



Natural Language Processing from Scratch

<https://github.com/DataForScience/NLP>

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www.data4sci.com

Question

- Where are you located?
 - Europe
 - Asia
 - Africa
 - US
 - Canada
 - Latin America
 - Oceania

Question

- What's your job title?
 - Data Scientist
 - Statistician
 - Data Engineer
 - Researcher
 - Business Analyst
 - Software Engineer
 - Other

Question

- How experienced are you in Python?
 - Beginner (<1 year)
 - Intermediate (1-5 years)
 - Expert (5+ years)



Lesson 1: Text Representations



Lesson 1.1: Represent words and Numbers

Words and Numbers

- How can computers **represent**, **analyze** and **understand** a piece of text?
- Computers are really good at **crunching numbers** but not so much when it comes to words.
- Perhaps we can substitute words with numbers?
 - Unfortunately, computers assume that numbers are sequential.
- **Vectors** work much better!
 - Each word corresponds to a unique **dimension**.

1	a
2	about
3	above
4	after
5	again
6	against
7	all
8	am
9	an
10	and
11	any
12	are
13	aren't
14	as
...	...



Lesson 1.2: Use One-hot Encoding

One-hot Encoding

$$\begin{aligned}v_{after} &= (0, 0, 0, 1, 0, 0, \dots)^T \\v_{above} &= (0, 0, 1, 0, 0, 0, \dots)^T\end{aligned}\quad \begin{array}{l}\text{One-hot} \\ \text{encoding}\end{array}$$

- What about **full texts** instead of single words?
- The vector representation of a text is simply the **vector sum** of all the words it contains:

Mary had a little lamb, little lamb,
little lamb, Mary had a little lamb
whose fleece was white as snow.
And everywhere that Mary went
Mary went, Mary went, everywhere
that Mary went
The lamb was sure to go.

$$v_{text} = (2, 4, 1, 2, 2, 1, 1, 2, 6, 1, 5, 1, 2, 1, 1, 1, 1, 4, 1)^T$$

0	had	10	lamb
1	went	11	as
2	and	12	that
3	a	13	sure
4	was	14	whose
5	to	15	go
6	snow	16	the
7	everywhere	17	little
8	mary	18	white
9	fleece		

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1	went	11	as
2	and	12	that
3	a	13	sure
4	was	14	whose
5	to	15	go
6	snow	16	the
7	everywhere	17	little
8	mary	18	white
9	fleece		



Lesson 1.3: Implement Bag of Words

Bag of Words

- In practice it's much more convenient to use a dictionary instead of an actual vector
- This is known as a bag-of-words, and word order is discarded.

Mary had a little lamb, little lamb,
little lamb, Mary had a little lamb
whose fleece was white as snow.
And everywhere that Mary went
Mary went, Mary went, everywhere
that Mary went
The lamb was sure to go.

$$v_{text} = (2, 4, 1, 2, 2, 1, 1, 2, 6, 1, 5, 1, 2, 1, 1, 1, 1, 4, 1)^T$$

had	2	lamb	5
went	4	as	1
and	1	that	2
a	2	sure	1
was	2	whose	1
to	1	go	1
snow	1	the	1
everywhere	2	little	4
mary	6	white	1
fleece	1		

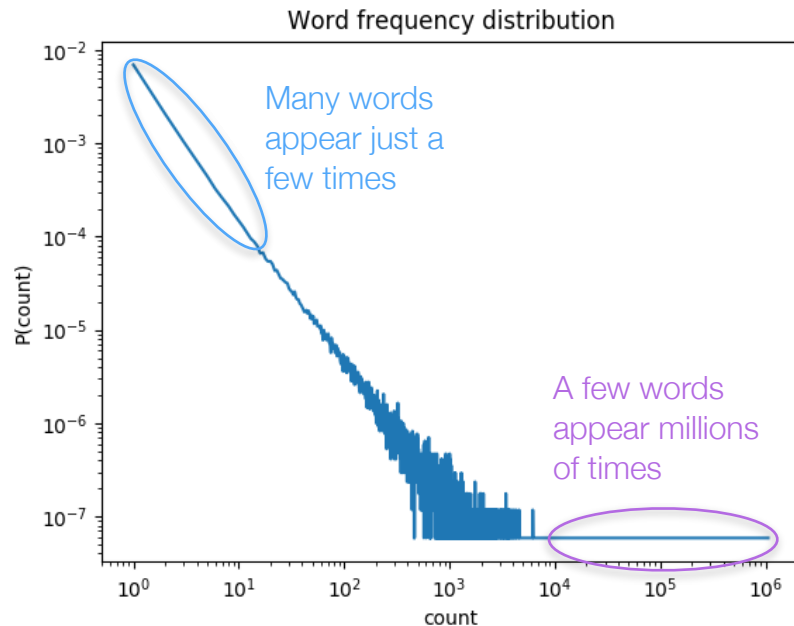


Lesson 1.4: Apply Stopwords

Word Frequency

- Some words are **much more common** than others.
- While most words are **very rare**.
- The most common words in a corpus of **17M** words:
- These are known as **“stopwords”**, words that carry little meaning and **can be discarded**.

the	1061396
of	593677
and	416629
one	411764
in	372201
a	325873
to	316376
zero	264975
nine	250430
two	192644



Stopwords

- After removing the most common words we go from 17M words to just 9M, without significantly losing any information!
- In practice, stopwords aren't simply the most common words but rather curated lists of common and non-informative words.
- Computational linguists have published lists of stop words that can easily be found online, and that were curated for different languages and purposes.
- Stopwords in 40 languages: <https://www.ranks.nl/stopwords>

Stopwords

- NLTK also includes stopwords from the 14 languages listed here: <http://anoncvs.postgresql.org/cvsweb.cgi/pgsql/src/backend/snowball/stopwords/> plus Romanian (<http://arlc.ro/resources/>) and Kasakh.
- And perhaps there is a better way to quantify how much information is carried by a word, other than just the number of times it is used in a single document?
- How can we compare different documents?



