

Marketing Strategy for Banks

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STAT 571- ADVANCED STATISTICS IN MANAGEMENT

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I would also like to thank all the TA's of the course for patiently assisting me during times when I need clarifications. I would also like to thank my colleagues without whom this course would not have been the same experience.

This is exactly how I feel having had this course experience!!



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STAT 471/571/701 Final Project Report Spring 2016 University of Pennsylvania

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PROJECT PROPOSAL

Objective:

The data is related with direct marketing campaigns of a Portuguese banking institution. The marketing campaigns were based on phone calls. Often, more than one contact to the same client was required, in order to access if the product (bank term deposit) would be ('yes') or not ('no') subscribed. The classification goal is to predict if the client will subscribe (yes/no) a term deposit.

<u>Data:</u>

The data set characteristic is of type multivariate. The data has 41188 observations, 20 predictor variables and the response variable (term deposit- variable 'y'). The data is ordered by date (from May 2008 to November 2010), and is very close to the data analyzed in [Moro et al., 2014]. On quick exploration of the data it is seen that around 89% of the response variable is 'no' while 11% is 'yes'.

Source:

[Moro et al., 2014] S. Moro, P. Cortez and P. Rita. A Data-Driven Approach to Predict the Success of Bank Telemarketing. Decision Support Systems, Elsevier, 62:22-31, June 2014

Link:

http://archive.ics.uci.edu/ml/datasets/Bank+Marketing

PROJECT REPORT- INTRODUCTION

Background:

At the banking institutions it's a very common practice to place calls to their customers to encourage them to open a term deposit with them. A term deposit is a deposit held at a financial institution that has a fixed term. These are generally short-term with maturities ranging anywhere from a month to a few years. When a term deposit is purchased, the lender (the customer) understands that the money can only be withdrawn after the term has ended or by giving a predetermined number of days' notice. These types of financial products are sold by banks, thrift institutions and credit unions.

Goal of the Study:

The goal of the study here is to determine the likelihood of a customer to open the term deposit and thereby classify him/her into two levels (yes or no).

Background on the Data Set:

Source of the data:

The data is available at the Machine Learning Repository of the Centre for Machine Learning and Intelligent Systems. It was originally obtained from the Elsevier journal scientific paper written in June 2014 by Moro et al.

Characteristics of the Data Set:

The data set has 41188 values which are essentially phone calls placed to these many clients. Often, more than one contact to the same client was required, in order to access if the product (bank term deposit) would be ('yes') or not ('no') subscribed. There are 20 predictor variables used and the response variable is y (has the client subscribed a term deposit? (Binary: 'yes', 'no')).

Description of variables:

- Bank Client Data
 - 1. Age of the client (numeric)
 - 2. Job: The type of job the client performs (categorical)

		•	Admin			•	Self-employ	yed	
		Blue collarEntrepreneur			•		Services		
						•		Student	
		•	Housemaid			•	Technician		
		•	Management			•	Unemploye	ed	
		•	Retired			•	Unknown		
3. Marital: It's the marital status of the client (categorical)									
		•	Divorced			•	Single		
		•	Married			•	Unknown		
	4.	Educ	ation: It's the educations	s level of th	e client (cate	gori	cal)		
		•	basic.4y (Till 4 th grade)	!		•	illiterate		
		•	basic.6y (Till 6 th grade))		•	professiona	l.cou	ırse
		•	basic.9y (Till 9th grade)	!		•	university.d	egre	ee
		•	high school			•	unknown		
	5.	Defau	ılt: Has the client got any	credit in d	lefault? (cate	gori	cal)		
		•	No	•	Yes			•	Unknown
	6.	Housi	ng: Has the client got an	y housing I	oan? (catego	rical)		
		•	No	•	Yes			•	Unknown
	7.	Loan:	Has the client got any p	ersonal loa	n? (categoric	al)			
		•	No	•	Yes			•	Unknown
•	Data related with the last contact of the current campaign								
	8.	Conta	ct: How was the client c	ontacted?	(categorical)				
		•	Cellular			•	Telephone		
	9.	Mont	h: Last contact month of	the year (categorical)				
		•	January	•	May			•	September
		•	February	•	June			•	October
		•	March	•	July			•	November
		•	April	•	August			•	December
	10	10. Day_of_week: Last contact day of the week (categorical)							
		•	Monday	•	Wednesday	,		•	Friday
		•	Tuesday	•	Thursday				
	11	. Durat	ion: It's the last contact	duration, i	n seconds (nu	ımer	ric).		
•	Ot	her att	ributes						

- 12. Campaign: Number of contacts performed during this campaign and for this client which includes the last contact (numeric)
- 13. Pdays: Number of days that passed by after the client was last contacted from a previous campaign and 999 means client was not previously contacted (numeric)
- 14. Previous: Number of contacts performed before this campaign and for this client (numeric)
- 15. Poutcome: Outcome of the previous marketing campaign (categorical)
 - FailureNonSuccesexistent
- Social and economic context attributes
 - 16. Emp.var.rate: Employment variation rate quarterly indicator (numeric)
 - 17. Cons.price.idx: Consumer price index monthly indicator (numeric)
 - 18. Cons.conf.idx: Consumer confidence index monthly indicator (numeric)
 - 19. Euribor3m: Euribor 3 month rate daily indicator (numeric)

 Euribor is short for Euro Interbank Offered Rate. The Euribor rates are based on the interest rates at which a panel of European banks borrow funds from one another.
 - 20. Nr.employed: Number of employees quarterly indicator (numeric)

Initial Data Cleaning:

The data that we have is already clean and has no missing values. Variable 'duration' has been removed because this attribute highly affects the output target (e.g., if duration=0 then y='no'). Yet, the duration is not known before a call is performed. Also, after the end of the call y is obviously known. Thus, this input should only be included for benchmark purposes and should be discarded if the intention is to have a realistic predictive model.

I have renamed the response variable as TD. The dimension of the data is 41188 into 21. Since it's important to keep in mind the computational speed to build models and train data, I have used 5000 data values of the 41188 available. In the original data, what's noticeable is that the percentage of TD=yes is just 11% roughly. This is highly skewed and hence to build a strong classifier, I have maintained a 55% TD=no to 45% TD=yes ratio amongst the randomly sub-setted dataset of 5000.

All the study has been performed on this cleaned dataset (data3=data.cleaned). The remaining data could be very well used for testing the classifier.

Approach adopted:

Essentially, I adopt a simple approach to build my final and the best model. First 1 build 3 models by logistic regression. The first model in it will contain all the variables. The second will have variables I obtain using the function Regsubsets. In this I explore all the types that include exhaustive search, forward selection and backward selection Last, I build a logistic regression model containing models I get from regularization (LASSO- L1 norm).

The next three models are built using the same approach as above but with 10 fold cross validation. This way we get three more models (again primarily by using Logistic Regression).

The next 3 models are built by Linear Discriminant Approach (LDA). The first of them is by using all the variables, while the second contains the same variables as obtained from Regsubsets used from above. The last one is built using variables I get from the LASSO regularization.

Finally, I explore the Random Forest method for classification. Again three models are built here, one having all the variables, the other having variables obtained from Regsubsets function and last one from the LASSO regularization. While studying this I also performed Bagging and Bootstrapping to build strong models.

Having obtained 12 models, I compare all the models through a common parameter like MCE on the test data and see which the best model out of them was. Lastly, I try to use an ensembled approach and use the models to formulate a common model. I use three ensemble approaches, just a mean of the predictions of all methods, fitting regression model on the model and then classifying them and finally fitting a random forest tree on the predictions of other models (this eventually was the selected model).

This ensembled model constituted to be the best model and was the chosen classifier.

Important Topics Touched Upon:

Logistic Regression, Linear Discriminant Analysis, Random Forest, Decision Trees, Bagging, Bootstrap, Cross Validation, LASSO, Subsets, Ensemble, Multiple Linear Regression

DETAILED MACHINE LEARNING ANALYSIS

The Study (of Original Data):

Firstly, I tried to understand the original data, the summary of which has been presented below. As can be seen the data is pleasant and has no missing values.

```
> summary(data)
                          job
                                         marital
      age
                 admin.
                            :10422
                                     divorced: 4612
 Min.
        :17.00
 1st Qu.:32.00
                 blue-collar: 9254
                                     married:24928
 Median :38.00
                 technician: 6743
                                     single :11568
 Mean
      :40.02
                 services
                            : 3969
                                     unknown:
 3rd Qu.:47.00
                 management: 2924
                           : 1720
        :98.00
                 retired
 Max.
                 (Other)
                            : 6156
                                default
               education
                                                housing
                                                                  loan
 university.degree
                   :12168
                             no
                                    :32588
                                             no
                                                    :18622
                                                             no
                                                                    :33950
 high.school
                    : 9515
                             unknown: 8597
                                             unknown: 990
                                                             unknown:
                                                                       990
 basic.9y
                    : 6045
                             yes
                                    :
                                             yes
                                                    :21576
                                                             yes
                                                                    : 6248
 professional.course: 5243
 basic.4y
                   : 4176
                    : 2292
 basic.6y
                    : 1749
 (Other)
                       month
      contact
                                   day_of_week
                                                  duration
                                   fri:7827
 cellular :26144
                          :13769
                                                    :
                                                          0.0
                   may
                                               Min.
                                               1st Qu.: 102.0
                   jul
                          : 7174
 telephone:15044
                                   mon:8514
                   aug
                          : 6178
                                   thu:8623
                                               Median : 180.0
                   jun
                          : 5318
                                   tue:8090
                                               Mean
                                                      : 258.3
                                               3rd Qu.: 319.0
                          : 4101
                                   wed:8134
                   nov
                          : 2632
                   apr
                                               Max.
                                                      :4918.0
                   (Other): 2016
                                     previous
    campaign
                      pdays
                                                         poutcome
                  Min.
 Min.
        : 1.000
                         : 0.0
                                  Min. :0.000
                                                  failure
                                                             : 4252
 1st Qu.: 1.000
                  1st Qu.:999.0
                                  1st Qu.:0.000
                                                  nonexistent:35563
 Median: 2.000
                  Median:999.0
                                  Median :0.000
                                                             : 1373
                                                  success
 Mean
      : 2.568
                  Mean
                        :962.5
                                  Mean
                                         :0.173
 3rd Qu.: 3.000
                                  3rd Qu.:0.000
                  3rd Qu.:999.0
        :56.000
                  Max.
                         :999.0
                                  Max.
                                         :7.000
 Max.
                    cons.price.idx cons.conf.idx
                                                      euribor3m
  emp.var.rate
 Min.
        :-3.40000
                    Min.
                           :92.20
                                    Min.
                                           :-50.8
                                                    Min.
                                                           :0.634
                                    1st Qu.:-42.7
 1st Qu.:-1.80000
                    1st Qu.:93.08
                                                    1st Qu.:1.344
 Median : 1.10000
                    Median :93.75
                                    Median :-41.8
                                                    Median :4.857
 Mean
      : 0.08189
                    Mean
                          :93.58
                                    Mean :-40.5
                                                    Mean :3.621
 3rd Qu.: 1.40000
                    3rd Qu.:93.99
                                    3rd Qu.:-36.4
                                                    3rd Qu.:4.961
        : 1.40000
                    Max.
                           :94.77
                                    Max.
                                           :-26.9
                                                    Max.
                                                           :5.045
 nr.employed
        :4964
                no:36548
Min.
1st Qu.:5099
                yes: 4640
Median:5191
      :5167
Mean
3rd Qu.:5228
       :5228
Max.
```

```
> str(data)
  'data.frame':
                                                                       41188 obs. of 21 variables:
                                                                       41188 obs. of 21 variables:
: int 56 57 37 40 56 45 59 41 24 25 ...
: Factor w/ 12 levels "admin.", "blue-collar",..: 4 8 8 1 8 8 1 2 10 8 ...
: Factor w/ 4 levels "divorced", "married",..: 2 2 2 2 2 2 2 2 3 3 ...
: Factor w/ 8 levels "basic.4y", "basic.6y",..: 1 4 4 2 4 3 6 8 6 4 ...
: Factor w/ 3 levels "no", "unknown",..: 1 2 1 1 1 2 1 2 1 1 ...
: Factor w/ 3 levels "no", "unknown",..: 1 3 1 1 1 1 1 3 3 ...
: Factor w/ 3 levels "no", "unknown",..: 1 1 1 1 3 1 1 1 1 1 1 ...
: Factor w/ 2 levels "cellular", "telephone": 2 2 2 2 2 2 2 2 2 2 2 ...
: Factor w/ 10 levels "apr", "aug", "dec",..: 7 7 7 7 7 7 7 7 7 7 7 ...
: Factor w/ 5 levels "fri", "mon", "thu",..: 2 2 2 2 2 2 2 2 2 2 ...
: int 261 149 226 151 307 198 139 217 380 50 ...
: int 1 1 1 1 1 1 1 1 1 ...
    $ age
    $ job
    $ marital
    $ education
    $ default
    $ housing
    $ loan
    $ contact
    $ month
    $ day_of_week
    $ duration
    $ campaign
                                                                            : int 1111111111...
                                                                            : int 999 999 999 999 999 999 999 999 ...
    $ pdays
                                                                            : int 0 0 0 0 0 0 0 0 0 0 ...
: Factor w/ 3 levels "failure", "nonexistent",..: 2 2 2 2 2 2 2 2 2 2 ...
    $ previous
    $ poutcome
    $ emp.var.rate : num 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1 ...
    $ cons.price.idx: num 94 94 94 94 ...
    $ cons.conf.idx : num -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -36.4 -3
    $ euribor3m
                                                                    : num 4.86 4.86 4.86 4.86 4.86 ...
    $ nr.employed
                                                                           : num 5191 5191 5191 5191 5191 ...
                                                                            : Factor w/ 2 levels "no", "yes": 1 1 1 1 1 1 1 1 1 1 ...
```

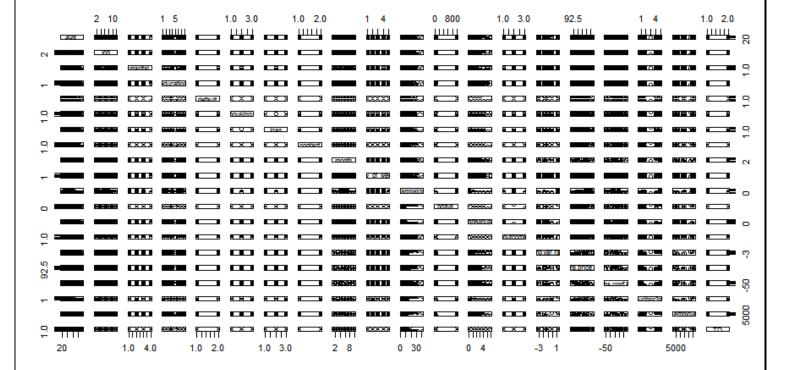
The Study (of Cleaned Data):

```
> summary(data.cleaned)
                         job
                                       marital
                                                                 education
                                                                                default
     age
       :17.00
                           :1338
                admin.
                                   divorced: 539
                                                   university.degree :1626
                                                                                   :4148
Min.
                                                                             no
                blue-collar: 994
1st Qu.:31.00
                                   married :2854
                                                   high.school
                                                                      :1112
                                                                             unknown: 852
Median :38.00
                technician: 813
                                   single :1595
                                                   basic.9y
                                                                      : 647
Mean :40.26
                services : 417
                                   unknown: 12
                                                   professional.course: 615
 3rd Qu.:48.00
                management: 347
                                                   basic.4y
                                                                       483
                         : 317
      :95.00
                retired
                                                   basic. 6y
                                                                       270
Max.
                (Other)
                           : 774
                                                   (Other)
                                                                      : 247
                                                              day_of_week
   housing
                    loan
                                   contact
                                                   month
                                                                            campaign
                     :4115
                                                                         Min.
no
      :2271
               no
                              cellular :3564
                                               may
                                                      :1407
                                                              fri: 921
                                                                                : 1.000
unknown: 118
               unknown: 118
                              telephone:1436
                                               jul
                                                      : 825
                                                              mon: 969
                                                                         1st Qu.: 1.000
      :2611
                     : 767
                                                      : 721
                                                              thu:1131
                                                                         Median : 2.000
ves
               yes
                                               jun
                                                        634
                                                              tue: 986
                                                                         Mean : 2.413
                                                       505
                                                              wed: 993
                                                                         3rd Qu.: 3.000
                                               nov
                                                        403
                                                                                :42.000
                                               apr
                                                                         Max.
                                               (Other): 505
                                                                      cons.price.idx cons.conf.idx
                   previous
    pdays
                                        poutcome
                                                     emp.var.rate
      : 0.0
Min.
                Min.
                      :0.0000
                                 failure
                                          : 551
                                                    Min. :-3.4000
                                                                     Min.
                                                                           :92.20
                                                                                     Min.
                                                                                            :-50.80
1st Qu.:999.0
                1st Qu.:0.0000
                                 nonexistent:3966
                                                    1st Qu.:-1.8000
                                                                     1st Qu.:92.89
                                                                                     1st Qu.:-42.70
Median :999.0
                Median :0.0000
                                 success
                                           : 483
                                                    Median :-0.1000
                                                                     Median :93.44
                                                                                     Median :-41.80
Mean :893.2
                Mean :0.2924
                                                    Mean :-0.3986
                                                                     Mean :93.49
                                                                                     Mean :-40.31
 3rd Qu.:999.0
                3rd Qu.:0.0000
                                                    3rd Qu.: 1.4000
                                                                      3rd Qu.:93.99
                                                                                     3rd Qu.:-36.40
       :999.0
                                                          : 1.4000
Max.
                Max.
                       :6.0000
                                                    Max.
                                                                     Max.
                                                                            :94.77
                                                                                     Max.
   euribor3m
                 nr.employed
                                 TD
                               no :2750
Min. :0.634
                Min. :4964
 1st Qu.:1.260
                1st Qu.:5099
                               yes:2250
                Median :5191
Median :4.120
Mean :3.073
                Mean :5141
 3rd Qu.:4.959
                3rd Qu.:5228
      :5.045
Max.
                Max.
                       :5228
```

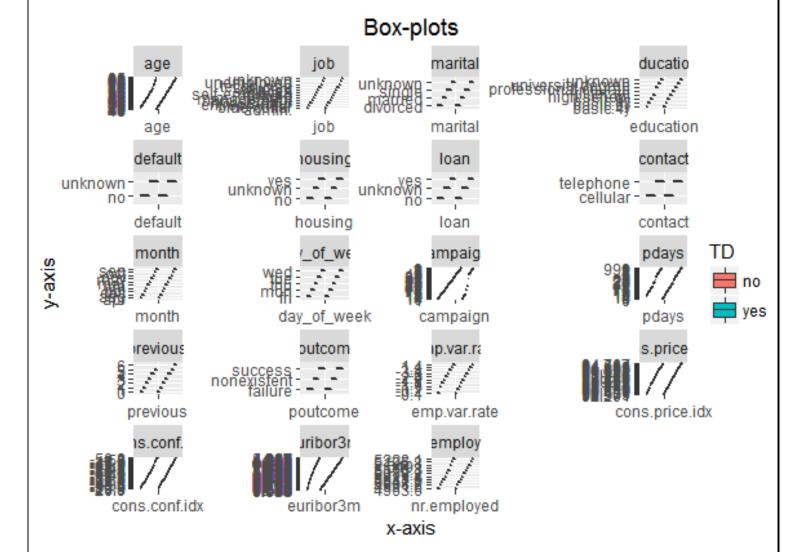
Below we can see how the 'duration' variable has been removed from the dataset.

