

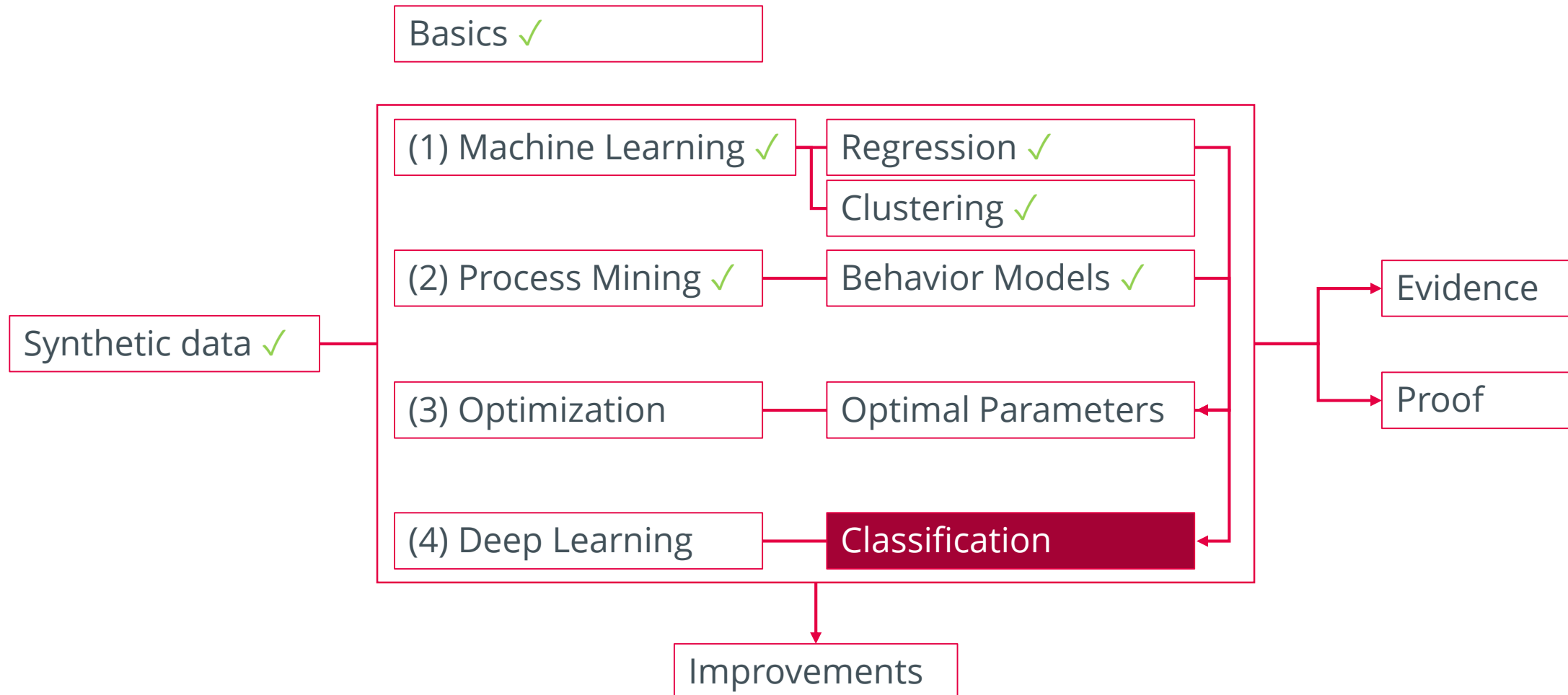


TECHNISCHE HOCHSCHULE
OSTWESTFALEN-LIPPE
UNIVERSITY OF
APPLIED SCIENCES
AND ARTS

Welcome

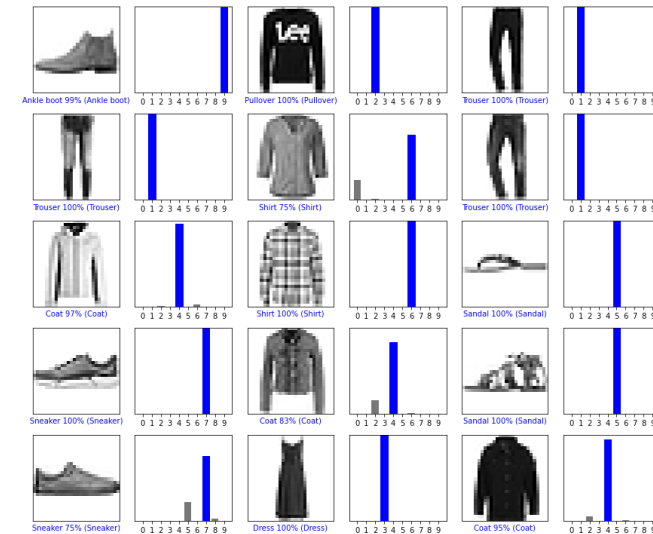
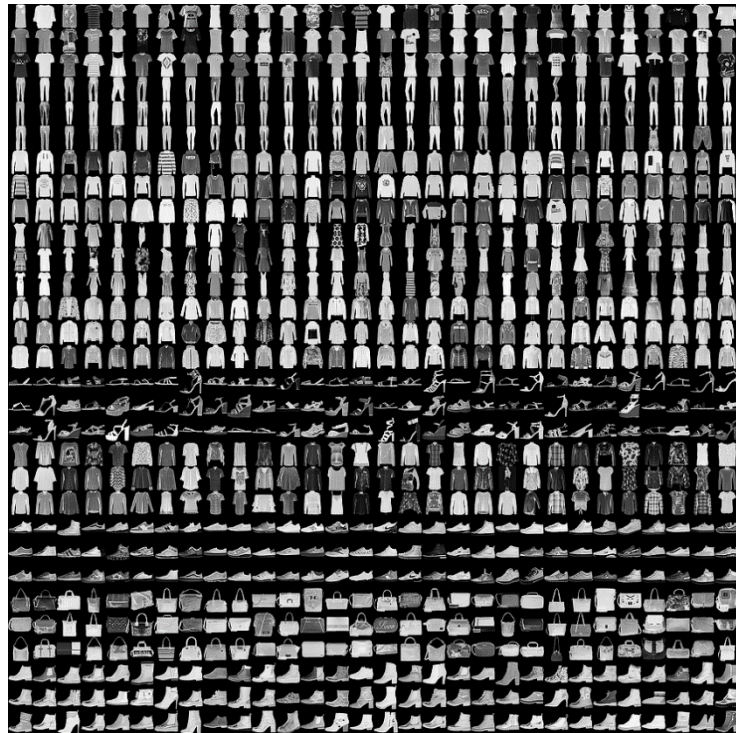
to Advanced Topics in Algorithms

Summary: Advanced Topics in Algorithms



Revision: [Deep] Learning: Classification

Fashion-MNIST is a dataset of Zalando's article images



<https://arxiv.org/pdf/1708.07747.pdf>

XIAO, Han; RASUL, Kashif; VOLLGRAF, Roland. Fashion-mnist: a novel image dataset for benchmarking machine learning algorithms. *arXiv preprint arXiv:1708.07747*, 2017.

Neural network models

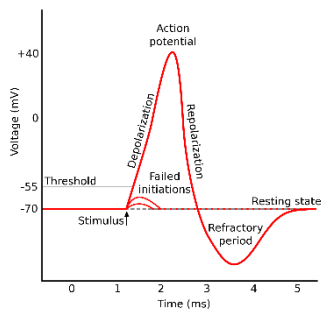
Multi-layer Perceptron (MLP)

MLP is a supervised learning algorithm that learns a function $f(\cdot): R^m \rightarrow R^o$ by training on a dataset, where m is the number of dimensions for input and o is the number of dimensions for output [1].