Lesson 1.5: Understand TF/IDF

Term Frequency

- We already saw that some words are much more common than others
- The number of times that a word appears in a document is known as the “term frequency” (TF)
- After the removal of stopwords, the term frequency is a good indicator of what words are most important. A book on Python programming will likely have words like “code”, “script”, “print”, “error”, etc much more frequently than a book on football.

the	1061396
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Inverse Document Frequency

- TF gives us an idea of how popular a specific term is within a document, but how can we **compare across documents** within a corpus?
- The **inverse document frequency** (IDF) tells us how **unusual** it is for a document to include that word. The idea is that words that appear in more documents are **less meaningful**.

the	1061396
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TF/IDF

- Mathematically there are several possible definitions for both TF and IDF

	TF	IDF
Number of times term t occurs in document d	$N_{t,d}$	$\log \left(\frac{N}{N_t} \right)$
	$\frac{N_{t,d}}{\sum_{t'} N_{t',d}}$	$\log \left(1 + \frac{N}{N_t} \right)$
	$1 + \log(N_{t,d})$	

Diagram illustrating the definitions of TF and IDF:

- Number of times term t occurs in document d points to $N_{t,d}$.
- Number of documents points to $\log \left(\frac{N}{N_t} \right)$.
- Number of documents in which term t appears points to $\log \left(1 + \frac{N}{N_t} \right)$.

- TF-IDF is the product of these two quantities and is useful for finding terms that are important for the specific document (high TF) and uncommon in the corpus as a whole (large IDF/ small DF).

TF/IDF

- In particular, a term that occurs in every document is meaningless when it comes to distinguishing between documents.
- Stopwords, are naturally weighed down due to appearing in all documents.



Lesson 1.6: Understand Stemming

Word variants

- So far we have seen multiple techniques to represent words and to reduce the number of words we have to deal with.
- But what about word variants? Verb conjugations, plurals, nouns and adverbs?

love
loved
loves
loving
lovingly
...

- In some cases they should just be represented by the same stem or root.

Word variants

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- But what about word variants? Verb conjugations, plurals, nouns and adverbs?

love
loved
loves love
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lovingly
...

- In some cases they should just be represented by the same **stem** or root.

Stemming

- Stemming is a series of techniques to automatically identify the stem or root of a word
- Naturally, the rules that must be applied depend on the **grammar** of the specific language being used
- For English, the most common algorithm is called **Porter stemmer**

Porter Stemmer Algorithm

- Let **V** be a set of one or more **vowels** (a, e, i, o, u, y) and **C** be a set of one or more **consonants** (b, c, d, f, ...).
- Any word in the English language is of the form:

$$[C](VC)^m[V]$$

where the contents of the $[]$ are optional and $m \geq 0$ is known as the measure, the number of times that the sequence VC repeats.

Porter Stemmer Algorithm

- The Porter stemmer algorithm develops over the course of several steps, by the successive application of hand-crafted rules of the form:

$$(condition) \text{ old_suffix} \rightarrow \text{new_suffix}$$

where *condition* is a boolean expression evaluated on the stem. Each rule can be read as “if *condition* is True, then replace *old_suffix* by *new_suffix* .

- Rules are grouped together and applied in a greedy fashion, such that the longest matching *old_suffix* takes precedence.
- *new_suffix* can be an empty string and *condition* can be null.

Porter Stemmer Algorithm

- For example, the rule:

$$(m > 0) \text{ } eed \rightarrow ed$$

would transform

$$agreed \rightarrow agree$$

$$feed \rightarrow feed$$

since

$$measure('agr') = 1$$

$$measure('f') = 0$$

- Of course, not all *conditions* rely only on the value of *measure*

Porter Stemmer Algorithm

- Other expressions commonly used in *condition* are:
 - **S* - The stem ends with the letter *S* (or any other specified)
 - **v** - The stem contains a vowel
 - **d* - The stem ends in a double consonant (-tt, -ss, etc)
 - **o* - The stem ends in cvc where the second c is not W, X, or Y
- Expressions can be combined using the usual boolean operators *and*, *or*, *not*, grouped using parenthesis, etc.
- For example
$$(*d \text{ and not } (*L \text{ or } *S \text{ or } *Z))$$

represents a stem ending with a double consonant other than L, S or Z.



Questions?