> str(data.cleaned) 'data.frame': 5000 obs. of 20 variables: 50 35 27 29 37 52 24 52 30 39 ... \$ age : int Factor w/ 12 levels "admin.", "blue-collar",..: 1 2 1 1 2 2 9 6 1 1 ... job \$: Factor w/ 4 levels "divorced", "married",..: 2 3 3 3 3 2 3 1 2 3 ... : Factor w/ 8 levels "basic.4y", "basic.6y",..: 7 3 7 7 6 3 4 7 7 4 ... \$ marital education 2 levels "no", "unknown": 2 1 1 1 1 2 1 1 1 1 1 . . . 3 levels "no", "unknown"...: 3 1 1 1 1 1 1 1 1 1 \$ default Factor w/ "no","unknown",..: 3 1 1 1 1 1 1 1 1 1 ... "no","unknown",..: 1 1 1 3 1 1 1 1 1 1 ... \$ housing Factor w/ \$ loan Factor w/ levels "cellular", "telephone": 2 1 1 1 1 2 1 1 2 2 ... \$ contact Factor w/ 2 levels : Factor w/ 10 levels "apr", "aug", "dec",..: 5 7 10 2 1 4 2 2 5 4 ... : Factor w/ 5 levels "fri", "mon", "thu",..: 3 1 5 4 1 1 3 3 1 3 ... \$ month day_of_week 6111121111... int \$ campaign \$ pdays int 999 999 999 999 999 999 15 999 999 ... 0000000100... previous int w/ 3 levels "failure", "nonexistent",..: 2 2 2 2 2 2 2 3 2 2 ... \$ poutcome Factor 1.4 -1.8 -3.4 1.4 -1.8 1.4 -2.9 -2.9 1.4 1.4 ... emp.var.rate : num cons.price.idx: num 94.5 92.9 92.4 93.4 93.1 .. -41.8 -46.2 -29.8 -36.1 -47.1 -42.7 -31.4 -31.4 -41.8 -42.7 ... cons.conf.idx : num 4.958 1.313 0.781 4.963 1.405 ... euribor3m : num \$ nr.employed : num 5228 5099 5018 5228 5099 ... : Factor w/ 2 levels "no", "yes": 1 2 2 1 1 2 2 2 1 1 ... \$ TD

The correlations among the variables can be seen from the pair plot as can be seen below.



Most importantly what could be observed is that duration is highly correlated with TD and hence was removed to build more robust model (as suggested on the website as well). The box plot below shows visually the categorical and numerical variables.



> cor(data.cleaned[,unlist(lapply(data.cleaned, is.numeric))]) pdays age campaign previous emp.var.rate cons.price.idx 1.000000000 0.03054528 -0.03569918 0.04746841 -0.02656427 0.007158971 age campaign 0.030545284 1.00000000 0.08763713 -0.08875156 0.18606153 0.127368127 pdays -0.035699177 0.08763713 1.00000000 -0.71083208 0.34123673 0.036930752 previous 0.047468410 -0.08875156 -0.71083208 1.00000000 -0.40684013 -0.091404963 emp.var.rate -0.026564268 0.18606153 0.34123673 -0.40684013 1.00000000 0.725716595 cons.price.idx 0.007158971 0.12736813 0.03693075 -0.09140496 0.72571660 1.000000000 0.107248305 -0.02459104 -0.13698801 0.08600497 cons.conf.idx -0.02721782 -0.126220160 euribor3m -0.024627011 0.17326860 0.39620558 -0.46544609 0.96121262 0.584376953 nr.employed -0.054663059 0.17419436 0.48578152 -0.53939334 0.87455829 0.369676023 cons.conf.idx euribor3m nr.emploved 0.10724830 -0.02462701 -0.05466306 age -0.02459104 0.17326860 0.17419436 campaign -0.13698801 0.39620558 0.48578152 pdays previous 0.08600497 -0.46544609 -0.53939334 0.96121262 emp.var.rate -0.02721782 0.87455829 cons.price.idx -0.12622016 0.58437695 0.36967602 1.00000000 0.07448255 -0.06296017 cons.conf.idx euribor3m 0.07448255 1.00000000 0.94214899 -0.06296017 nr.employed 0.94214899 1.00000000

The above shows in numbers how the variables are correlated. This has been done only for numeric variables. It is logical that the euribor rate (rate of interest) would be correlated to how often employment is changed by people in the market. More change suggests instability and hence the rate would be lower (low job security).

Next, thing I divided the dataset into training and testing data, so that I can train my model on the training set and then test it on the hidden test set to check for accuracy. This helps in understanding model accuracies and to pick amongst the best models. For this purpose I am taking the 4000 values to be training set and the remaining 1000 to be the test set.

Building the classifier:

The most important task to build the classifier is to build several models of different types and see their prediction performance on the dataset. The final classifier will be the one that performs the best amongst the lot.

Model 1:

Here I performed logistic regression to build a model by considering all the variables. The summary of this fit is given below.

```
> fit1=glm(TD~., data.cleaned.train, family=binomial(logit))
> summary(fit1)
                                                                                                1oanunknown
glm(formula = TD \sim ., family = binomial(logit), data = data.cleaned.train)
                                                                                               loanyes
contacttelephone
                                                                                                                                 -3.682e-03
                                                                                                                                             1.077e-01
                                                                                                                                                          -0.034 0.972738
                                                                                                                                -6.947e-01
                                                                                                                                             1.487e-01
                                                                                                                                                          -4.672 2.98e-06
Deviance Residuals:
                                                                                                monthaug
                                                                                                                                 5.028e-01
                                                                                                                                              3.097e-01
                                                                                                                                                           1.624 0.104450
Min 1Q Median
-3.1304 -0.8085 -0.5760
                                                                                                                                 2.308e+00
1.975e-01
                                                                                                                                             1.178e+00
                                                                                                                                                           1.959 0.050131
                                0.7846
                                            2,1051
                                                                                                                                                           1.014
                                                                                                monthjun
                                                                                                                                 -3.328e-01
                                                                                                                                              2.955e-01
                                                                                                                                                          -1.126 0.260020
4.501 6.76e-06
Coefficients: (1 not defined because of singularities)
                                                                                                monthmar
                                                                                                                                 1.965e+00
                                                                                                                                              4.367e-01
                                     Estimate Std. Error z value Pr(>|z|)
                                                                                               monthmay
monthnov
                                                                                                                                -5.219e-01
-7.347e-01
                                                                                                                                               . 697e-01
. 388e-01
                                                                                                                                                          -3.076 0.002101
-3.077 0.002091
                                                 8.385e+01
                                   -9.155e+01
                                                              -1.092 0.274905
(Intercept)
                                                               0.524 0.600445
age
jobblue-collar
                                    2.410e-03
                                                 4.602e-03
                                                                                                monthoct
                                                                                                                                -6.099e-01
                                                                                                                                              3.355e-01
                                                                                                                                                          -1.818 0.069077
                                                                                               monthoct
monthsep
day_of_weekmon
day_of_weekthu
day_of_weektue
day_of_weekwed
campaign
pdays
previous
                                                                                                                                                          -0.629 0.529312
                                   -6.776e-02
                                                 1.427e-01
                                                               -0.475 0.634817
                                                                                                                                -2.606e-01
                                                                                                                                              4.142e-01
                                                                                                                                -3.191e-01
-3.628e-01
                                                                                                                                                          -2.578 0.009951 **
-2.996 0.002736 **
jobentrepreneur
                                    1.753e-01
                                                 2.180e-01
                                                               0.804
                                                                       0.421114
                                                                                                                                              1.238e-01
iobhousemaid
                                    3.188e-01
                                                 2.800e-01
                                                               1.139 0.254852
                                                                                                                                -1.837e-01
                                                                                                                                              1.250e-01
                                                                                                                                                          -1.470 0.141554
jobmanagement
                                                                                                                                -3.907e-02
                                                                                                                                             1.225e-01
                                                                                                                                                          -0.319 0.749809
iobretired
                                    3.272e-01
                                                 2.146e-01
                                                               1.525 0.127352
                                                                                                                                -4.337e-02
-3.448e-04
                                                                                                                                               . 728e-02
. 639e-04
                                                                                                                                                          -2.510 0.012068
-0.743 0.457300
jobself-employed
                                    2.132e-01
                                                 2.213e-01
                                                               0.964 0.335204
iobservices
                                    1.317e-01
                                                 1.586e-01
                                                               0.830 0.406525
                                                                                                previous
                                                                                                                                -2.414e-01
                                                                                                                                             1.602e-01
                                                                                                                                                          -1.507 0.131824
iobstudent
                                    5.058e-01
                                                 2.490e-01
                                                               2.032 0.042203 *
                                                                                                poutcomenonexistent
                                                                                                                                 3.238e-01
                                                                                                                                              2.246e-01
                                                                                                                                                           1.442 0.149282
                                                 1.343e-01
iobtechnician
                                    2.013e-02
                                                                                                                                              4.628e-01
3.348e-01
                                                                                                                                                          3.436 0.000591
-3.644 0.000269
jobunemployed
                                    3.735e-01
                                                 2.644e-01
                                                               1.413 0.157732
                                                                                                emp.var.rate
                                                                                                                                 -1.220e+00
jobunknown
                                    6.782e-02
                                                    453e-01
                                                                                                cons.price.idx
                                                                                                                                 1.287e+00
                                                                                                                                              5.617e-01
                                                                                                                                                           2.291 0.021981
maritalmarried
                                    7.602e-02
                                                 1.267e-01
                                                               0.600 0.548451
                                                                                                cons.conf.idx
                                                                                                                                 1.907e-03
                                                                                                                                              1.910e-02
                                                                                                                                                           0.100 0.920492
maritalsingle
maritalunknown
                                    4.717e-02
3.705e-01
                                                                                                                                             2.827e-01
6.709e-03
                                                 1.447e-01
                                                               0.326 0.744447
                                                                                                                                6.010e-01
-5.994e-03
                                                                                               nr.employed
                                                                                                                                                          -0.894 0.371589
                                                 8.224e-01
                                                               0.451 0.652348
educationbasic.6v
                                    2.048e-01
                                                 2.078e-01
                                                               0.986 0.324335
                                                                                               Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
educationbasic.9y
                                                 1.734e-01
                                                                0.419 0.675081
educationhigh.school
educationilliterate
                                    8.216e-02
                                                 1.736e-01
                                                               0.473 0.635981
                                                                                                (Dispersion parameter for binomial family taken to be 1)
                                                 1.970e+02
                                                               0.056 0.954985
                                    1.112e+01
educationprofessional.course 1.567e-01
                                                 1.961e-01
                                                               0.799 0.424139
                                                                                                    Null deviance: 5512.4 on 3999 degrees of freedom
educationuniversity.degree
                                    2.241e-01
                                                 1.755e-01
                                                               1.277 0.201709
                                                                                                         deviance: 4149.5 on 3949 degrees of freedom
                                                 2.304e-01
                                                               -0.122 0.902765
educationunknown
                                   -2.815e-02
                                                                                               AIC: 4251.5
defaultunknown
                                   -2.038e-01
                                                 1.114e-01
                                                              -1.830 0.067257
housingunknown
                                                                                               Number of Fisher Scoring iterations: 10
                                                 7.813e-02
housingyes
                                   -6.773e-03
                                                              -0.087 0.930917
```

What can be seen here is that a lot of variables have very low significance.

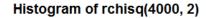
Now, the next thing I do is the chi-square test. This was done using anova function. This is type 1 test where each variable gets added sequentially. If a particular variable is of high significance then the reduction in the residual deviance will be great. This could be seen in the AIC value.

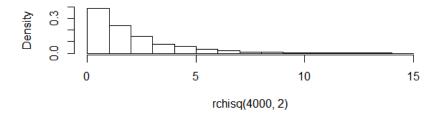
```
> anova(fit1, test="Chisq") # to test if the model is useful: null hypothesis is
 all (but the intercept) coeff's are 0
Analysis of Deviance Table
Model: binomial, link: logit
Response: TD
Terms added sequentially (first to last)
             Df Deviance Resid. Df Resid. Dev
                                            Pr(>Chi)
NULL
                             3999
                                     5512.4
              1
age
                  4.931
                             3998
                                     5507.4 0.026374 *
             11 177.414
                                     5330.0 < 2.2e-16 ***
job
                             3987
marital
                                     5315.3 0.002102 **
              3
                 14.689
                             3984
                                     5296.1 0.007574 **
education
              7
                  19.203
                             3977
default
                             3976
                                     5201.1 < 2.2e-16 ***
              1
                 94.995
housing
                 0.748
              2
                             3974
                                     5200.4 0.688022
              1
                  0.905
                             3973
                                     5199.5 0.341414
loan
contact
              1 174.992
                             3972
                                     5024.5 < 2.2e-16 ***
                             3963
month
              9 314.283
                                     4710.2 < 2.2e-16 ***
day_of_week
campaign
             4
                  9.712
                             3959
                                     4700.5 0.045562 *
                                     4676.0 7.626e-07 ***
             1 24.450
                             3958
             1 213.801
                                     4462.2 < 2.2e-16 ***
pdays
                             3957
             1
previous
                  0.180
                             3956
                                     4462.1 0.671072
             2 13.657
                             3954
                                    4448.4 0.001083 **
poutcome
emp.var.rate 1 209.450
                             3953
                                    4239.0 < 2.2e-16 ***
cons.price.idx 1 76.782
                                    4162.2 < 2.2e-16 ***
                             3952
cons.conf.idx 1
                  7.405
                             3951
                                    4154.8 0.006505 **
euribor3m
             1
                  4.495
                             3950
                                    4150.3 0.033999 *
nr.employed
                                     4149.5 0.368488
             1
                  0.809
                             3949
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
```

Here it is seen that the adding job variable on top of the age variable is helpful since the significance is high. AIC value of Model 1 is 4251.5. A model will be better than this if its AIC value is lower.

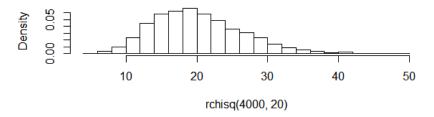
So to select the variables I use Regsubsets function. To keep my model size feasible I choose 8 variables (There are 8 variables whose significance level is <0.001). This is a good way to limit the model size. Exhaustive, forward and backward searches could be done to obtain the 8 variables. This has been done in subsequent models.

The chi-square distribution is as follows:



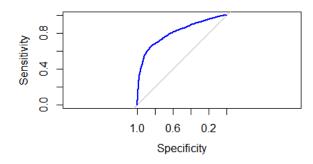


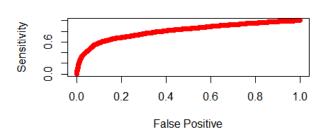
Histogram of rchisq(4000, 20)



Continuing with the process of prediction using this classifier and calculating the miss-calculation error and the Area under the ROC curve as a performance measure of this model, I get the MCE on the testing data to be 0.348. The confusion matrix I obtain for the test data is as follows:

The specificity is 0.98594, sensitivity is 0.2111 and the false positive value is 0.01406.