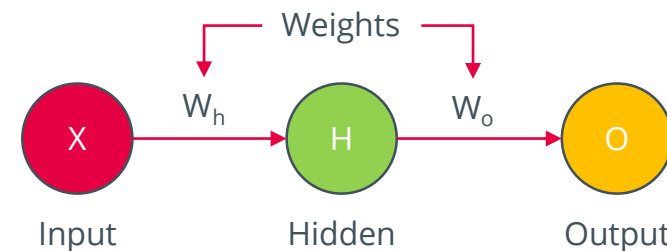
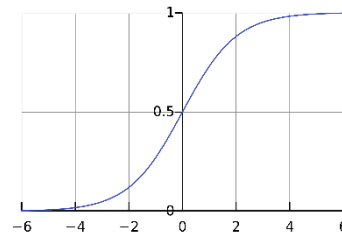


Neurons

Action potential



Sigmoid function

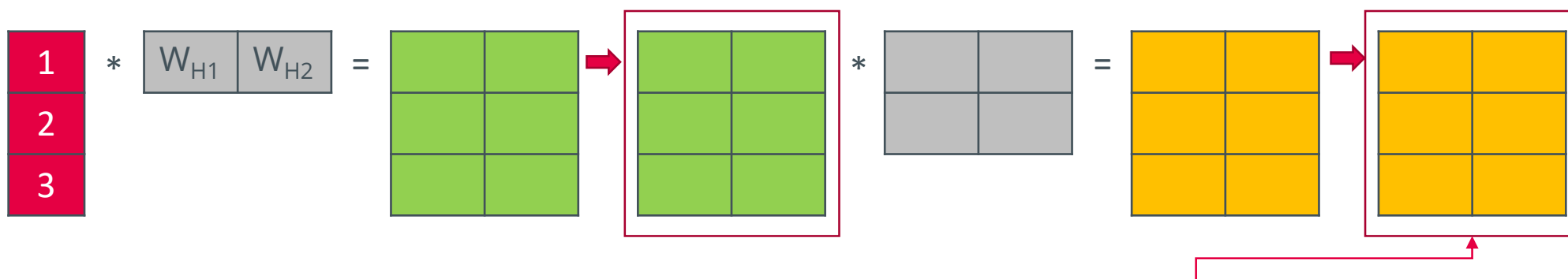
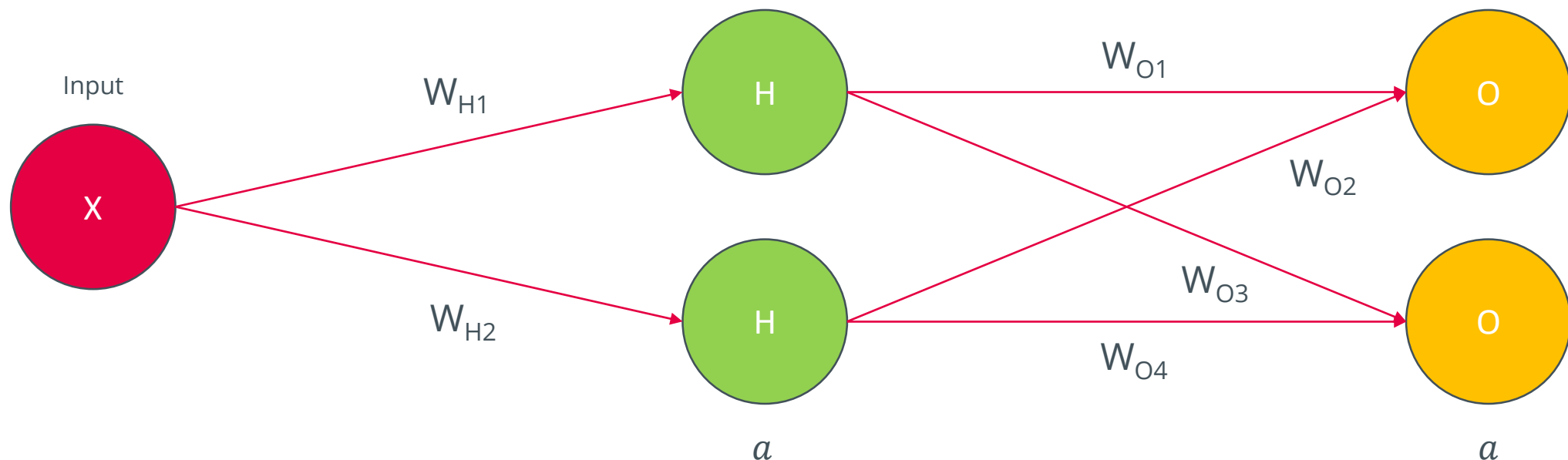


