# Results

#### **Problem 1**

A2e, B3a, C5c, D1d, E4b

#### **Problem 2**

2.1 
$$B_1 = \max(a,b)$$
,  $B_2 = \min(a,b)$ 

2.2 
$$X(f) = si^2(\pi f)$$
,  $Y(f) = j \cdot 4 \cdot si^2(\pi f) \cdot sin(\pi f)$ 

### **Problem 3**

3.1 
$$H(s) = \frac{3s+2}{s^2+3s+2}$$

3.2 
$$y(t) = 2 \cdot (1 + e^{-t} - 2e^{-2t}) \cdot u(t)$$
,  $y(0) = 0$ ,  $y(\infty) = 2$ 

3.3 
$$\hat{y} = |H(s = j\omega)| \cdot \hat{x}$$

#### **Problem 4**

4.1 
$$X(f) = \frac{j}{4} \cdot \left\{ \delta(f+5 \text{ Hz}) + \delta(f+1 \text{ Hz}) - \delta(f-1 \text{ Hz}) - \delta(f-5 \text{ Hz}) \right\}$$

4.2 
$$X_s(f) = 6 \text{ Hz} \cdot \sum_{k=-\infty}^{+\infty} X(f - k \cdot 6 \text{ Hz}) = 0$$

### **Problem 5**

**5.1** N even: 
$$M \ge N/2$$
, N odd:  $M \ge (N-1)/2$ 

**5.2** 
$$X[k] = X^* \lceil \langle -k \rangle_N \rceil$$
 **5.3**  $X[4] = 2$ ,  $X[5] = 1 - j$ 

5.4 
$$x[n] = \frac{1}{6} \cdot \left\{ \left(-1\right)^n - 2 \cdot \sin\left(\frac{\pi n}{3}\right) \right\}$$

## Problem 6

**6.1** IIR

**6.2** 
$$y[n] + 2 \cdot y[n-1] + 2 \cdot y[n-2] = x[n] - x[n-1] - 5 \cdot x[n-2]$$

**6.3** 
$$H(z) = \frac{1-z^{-1}-5\cdot z^{-2}}{1+2\cdot z^{-1}+2\cdot z^{-2}}$$

**6.4** 
$$p_{1,2} = -1 \pm j$$
, not stable **6.5**  $|H(0)| = 1 = 0$  dB

**6.6** 
$$z_1 = 2.79$$
,  $z_2 = -1.79$ ; curve similar to problem 1, d **6.7** ...