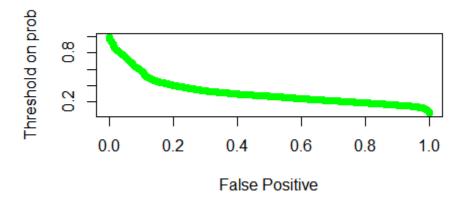


The above are the ROC curves. The Area under this curve (AUC) is 0.8063. For model selection higher the AUC better is the model.

To tune it we can use the correct threshhold value for probabilty which has been kept to 0.9. This makes sure that the false positive value is very small. This is the Bayes rule. Essentially if the loss (cost) of making a '1' to a '0' is given by a_{1,0} and if the loss (cost) of making a '0' to a '1' is given by a {0,1}, then

$$P(Y=1|X)> (a_{0,1}/a_{1,0})/(1+(a_{0,1}/a_{1,0}))$$

In this case, I have taken a_{0,1}/a_{1,0}=9



To summarize the model here, it constitutes all the variables whose coefficients are shown before through the summary of the fit. Its not a great model. The classification boundary is essentially the log odds ratio of the hat Y=1 to hat Y=0 equal to the model. Using a different threshhold on probabilities (different loss function) we get different classifiers and overlaying the ROC curves together we can see which one does better (It's a challenge to visualize the classification boundary for such high dimension). Here we stick to 0.9 because of the lot this perfoms the best.

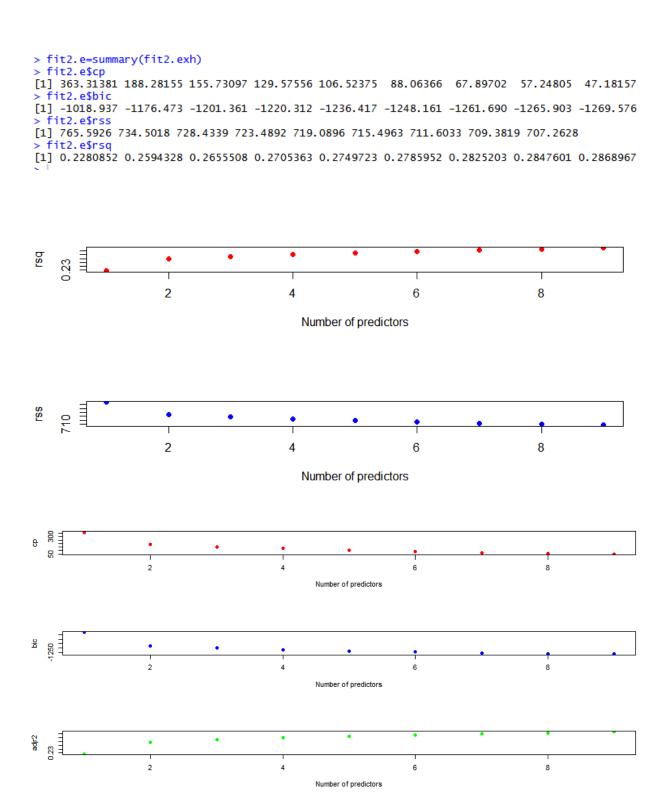
TD = - 9.155e+01 + sum across all variables (Corresponding Coeff * Correspoding Variable)

♣ Model 2:

Here I used model selection method to get 8 variables using Regsubsets.

1. Exhaustive Search

The values of the different criterions that were obtained is given below. RSS and RSQ and not the best criterions to be used for model selection. RSS will of course reduce when more variables are used



The 8 variables and their corresponding coefficients that we obtain are

```
> coef(fit2.exh,8)
    (Intercept)
                      monthaug
                                      monthmay
                                                      monthnov
                                                                      monthoct
   -13.38889017
                    0.06402441
                                   -0.17817079
                                                   -0.13256959
                                                                   -0.03979464
poutcomesuccess
                  emp.var.rate cons.price.idx
                                                   loanunknown
    0.21224067
                  -0.15925222
                                    0.14776708
                                                   -0.09273530
```

Now fitting a logistic regression model on the chosen variables, we get

```
call:
glm(formula = TD ~ month + poutcome + emp.var.rate + cons.price.idx +
    loan, family = binomial(logit), data = data.cleaned.train)
Deviance Residuals:
Min 1Q Median 3Q
-2.9327 -0.7809 -0.6074 0.8085
                                  2.1173
Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
(Intercept)
                  -113.44041 14.09008 -8.051 8.21e-16 ***
                             0.19455 4.712 2.45e-06 ***
monthaud
                    0.91670
                    2.37249 1.05456 2.250 0.02447 *
monthdec
monthiul
                    0.55310
                              0.17055
                                       3.243 0.00118 **
                               0.17451 -2.093 0.03637 *
monthjun
                    -0.36521
                    monthmar
                    -0.57024 0.14202 -4.015 5.94e-05 ***
monthmay
monthnov
                   -0.17439 0.17937 -0.972 0.33091
                    0.04623
monthoct
                               0.25262
                                       0.183 0.85479
                    0.23474 0.28783 0.816 0.41475
monthsep
poutcomenonexistent 0.58904 0.12727 4.628 3.69e-06 ***
                    1.83650 0.22553 8.143 3.85e-16 ***
poutcomesuccess
                    -0.92714 0.05725 -16.196 < 2e-16 ***
1.20055 0.15019 7.994 1.31e-15 ***
emp.var.rate
                              0.15019 7.994 1.31e-15 ***
cons.price.idx
loanunknown
                               0.26141 -2.036 0.04170 *
                    -0.53236
                    0.01664
                               0.10554 0.158 0.87473
loanyes
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 5512.4 on 3999
                                 degrees of freedom
Residual deviance: 4226.9 on 3984
                                 degrees of freedom
AIC: 4258.9
Number of Fisher Scoring iterations: 6
> anova(fit1,fit2)
Analysis of Deviance Table
Model 1: TD ~ age + job + marital + education + default + housing + loan +
    contact + month + day_of_week + campaign + pdays + previous +
    poutcome + emp.var.rate + cons.price.idx + cons.conf.idx +
    euribor3m + nr.employed + month.f
Model 2: TD ~ month + poutcome + emp.var.rate + cons.price.idx + loan
  Resid. Df Resid. Dev Df Deviance
       3949
                 4149.5
1
2
       3984
                 4226.9 -35 -77.471
```

The above compares the 2 models generated so far. Surprisingly model 2 doesn't perform as well than model 1 because we see that the deviance actually increased as compared to model 1.

2. Forward Selection

The same practice as done for Exhaustive search was performed for Forward selection under Regsubsets.

```
> fit2.f$cp
[1] 353.37616 178.74747 146.27565 120.18443 97.18973 78.77628 62.38800 48.04004 38.00107
> fit2.f$bic
[1] -1018.937 -1176.473 -1201.361 -1220.312 -1236.417 -1248.161 -1258.003 -1265.903 -1269.576
> fit2.f$rss
[1] 765.5926 734.5018 728.4339 723.4892 719.0896 715.4963 712.2595 709.3819 707.2628
> fit2.f$rsq
[1] 0.2280852 0.2594328 0.2655508 0.2705363 0.2749723 0.2785952 0.2818587 0.2847601 0.2868967
```

The 8 variables and their corresponding coefficients that we obtain are,

```
> coef(fit2.for,8)
    (Intercept)
                      monthaug
                                      monthmav
                                                      monthnov
                                                                      monthoct poutcomesuccess
   -13.38889001
                    0.06402441
                                   -0.17817079
                                                                   -0.03979464
                                                                                   0.21224068
                                                   -0.13256959
  emp.var.rate cons.price.idx
                                   loanunknown
    -0.15925222
                    0.14776708
                                   -0.09273530
```

We see that forward selection produces the exact same model as exhaustive search.

3. Backward Selection

Finally, backward selection was performed under Regsubsets. The corresponding criterion values we get are:

```
> fit2.b$cp
[1] 363.31381 188.28154 155.73096 135.59183 113.88276 89.15171 67.89701 57.24805 47.18157
> fit2.b$bic
[1] -1018.937 -1176.473 -1201.361 -1214.475 -1229.235 -1247.093 -1261.690 -1265.903 -1269.576
> fit2.b$rss
[1] 765.5926 734.5018 728.4339 724.5458 720.3820 715.6874 711.6033 709.3819 707.2628
> fit2.b$rsq
[1] 0.2280852 0.2594328 0.2655508 0.2694710 0.2736692 0.2784025 0.2825203 0.2847601 0.2868967
```

Observe that the criterion values for the backward and forward selection are the same.

The 8 variables and their corresponding coefficients that we obtain are,

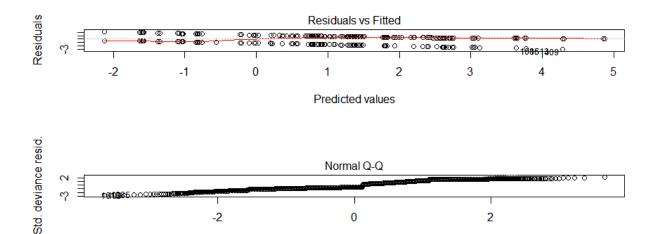
```
> coef(fit2.bac,8)
    (Intercept)
                      monthaug
                                      monthmay
                                                      monthnov
                                                                      monthoct poutcomesuccess
                    0.06402441
                                   -0.17817079
                                                                                    0.21224068
   -13.38889001
                                                   -0.13256959
                                                                   -0.03979464
   emp.var.rate cons.price.idx
                                   1oanunknown
   -0.15925222
                    0.14776708
                                   -0.09273530
```

The coefficient values of this is also the same as the above 2 methods.

Thus the model (Model 2) we get is on performing logistic regression and retaining variables with significance level of ***:

```
TD = -113.44 + 0.9167*monthaug + 2.127*monthmar - 0.57*monthmay + 0.589*poutcomenonexistent + 1.8365*poutcomesuccess - 0.927*emp.var.rate + 1.2*cons.price.idx
```

The above fit can be seen graphically below.



0

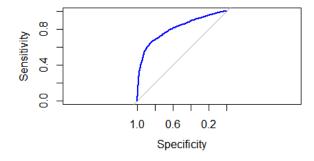
Theoretical Quantiles

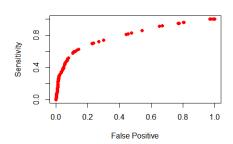
The MCE of this model on the test data is 0.346 and the confusion matrix is given below.

```
> fit2.mce.test
[1] 0.346
> sensitivity=cm[2,2]/sum(data.cleaned.test$TD =="1")
> cm
fit2.pred.test
             0 561 338
             1
                 8 93
```

-2

The ROC curve obtained is show below. The AUC value is 0.7967.

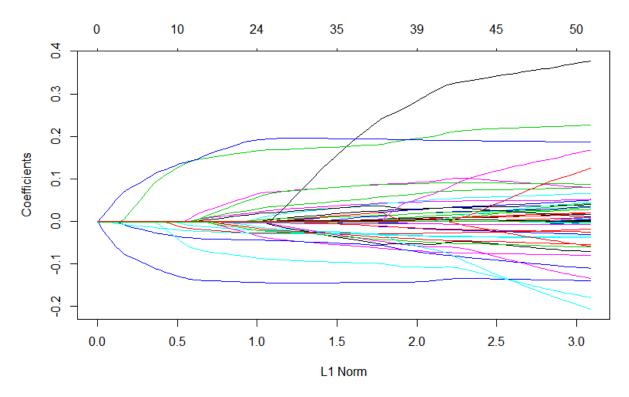




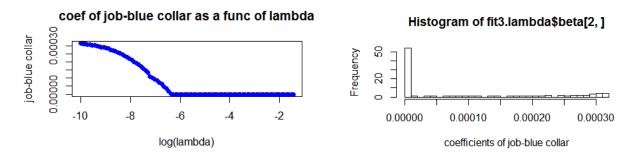
2

♣ Model 3:

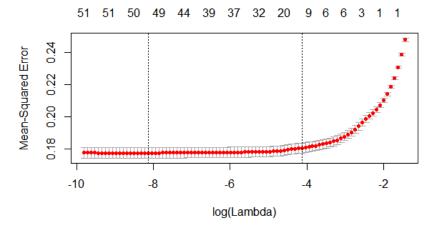
Here the model has been built by using regularization methods. I stick with LASSO than ridge since LASSO has the ability to do feature selection. When the lambda value is not specified in glmnet, the output consists of 100 outputs, one for each lambda. A plot of it shows that each hat beta is shrinking towards a 0 as L2 norm of beta is smaller, which is equivalent to lambda getting larger as can be seen below.



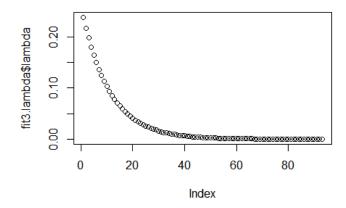
Also lambda values here have huge variability and hence log value is applied. The coefficients also have variability as shown below.



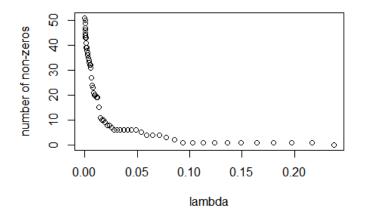
The below graph is an important one on basis of which I can choose the lambda value. Low lambda value means less penalty and the beta values will be high and vice versa.



The 100 lambda values used are shown, and the min lambda value is 0.00029318.



The number of non-zero terms as a function of the lambda used is shown below. As can be seen, higher the value of lambda lesser are the number of non-zeros.



Here I used lambda.1se so that I can keep a tight hold on the number of features selected. The variables (10 make it) and their respective coefficients that make it are,

```
> coef.1se
     (Intercept)
                   jobblue-collar
                                    defaultunknown contacttelephone
                                                                            monthmar
     9.938190133
                     -0.015419691
                                      -0.007625655
                                                       -0.038230522
                                                                         0.134076640
        monthmay
                         monthnov
                                          campaign poutcomesuccess
                                                                        emp.var.rate
    -0.134229551
                     -0.053642490
                                      -0.001189384
                                                        0.138269658
                                                                        -0.022161746
     nr.employed
    -0.001838291
Now fitting a logistic regression model on the chosen variables,
> summary(fit3)
call:
glm(formula = TD ~ job + default + contact + month + campaign +
    poutcome + emp.var.rate + nr.employed, data = data.cleaned.train)
Deviance Residuals:
    Min
             1Q
                 Median
                              30
                                      Max
-1.1966
        -0.2959
                 -0.1371
                           0.3071
                                   0.9838
coefficients:
                     Estimate Std. Error t value Pr(>|t|)
                   10.4800215 1.0419321 10.058 < 2e-16 ***
(Intercept)
jobblue-collar
                   -0.0356227 0.0204801 -1.739 0.08205 .
jobentrepreneur
                    0.0235024 0.0393961
                                          0.597
                                                0.55083
jobhousemaid
                    0.0404111 0.0479769
                                         0.842
                                                0.39967
                   -0.0298658 0.0288106 -1.037
                                                0.29997
jobmanagement
iobretired
                   0.0530143 0.0297877
                                         1.780 0.07520
jobself-employed
                   0.0419854 0.0403614 1.040 0.29829
                                        0.173 0.86275
jobservices
                    0.0046227 0.0267377
                              iobstudent
                   0.0627833 0.0369714
iobtechnician
                   -0.0040397
                   0.0539618 0.0441653
                                        1.222 0.22185
jobunemployed
jobunknown
                   0.0040250 0.0745117 0.054 0.95692
defaultunknown
                   -0.0370676 0.0191456 -1.936 0.05293
                   contacttelephone

    0.0213123
    0.0319364
    0.667
    0.50460

    0.1256609
    0.0763830
    1.645
    0.10002

    0.0525545
    0.0318432
    1.650
    0.09894

monthaug
monthdec
monthjul
                   0.0354515 0.0319001 1.111 0.26649
monthjun
                   monthmar
                   monthmay
                   -0.0971096 0.0322683 -3.009 0.00263 **
monthnov
                              0.0439255 -1.118 0.26346
monthoct
                   -0.0491267
                   -0.0606407 0.0473729 -1.280 0.20059
monthsep
                   -0.0080671 0.0027088 -2.978 0.00292 **
campaign
poutcomenonexistent 0.1203691 0.0234728 5.128 3.07e-07 ***
                                        8.160 4.44e-16 ***
poutcomesuccess
                   0.2505528 0.0307041
                              0.0095170 -3.274 0.00107 **
                   -0.0311557
emp.var.rate
nr.employed
                   -0.0019628 0.0002024 -9.698 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for gaussian family taken to be 0.1768263)
                                    degrees of freedom
    Null deviance: 991.81
                           on 3999
Residual deviance: 702.35 on 3972
                                    degrees of freedom
AIC: 4451.1
Number of Fisher Scoring iterations: 2
```

Comparing the three models we have thus far

```
> anova(fit1,fit3)
Analysis of Deviance Table
Model 1: TD ~ age + job + marital + education + default + housing + loan +
    contact + month + day_of_week + campaign + pdays + previous +
    poutcome + emp.var.rate + cons.price.idx + cons.conf.idx +
    euribor3m + nr.employed
Model 2: TD ~ job + default + contact + month + campaign + poutcome +
   emp.var.rate + nr.employed
  Resid. Df Resid. Dev Df Deviance
1
       3949
               4149.5
       3972
                702.4 -23 3447.1
2
> anova(fit2,fit3)
Analysis of Deviance Table
Model 1: TD ~ month + poutcome + emp.var.rate + cons.price.idx + loan
Model 2: TD ~ job + default + contact + month + campaign + poutcome +
    emp.var.rate + nr.employed
 Resid. Df Resid. Dev Df Deviance
    3984 4226.9
1
2
      3972
               702.4 12 3524.6
```

It can be seen that the deviance of model 3 from model 1 is lesser than its deviance from model 2. Hence Model 3 is the best so far amongst the three models.