Lesson 2: Topic Modeling



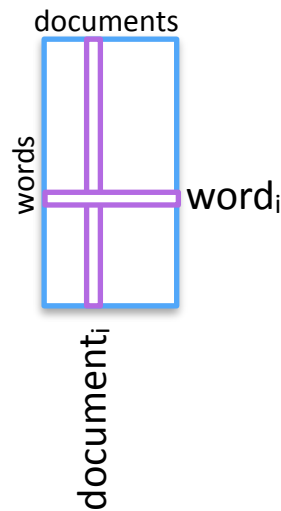
Lesson 2.1: Find Topics in Documents

Topics

- A common application of NLP is to Search and Information Extraction.
- Can we automatically define the subject of a document?
- We saw in the previous lesson that some words are more meaningful than others.
- Based on the importance of each word for a specific document, it should be possible to characterize its topic.

Term-Document Matrix

- We already know how to represent documents in terms of the TFIDF weights of each of their words.
- If we similarly use a vector representation where each element corresponds to a specific word, we can represent a corpus of documents as a matrix where each column is a document.
- Conversely, each word can be thought of as being represented by a row vector defined by its importance over all documents.

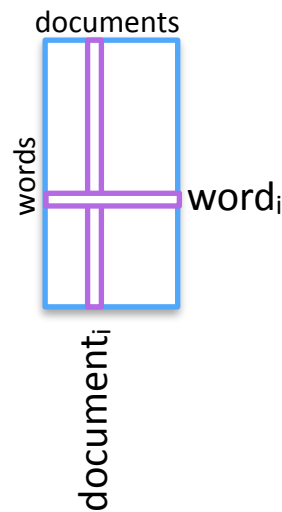




Lesson 2.2: Perform Explicit Semantic Analysis

Explicit Semantic Analysis

- In the **term document matrix**, each word is defined, explicitly, by its contribution for each document.
- We can infer the meaning of each word by the concepts (documents) it contributes to.
- Typically, the **English Wikipedia** is used as the knowledge base (corpus).
- Using the TD matrix we can represent any (other) document by the sum (or average) over all the words it contains. This is similar to what we did with one-hot encodings to define bag-of-words.



Explicit Semantic Analysis

- The similarity of words or new documents can be measured using the **cosine similarity**:

$$\text{sim}(\vec{u}, \vec{v}) = \frac{\vec{u} \cdot \vec{v}}{||\vec{u}|| ||\vec{v}||}$$

- Explicit semantic analysis**, despite its simplicity, has been shown to improve the performance of different kinds of systems for search.
- The main disadvantage of ESA is that it requires the use of a large knowledge base corpus (the entire English Wikipedia!), resulting in high dimensional representations of words and documents.



Lesson 2.3: Understand Document clustering

Document Clustering

- Using the cosine similarity:

$$\text{sim}(\vec{u}, \vec{v}) = \frac{\vec{u} \cdot \vec{v}}{||\vec{u}|| ||\vec{v}||}$$

we can easily measure the similarity between every pair of documents in our corpus to generate a **square similarity matrix**.

- There is a large literature on clustering algorithms for matrices.
- The simplest approach is to impose a **minimum similarity** cutoff and consider any pair of documents with higher similarity to be part of the same cluster.

Hierarchical Document Clustering

- Algorithm
 - Assign each document to its own cluster.
 - Calculate the similarity matrix between all clusters.
 - Identify the two most similar clusters and merge them.
 - Recompute the similarity matrix for this reduced set of clusters.
 - Repeat until we reach the desired number of clusters.
- Library implementations will usually merge all the clusters until there is just one left so that any cutoff can be imposed a posteriori.



Lesson 2.4: Implement Latent Semantic Analysis

Singular Value Decomposition (SVD)

- Any matrix M , such as the TD matrix seen above, can be decomposed into three matrices of the form:

$$\begin{array}{c} M \\ m \times n \end{array} = \begin{array}{c} U \\ m \times m \end{array} \begin{array}{c} \Sigma \\ m \times n \end{array} \begin{array}{c} V^\dagger \\ n \times n \end{array}$$

where

U is a unitary matrix ($UU^\dagger = 1$)

Σ is diagonal with non-negative elements

V^\dagger is a unitary matrix

Singular Value Decomposition (SVD)

- The diagonal elements of Σ , σ_i are called the **singular values** of the matrix M and are conceptually similar to **eigenvalues** in the case of square matrices.
- σ_i are sorted from largest to smallest.
- The original matrix M can be **approximated** by keeping only the **top k dimensions** of the SVD decomposition.

$$M_k = U_k \Sigma_k V_k^\dagger$$

- Naturally, the larger the value of k the better the approximation.

Latent Semantic Analysis (LSA)

- While ESA explicit defines each word based on the documents in contributes to in the knowledge base, LSA tries to implicitly determine a “latent” representation for each word and document.
- LSA defines the **term-document** matrix for the corpus under consideration (as opposed to an external knowledge base).
- The DT matrix is approximated using a k dimensional **singular value decomposition**
- Each of the k latent dimensions used represents a latent dimension (topic) of the underlying dataset.

Latent Semantic Analysis (LSA)

- The U_k represents the distribution of each topic among the words in our vocabulary, while the V_k matrix describes the distribution of each document across topics.
- Documents and words can be more effectively clustered in the singular space.
- New documents (or queries) can be mapped into the singular space using:

$$\hat{v} = \Sigma_k^{-1} U_k^\dagger v$$

where v is the column vector representing the original query and \hat{v} the transformed document vector.



