

# Day55\_Naive\_Bayes\_Classifier

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## Naive Bayes Classifier

Naive Bayes is a family of **probabilistic classifiers** based on Bayes' Theorem, with the “naive” assumption of conditional independence between features.

It works surprisingly well for many real-world problems like spam detection, sentiment analysis, and recommendation systems.

## Bayes Theorem

Bayes' Theorem allows us to reverse conditional probabilities:

$$P(A|B) = (P(B|A) * P(A)) / P(B)$$

- **P(A|B)**: Posterior Probability (What we want to find)
- **P(B|A)**: Likelihood
- **P(A)**: Prior Probability
- **P(B)**: Marginal Probability

## Types of Naive Bayes:

1. **GaussianNB** – works with continuous data, assumes Gaussian (normal) distribution.
2. **BernoulliNB** – works with binary data (0/1 features).
3. **MultinomialNB** – works with counts (e.g., word frequencies in NLP).

## Real-Life Examples

- Booking Sites: “80% seats sold out” → Predict urgency using probabilities
- Emails: Classify as spam or not based on keywords
- Sentiment Analysis: Based on word distribution, classify a review as positive or negative

## Real-Life Example: Manual Naive Bayes Calculation – Spam Classification

### Problem:

We want to classify whether a new email is **Spam** or **Not Spam** based on whether it contains the words "offer" and "win".

### Step 1: Training Data

Email ID	offer	win	Class
E1	1	1	Spam
E2	1	0	Spam
E3	0	1	Not Spam
E4	0	0	Not Spam

Email ID	offer	win	Class
E5	1	1	Spam

### Step 2: New Email to Predict

- The email contains both “**offer**” and “**win**”
- Features: offer = 1, win = 1

We calculate:

- $P(\text{Spam} \mid \text{offer}=1, \text{win}=1)$
- $P(\text{Not Spam} \mid \text{offer}=1, \text{win}=1)$

### Step 3: Naive Bayes Components

#### Prior Probabilities

- $P(\text{Spam}) = 3/5 = 0.6$
- $P(\text{Not Spam}) = 2/5 = 0.4$

#### Likelihoods

**Among Spam emails (3 total):** -  $P(\text{offer}=1 \mid \text{Spam}) = 3/3 = 1.0$   
-  $P(\text{win}=1 \mid \text{Spam}) = 2/3 = 0.67$

**Among Not Spam emails (2 total):**

- $P(\text{offer}=1 \mid \text{Not Spam}) = 0/2 = 0$
- $P(\text{win}=1 \mid \text{Not Spam}) = 1/2 = 0.5$

### Step 4: Naive Bayes Formula (Ignoring denominator):

$P(\text{Spam} \mid \text{offer}=1, \text{win}=1) = P(\text{offer}=1 \mid \text{Spam}) \times P(\text{win}=1 \mid \text{Spam}) \times P(\text{Spam})$   
 $= 1.0 \times 0.67 \times 0.6 = \mathbf{0.402}$

No  $P(\text{Not Spam} \mid \text{offer}=1, \text{win}=1)$   
 $= 0 \times 0.5 \times 0.4 = \mathbf{0}$

#### Final Prediction:

Since  $0.402 > 0$ , the email is predicted to be **SPAM**.

**Note:** Laplace Smoothing (Bonus)

To avoid zero probabilities: -  $P(\text{offer}=1 \mid \text{Not Spam}) = (0 + 1) / (2 + 2) = 0.25$

Smoothing avoids multiplying by 0 and improves model stability.

## 1 Importing Libraries

```
[2]: import pandas as pd
import numpy as np
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler, MinMaxScaler
from sklearn.naive_bayes import GaussianNB, BernoulliNB, MultinomialNB
from sklearn.metrics import accuracy_score, confusion_matrix, \
    classification_report
import warnings
warnings.filterwarnings('ignore')
```

## 2 Load and Explore Dataset

```
[3]: # Load dataset
dataset = pd.read_csv(r"C:\Users\Lenovo\Downloads\logit_classification.csv")
dataset.head()
```

```
[3]:
```

	User ID	Gender	Age	EstimatedSalary	Purchased
0	15624510	Male	19	19000	0
1	15810944	Male	35	20000	0
2	15668575	Female	26	43000	0
3	15603246	Female	27	57000	0
4	15804002	Male	19	76000	0

## 3 Feature Selection and Splitting

```
[4]: X = dataset[["Age", "EstimatedSalary"]].values
y = dataset["Purchased"].values

X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, \
    random_state=42)
```