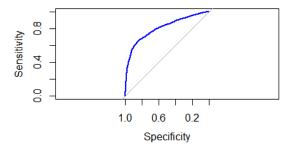
Thus the model (Model 3) we get is on performing logistic regression and retaining variables with significance level of *** and **:

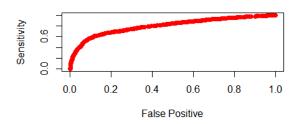
```
TD = 10.48 + 0.196*monthmar - 0.1372*monthmay + 0.12037*poutcomenonexistent + 0.25055*poutcomesuccess - 0.00196*nr.employed - 0.543*contacttelephone - 0.097*monthnov - 0.0311*emp.var.rate - 0.0081*campaign
```

The MCE of this model on the test data is 0.377 and the confusion matrix is given below.

```
> fit3.mce.test
[1] 0.377
> cm
fit3.pred.test 0 1
0 567 375
1 2 56
```

The specificity is 0.996485, sensitivity is 0.12993 and the false positive value is 0.0035149. The ROC curve obtained is show below. The AUC value is 0.7999.



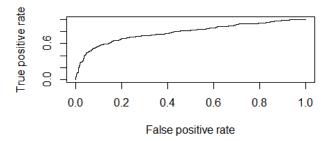


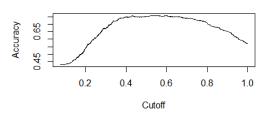
So far we have seen three models in which the training set constituted of 4000 data points and the testing set constitutes of 1000 data points. There was no Cross Validation done. The next three models have cross validation done in order to improve the training of the model and thereby reduce overfitting.

Model 4:

Here I basically use the same model as Model 1 but with cross validation done. I do a 10 fold cross validation. The code snippet is as shown below.

The AUC value is 0.787322. The mean accuracy is 0.641 while the max accuracy obtained is 0.757.





Above I have the ROC curve and the accuracy curve which corresponds to the values of the accuracy reported before. The sensitivity and specificity are as follows,

```
> Sensitivity= performance(abc, "sens")
> mean(sensitivity@y.values[[1]])
[1] 0.6628345
> Specificity= performance(abc, "spec")
> mean(specificity@y.values[[1]])
[1] 0.6243924
```

Hence the MCE mean is 1-0.641=0.359. The model parameters are the same as that of Model 1. The summary is,

```
1oanunknown
                                                                                                                       NA
-3.682e-03
                                                                                                                                    NA
1.077e-01
Deviance Residuals:
                                                                                                                                                -0.034 0.972738
                                                                                        loanves |
                                                                                                                       -6.947e-01
5.028e-01
                                                                                                                                    1.487e-01
3.097e-01
                                                                                                                                                -4.672 2.98e-06
1.624 0.104450
                                                                                        contacttelephone
-3.1304
          -0.8085
                     -0.5760
                                 0.7846
                                            2.1051
                                                                                        monthaug
                                                                                        monthded
                                                                                                                        2.308e+00
                                                                                                                                    1.178e+00
                                                                                                                                                 1.959 0.050131
                                                                                                                        1.975e-01
                                                                                                                                                 1.014
                                                                                                                                                       0.310530
Coefficients: (1 not defined because of singularities)
                                               Std. Error
                                     Estimate
                                                                                        monthjun
                                                                                                                       -3.328e-01
                                                                                                                                    2.955e-01
                                                                                                                                                -1.126 0.260020
                                                                                                                        1.965e+00
                                                                                                                                      367e-01
                                                                                                                                                 4.501
                                                                                                                                                       6.76e-06
(Intercept)
                                                 8.385e+01
                                   -9.155e+01
                                                               -1.092 0.274905
                                                                                        monthmay
                                                                                                                        -5.219e-01
                                                                                                                                      697e-01
                                                                                                                                                -3.076 0.002101
                                                 4.602e-03
                                   2.410e-03
                                                               0.524 0.600445
age
`jobblue-collar
                                                                                        mont hnov
                                                                                                                       -7.347e-01
                                                                                                                                      388e-01
                                                                                                                                                -3.077 0.002091
                                                   427e-01
                                   -6.776e-02
                                                               -0.475 0.634817
                                                                                                                        -6.099e-01
iobentrepreneur
                                   1.753e-01
                                                 2.180e-01
                                                               0.804 0.421114
                                                                                        monthsep
                                                                                                                       -2.606e-01
                                                                                                                                      142e-01
                                                                                                                                                -0.629 0.529312
jobhousemaid
                                   3.188e-01
                                                 2.800e-01
                                                               1.139 0.254852
                                                                                        day_of_weekmon
day_of_weekthu
                                                                                                                       -3.191e-01
-3.628e-01
                                                                                                                                      238e-01
211e-01
                                                                                                                                                -2.578 0.009951
jobmanagement
                                   -2.091e-01
                                                   701e-01
                                                               1.229 0.218978
                                                                                                                                                -2.996 0.002736
jobretired
                                   3.272e-01
                                                 2.146e-01
                                                               1.525 0.127352
                                                                                        day_of_weektue
day_of_weekwed
                                                                                                                       -1.837e-01
                                                                                                                                    1.250e-01
                                                                                                                                                -1.470 0.141554
 jobself-employed
                                                                                                                       -3.907e-02
                                                 2.213e-01
                                                               0.964 0.335204
                                   2.132e-01
jobservices
                                   1.317e-01
                                                   586e-01
                                                               0.830 0.406525
                                                                                        campaign
                                                                                                                       -4.337e-02
                                                                                                                                      728e-02
                                                                                                                                                -2.510 0.012068
                                                                                                                       -3.448e-04
-2.414e-01
                                                                                                                                      .639e-04
.602e-01
                                                                                                                                                -0.743 0.457300
-1.507 0.131824
                                                                                        pdays
previous
iobstudent
                                   5.058e-01
                                                 2.490e-01
                                                               2.032 0.042203
                                                 1.343e-01
                                                               0.150 0.880823
                                   2.013e-02
iobtechnician
                                                                                        poutcomenonexistent
                                                                                                                        3.238e-01
                                                                                                                                      246e-01
                                                                                                                                                 1.442 0.149282
jobunemployed
                                                   644e-01
jobunknown
                                    6.782e-02
                                                 4.453e-01
                                                               0.152 0.878954
                                                                                        emp.var.rate
                                                                                                                        -1.220e+00
                                                                                                                                    3.348e-01
                                                                                                                                                 -3.644 0.000269
maritalmarried
                                   7.602e-02
                                                 1.267e-01
                                                               0.600 0.548451
                                                                                        cons.price.idx
cons.conf.idx
                                                                                                                                                 2.291 0.021981
0.100 0.920492
                                                                                                                        1.287e+00
                                                                                                                                      617e-01
                                                                                                                        1.907e-03
maritalsingle
                                                               0.326 0.744447
                                                                                                                                    1.910e-02
maritalunknown
                                    3.705e-01
                                                 8.224e-01
                                                               0.451 0.652348
                                                                                        euribor3m
                                                                                                                        6.010e-01
                                                                                                                                    2.827e-01
                                                                                                                                                 2.126 0.033489
                                                                                        nr.employed
                                                                                                                                    6.709e-03
educationbasic. 6v
                                   2.048e-01
                                                 2.078e-01
                                                               0.986 0.324335
educationbasic.9y
                                    7.268e-02
                                                 1.734e-01
                                                               0.419 0.675081
                                                                                        Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
educationhigh.school
educationilliterate
                                    8.216e-02
                                                 1.736e-01
                                                               0.473 0.635981
                                                 1.970e+02
                                   1.112e+01
                                                               0.056 0.954985
                                                                                        (Dispersion parameter for binomial family taken to be 1)
educationprofessional.course
                                   1.567e-01
                                                 1.961e-01
                                                               0.799 0.424139
educationuniversity.degree
                                   2.241e-01
                                                   .755e-01
                                                              1.277 0.201709
-0.122 0.902765
                                                                                            Null deviance: 5512.4 on 3999 degrees of freedom
                                                                                        Residual deviance: 4149.5
                                                                                                                              degrees of freedom
educationunknown
                                   -2.815e-02
                                                 2.304e-01
                                                                                                                     on 3949
defaultunknown
                                   -2.038e-01
                                                 1.114e-01
                                                              -1.830 0.067257
                                                                                        AIC: 4251.5
housingunknown
                                   -5.376e-01
                                                 2.709e-01
                                                              -1.985 0.047142
                                                                                        Number of Fisher Scoring iterations: 10
                                                 7.813e-02
housingyes
                                  -6.773e-03
                                                              -0.087 0.930917
```

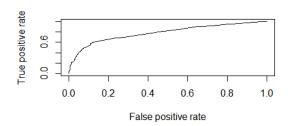
TD = -9.155e+01 + sum across all variables (Corresponding Coeff * Correspoding Variable)

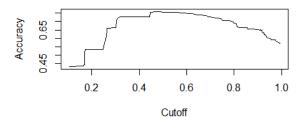
Model 5:

Here I basically use the same model as Model 2 but with cross validation done. I do a 10 fold cross validation. The predictor variables that are chosen here are the same as that of Model 2.

The AUC value is 0.781377. The mean accuracy is 0.65098 while the max accuracy obtained is 0.76.

Below I have the ROC curve and the accuracy curve which corresponds to the values of the accuracy reported before. The sensitivity and specificity are 0.40627 and 0.83634 respectively.





Hence the MCE mean is 1-0.65098=0.34902. The model parameters are the same as that of Model 2. The summary is,

```
call:
NULL
Deviance Residuals:
                  Median
                                3Q
   Min
             1Q
                                         Max
-2.9327
        -0.7809
                  -0.6074
                            0.8085
                                     2.1173
Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
                    -113.44041
                                 14.09008
                                           -8.051 8.21e-16 ***
(Intercept)
monthaug
                       0.91670
                                  0.19455
                                            4.712 2.45e-06
monthdec
                       2.37249
                                  1.05456
                                             2.250
                                                   0.02447
monthjul
                       0.55310
                                  0.17055
                                             3.243
                                                    0.00118 **
monthjun
                      -0.36521
                                  0.17451
                                            -2.093
                                                   0.03637
                                             5.474 4.40e-08 ***
monthmar
                       2.12738
                                  0.38864
                                            -4.015 5.94e-05 ***
monthmay
                      -0.57024
                                  0.14202
                      -0.17439
                                  0.17937
monthnov
                                            -0.972
                                                    0.33091
                       0.04623
monthoct
                                  0.25262
                                            0.183
                                                    0.85479
monthsep
                       0.23474
                                  0.28783
                                             0.816
                                                   0.41475
poutcomenonexistent
                       0.58904
                                  0.12727
                                             4.628 3.69e-06 ***
                                             8.143 3.85e-16 ***
                       1.83650
                                  0.22553
poutcomesuccess
                                                   < 2e-16 ***
                      -0.92714
                                  0.05725 -16.196
emp.var.rate
                                             7.994 1.31e-15 ***
cons.price.idx
                       1.20055
                                  0.15019
loanunknown
                       -0.53236
                                  0.26141
                                            -2.036 0.04170
loanves
                       0.01664
                                  0.10554
                                            0.158 0.87473
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for binomial family taken to be 1)
                           on 3999
   Null deviance: 5512.4
                                    degrees of freedom
                           on 3984
Residual deviance: 4226.9
                                    degrees of freedom
AIC: 4258.9
Number of Fisher Scoring iterations: 6
```

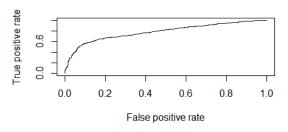
TD = -113.44 + 0.9167*monthaug + 2.127*monthmar - 0.57*monthmay + 0.589*poutcomenonexistent + 1.8365*poutcomesuccess - 0.927*emp.var.rate + 1.2*cons.price.idx

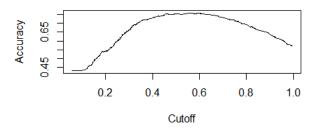
Model 6:

Here I basically use the same model as Model 3 but with cross validation done. I do a 10 fold cross validation. The predictor variables that are chosen here are the same as that of Model 3.

The AUC value is 0.7834. The mean accuracy is 0.63986 while the max accuracy obtained is 0.759.

Below I have the ROC curve and the accuracy curve which corresponds to the values of the accuracy reported before. The sensitivity and specificity are 0.6136 and 0.6597 respectively.





Hence the MCE mean is 1-0.63986=0.36014. The model parameters are the same as that of Model 3. The summary is,

```
Call:
Deviance Residuals:
Min
-3.1198
            1Q Median
-0.8229 -0.5600
                                         3Q
0.8025
Coefficients:
                               Estimate Std. Error z value Pr(>|z|)
55.372751 7.147319 7.747 9.38e-15
(Intercept)
                              55.372751
  iobblue-collar
                              -0.175614
                                               0.115120
                                                               -1.525
                                                                         0.12714
jobentrepreneur
jobhousemaid
                               0.145058
                                               0.213286
                               -0.176864
 iobmanagement
                                               0.164681
                                                               -1.074
                                                                          0.28283
jobself-employed`
jobservices
                               0.318439
0.219884
0.035977
                                               0.181997
0.216805
                                                                1 750
                                                                          0.08017
                                                                0.243
                                               0.148155
                                                                          0.80814
iobstudent
                               0.378868
                                               0.230505
                                                                1.644
                                                                          0.10025
                               -0.027703
0.290445
0.042285
                                               0.119410
0.256341
0.424649
jobseddene
jobtechnician
jobunemployed
                                                                0.232
jobunknown
                                                               0.100
                                                                          0.92068
                              -0.196680
-0.368349
0.189735
2.114277
defaultunknown
                                               0.109059
                                                               -1.803
                                                                          0.07132
contacttelephone
monthaug
                                                               -3.141
1.087
                                                                          0.00168
0.27711
                                               1.049108
monthded
                                                                2.015
                                                                          0.04387
                                               0.175015
0.177848
0.390289
                                                                2.121
1.793
4.454
monthjul
monthjun
                               0.371146
0.318958
                                                                          0.03395
0.07290
                               1.738184
monthman
                                                                         8.45e-06
monthmay
                               -0.607984
                                                0.143953
                                                               -4.223
                                                                         2.41e-05
monthnov
monthoct
                              -0.352807
-0.174054
                                               0.176442
                                                               -2.000
-0.649
                                                                          0.04555
monthsep
                              -0.338307
                                               0.304167
                                                               -1.112
                                                                          0.26603
campaign
poutcomenonexistent
                              -0.050453
0.596863
1.826423
                                               0.017453
                                                              -2.891 0.00384
4.690 2.74e-06
8.093 5.84e-16
                                               0.127271
poutcomesuccess
emp.var.rate
nr.employed
                               -0.055913
                                               0.062098
                                                               -0.900
                                                                         0.36790
                              -0.010871
                                               0.001387
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 5512.4 on 3999 degrees of freedom Residual deviance: 4194.9 on 3972 degrees of freedom AIC: 4250.9

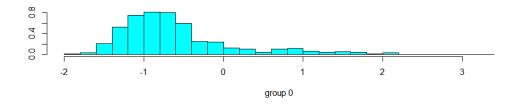
Number of Fisher Scoring iterations: 6
```

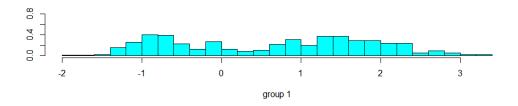
TD = 10.48 + 0.196*monthmar - 0.1372*monthmay + 0.12037*poutcomenonexistent + 0.25055*poutcomesuccess - 0.00196*nr.employed - 0.543*contacttelephone - 0.097*monthnov - 0.0311*emp.var.rate - 0.0081*campaign

Model 7:

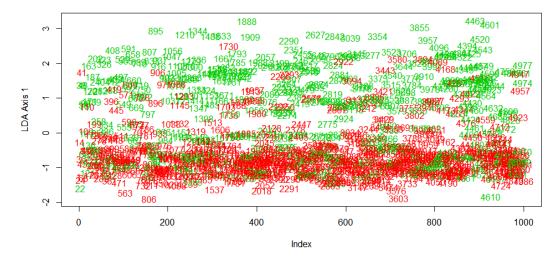
In this method I use Linear Discriminant Analysis (LDA) which is a dimensionality reduction method in supervised learning. Here I use all the variables. Since the response variable has only 2 levels –yes or no, we have only one principal axis (LD1).