Lesson 2.5: Implement Non-negative Matrix Factorization

Non-Negative Matrix Factorization

- Matrix factorization methods, like SVD, have a long history of application to **natural language processing**.
- Another common factorization method used to identify a **latent structure** to a dataset is **non-negative matrix factorization** (NMF).

$$\begin{array}{c} M \\ m \times n \end{array} = \begin{array}{c} W \\ m \times k \end{array} \begin{array}{c} H \\ k \times n \end{array}$$

- NMF directly approximates the matrix M for a given value of k .

Non-Negative Matrix Factorization

- In this formulation, it has the advantage of being easily interpretable:
 - Columns of W are the underlying basis vectors for each topic.
 - Columns of H are the contribution of each topic to a specific document.

Non-Negative Matrix Factorization

- The value of W and H are found through an optimization procedure where we minimize the error of the approximation:

$$\min_{W,H} ||V - WH||_F^2$$

- One simple way to do this is given by:

$$h_{ij} \leftarrow h_{ij} \frac{(W^\dagger V)_{ij}}{(W^\dagger WH)_{ij}} \quad w_{ij} \leftarrow w_{ij} \frac{(VH^\dagger)_{ij}}{(WHH^\dagger)_{ij}}$$

- And we initiate the process by assigning random non-negative values to W and H .
- We stop updating the values of h_{ij} and w_{ij} when the cost function converges.



Questions?



Lesson 3: Sentiment Analysis



Lesson 3.1: Quantify words and feelings

Positive and Negative Words

- We often use words to describe how we are **feeling** or how we feel about something
- People associate **specific** connotations and meanings to words
- Some are obvious:
 - Love, yes, friendship, good, ... transmit **positive** feelings
 - Hate, no, animosity, bad, ... transmit **negative** feelings
- Others less so:
 - Blue, maybe, indifference, ...

Positive and Negative Texts

- We can use the words in a text to determine the sentiment behind the text
- The simplest approach:
 - count **positive** P and **negative** N words
 - define sentiment as:
$$\text{sentiment} = \frac{P - N}{P + N}$$
- This effectively weighs **positive** words as +1 and **negative** words as -1 and defines sentiment as how dominant one sentiment is over another
- Despite it's simplicity, this approach is surprisingly powerful

Word Valence

- Many lexicons of **positive** and **negative** words are available online:
 - Opinion Lexicon: <https://www.cs.uic.edu/~liub/FBS/sentiment-analysis.html>
 - Opinion Finder: <https://mpqa.cs.pitt.edu/opinionfinder/>
- Even commercial products use similar approaches:
 - Linguistic Inquiry and Word Count (LIWC) <http://liwc.wpengine.com/>
 - Valence Aware Dictionary and sEntiment Reasoner (VADER) <https://github.com/cjhutto/vaderSentiment>



Lesson 3.2: Use negations and modifiers

Negations and Modifiers

- So far, our approach to sentiment analysis has relied on considering just **individual words**
- However it's clear that context matters.
- “not pretty” is very different from “pretty”
- **n-grams** are a natural extension, but increase significantly the memory requirements
- An intermediate approach is to consider modifier words like “not”, “much”, “little”, “very”, etc.
- By keeping track of the modifiers we can generate n-grams on the fly

Modifiers

- While sentiment words contribute **additively** to the sentiment score, modifiers have a **multiplicative** effect
- If we define the weights of each modifier

not	-1
very	1.5
somewhat	1.2
pretty	1.5
...	...

- We just have to check the previous word whenever we encounter one of the sentiment words in our lexicon
- Special care must be taken whenever a modifier word can also be a sentiment word (such as “pretty”).

Modifiers

- We must keep two separate dictionaries of words: **modifiers** and **valence** words.
- For each word we encounter, we first check whether it is a **modifier** and only then whether it is **valence** word.
- Words that are in neither list act as a signal to end the current n-gram
- With this simple approach we can handle even long sequences of modifiers, double negatives, etc.



Lesson 3.3: Understanding corpus-based approaches

Corpus-based Approaches

- Sentiment analyses often rely on dictionaries of words and valences
- In many cases, these lists are curated manually with varying degrees of care
- Can we automatically generate them?
- With the advent of the Web, large corpora of product reviews became available
- Each review associates a piece of text with a numerical evaluation (typically 1-5 stars)

Corpus-based Approaches

- Corpus based approaches to sentiment analysis rely on these datasets to generate the lexicons used
- These approaches leverage sophisticated supervised machine learning techniques to automatically determine the weight that should be assigned to each word
- Modifiers can be identified using Part-of-Speech (POS) tagging
- The details of these techniques are beyond the scope of this introductory course, but it's important to understand their advantages and disadvantages

Corpus-based Approaches

- Hand curated lexicons are naturally **subjective** and potentially **incomplete**
- Lexicons generated automatically from large corpora can cover a **wider range of languages** and subjects
- Hand curation is more powerful when only **smaller datasets** are available
- Automatic generation relies on **large datasets** and their inherent biases. They are typically only applicable to specific domains and may **appear** to be more **objective**.
- Your results will only be as good as your lexicon. Make sure to understand its **biases** and **limitations**.



Questions?



