model": ["A", "B", "C", "D", "E", "F", "G (No Scale)"],
          "k": [3, 3, 4, 4, 5, 5, 4],
          "Distance Metric (p)": [1, 2, 1, 2, 1, 2, 1],
          "Accuracy": [
              accuracy_score(y_test, y_pred_a),
              accuracy_score(y_test, y_pred_b),
              accuracy_score(y_test, y_pred_c),
              accuracy_score(y_test, y_pred_d),
              accuracy_score(y_test, y_pred_e),
              accuracy_score(y_test, y_pred_f),
              acc_raw
          ]
      })
      print("\nComparison Table:\n")
      print(results_df)
```

Comparison Table:

Model k Distance Metric (p) Accuracy

```
0
               A 3
                                                   0.93
                                           1
                  3
                                           2
                                                   0.93
1
               В
2
               С
                  4
                                           1
                                                   0.93
3
               D
                  4
                                           2
                                                   0.92
                                                   0.93
4
                  5
                                           1
5
               F
                   5
                                           2
                                                   0.93
6
   G (No Scale)
                                                   0.81
```

9 Bonus: Loop all combinations for flexibility

9.1 Try different KNN parameters and compare using list logic (for advanced learners)

```
results_loop = []
for k in [3, 4, 5]:
    for p in [1, 2]:
        model = KNeighborsClassifier(n_neighbors=k, p=p)
        model.fit(X_train_scaled, y_train)
        y_pred = model.predict(X_test_scaled)
        acc = accuracy_score(y_test, y_pred)
        results_loop.append((k, p, acc))
        print(f"k={k}, p={p} → Accuracy: {acc:.4f}")
```

10 Conclusion

- KNN works well for both classification and regression when properly scaled.
- Euclidean (p=2) and Manhattan (p=1) distances give slightly different results depending on data.
- Accuracy varies with k; optimal value of k must be found using testing or cross-validation.
- Scaling improved accuracy from 0.81 (raw) to over 0.93 in some configurations.
- We manually verified prediction with distance calculations.
- Use a comparison table to select the best k and distance combination.