The histogram of the discriminant functions is shown below.





The scatter plot of the discriminant function values is,



As can be seen we can separate the data along LD1 fairly well. The confusion matrix post prediction on test data is obtained as,

The MCE is 0.754. Clearly, this method does not do as well with high miss-classifications. The group means obtained are as follows,

```
lda(data.cleaned.train$TD ~ ., data = data.cleaned.train)
Prior probabilities of groups:
0.54525 0.45475
0.07336084 0.03805594
                 0.1401869
 40.78615
                                   0.02858714
                                                 0.02308961
                                                                 0.06102254 0.09455745
  jobself-employed jobservices
                                  jobstudent
                                               jobtechnician
0
                                                                  0.01879872 0.008711600
        0.03026135
                     0.08986703 0.01834021
                                                   0.1659789
        0.03078615
                     0.07421660 0.06157229
                                                    0.1550302
                                                                  0.03243540 0.007696537
  maritalmarried maritalsingle maritalunknown educationbasic.6y educationbasic.9y
                       0.2879413
0
                                      0.001834021
                                                           0.06189821
       0.5951398
                                                                                 0.1485557
        0.5327103
                       0.3567894
                                      0.003298516
                                                           0.04398021
  educationhigh.school educationilliterate educationprofessional.course 0.2251261 0.0000000000 0.1182944
0
              0.2221001
                                 0.0005497526
                                                                      0.1242441
  educationuniversity.degree educationunknown defaultunknown housingunknown
                     0.2929849
                                       0.04951857
                                                                         0.02308961
monthdec
                     0.3628367
                                       0.05552501
                                                         0.0951072
  housingyes loanunknown
0.5066483 0.02475928
                              loanyes contacttelephone monthaug
.1531408 0.3915635 0.1480972
               0.02475928 0.1531408
                                                                     0.0004585053
   0.5305113
              0.02308961 0.1473337
                                               0.1605278 0.1330401 0.0181418362
 monthjul monthjun monthmar monthmay monthnov monthoct monthsep
0.1838606 0.1325080 0.003668042 0.3452545 0.11095828 0.01329665 0.00871160
 0.1456844 0.1198461 0.066520066 0.1940627 0.09015943 0.05992303 0.05717427
  day_of_weekmon day_of_weekthu day_of_weektue day_of_weekwed campaign
                                                          0.1934892 2.678588 980.3787
       0.2090784
                        0.2310867
                                         0.1856946
        0.1852666
                        0.2210005
                                         0.2078065
                                                          0.1962617 2.097306 781.7081
 previous poutcomenonexistent poutcomesuccess 0.1361761 0.8890417 0.01421366
                                                     emp.var.rate cons.price.idx
0.2748739 93.60807
                        0.6734469
                                         0.20340847
                                                        -1.2249038
  cons.conf.idx euribor3m nr.employed
-40.58588 3.848534 5178.006
      -39.92216
                  2.125677
```

The LD1 values are as follows,

Coefficients of linear discriminants:

Coefficients of linear discri	iminants:
	LD1
age	0.0014563363
jobblue-collar	-0.0786599250
jobentrepreneur	0.1249738089
jobhousemaid	0.2227055772
jobmanagement	-0.1548487714
jobretired	0.2249341146
jobself-employed	0.1708972542
jobservices	0.0912037336
jobstudent	0.3488597093
jobtechnician	0.0182163636
jobunemployed	0.2909971100
jobunknown	0.0231406650
maritalmarried	0.0709444450
maritalsingle	0.0395675802
maritalunknown	0.1930393227
educationbasic.6y	0.1569858453
educationbasic.9y	0.0301274685
educationhigh.school	0.0442722629
educationilliterate	1.6604400272
educationprofessional.course	0.0873517523
educationuniversity.degree	0.1487739834
educationunknown	-0.0052079733
defaultunknown	-0.1696857763
housingunknown	-0.1774168404
housingyes	-0.0030956961
loanunknown	-0.1774168404
loanyes	-0.0053904219
contacttelephone	-0.4997818875
monthaug	0.2303522985
monthdec	0.3467920818
monthjul	0.0370097776
monthjun	-0.2965808143
monthmar	1.0114766515
monthmay	-0.6080989995
monthnov	-0.8133743847
monthoct	-0.6087753863
monthsep	-0.3008753077
	-0.2437638515
day_of_weekmon day_of_weekthu	-0.2710833401
day_of_weektue	-0.1399335159
day_of_weekwed	-0.0293803490
campaign	-0.0311724847
pdays	-0.0003152017
previous	-0.1139838991
poutcomenonexistent	0.3787037055
poutcomesuccess	0.8143806286
emp.var.rate	-0.9846632716
cons.price.idx	0.8031477149
cons.conf.idx	-0.0048874518
euribor3m	0.5931692381
nr.employed	-0.0076966992
	-

Hence the model we get is

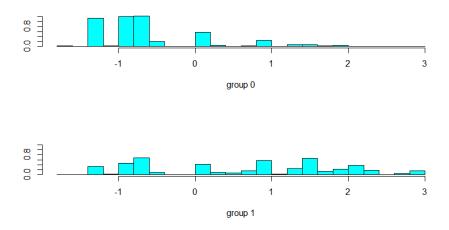
TD= sum across all the variables (Variable * Corresponding LD1)

Source: http://www.talkstats.com/showthread.php/39958-discriminant-linear-analysis-coefficient-interpretation

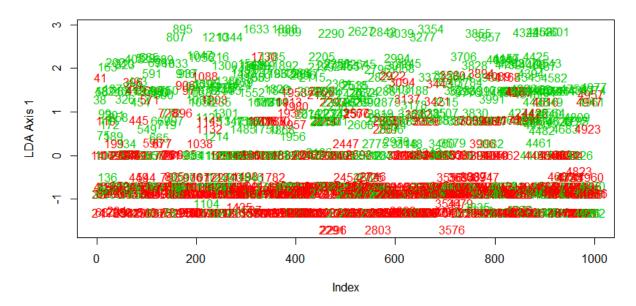
♣ Model 8:

In this method I use Linear Discriminant Analysis (LDA) which is a dimensionality reduction method in supervised learning. Here I use only those variables I had gotten from Regsubsets. These are the same variables used in Model 2 and Model 5. Since the response variable has only 2 levels –yes or no, we have only one principal axis (LD1).

The histogram of the discriminant functions is shown below.



The scatter plot of the discriminant function values is,



The data separation in this case along LD1 is not as well as the previous case. The confusion matrix post prediction on test data is obtained as,

> ct 0 1 0 501 68 1 174 257

The MCE is 0.758. Clearly, this method does not do as well with high miss-classifications just like the above.

The LD1 values are as follows,

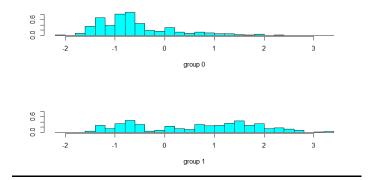
Coefficients of line	ear discriminants:
	LD1
monthaug	0.608473654
monthdec	0.765063034
monthjul	0.318761707
monthjun	-0.365859861
monthmar	1.231861485
monthmay	-0.607254726
monthnov	-0.317856628
monthoct	-0.008343567
monthsep	0.206084596
poutcomenonexistent	0.518893802
poutcomesuccess	1.119683043
emp.var.rate	-0.825092988
cons.price.idx	0.959560411
loanunknown	-0.382976615
loanyes	0.016374598

TD= sum across all the variables above (Variable * Corresponding LD1)

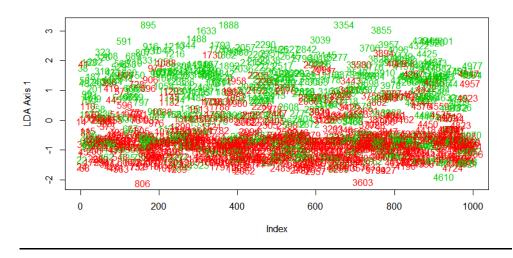
Model 9:

In this method I use Linear Discriminant Analysis (LDA) which is a dimensionality reduction method in supervised learning. Here I use only those variables I had gotten from LASSO regularization. These are the same variables used in Model 3 and Model 6. Since the response variable has only 2 levels –yes or no, we have only one principal axis (LD1).

The histogram of the discriminant functions is shown below.



The scatter plot of the discriminant function values is,



The data separation in this case along LD1 is decent with still some values abruptly present farther from the cluster. The confusion matrix post prediction on test data is obtained as,

The MCE is 0.753. Clearly, this method does not do as well with high miss-classifications just like the above. The LD1 values are as follows,

Coefficients of lin	
3-1-1-2	LD1
jobblue-collar	-0.157323455
jobentrepreneur	0.103795632
jobhousemaid	0.178470710
jobmanagement	-0.131898592
jobretired	0.234131238
jobself-employed	0.185423511
jobservices	0.020415625
jobstudent	0.277274786
jobtechnician	-0.017840816
jobunemployed	0.238315892
jobunknown	0.017776040
defaultunknown	-0.163704460
contacttelephone	-0.239737792
monthaug	0.094123028
monthdec	0.554966226
monthjul	0.232100501
monthjun	0.156567178
monthmar	0.865664120
monthmay	-0.605994817
monthnov	-0.428872814
monthoct	-0.216962015
monthsep	-0.267812237
campaign	-0.035627585
poutcomenonexistent	0.531595828
poutcomesuccess	1.106536423
emp.var.rate	-0.137595411
nr.employed	-0.008668464

TD= sum across all the variables above (Variable * Corresponding LD1)

What can be summarized out of the last 3 models that we obtain from LDA is that the MCE has significantly higher as compared to logistic regressions. The models don't do well to classify the dataset.

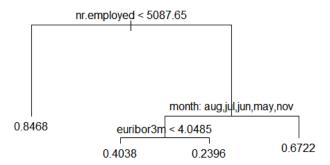
Finally, I explore the Tree methods along with Random Forest to generate 3 more models.

♣ Model 10:

This is a tree based approach on all the variables that are there in the dataset. The frame showing the splits and the tree itself is shown below.

> fit10.1\$frame

```
dev
                                    yval splits.cutleft splits.cutright
           var
                  n
1
 nr.employed 4000 991.80975 0.4547500
                                                <5087.65
                                                                >5087.65
2
        <le><leaf> 1005 130.40199 0.8467662
3
         month 2995 655.13723 0.3232053
                                                  :bdegh
                                                                    :acfi
     euribor3m 2635 525.97116 0.2755218
                                                 <4.0485
                                                                 >4.0485
6
12
        <le><leaf> 577 138.91161 0.4038128
13
        <le><leaf> 2058 374.90039 0.2395530
        <le><leaf> 360 79.32222 0.6722222
```



There are 3 variables that the tree is split on and it leads to 4 leaves. Basically they are the mean values in the 4 regions the entire data set get divided into. The summary of this tree is given below,

```
Regression tree:
tree(formula = TD ~ ., data = data.cleaned.train)
Variables actually used in tree construction:
[1] "nr.employed" "month" "euribor3m"
Number of terminal nodes: 4
Residual mean deviance: 0.1811 = 723.5 / 3996
Distribution of residuals:
   Min. 1st Qu. Median Mean 3rd Qu. Max.
-0.8468 -0.2396 -0.2396 0.0000 0.1532 0.7604
```

The default split is on deviance. The other split is on Gini. The tree obtained from that is,

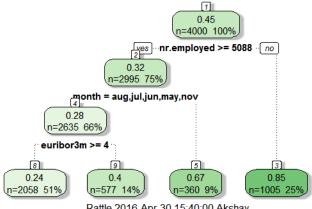


The summary of this tree is as shown below,

```
Regression tree:
tree(formula = TD ~ ., data = data.cleaned.train, split = "gini")
Variables actually used in tree construction:
 [1] "nr.employed"
[5] "euribor3m"
                                         "job"
"campaign"
                                                           "month"
                       "pdays"
                       "age"
                                                           "cons.price.idx"
 [9] "day_of_week"
                       "marital"
                                        "previous"
                                                           "housing"
                       "emp.var.rate"
[13] "education"
                                         "contact"
                                                           "poutcome"
                       "loan"
[17] "default"
Number of terminal nodes: 631
Residual mean deviance: 0.1133 = 381.6 / 3369
Distribution of residuals:
   Min. 1st Qu. Median
                            Mean 3rd Qu.
-0.8889 -0.1250 0.0000 0.0000 0.0000 0.8889
```

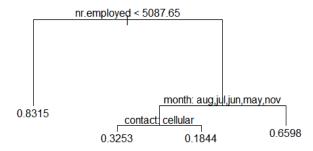
As can be seen in the gini split, the number of tree leaves are far more and also the residual mean deviance is lesser than when the split occurs on deviance.

A fancier version of the plot is shown below. Here the number of observation in a particular node and its accuracy is shown.

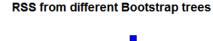


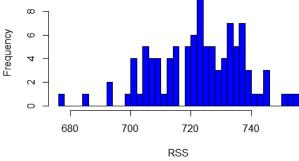
Rattle 2016-Apr-30 15:40:00 Akshay

The RSS that has been computed is 723.5 for the default split. A quick insight into the RSS of the logistic model shows that for the same variables the deviance is much larger. Next I performed Bootstrap to get more sampled dataset and get better trees. I get 100 trees, one for each bootstrap sample. One such tree is given below.



A plot of the RSS that we get across the Bootstrap samples is shown by the below histogram.

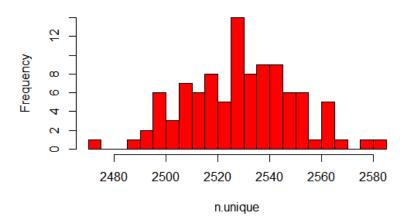




Here it can be seen that the RSS varies from 680 to 740.

The number of unique data points in each bootstrap sample is shown in the below histogram.

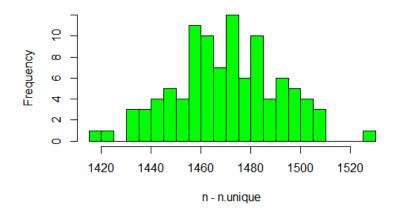
number of unique subjects included in each Bootstrap sar



This shows that anywhere between 2480 and 2580 samples are unique out of 4000, while the rest are repeated.

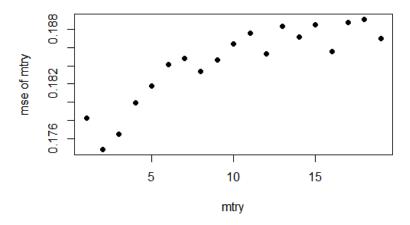
Number of Out of Bag (OOB) samples not included in each Bootstrap sample is shown below.

number of OOB subjects not included in each Bootstrap sa

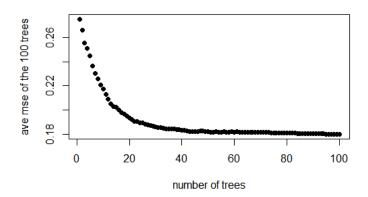


Basically while bootstrapping two thirds of the observations are used to make the tree. The rest one third are out of bag samples. The response of the i'th observation in the OOB was predicted using each of the tree in which that observation was OOB. This meant that I got roughly around B/3 responses for each observation, where B is the number of Bootstrap sample and then I averaged those responses to be able to finally obtain one response for each observation. This entire process is called bagging.

Additionally to improve performance, I built random forest on top of each bootstrapped sample. The effect of mtry parameter, which is the number of random split at each leaf can be seen below.

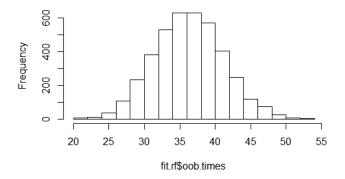


As mtry increases the MSE also increases. Hence I used a value like mtry =4 (square root of 20 roughly) to obtain the Random Forest. The average MSE that I get for 100 trees is shown. Clearly, more the number of trees, less is the MSE.

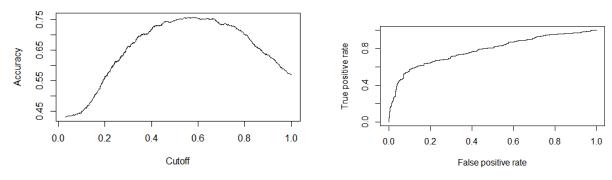


The histogram below how many times each observation is OOB. Most of the observations are OOB roughly 30-40% times.





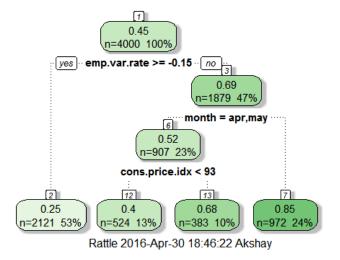
The training error I obtain is 0.18 (18%). This means a mean accuracy of 82% on the training dataset (OOB accuracy). Upon prediction using the test data, I got the mean test accuracy of 63.81% and the max test accuracy to be 75.8%. The accuracy curve on the test data is given below. The ROC curve is also shown.