Lesson 4: Applications



Lesson 4.1: Understand Word2vec word embeddings

Distributional hypothesis

- We already saw various way in which to represent word in a vectorial form, but never in a way that was semantically meaningful.
- The distributional hypothesis in linguistics states that words with similar meanings should occur in similar contexts.
- In other words, from a word we can get some idea about the context where it might appear.

____ house ____
____ car ____

$$\max p(C|w)$$

- And from the context we have some idea about possible words.

The red ____ is beautiful.
The blue ____ is old.

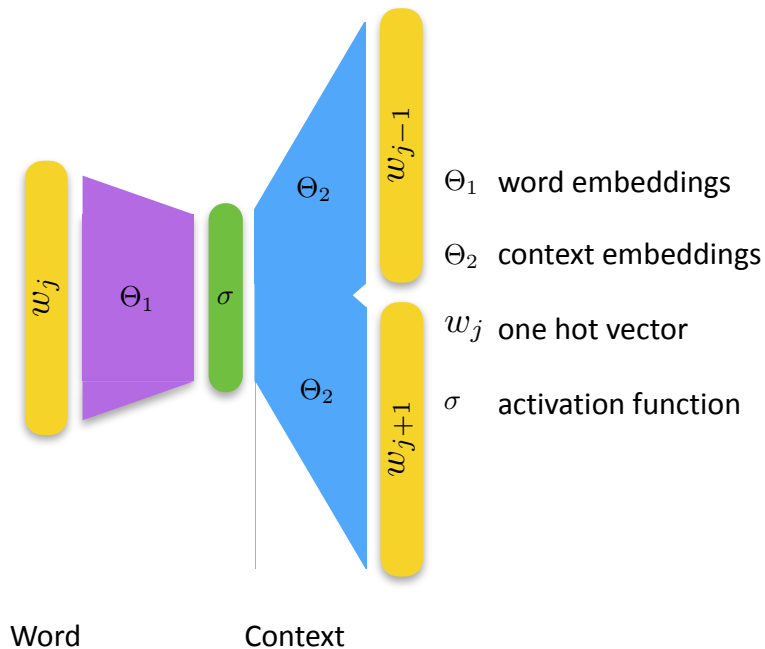
$$\max p(w|C)$$

word2vec

Mikolov 2013

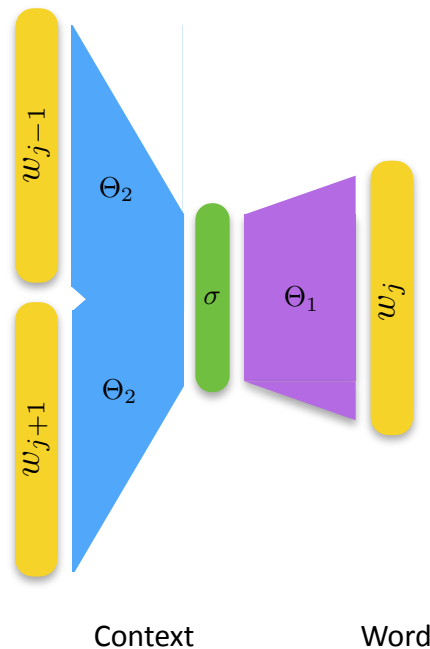
Skipgram

$$\max p(C|w)$$



Continuous Bag of Words

$$\max p(w|C)$$



word2vec variations

- Hierarchical Softmax:
 - Approximate the softmax using a binary tree
 - Reduces the number of calculations per training example from V to $\log_2 V$ and increases performance by orders of magnitude.
- Negative Sampling:
 - Under sample the most frequent words by removing them from the text before generating the contexts
 - Similar idea to removing stop-words — very frequent words are less informative.
 - Effectively makes the window larger, increasing the amount of information available for context