$$f(X) = a(a(XW_h)W_o)$$

a = activation function

- [1] https://scikit-learn.org/stable/modules/neural_networks_supervised.html
- [2] https://en.wikipedia.org/wiki/Action_potential#/media/File:Action_potential.svg
- [3] https://en.wikipedia.org/wiki/Sigmoid_function#/media/File:Logistic-curve.svg

Matrix representation



Each row represents a prediction for a single observation in our training set

Backpropagation 1/2

Training data

```
x = np.array([[0, 0, 1], [0, 1, 1], [1, 0, 1], [1, 1, 1]], dtype=float)
y = np.array([[0], [1], [1], [0]], dtype=float)
```

x			y
0	0	1	0
0	1	1	1
1	0	1	1
1	1	1	0

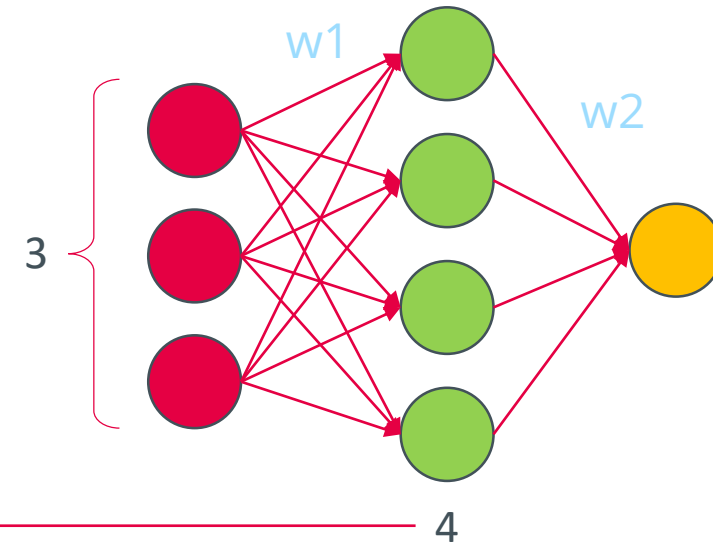
3

```
w1 = np.random.rand(3, 4)
```

0.1980562	0.8675463	0.25031689	0.61791776
0.56455728	0.64895493	0.73713434	0.69868288
0.33841526	0.91953443	0.0589787	0.8731658

```
w2 = np.random.rand(4, 1)
```

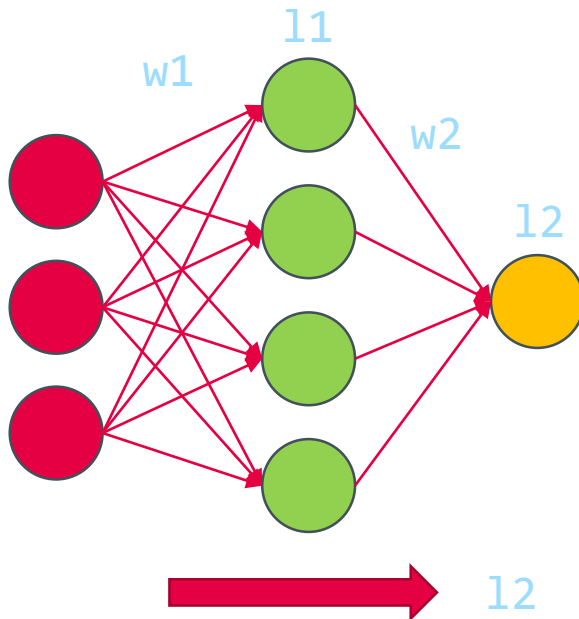
0.25678541
0.7534222
0.56365436
0.17331184