The mean sensitivity which is the probability of a point being classified as positive when it is indeed positive is 0.6626 while the specificity which is the probability of a point being classified as negative when it is indeed negative is 0.6196.

Model 11:

This is a tree based approach on all the variables that I got from regsubsets. The frame showing the splits and the tree itself is shown below. Note I use the default deviance split here on.

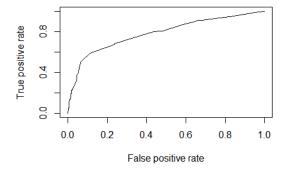


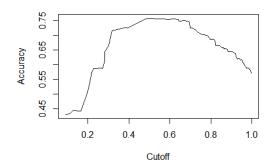
> fit.tree\$frame

```
var
                          wt
                                    dev
                                             yval
                                                    complexity ncompete nsurrogate
     emp.var.rate 4000 4000 991.80975 0.4547500 0.197276010
1
                                                                       4
                                                                       0
2
           <le><leaf> 2121 2121 394.03772 0.2465818 0.005774646
                                                                                   0
3
                             402.11176 0.6897286 0.050031305
                                                                       4
                                                                                   3
            month 1879
                        1879
6
  cons.price.idx
                    907
                         907 226.33076 0.5214994 0.017666347
                                                                       3
                                                                                   3
12
                         524 126.03626 0.4026718 0.004524817
                                                                       0
                                                                                   0
           <leaf>
                    524
13
                              82.77285 0.6840731 0.006217674
                                                                                   0
           <leaf>
                    383
                         383
                                                                       0
7
                         972 126.15947 0.8467078 0.004380722
                                                                                   0
```

Like the previous model, I use bootstrap to improve the model performance. Additionally to improve performance, I built random forest on top of each bootstrapped sample. As mtry increases the MSE also increases. Hence I used a value like mtry =2 (square root of 5 roughly) to obtain the Random Forest. Also I build 500 trees for a good result.

The training error I obtain is 0.17738 (17.738%). This means a mean accuracy of over 82% on the training dataset (OOB accuracy). Upon prediction using the test data, I got the mean test accuracy of 64.85377% and the max test accuracy to be 75.8%. The accuracy curve on the test data is given below. The ROC curve is also shown.

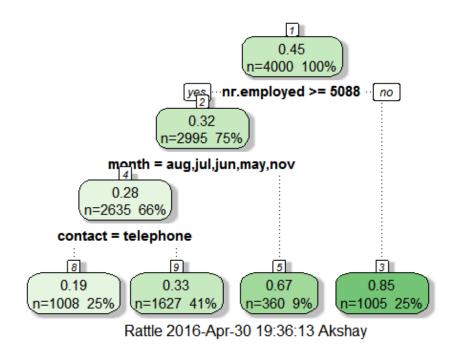




The mean sensitivity which is the probability of a point being classified as positive when it is indeed positive is 0.395329 while the specificity which is the probability of a point being classified as negative when it is indeed negative is 0.8403356.

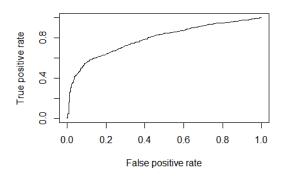
Model 12:

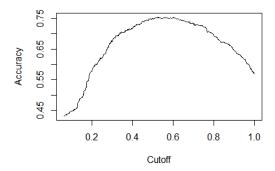
This is a tree based approach on all the variables that I got from LASSO regularization. The frame showing the splits and the tree itself is shown below. The trees have been split with the default deviance parameter.



Like the previous model, I use bootstrap to improve the model performance. Additionally to improve performance, I built random forest on top of each bootstrapped sample. As mtry increases the MSE also increases. Hence I used a value like mtry =3 (square root of 8 roughly) to obtain the Random Forest. Also I build 500 trees for a good result.

The training error I obtain is 0.18154 (18.154%). This means a mean accuracy of over 81% on the training dataset (OOB accuracy). Upon prediction using the test data, I got the mean test accuracy of 64.21414% and the max test accuracy to be 75.4%. The accuracy curve on the test data is given below. The ROC curve is also shown.





The mean sensitivity which is the probability of a point being classified as positive when it is indeed positive is 0.6146369 while the specificity which is the probability of a point being classified as negative when it is indeed negative is 0.6629753.

Ensemble Model:

Having obtained all the above models, I ensemble them to boost the performance of the classifier. First I obtained all the predictions made by the models on the train data set. From the above analysis it was clear that cross validation did not provide much difference in test scores from what was reported in the respective first three models and hence it is not considered here to build the ensemble model.

Using the 9 models, I created a common data frame and obtained the mean values and classified them as 0 if it was lesser than 0.5 or 1 if it was greater. This way I got the training accuracy to be around 69%.

Lastly, I built a linear regression model on top of all the models considering these models as predictors. This helped me weigh the models.

```
> summary(fitfinal2)
call:
lm(formula = data.cleaned.train.TD ~ TD.Label.Predicted1 + TD.Label.Predicted7 +
    TD.Label.Predicted8 + TD.Label.Predicted9 + TD.Label.Predicted10 +
    TD.Label.Predicted11 + TD.Label.Predicted12, data = df.main)
Residuals:
            1Q Median
                            3Q
    Min
                                   Max
-0.7235 -0.2646 -0.2646 0.3659 0.7955
Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
(Intercept)
                     0.264652
                                0.008151 32.469 < 2e-16 ***
TD.Label.Predicted1 -0.091333
                                0.038452 -2.375
                                                   0.0176 *
TD.Label.Predicted7
                     0.310055
                                0.064151
                                           4.833 1.39e-06
TD.Label.Predicted8 -0.060157
                                0.055673
                                          -1.081
                                                   0.2800
                                                   0.0079 **
TD.Label.Predicted9
                    0.119605
                                0.045003
                                           2.658
TD.Label.Predicted10 0.294018
                                0.030414
                                           9.667
                                                  < 2e-16 ***
TD.Label.Predicted11 0.036085
                                0.038891
                                           0.928
                                                   0.3535
                                           4.310 1.67e-05 ***
TD.Label.Predicted12 0.144576
                                0.033543
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.4114 on 3992 degrees of freedom
Multiple R-squared: 0.3187,
                              Adjusted R-squared: 0.3175
F-statistic: 266.8 on 7 and 3992 DF, p-value: < 2.2e-16
```

FINAL MODEL FINDINGS AND SUMMARY

To summarize, the entire study began the idea to create multiple models and compare them and at the end ensemble them. Data was initially cleaned and subsetted for training and testing purposes. A summary of the model is as follows:

Model Number	Model Type	Test MCE
1	Logistic Regression on all variables	0.348
2	Logistic Regression on variables selected from Backward	0.346
	Selection of Regsubsets	
3	Logistic Regression after feature selection by LASSO	0.377
4	Logistic Regression on all variables along with 10 fold Cross	0.359
	Validation	
5	Logistic Regression on variables selected from Backward	0.349
	Selection of Regsubsets along with 10 fold Cross Validation	
6	Logistic Regression after feature selection by LASSO along	0.360
	with 10 fold Cross Validation	
7	LDA on all variables	0.754
8	LDA on variables selected from Backward Selection of	0.758
	Regsubsets	
9	LDA on variables left after feature selection by LASSO	0.753
10	Random Forest after bagging and bootsrapping on all	0.362
	variables	
11	Random Forest after bagging and bootsrapping on variables	0.351
	selected from Backward Selection of Regsubsets	
12	Random Forest after bagging and bootsrapping on variables	0.358
	left after feature selection by LASSO	

The variables that get selected from Regsubsets are:

month + poutcome + emp.var.rate + cons.price.idx + loan

The variables that get selected from LASSO are:

```
Job + default + contact + month + campaign + poutcome + emp.var.rate +nr.employed
```

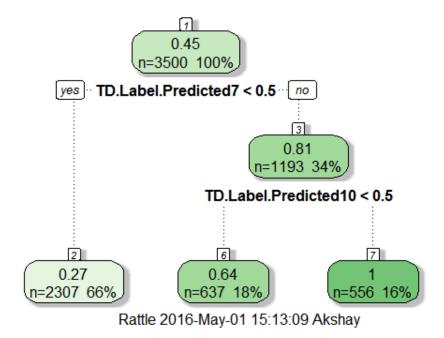
The above is the mean MCE. The least MCE (Max Accuracy) computed is around 75% for the test data set and 82% for the training data set. LDA doesn't perform well as compared to Logistic Regression. Cross Validation also surprisingly does not go a long way in improving accuracy. Random Forest performs the best. Some trees do really well but on an average the accuracy is comparable to those of logistic regression.

I then took the 9 models barring the cross validated ones and ensembled them in three ways. First by taking mean of the predictions made on test data and then classifying them and the other was to fit a linear regression model on the 7 models itself to weigh the models for classifications. For this I made a data frame consisting of predictions of all the 7 models and the response variable and fit a linear model. The data frame is made of 0's and 1's. A coupe of the models were correlated and hence those are removed and the fit is updated. Upon regression, if the response obtained is <0.5 then the classification would be 0 and if more than it would be 1.

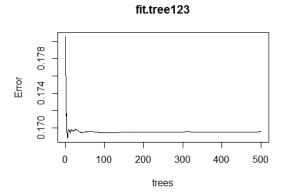
Data.cleaned.train.TD = 0.264652 - 0.091333*TD.Label.Predicted1 + 0.31* TD.Label.Predicted7 - 0.060157* TD.Label.Predicted8 + 0.1196* TD.Label.Predicted9 + 0.294* TD.Label.Predicted10 + 0.0361* TD.Label.Predicted11 + 0.144576* TD.Label.Predicted12

So then the final model!!

Random Forest did the best of all the models. And hence I used the prediction data frame and performed a Random Forest on them. I again divided the data frame into training and testing and performed my analysis. I then fit a random forest tree (fit.tree123 in code) on my training data set shown below,

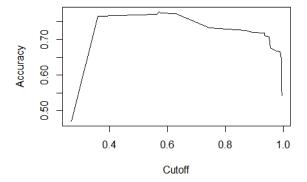


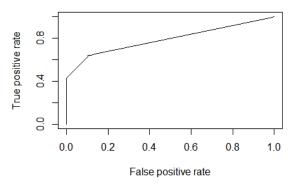
The plot of the final tree is as follows:



I do the prediction on the test data and the confusion matrix I get is as shown,

The test MCE that I finally get is 0.23!!!! This means an accuracy of 77% on the test data which is far more than the accuracy we had from the individual models. The max accuracy reported is 77.8%. The roc curve and the accuracy curve is as shown below. The mean sensitivity is 0.4487 and the mean specificity is 0.879





What I also noticed when building these models is that some variables were consistently part of it and had significance level in the order of ***. These are:

month, poutcome, emp.var.rate and cons.price.idx

Even among the levels of the month, March and May were of great significance. These make sense because essentially these months constitute the end of Quarter 1 and midway Quarter 2. The primary reason behind a lot of customers opening the term deposit with the bank during these months could be because of reasons like the onset of spring, to the schooling season of Portugal is midway and parents have to make savings to pay for the schooling of the next year.

Also most government holidays in Portugal are in December. Opening a half yearly term deposit is a good investment option to quickly save money to splurge on the holiday season. 81% of the population in Portugal is Roman Catholic. Expenditures during Christmas and the holiday season could be a lot. Hence could be the reason. Also, historically, the banks have done well in the first two quarters in Portugal and this might be another reason.

Poutcome is an important predictor. This is because if a client has not responded positively in the previous marketing campaigns it is highly likely that he would not do so in the future. It is usual that an average person would gets calls and emails from various sources and on an average people unsubscribe/subscribe to such notifications out of sheer disinterest/interest for them. Marketing calls similarly are prone to such response from the customer. Hence naturally it's a strong predictor. If a person in the past has responded favorably, is it highly probable that he would lend an ear to such calls in the future as well.

Em.var.rate indicates the quarterly variation in the employment of the client. This is a strong indicator on the financial status/background of the client. Hence naturally this becomes an important predictor for the client opening a term deposit.

Cons.price.index is avery important predictor because this represents the consumer price index, another financial determinant of a customer to be able to open (or have the willingness) or not open a term deposit with the bank.

Thus as an overview of how I obtain my final model:

I take the predictions on the train data (4000 of them) of my models (Logistic Regression, LASSO and Random Forest ones- Totally 7 of them) and create a data frame of them with the corresponding true label. I take 3500 of them as the new training set and train a Random Forest and use this model to predict on the 500 to get my final model having superior accuracy and least MCE.

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APPENDIX

```
# Advanced Statistics for Management (STAT 471/571/701)
# Spring 2016
# Final Project
# Prof: Dr. Linda Zhao
# Name: Akshay Varik
# Penn ID: 73531118
# Task:
# The data is related with direct marketing campaigns of a Portuguese banking
# institution. The marketing campaigns were based on phone calls. Often, more than one
# contact to the same client was required, in order to access if the product (bank term
# deposit) would be ('yes') or not ('no') subscribed. The classification goal is to predict
# if the client will subscribe (yes/no) a term deposit.
# Loading the file and set the working directory
rm(list=ls()) # Remove all the existing variables
dir=c("E:/Data Mining-STAT 571") # my laptop
setwd(dir)
# Include all the libraries
library(plyr)
library(dplyr)
library(leaps)
library(glmnet)
library(pROC)
library(MASS)
library(car)
library(data.table)
library(rockchalk)
library(caret)
library(e1071)
library(ROCR)
library(calibrate)
library(gridExtra)
library(boot)
library(rpart)
library(tree)
library(randomForest)
library(rattle)
library(rpart.plot)
# Read the data file
data=read.csv("Data_FinalProject.csv",header=T)
```

```
# Preliminary familiarity with the data and cleaning the data
names(data)[21]="TD" # Rename the response varible as TD (Term deposit)
levels(data$TD) # Get the levels in the response variable
a=length(which(data$TD == "yes")) # Checking out the proportion of the response
yes.percentage=a/dim(data)[1]*100
data$TD=as.factor(data$TD)
summary(data)
str(data)
data1=data[,-11] # Removed the duration variable (as per the suggestion on the site to
         # obtain realistic predictive model)
         # Since after the call the outcome of it would be known
data1$SI_no=1:nrow(data1) # Created a column of serial number
sum(is.na(data)) # Check for missing values
# To subset data randomly i.e. extract 5000 rows
# data2=data1[sample(1:nrow(data1), 5000, replace=FALSE),]
# But I am creating a new file of 55% no and 45% yes in 5000 random subset
set.seed(1)
data_TD_no=subset(data1, TD=="no") # obtain all TD=no rows
data TD yes=subset(data1, TD=="yes") # obtain all TD=yes rows
data2_TD_no=data_TD_no[sample(1:nrow(data_TD_no), 2750, replace=FALSE),] # 3500 random values of
TD=no
data2_TD_yes=data_TD_yes[sample(1:nrow(data_TD_yes), 2250, replace=FALSE),] # 1500 random values
of TD=ves
data2=rbind(data2_TD_no, data2_TD_yes) # concatenated the two dataframes to get 1 dataframe
                     # This data frame will kind of constitue our entire dataset.
a=length(which(data2$TD == "yes")) # Cross checking out the proportion of the response
yes.percentage=a/dim(data2)[1]*100
data2=data2[sample(nrow(data2)),] # Randomly shuffled the rows of the dataframe
data3=data1[!(data1$SI_no %in% data2$SI_no),] # Data1-Data2 (All the rows we did not pick)
# Data: Original Dataset as I downloaded
# Data1: Here I have added the serial no column and removed the Duration column from Data
# Data2: I will work on this. Contains 55% no and 45% yes TD response. Randomly obtained from Data1
# Data3: All the rows of Data2 not included in Data1
write.csv(data1,file="E:/Data Mining- STAT 571/Data1.csv") # save the data files
write.csv(data2,file="E:/Data Mining- STAT 571/Data2.csv")
write.csv(data3,file="E:/Data Mining- STAT 571/Data3.csv")
```

```
data.cleaned=read.csv("Data2.csv",header=T) # read Data2 that I will be using
data.cleaned$TD=as.factor(data.cleaned$TD) # generate levels for categorical variable
data.cleaned$TD = ifelse(data.cleaned$TD=="yes", 1, 0) # add new comun of 1 for TD=yes and for TD=no
a=length(which(data.cleaned\$TD == 1)) # Cross checking out the proportion of the response
yes.percentage=a/dim(data.cleaned)[1]*100
summary(data.cleaned)
str(data.cleaned)
data.cleaned=data.cleaned[-c(1,22)] # Dropped the unnecessary serial number columns
cor(data.cleaned[,unlist(lapply(data.cleaned, is.numeric))]) # correlation between
                          # numeric varaibles in the dataset
# Preliminary Visualization
require(ggplot2)
# pairs(data.cleaned[1:20], pch = 21)
# df.m = melt(data.cleaned, id.var = "TD")
# p <- ggplot(data = df.m, aes(x=variable, y=value))
# p <- p + geom_boxplot(aes(fill=TD))
#p <- p + facet wrap( ~ variable, scales="free", ncol=4)
# p <- p + xlab("x-axis") + ylab("y-axis") + ggtitle("Box-plots")
# p <- p + guides(fill=guide_legend(title="TD"))</pre>
# Now in this I divide the dataset into training data-80% and testing data-20%
data.cleaned=na.omit(data.cleaned)
set.seed(1) # set a random seed so that we will be able to reproduce the random sample
index.train=sample(dim(data.cleaned)[1], 4000) # Take a random sample of n=4000 from 1 to N=5000
data.cleaned.train=data.cleaned[index.train,] # Set the 1000 randomly chosen subjects as a training data
data.cleaned.test=data.cleaned[-index.train,] # The remaining subjects will be reserved for testing purposes.
dim(data.cleaned.train)
dim(data.cleaned.test)
# Model 1: Performing Logistic Regression with all variables.
fit1=glm(TD~., data.cleaned.train, family=binomial(logit))
summary(fit1)
chi.sq= 5512.4-4149.5 # get the Chi-square stat
pchisq(chi.sq, 1, lower.tail=FALSE) # p-value: from the likelihood Ratio test
anova(fit1, test="Chisq") # to test if the model is useful: null hypothesis is all (but the intercept) coeff's are 0
confint.default(fit1) # obtain the confidence level of the coefficient of
            # the variables in this model.
```