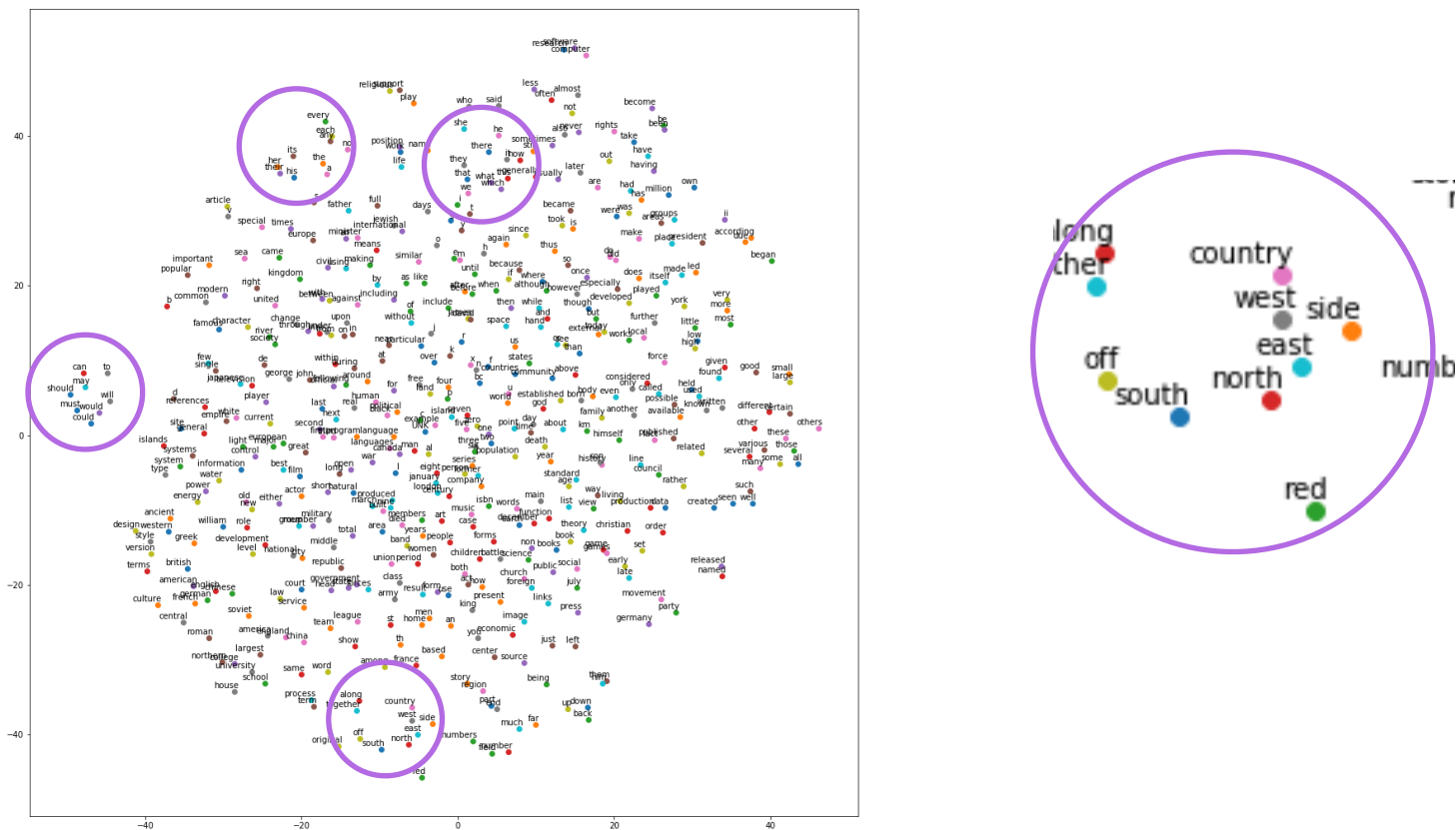
word2vec details

- The output of this neural network is deterministic:
 - If two words appear in the same context (“blue” vs “red”, for e.g.), they will have similar internal representations in Θ_1 and Θ_2
 - Θ_1 and Θ_2 are vector embeddings of the input words and the context words respectively
- Words that are too rare are also removed.
- The original implementation had a dynamic window size:
 - for each word in the corpus a window size k' is sampled uniformly between 1 and k

Reference implementations

- C - <https://code.google.com/archive/p/word2vec/> (the original one)
- Python/tensorflow - <https://www.tensorflow.org/tutorials/word2vec>
- Python/gensim - <https://radimrehurek.com/gensim/models/word2vec.html>
- Pretrained embeddings:
 - 30+ languages, <https://github.com/Kyubyong/wordvectors>
 - 100+ languages trained using wikipedia: <https://sites.google.com/site/rmyeid/projects/polyglot>

Visualization



Analogies

- The embedding of each word is a function of the context it appears in:

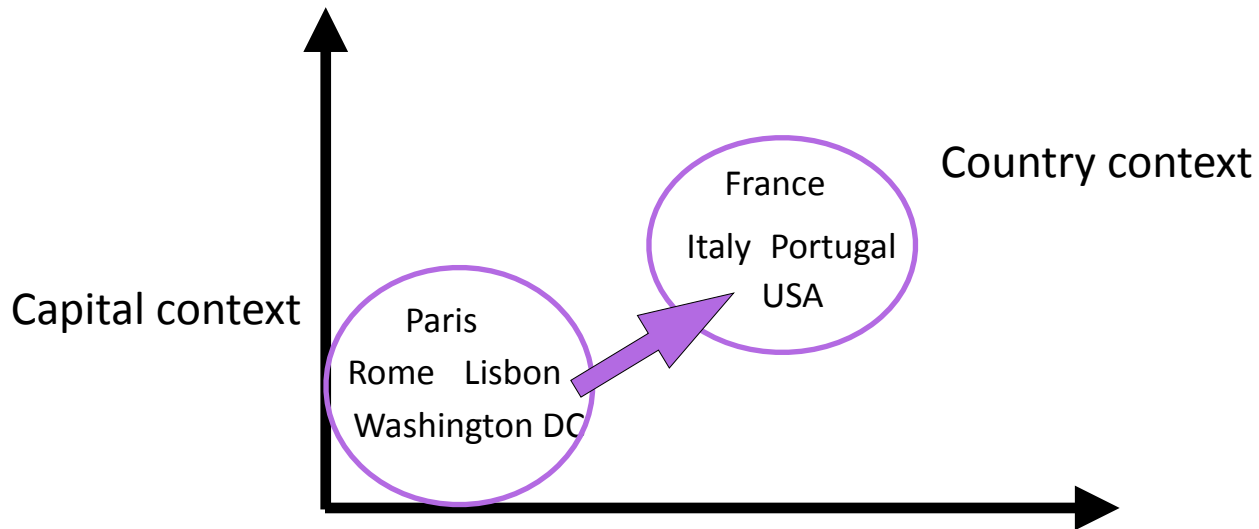
$$\sigma(\textit{red}) = f(\textit{context}(\textit{red}))$$