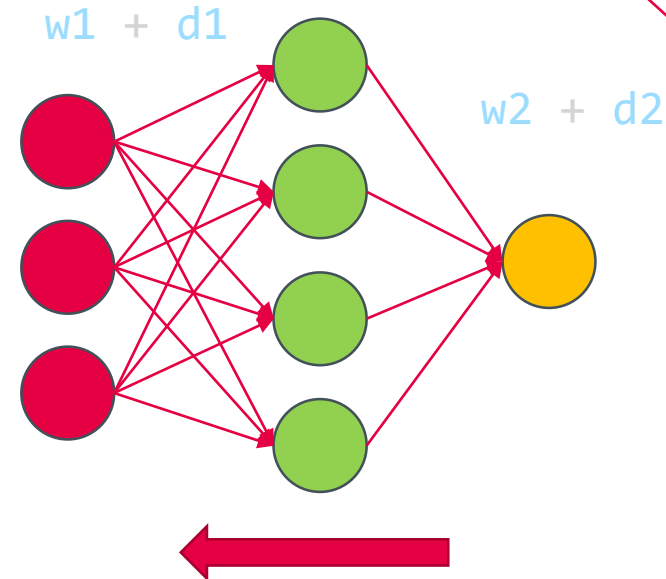
Backpropagation 2/2

Adjust each weight in the network in proportion to how much it contributes to overall error

```
def feedforward(X, w1, w2):
    l1 = a(np.dot(X, w1))
    l2 = a(np.dot(l1, w2))
    return l1, l2
```



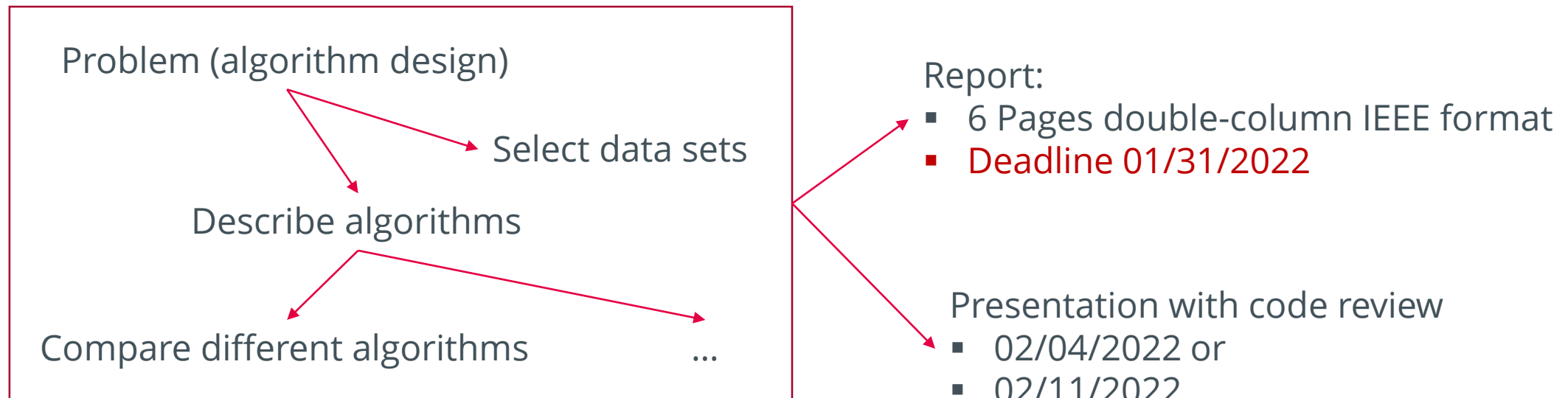
```
def backpropagation(w1, w2, l1, l2, y):
    d2 = np.dot(l1.T, 2*(y - l2) * ad(l2))
    d1 = np.dot(X.T, np.dot(2 * (y - l2) * ad(l2), w2.T) * ad(l1))
    return w1 + d1, w2 + d2
```



$$C = 1/2 * (y - 12)^2$$

$$C' = 2 * (y - 12)$$

Exam 2022





TECHNISCHE HOCHSCHULE
OSTWESTFALEN-LIPPE
UNIVERSITY OF
APPLIED SCIENCES
AND ARTS

Thank you!