The chi-square distribution

```
par(mfrow=c(2,1))
hist(rchisq(4000, 2), freq=FALSE, breaks=20)
hist(rchisq(4000, 20), freq=FALSE, breaks=20)
# When DF is getting larger, Chi-Squared dis is approx. normal
#prediction on training data
fit1.pred.train=rep("0", 4000) # prediction step 1
fit1.pred.train[fit1$fitted > 0.9]="1" # prediction step 2 to get a classifier
fit1.pred.train=as.factor(fit1.pred.train)
cm.train=table(fit1.pred.train, data.cleaned.train$TD)
#Training error
fit1.mce.train=mean(fit1.pred.train != data.cleaned.train$TD)
#prediction on test data
fit1.predict=predict(fit1, data.cleaned.test, type="response", interval="confidence", se.fit=T)
fit1.pred.test=rep("0", 1000) # prediction step 1
fit1.pred.test[fit1.predict$fit > 0.9]="1" # prediction step 2 to get a classifier
fit1.pred.test=as.factor(fit1.pred.test)
data.frame(data.cleaned.test$TD, fit1.pred.test) # put observed y and predicted y's together
cm=table(fit1.pred.test, data.cleaned.test$TD)
confusionMatrix(data=fit1.pred.test, data.cleaned.test$TD)
#Testing error
fit1.mce.test=mean(fit1.pred.test != data.cleaned.test$TD)
sensitivity=cm[2,2]/sum(data.cleaned.test$TD =="1")
specificity=cm[1,1]/ sum(data.cleaned.test$TD == "0")
false.positive=cm[2,1]/sum(data.cleaned.test$TD == "0")
#ROC Curve
fit1.roc=roc(data.cleaned.train$TD, fit1$fitted, plot=T, col="blue")
names(fit1.roc)
auc(fit1.roc)
##### False Positive vs. Sensitivity curve is called ROC
plot(1-fit1.roc$specificities, fit1.roc$sensitivities, col="red", pch=16,
   xlab="False Positive",
   ylab="Sensitivity")
#### Given a False positive rate, locate the prob threshold
plot(1-fit1.roc$specificities, fit1.roc$thresholds, col="green", pch=16,
   xlab="False Positive",
   ylab="Threshold on prob")
# Tried to plot classifier boundary, but due to high dimension its hard!. Visualization
# would be hard.
```

#Model 2:Done regsubset generation to obtain 8 variables and logistic model fit #Exhaustive search

```
fit2.exh=regsubsets(data.cleaned.train$TD~.,data.cleaned.train,
                                                                                   method="exhaustive",
                                                                    nvmax=8,
really.big=T)
fit2.e=summary(fit2.exh)
fit2.e$bic
par(mfrow=c(2,1)) # Compare different criterions: as expected rsq ^ when p is larger
plot(fit2.e$rsq, xlab="Number of predictors", ylab="rsq", col="red", type="p", pch=16)
plot(fit2.e$rss, xlab="Number of predictors", ylab="rss", col="blue", type="p", pch=16)
coef(fit2.exh,8)
par(mfrow=c(3,1))
plot(fit2.e$cp, xlab="Number of predictors",
   ylab="cp", col="red", type="p", pch=16)
plot(fit2.e$bic, xlab="Number of predictors",
   ylab="bic", col="blue", type="p", pch=16)
plot(fit2.e$adjr2, xlab="Number of predictors",
   ylab="adjr2", col="green", type="p", pch=16)
Reg.var=rownames(as.matrix(coef(fit2.exh,8))) # variables chosen
fit2.1=qlm(TD~month+poutcome+emp.var.rate+cons.price.idx #Building a logistic regression model
     +loan, data.cleaned.train, family=binomial(logit))
summary(fit2.1)
anova(fit1,fit2.1) # Compare Model 1 and Model 2.1
# Forward selection
fit2.for=regsubsets(data.cleaned.train$TD~.,data.cleaned.train, nvmax=8, method="forward", really.big=T)
fit2.f=summary(fit2.for)
fit2.f$cp
coef(fit2.for,8)
Reg.var=rownames(as.matrix(coef(fit2.for,8)))
fit2.2=glm(TD~month+poutcome+emp.var.rate+cons.price.idx
                                                                #Building a logistic regression model
      +loan, data.cleaned.train, family=binomial(logit))
summary(fit2.2)
# Backward Selection
fit2.bac=regsubsets(data.cleaned.train$TD~.,data.cleaned.train,
                                                                                    method="backward",
                                                                    nvmax=8,
really.big=T)
fit2.b=summary(fit2.bac)
fit2.b$rsq
coef(fit2.bac,8)
Reg.var=rownames(as.matrix(coef(fit2.bac,8)))
```

```
fit2.3=glm(TD~month+poutcome+emp.var.rate+cons.price.idx
                                                                  #Building a logistic regression model
      +loan, data.cleaned.train, family=binomial(logit))
summary(fit2.3)
fit2=fit2.3
par(mfrow=c(2,1))
plot(fit2,1)
plot(fit2,2)
chi.sq= 5512.4-4226.9 # get the Chi-square stat
pchisq(chi.sq, 1, lower.tail=FALSE) # p-value: from the likelihood Ratio test
anova(fit2, test="Chisq") # to test if the model is useful: null hypothesis is all (but the intercept) coeff's are 0
#prediction on training data
fit2.pred.train=rep("0", 4000) # prediction step 1
fit2.pred.train[fit1$fitted > 0.9]="1" # prediction step 2 to get a classifier
fit2.pred.train=as.factor(fit2.pred.train)
cm.train=table(fit2.pred.train, data.cleaned.train$TD)
#Training error
fit2.mce.train=mean(fit2.pred.train != data.cleaned.train$TD)
#prediction on test data
fit2.predict=predict(fit2, data.cleaned.test, type="response", interval="confidence", se.fit=T)
fit2.pred.test=rep("0", 1000) # prediction step 1
fit2.pred.test[fit2.predict$fit > 0.9]="1" # prediction step 2 to get a classifier
fit2.pred.test=as.factor(fit2.pred.test)
data.frame(data.cleaned.test$TD, fit2.pred.test) # put observed y and predicted y's together
cm=table(fit2.pred.test, data.cleaned.test$TD)
confusionMatrix(data=fit2.pred.test, data.cleaned.test$TD)
#Testing error
fit2.mce.test=mean(fit2.pred.test != data.cleaned.test$TD)
sensitivity=cm[2,2]/sum(data.cleaned.test$TD =="1")
specificity=cm[1,1]/ sum(data.cleaned.test$TD == "0")
false.positive=cm[2,1]/sum(data.cleaned.test$TD == "0")
#ROC Curve
fit2.roc=roc(data.cleaned.train$TD, fit2$fitted, plot=T, col="blue")
names(fit2.roc)
auc(fit2.roc)
##### False Positive vs. Sensitivity curve is called ROC
plot(1-fit2.roc$specificities, fit2.roc$sensitivities, col="red", pch=16,
   xlab="False Positive",
   ylab="Sensitivity")
#### Given a False positive rate, locate the prob threshold
plot(1-fit2.roc$specificities, fit2.roc$thresholds, col="green", pch=16,
   xlab="False Positive",
   ylab="Threshold on prob")
```

```
# Model3: Using Regularization Techniques
X.fl=model.matrix(~., data.cleaned.train) # put data.frame into a matrix
colnames(X.fl)
Y=X.fl[, 53] # extract y
X.fl=X.fl[, -c(53)]
fit3.lambda=cv.glmnet(X.fl, Y, alpha=1,nfolds=10)
names(fit3.lambda)
plot(fit3.lambda)
plot(fit3.lambda$lambda)
meancverror=fit3.lambda$cvm
                                       # the mean cv error
plot(fit3.lambda$lambda, fit3.lambda$cvm, xlab="lambda", ylab="mean cv errors")
fit3.lambda$lambda.min
                             # min lambda changes a lot as a function of nfolds!
nonzeros=fit3.lambda$nzero
plot(fit3.lambda$lambda, fit3.lambda$nzero, xlab="lambda", ylab="number of non-zeros")
#output beta's from lambda.1se (this way we use smaller set of variables.)
coef.1se=coef(fit3.lambda, s="lambda.1se")
coef.1se=coef.1se[which(coef.1se !=0),]
pvariables=rownames(as.matrix(coef.1se))
# Fit the model
glm.input=as.formula(paste("TD", "\sim", paste(pvariables[-1], collapse = "+"))) # formula
fit3=glm(TD\sim job+default+contact+month+campaign+poutcome+emp.var.rate
     +nr.employed, data=data.cleaned.train)
summary(fit3)
anova(fit1,fit3)
anova(fit2,fit3)
chi.sq= 991.81-702.35 # get the Chi-square stat
pchisq(chi.sq, 1, lower.tail=FALSE) # p-value: from the likelihood Ratio test
anova(fit3, test="Chisq") # to test if the model is useful: null hypothesis is all (but the intercept) coeff's are 0
#prediction on training data
fit3.pred.train=rep("0", 4000) # prediction step 1
fit3.pred.train[fit1$fitted > 0.9]="1" # prediction step 2 to get a classifier
fit3.pred.train=as.factor(fit3.pred.train)
cm.train=table(fit3.pred.train, data.cleaned.train$TD)
```

Tried to plot classifier boundary, but due to high dimension its hard!. Visualization

would be hard.

#Training error

```
fit3.mce.train=mean(fit3.pred.train != data.cleaned.train$TD)
#prediction on test data
fit3.predict=predict(fit3, data.cleaned.test, type="response", interval="confidence", se.fit=T)
fit3.pred.test=rep("0", 1000) # prediction step 1
fit3.pred.test[fit3.predict$fit > 0.9]="1" # prediction step 2 to get a classifier
fit3.pred.test=as.factor(fit3.pred.test)
data.frame(data.cleaned.test$TD, fit3.pred.test) # put observed y and predicted y's together
cm=table(fit3.pred.test, data.cleaned.test$TD)
confusionMatrix(data=fit3.pred.test, data.cleaned.test$TD)
#Testing error
fit3.mce.test=mean(fit3.pred.test != data.cleaned.test$TD)
sensitivity=cm[2,2]/sum(data.cleaned.test$TD =="1")
specificity=cm[1,1]/ sum(data.cleaned.test$TD == "0")
false.positive=cm[2,1]/sum(data.cleaned.test$TD == "0")
#ROC Curve
fit3.roc=roc(data.cleaned.train$TD, fit3$fitted, plot=T, col="blue")
names(fit3.roc)
auc(fit3.roc)
##### False Positive vs. Sensitivity curve is called ROC
plot(1-fit3.roc$specificities, fit3.roc$sensitivities, col="red", pch=16,
   xlab="False Positive",
   ylab="Sensitivity")
#### Given a False positive rate, locate the prob threshold
plot(1-fit3.roc$specificities, fit3.roc$thresholds, col="green", pch=16,
   xlab="False Positive",
   ylab="Threshold on prob")
# Tried to plot classifier boundary, but due to high dimension its hard!. Visualization
# would be hard.
# Model 4: Cross Validation on training set of Model 1
ctrl <- trainControl(method = "repeatedcv", number = 10, savePredictions = TRUE)
fit4 <- train(TD ~.,data=data.cleaned.train, method="glm", family="binomial",
          trControl = ctrl, tuneLength = 5) # Fit the model
summary(fit4)
pred = predict(fit4, data.cleaned.test) # predict on the testing data set
```

```
# try=rep("0", 1000) # prediction step 1
# try[pred > 0.9]="1" # prediction step 2 to get a classifier
# try=as.factor(try)
# data.frame(data.cleaned.test$TD, try) # put observed y and predicted y's together
# cm=table(try, data.cleaned.test$TD)
# confusionMatrix(data=try, data.cleaned.test$TD)
# try.mce=mean(try != data.cleaned.test$TD)
abc=prediction(pred,data.cleaned.test$TD)
AUC = as.numeric(performance(abc, "auc")@y.values)
ACC= performance(abc, "acc")
mean(ACC@y.values[[1]])
plot(performance(abc, 'tpr', 'fpr'))
plot(ACC)
Sensitivity= performance(abc, "sens")
mean(Sensitivity@y.values[[1]])
Specificity= performance(abc, "spec")
mean(Specificity@y.values[[1]])
# Model 5: Cross Validation on training set of Model 2
ctrl <- trainControl(method = "repeatedcv", number = 10, savePredictions = TRUE)
fit5 <- train(TD ~month+poutcome+emp.var.rate+cons.price.idx+loan,
        data=data.cleaned.train, method="glm", family="binomial",
        trControl = ctrl, tuneLength = 5) # Fit the model
summary(fit5)
pred = predict(fit5, data.cleaned.test) # predict on the testing data set
abc=prediction(pred,data.cleaned.test$TD)
AUC = as.numeric(performance(abc, "auc")@y.values)
ACC= performance(abc, "acc")
max(ACC@y.values[[1]])
plot(performance(abc, 'tpr', 'fpr'))
plot(ACC)
Sensitivity= performance(abc, "sens")
mean(Sensitivity@y.values[[1]])
Specificity= performance(abc, "spec")
mean(Specificity@y.values[[1]])
```

```
# Model 6: Cross Validation on training set of Model 3
ctrl <- trainControl(method = "repeatedcv", number = 10, savePredictions = TRUE)
fit6 <- train(TD ~job+default+contact+month+campaign+poutcome+emp.var.rate
          +nr.employed, data=data.cleaned.train, method="glm", family="binomial",
          trControl = ctrl, tuneLength = 5) # Fit the model
summary(fit6)
pred = predict(fit6, data.cleaned.test) # predict on the testing data set
abc=prediction(pred,data.cleaned.test$TD)
AUC = as.numeric(performance(abc, "auc")@y.values)
ACC= performance(abc, "acc")
max(ACC@y.values[[1]])
plot(performance(abc, 'tpr', 'fpr'))
plot(ACC)
Sensitivity= performance(abc, "sens")
mean(Sensitivity@y.values[[1]])
Specificity= performance(abc, "spec")
mean(Specificity@y.values[[1]])
# Model 7: LDA on all variables
fit7 <- Ida(data.cleaned.train$TD ~., data=data.cleaned.train) # fit the Ida model
plda <- predict(object = fit7,newdata = data.cleaned.test) #predict on test data</pre>
summary(fit7)
plda.class.1=predict(fit7, data.cleaned.test)$class # gives the class of the test data
plda.class.train.1=predict(fit7, data.cleaned.train)$class # gives the class of the train data
# create a histogram of the discriminant function values
Idahist(data = plda$x[,1], g=data.cleaned.test$TD)
# create a scatterplot of the discriminant function values
plot(plda$x[,1], type="n", ylab=c("LDA Axis 1"))
text(plda$x[,1], row.names(data.cleaned.test), col=c(as.numeric(data.cleaned.test$TD)+10))
# Compute the misclasification error of the model
ct <- table(data.cleaned.test$TD, plda$class)
```

```
(ct[1,1]+ct[2,2])/sum(ct)
```

```
# Model 8: LDA on variables otained from regsubsets
fit8 <- Ida(data.cleaned.train$TD ~ month+poutcome+emp.var.rate+cons.price.idx
       +loan, data=data.cleaned.train) # fit the lda model
plda <- predict(object = fit8,newdata = data.cleaned.test) #predict on test data</pre>
summary(fit8)
plda.class.2=predict(fit8,data.cleaned.test)$class # gives the class of the test data
plda.class.train.2=predict(fit8,data.cleaned.train)$class # gives the class of the train data
# create a histogram of the discriminant function values
Idahist(data = plda$x[,1], g=data.cleaned.test$TD)
# create a scatterplot of the discriminant function values
plot(plda$x[,1], type="n", ylab=c("LDA Axis 1"))
text(p|da$x[,1], row.names(data.cleaned.test), col=c(as.numeric(data.cleaned.test$TD)+10))
# Compute the misclasification error of the model
ct <- table(data.cleaned.test$TD, plda$class)
(ct[1,1]+ct[2,2])/sum(ct)
# Model 9: LDA on variables obtained from LASSO
fit9 <- Ida(data.cleaned.train$TD ~job+default+contact+month+campaign+poutcome+emp.var.rate
       +nr.employed, data=data.cleaned.train) # fit the Ida model
plda <- predict(object = fit9,newdata = data.cleaned.test) #predict on test data</pre>
summary(fit7)
plda.class.3=predict(fit9, data.cleaned.test)$class # gives the class of the test data
plda.class.train.3=predict(fit9, data.cleaned.train)$class # gives the class of the train data
# create a histogram of the discriminant function values
Idahist(data = pIda$x[,1], g=data.cleaned.test$TD)
# create a scatterplot of the discriminant function values
plot(plda$x[,1], type="n", ylab=c("LDA Axis 1"))
text(plda$x[,1], row.names(data.cleaned.test), col=c(as.numeric(data.cleaned.test$TD)+10))
```

```
# Compute the misclasification error of the model ct <- table(data.cleaned.test$TD, plda$class) (ct[1,1]+ct[2,2])/sum(ct)
```

```
# Model 10: Random Forest on all variables
fit10.1= tree(TD~., data=data.cleaned.train)
plot(fit10.1)
text(fit10.1, pretty=0)
fit10.1$frame
fit10.1.result=summary(fit10.1)
fit10.1.result$dev
\#xyz=summary(gIm(TD^nr.employed+euribor3m+month,data.cleaned.train, family=binomial(logit)))
#names(xyz)
#RSS.LogReg=(4000-4)*((xyz)$deviance)^2
fit.tree=rpart(TD~., data.cleaned.train)
fancyRpartPlot(fit.tree) # The plot shows the split together with more information
fit.tree$frame
# Split on gini
fit10.1.gini=tree(TD~., data.cleaned.train, split="gini")
plot(fit10.1.gini)
text(fit10.1.gini, pretty=TRUE) # plot the labels
fit10.1.gini$frame
summary(fit10.1.gini)$dev
#Bootstrap
RSS=0 #initial values
n.unique=0
n=nrow(data.cleaned.train)
for (i in 1:100)
 index1=sample(n, n, replace=TRUE)
 Sample1=data.cleaned.train[index1, ] # Take a bootstrap sample
 fit1.boot=tree(TD~., Sample1) # Get a tree fit
 plot(fit1.boot,
    title="Trees with a Bootstrap sample")
 text(fit1.boot, pretty=0)
 RSS[i]=summary(fit1.boot)$dev # output RSS for each bootstrap tree
 n.unique[i]=length(unique(index1))
 Sys.sleep(2)
                          # Pause for 2 seconds before running for next round
hist(RSS, breaks=30,
```

```
col="blue",
   main="RSS from different Bootstrap trees")
hist(n.unique, breaks=30,
   col="red",
   main="number of unique subjects included in each Bootstrap sample")
hist(n-n.unique, breaks=30,
   col="green",
   main="number of OOB subjects not included in each Bootstrap sample")
#Random Forest
rf.error.p=1:19
for (p in 1:19)
{
 fit.rf=randomForest(TD~., data.cleaned.train, mtry=p, ntree=100)
 rf.error.p[p]=fit.rf$mse[100]
rf.error.p
plot(1:19, rf.error.p, pch=16,
   xlab="mtry",
   ylab="mse of mtry")
# For a fixed mtry= 4
fit10.2=randomForest(TD~., data.cleaned.train, mtry=4, ntree=100)
str(fit10.2)
plot(fit10.2)
summary(fit10.2)
plot(fit10.2$mse, xlab="number of trees",
   ylab="ave mse of the 100 trees",
   pch=16)
# oob times for each obs'n
fit10.2$oob.times # Out of bags for each observation.
hist(fit10.2$oob.times)
trainingerror=mean((fit10.2$y-fit10.2$predicted)^2) # this will output the oob errors
pred1=predict(fit10.2, data.cleaned.test) # make predictions on the test data
pred1.train=predict(fit10.2, data.cleaned.train) # predictions on trained data
try1=rep("0", 1000)
try1[pred1 > 0.9]="1"
try1=as.factor(try1)
data.frame(data.cleaned.test$TD, try1) # put observed y and predicted y's together
cm=table(try1, data.cleaned.test$TD)
confusionMatrix(data=try1, data.cleaned.test$TD)
try1.mce=mean(try1 != data.cleaned.test$TD)
try1.train=rep("0", 4000)
try1.train[pred1.train > 0.9] = "1"
```

```
abc=prediction(pred1,data.cleaned.test$TD)
AUC = as.numeric(performance(abc, "auc")@y.values)
ACC= performance(abc, "acc")
mean(ACC@y.values[[1]])
plot(performance(abc, 'tpr', 'fpr'))
plot(ACC)
Sensitivity= performance(abc, "sens")
mean(Sensitivity@y.values[[1]])
Specificity= performance(abc, "spec")
mean(Specificity@y.values[[1]])
# Model 11: Random Forest on variables obtained from Regsubsets
fit11.1= tree(TD~month+poutcome+emp.var.rate+cons.price.idx
       +loan, data=data.cleaned.train)
plot(fit11.1)
text(fit11.1, pretty=0)
fit11.1$frame
fit11.1.result=summary(fit11.1)
fit11.1.result$dev
fit.tree=rpart(TD~month+poutcome+emp.var.rate+cons.price.idx
        +loan, data.cleaned.train)
fancyRpartPlot(fit.tree) # The plot shows the split together with more information
fit.tree$frame
# Split on gini
fit11.1.gini=tree(TD~month+poutcome+emp.var.rate+cons.price.idx
          +loan, data.cleaned.train, split="gini")
plot(fit11.1.gini)
text(fit11.1.gini, pretty=TRUE) # plot the labels
fit11.1.gini$frame
summary(fit11.1.gini)$dev
#Bootstrap
RSS=0 # initial values
n.unique=0
n=nrow(data.cleaned.train)
for (i in 1:100)
{
```