- words that appear in similar contexts will have similar embeddings:

$$\textit{context}(\textit{red}) \approx \textit{context}(\textit{blue}) \implies \sigma(\textit{red}) \approx \sigma(\textit{blue})$$

- “Distributional hypotesis” in linguistics

Analogies



$$\sigma(France) - \sigma(Paris) + \sigma(Rome) = \sigma(Italy)$$

$$\vec{b} - \vec{a} + \vec{c} = \vec{d}$$

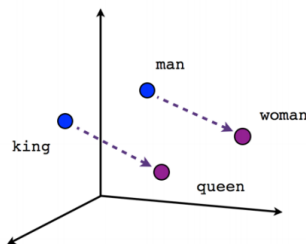
Analogies

$$\vec{b} - \vec{a} + \vec{c} = \vec{d}$$

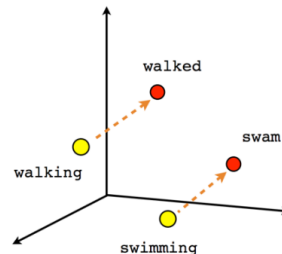
$$d^\dagger = \operatorname{argmax}_x \frac{(\vec{b} - \vec{a} + \vec{c})^T}{\|\vec{b} - \vec{a} + \vec{c}\|} \vec{x}$$

$$d^\dagger \sim \operatorname{argmax}_x \left(\vec{b}^T \vec{x} - \vec{a}^T \vec{x} + \vec{c}^T \vec{x} \right)$$

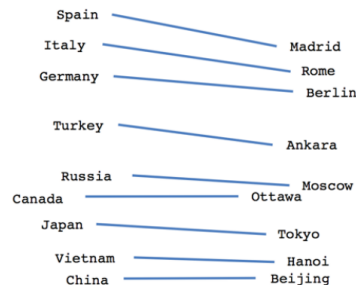
What is the word **d** that is most similar to **b** and **c** and most dissimilar to **a**?



Male-Female



Verb tense



Country-Capital



Lesson 4.2: Define GloVe

Global Vectors (GloVe)

- An alternative to [word2vec](#) developed by the Stanford NLP Group in 2014
- Explicitly models word [cooccurrences](#) by a cooccurrence matrix X where rows correspond to input words and columns to context words
- X_{ij} is the number of times word i occurred with context word j
- Contexts are defined through a sliding window

Global Vectors (GloVe)

- Embedding vectors for word i is defined as:

$$w_i^T \tilde{w}_k + b_i + \tilde{b}_k = \log(X_{ik})$$

- Embedding vectors are found through an optimization procedure with a cost function of the form:

$$J = \sum_{i,j=1}^V f(X_{ij}) \left(w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log(X_{ij}) \right)^2$$

$$f(X_{ij}) = \begin{cases} \left(\frac{X_{ij}}{X_{max}} \right) & \text{if } X_{ij} < x_{max} \\ 1 & \text{otherwise} \end{cases}$$

Global Vectors (GloVe)

- $f(X_{ij})$ prevents common word pairs from skewing our cost function
- Explicitly considers the context in which each word appears
- Word-context matrix is large, but sparse
- Relatively fast to train
- Highlights the importance of relative frequency of words
- Impractical to use as a language model (to explicitly calculate the value of $\max p(w|C)$)

Resources

- The original implementation: <https://nlp.stanford.edu/projects/glove/>
- Python package: <https://pypi.org/project/glove/>
- Pre-trained vectors: <https://github.com/stanfordnlp/GloVe>



Lesson 4.3:

Apply Language detection

Language Detection

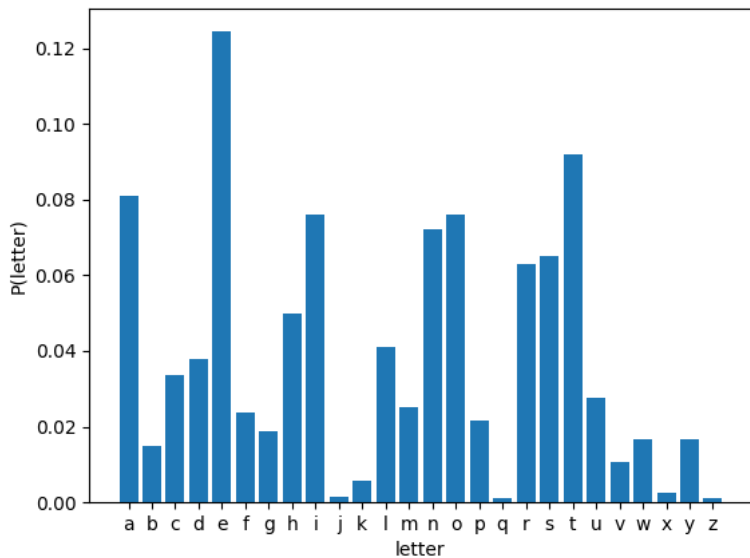
- Sometimes a given corpus will contain documents written in different languages (comment boxes in international websites, for example)
- We intrinsically assumed that each individual documents is comparable with all others.
- When multiple languages are present within the same corpus (on Twitter, in the comment boxes of an international website, etc) this is no longer true.

