

## Simple Sieve Algorithm

### Solution

**Following are the prime numbers smaller than or equal to 10**

```
class SieveOfEratosthenes
{
    void sieveOfEratosthenes(int n)
    {
        boolean prime[] = new boolean[n+1];
        for(int i=0;i<=n;i++)
            prime[i] = true;
        for(int p = 2; p*p <=n; p++)
        {
            // If prime[p] is not changed, then it is a prime
            if(prime[p] == true)
            {
                // Update all multiples of p
                for(int i = p*p; i <= n; i += p)
                    prime[i] = false;
            }
        }
        for(int i = 2; i <= n; i++)
        {
            if(prime[i] == true)
                System.out.print(i + " ");
        }
    }

    public static void main(String args[])
    {
        int n = 10;
        System.out.print("Following are the prime numbers ");
        System.out.println("smaller than or equal to " + n);
        SieveOfEratosthenes g = new SieveOfEratosthenes();
        g.sieveOfEratosthenes(n);
    }
}
```

**Output: 10**

## Segmented & Incremental Sieve Algorithm

### Solution

```
import java.util.Scanner;

class SievePrimeGenerator
{
    static int array[];
    static int primes[];

    public static void calculate(int n, int m)
    {
        int j = 0;
        int sqrt = (int) Math.sqrt(m);
        array = new int[sqrt + 1];
        primes = new int[sqrt + 1];
        initialise(sqrt + 1);
        for (int i = 2; i <= sqrt; i++) {
            if (array[i] == 1) {
                primes[j] = i;
                j++;
                for (int k = i + i; k <= sqrt; k += i) {
                    array[k] = 0;
                }
            }
        }
        int diff = (m - n + 1);
        array = new int[diff];
        initialise(diff);
        for (int k = 0; k < j; k++) {
            int div = n / primes[k];
            div *= primes[k];
            while (div <= m) {
                if (div >= n && primes[k] != div)
                    array[div - n] = 0;
                div += primes[k];
            }
        }
    }
}
```

```

for (int i = 0; i < diff; i++) {
    if (array[i] == 1 && (i+n) !=1)
        System.out.println(i + n);
    } }

public static void initialise(int sqt) {
    for (int i = 0; i < sqt; i++) {
        array[i] = 1;
    }
}

public static void main(String arg[]) {
    int t, n, m;
    Scanner in = new Scanner(System.in);
    t = in.nextInt();
    for (int i = 0; i < t; i++)
    { n = in.nextInt();
      m = in.nextInt();
      calculate(n, m);
      System.out.println();
    }
    in.close();
}
}

```

### **Output**

Primes in Range 2 to 100 are

2 3 5 7 11 13 17 19 23 29 31 37 41 43 47 53 59 61 67 71 73 79 83 89 97

## The Euler Phi Function

### Solution

```
class Euler{
    // Function to return GCD of a and b
    static int gcd(int a, int b)
    {
        if (a == 0)
            return b;
        return gcd(b % a, a);
    }
    static int phi(int n)
    {
        int result = 1;
        for (int i = 2; i < n; i++)
            if (gcd(i, n) == 1)
                result++;
        return result;
    }
    public static void main(String[] args)
    {
        int n;
        for (n = 1; n <= 10; n++)
            System.out.println("phi(" + n + ") = " + phi(n));
    }
}
```

### Output

phi(1) = 1

phi(2) = 1

phi(3) = 2

phi(6) = 2

phi(7) = 6

phi(8) = 4

phi(9) = 6

phi(10) = 4