try1.train=as.factor(try1.train)

```
index1=sample(n, n, replace=TRUE)
 Sample1=data.cleaned.train[index1, ] # Take a bootstrap sample
 fit1.boot=tree(TD~month+poutcome+emp.var.rate+cons.price.idx
         +loan, Sample1) # Get a tree fit
 plot(fit1.boot,
    title="Trees with a Bootstrap sample")
 text(fit1.boot, pretty=0)
 RSS[i]=summary(fit1.boot)$dev # output RSS for each bootstrap tree
 n.unique[i]=length(unique(index1))
 Sys.sleep(2)
                         # Pause for 2 seconds before running for next round
hist(RSS, breaks=30,
   col="blue",
   main="RSS from different Bootstrap trees")
hist(n.unique, breaks=30,
   col="red",
   main="number of unique subjects included in each Bootstrap sample")
hist(n-n.unique, breaks=30,
   col="green",
   main="number of OOB subjects not included in each Bootstrap sample")
#Random Forest
rf.error.p=1:4
for (p in 1:4)
 fit.rf=randomForest(TD~month+poutcome+emp.var.rate+cons.price.idx
            +loan, data.cleaned.train, mtry=p, ntree=500)
 rf.error.p[p]=fit.rf$mse[500]
rf.error.p
plot(1:4, rf.error.p, pch=16,
   xlab="mtry",
   ylab="mse of mtry")
# For a fixed mtry= 2
fit11=randomForest(TD~month+poutcome+emp.var.rate+cons.price.idx
          +loan, data.cleaned.train, mtry=2, ntree=500)
str(fit11)
plot(fit11)
summary(fit11)
plot(fit11$mse, xlab="number of trees",
   ylab="ave mse of the 500 trees",
   pch=16)
# oob times for each obs'n
fit11$00b.times # Out of bags for each observation.
hist(fit11$00b.times)
```

```
trainingerror=mean((fit11$y-fit11$predicted)^2) # this will output the oob errors
pred2=predict(fit11, data.cleaned.test) # make predictions on the test data
pred2.train=predict(fit11, data.cleaned.train) # make predictions on the train data
try2=rep("0", 1000)
try2[pred2 > 0.9] = "1"
try2=as.factor(try2)
data.frame(data.cleaned.test$TD, try2) # put observed y and predicted y's together
cm=table(try2, data.cleaned.test$TD)
confusionMatrix(data=try2, data.cleaned.test$TD)
try2.mce=mean(try2 != data.cleaned.test$TD)
try2.train=rep("0", 4000)
try2.train[pred2.train > 0.9] = "1"
try2.train=as.factor(try2.train)
abc=prediction(pred2,data.cleaned.test$TD)
AUC = as.numeric(performance(abc, "auc")@y.values)
ACC= performance(abc, "acc")
mean(ACC@y.values[[1]])
max(ACC@y.values[[1]])
plot(performance(abc, 'tpr', 'fpr'))
plot(ACC)
Sensitivity= performance(abc, "sens")
mean(Sensitivity@y.values[[1]])
Specificity= performance(abc, "spec")
mean(Specificity@y.values[[1]])
# Model 12: Random Forest on variables obtained from LASSO
fit12.1= tree(TD~job+default+contact+month+campaign+poutcome+emp.var.rate
       +nr.employed, data=data.cleaned.train)
plot(fit12.1)
text(fit12.1, pretty=0)
fit12.1$frame
fit12.1.result=summary(fit12.1)
fit12.1.result$dev
fit.tree=rpart(TD~job+default+contact+month+campaign+poutcome+emp.var.rate
        +nr.employed, data.cleaned.train)
fancyRpartPlot(fit.tree) # The plot shows the split together with more information
```

fit.tree\$frame

```
# Split on gini
fit12.1.gini=tree(TD~job+default+contact+month+campaign+poutcome+emp.var.rate
          +nr.employed, data.cleaned.train, split="gini")
plot(fit12.1.gini)
text(fit12.1.gini, pretty=TRUE) # plot the labels
fit12.1.qini$frame
summary(fit12.1.gini)$dev
#Bootstrap
RSS=0 # initial values
n.unique=0
n=nrow(data.cleaned.train)
for (i in 1:100)
{
 index1=sample(n, n, replace=TRUE)
 Sample1=data.cleaned.train[index1, ] # Take a bootstrap sample
 fit1.boot=tree(TD\sim job+default+contact+month+campaign+poutcome+emp.var.rate)
         +nr.employed, Sample1) # Get a tree fit
 plot(fit1.boot,
    title="Trees with a Bootstrap sample")
 text(fit1.boot, pretty=0)
 RSS[i]=summary(fit1.boot)$dev # output RSS for each bootstrap tree
 n.unique[i]=length(unique(index1))
                          # Pause for 2 seconds before running for next round
 Sys.sleep(2)
}
hist(RSS, breaks=30,
   col="blue",
   main="RSS from different Bootstrap trees")
hist(n.unique, breaks=30,
   col="red",
   main="number of unique subjects included in each Bootstrap sample")
hist(n-n.unique, breaks=30,
   col="green",
   main="number of OOB subjects not included in each Bootstrap sample")
#Random Forest
rf.error.p=1:7
for (p in 1:7)
 fit.rf = random Forest (TD ``job + default + contact + month + campaign + poutcome + emp.var.rate) \\
            +nr.employed, data.cleaned.train, mtry=p, ntree=500)
 rf.error.p[p]=fit.rf$mse[500]
}
rf.error.p
plot(1:7, rf.error.p, pch=16,
   xlab="mtry",
   ylab="mse of mtry")
```

```
# For a fixed mtry= 3
fit12=randomForest(TD~job+default+contact+month+campaign+poutcome+emp.var.rate
            +nr.employed, data.cleaned.train, mtry=3, ntree=500)
str(fit12)
plot(fit12)
summary(fit12)
plot(fit12$mse, xlab="number of trees",
   ylab="ave mse of the 500 trees",
   pch=16)
# oob times for each obs'n
fit12$00b.times # Out of bags for each observation.
hist(fit12$oob.times)
trainingerror=mean((fit12$y-fit12$predicted)^2) # this will output the oob errors
pred3=predict(fit12, data.cleaned.test) # make predictions on the test data
pred3.train=predict(fit12, data.cleaned.train) # make predictions on the train data
try3=rep("0", 1000)
try3[pred3 > 0.9]="1"
try3=as.factor(try3)
data.frame(data.cleaned.test$TD, try3) # put observed y and predicted y's together
cm=table(try3, data.cleaned.test$TD)
confusionMatrix(data=try3, data.cleaned.test$TD)
try3.mce=mean(try3 != data.cleaned.test$TD)
try3.train=rep("0", 4000)
try3.train[pred3.train > 0.9] = "1"
try3.train=as.factor(try3.train)
abc=prediction(pred3,data.cleaned.test$TD)
AUC = as.numeric(performance(abc, "auc")@y.values)
ACC= performance(abc, "acc")
max(ACC@y.values[[1]])
plot(performance(abc, 'tpr', 'fpr'))
plot(ACC)
Sensitivity= performance(abc, "sens")
mean(Sensitivity@y.values[[1]])
Specificity= performance(abc, "spec")
mean(Specificity@y.values[[1]])
```

```
df1.1=data.frame(fit1.pred.train)
colnames(df1.1)="TD.Label.Predicted1"
#Model2
df2.1=data.frame(fit2.pred.train)
colnames(df2.1)="TD.Label.Predicted2"
#Model3
df3.1=data.frame(fit3.pred.train)
colnames(df3.1)="TD.Label.Predicted3"
#Model7
df7.1=data.frame(plda.class.train.1)
colnames(df7.1)="TD.Label.Predicted7"
#Model8
df8.1=data.frame(plda.class.train.2)
colnames(df8.1)="TD.Label.Predicted8"
#Model9
df9.1=data.frame(plda.class.train.3)
colnames(df9.1)="TD.Label.Predicted9"
#Model10
df10.1=data.frame(try1.train)
colnames(df10.1)="TD.Label.Predicted10"
#Model11
df11.1=data.frame(try2.train)
colnames(df11.1)="TD.Label.Predicted11"
#Model12
df12.1=data.frame(try3.train)
colnames(df12.1)="TD.Label.Predicted12"
# combine all the dataframes
df.predictions=cbind(df1.1, df2.1, df3.1, df7.1, df8.1, df9.1, df10.1, df11.1, df12.1)
str(df.predictions)
# convert the dataframe to numeric type
indx <- sapply(df.predictions, is.factor)</pre>
df.predictions[indx] <- lapply(df.predictions[indx], function(x) as.numeric(as.character(x)))
#get mean value of predictions
df.predictions.mean=data.frame(Mean.Prediction=rowMeans(df.predictions))
# Final Classifier By Equal Weights
try.final1=rep("0", 4000)
try.final1[df.predictions.mean > 0.5]="1"
try.final1=as.factor(try.final1)
data.frame(data.cleaned.train$TD, try.final1) # put observed y and predicted y's together
cm=table(try.final1, data.cleaned.train$TD)
confusionMatrix(data=try.final1, data.cleaned.train$TD)
try.final1.mce=mean(try.final1 != data.cleaned.train$TD)
# Linear Regression
df.main=data.frame(data.cleaned.train$TD, df.predictions)
fitfinal1=lm(data.cleaned.train.TD~., data=df.main)
summary(fitfinal1)
fitfinal2=update(fitfinal1, .~. -TD.Label.Predicted2 -TD.Label.Predicted3) # Removed coorelated variables
```

#Model1

```
summary(fitfinal2)
```

```
# FINAL MODEL!!!!!!!!!!!!!!
# Random Forest
#Divide the dataset into training and testing
set.seed(1) # set a random seed so that we will be able to reproduce the random sample
index.train1=sample(dim(df.main)[1], 3500) # Take a random sample of n=3500 from 1 to N=4000
df.main.train=df.main[index.train1,] # Set the 500 randomly chosen subjects as a training data
df.main.test=df.main[-index.train1,]
# Fit a random forest tree
fit.tree123=randomForest(data.cleaned.train.TD~., df.main.train, mtry=3, ntree=500)
fit.tree1234=rpart(data.cleaned.train.TD~., df.main.train)
fancyRpartPlot(fit.tree1234) # The plot shows the split together with more information
fit.tree1234$frame
summary(fit.tree123)
plot(fit.tree123)
finaltree.pred=predict(fit.tree123, df.main.test)
try5=rep("0", 500)
try5[finaltree.pred > 0.5]="1"
try5=as.factor(try5)
data.frame(df.main.test$data.cleaned.train.TD, try5) # put observed y and predicted y's together
cm=table(try5, df.main.test$data.cleaned.train.TD)
confusionMatrix(data=try5, df.main.test$data.cleaned.train.TD)
try5.mce=mean(try5 != df.main.test$data.cleaned.train.TD)
abc1=prediction(finaltree.pred, df.main.test$data.cleaned.train.TD)
AUC1 = as.numeric(performance(abc1, "auc")@y.values)
ACC1= performance(abc1, "acc")
max(ACC1@y.values[[1]])
plot(performance(abc1, 'tpr', 'fpr'))
plot(ACC1)
Sensitivity= performance(abc1, "sens")
mean(Sensitivity@y.values[[1]])
Specificity= performance(abc1, "spec")
mean(Specificity@y.values[[1]])
```