Language Detection

- One way to handle this would be to cluster documents, as documents in the same language will naturally cluster together. However:
 - there might be multiple clusters using the same language
 - We might not be interested in doing all this work for languages other than, say, English
- Language detection allows us to preprocess our corpus so that we can focus on specific languages, sort documents by language (to use different stopwords lists), etc.
- Languages can be characterized by their character (letter) distribution.

Character distributions

- The character level distribution for English, obtained using Google Books 1-gram dataset is:

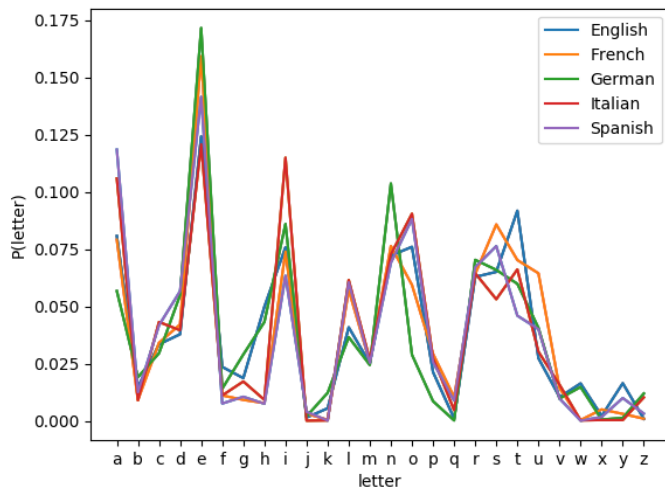


Character distributions

- We measured the probability **distribution of letters in the english language**. In effect, we calculated: $P(\text{letter}|\text{english})$
- The probability of seeing a specific letter given that the text is in English. If we do this for a few other languages we can have a table of the form: $P(\text{letter}|\text{language})$
- Google Books covers several different languages, among which we can find 5 different European languages: **English, French, German, Italian and Spanish**.

Character distributions

- Character distributions for different languages look different in at least a few of the characters due to the idiosyncrasies of each language, even in the case of closely related languages.



Conditional Probabilities

- Using these conditional probabilities, and Bayes Theorem, we can easily build a language detector. For that we just need to calculate:

$$P(\text{language}|\text{text})$$

- Which we can rewrite as:

$$P(\text{language}|\text{letter}_1, \text{letter}_2, \dots, \text{letter}_n)$$

- If we treat each letter independently, we obtain:

$$P(\text{language}|\text{letter}_1, \text{letter}_2, \dots, \text{letter}_n) = \prod_i P(\text{language}|\text{letter}_i)$$

Naive Bayes

- This is known as the **Naive Bayes Approach** and is an obvious oversimplification: It completely ignores correlations present in the sequence of letters.
- All we have to do now is apply Bayes Theorem to our original table:

$$P(\text{language}|\text{letter}) = \frac{P(\text{letter}|\text{language}) P(\text{language})}{P(\text{letter})}$$

- And if we assume that all languages are equally probable (**non-informative prior**):

$$P(\text{language}) = \frac{1}{N_{\text{langs}}}$$

Naive Bayes

- Naive Bayes approaches (and many others) use terms of the form:

$$\prod_i P(A|B_i)$$

- which implies multiplying many **small** numbers. To avoid numerical complications, it is best to use, instead:

$$\sum_i \log P(A|B_i)$$

- Which is commonly referred to as the “Log-Likelihood”. Our expression then becomes:

$$\mathcal{L}(\text{language}|\text{letter}_1, \text{letter}_2, \dots, \text{letter}_n) = \sum_i \log \left[\frac{P(\text{letter}_i|\text{language}) P(\text{language})}{P(\text{letter}_i)} \right]$$

Language detection

- Or more simply:

$$\mathcal{L}(\text{language}|\text{text}) = \sum_i \log \left[\frac{P(\text{letter}_i|\text{language}) P(\text{language})}{P(\text{letter}_i)} \right]$$

- And finally:

$$\mathcal{L}(\text{language}|\text{text}) = \sum_i \mathcal{L}(\text{language}|\text{letter}_i)$$

- Providing us with a quick and easy way to determine which language is more likely to be the correct one.

Question

- How was the technical level?
 - 1 — Too Low
 - 2 — Low
 - 3 — Just Right
 - 4 — High
 - 5 — Too High

Question

- How was the level of Python code/explanations?
 - 1 — Too Low
 - 2 — Low
 - 3 — Just Right
 - 4 — High
 - 5 — Too High



Questions?

Other Tutorials



Data Visualization With Matplotlib and Seaborn

- Aug 9, 2019 - 5am-9pm (PST)

Graphs and Network Algorithms from Scratch

- Sep 16, 2019 - 5am-9pm (PST)

Deep Learning from Scratch

- Sept 24, 2019 - Strata NYC



Deep Learning from Scratch

- Sept 30, 2019 - 5am-9pm (PST)

Natural Language Processing (NLP) from Scratch

- <http://bit.ly/LiveLessonNLP> (On Demand)



**Sunday
Briefing**

by Data For Science





END