## 4 Feature Scaling

### 4.1 Standardization (for Gaussian & Bernoulli)

```
[5]: # Standardization (for Gaussian & Bernoulli)
scaler = StandardScaler()
X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.transform(X_test)
```

## 4.2 MinMax Scaling (for MultinomialNB)

```
[6]: minmax = MinMaxScaler()
X_train_minmax = minmax.fit_transform(X_train)
X_test_minmax = minmax.transform(X_test)
```

# 5 Model Training and Evaluation

## 5.1 GaussianNB

```
[7]: print("=== GaussianNB ===")
gnb = GaussianNB()
gnb.fit(X_train, y_train)
y_pred_gnb = gnb.predict(X_test)
print("Accuracy:", accuracy_score(y_test, y_pred_gnb))
print(confusion_matrix(y_test, y_pred_gnb))
print(classification_report(y_test, y_pred_gnb))
```

=== GaussianNB ===

Accuracy: 0.925

[[50 2]

[ 4 24]]

	precision	recall	f1-score	support
0	0.93	0.96	0.94	52
1	0.92	0.86	0.89	28
accuracy			0.93	80
macro avg	0.92	0.91	0.92	80
weighted avg	0.92	0.93	0.92	80

## 5.2 BernoulliNB

```
[8]: print("=== BernoulliNB ===")
bnb = BernoulliNB()
bnb.fit(X_train_scaled, y_train)
y_pred_bnb = bnb.predict(X_test_scaled)
print("Accuracy:", accuracy_score(y_test, y_pred_bnb))
print(confusion_matrix(y_test, y_pred_bnb))
print(classification_report(y_test, y_pred_bnb))
```

=== BernoulliNB ===

Accuracy: 0.7875

[[49 3]

[14 14]]

	precision	recall	f1-score	support
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0	0.78	0.94	0.85	52
1	0.82	0.50	0.62	28
accuracy			0.79	80
macro avg	0.80	0.72	0.74	80
weighted avg	0.79	0.79	0.77	80

### 5.3 MultinomialNB

```
[9]: print("=== MultinomialNB ===")
mnb = MultinomialNB()
mnb.fit(X_train_minmax, y_train)
y_pred_mnb = mnb.predict(X_test_minmax)
print("Accuracy:", accuracy_score(y_test, y_pred_mnb))
print(confusion_matrix(y_test, y_pred_mnb))
print(classification_report(y_test, y_pred_mnb))
```

```
=== MultinomialNB ===
Accuracy: 0.65
[[52  0]
 [28  0]]
```

	precision	recall	f1-score	support
0	0.65	1.00	0.79	52
1	0.00	0.00	0.00	28
accuracy			0.65	80
macro avg	0.33	0.50	0.39	80
weighted avg	0.42	0.65	0.51	80

## 6 Observations

- **GaussianNB** works best for continuous data like Age and Salary.
- **BernoulliNB** assumes binary features — accuracy may be lower here.
- **MultinomialNB** requires positive features — MinMaxScaler helps here.

Always choose the right NB variant depending on the feature types in your dataset

## 7 Summary: Naive Bayes Classifiers

In this notebook, we explored and implemented three types of Naive Bayes algorithms:

### 7.1 GaussianNB

- Best suited for continuous features like **Age** and **Salary**
- Achieved **92.5% accuracy**

- Provided a balanced performance with high precision and recall
- **Recommended for this dataset**

## 7.2 BernoulliNB

- Designed for **binary features** (0 or 1)
- Achieved **78.75% accuracy**
- Performed well for class 0, but poorly for class 1
- **Not ideal** for this type of dataset

## 7.3 MultinomialNB

- Designed for **count-based features** (e.g., word frequencies)
- Achieved **65% accuracy**
- Completely failed to predict class 1
- **Not suitable** for continuous features

## 7.4 Key Takeaways

- Naive Bayes is a **fast and simple** algorithm with solid performance for classification tasks.
- Choosing the **right variant (Gaussian, Bernoulli, Multinomial)** is critical based on your feature types.
- Always consider **scaling**, especially for BernoulliNB and GaussianNB, to improve performance.
- **GaussianNB** gave the best results in our case due to the nature of our numerical features.

## 7.5 Real-Life Tip:

Naive Bayes is commonly used in **spam detection, recommendation systems, and text classification**. Even though it makes strong independence assumptions, it performs surprisingly well in many real-world situations.