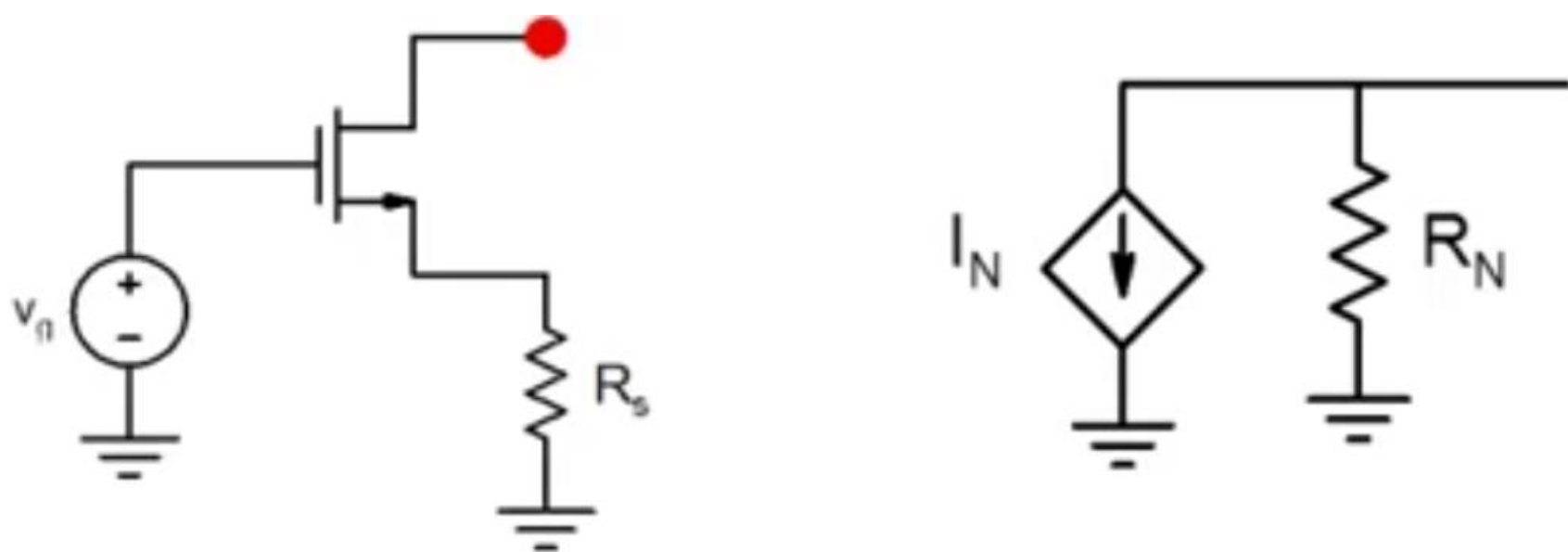


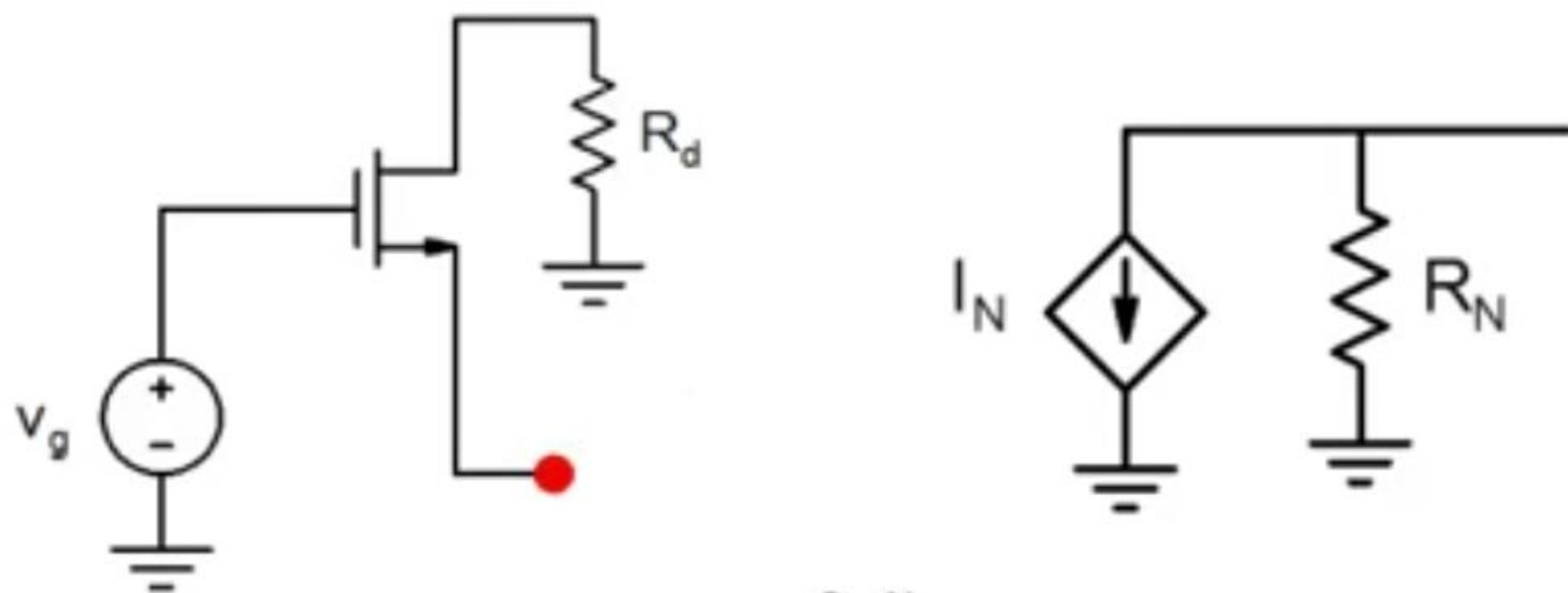
## Useful Results



$$i_n \cong \frac{g_m v_g}{1 + (g_m + g_{mb}) R_S}$$

$$R_n \cong r_o \times \{1 + (g_m + g_{mb}) R_S\}$$

## Useful Results



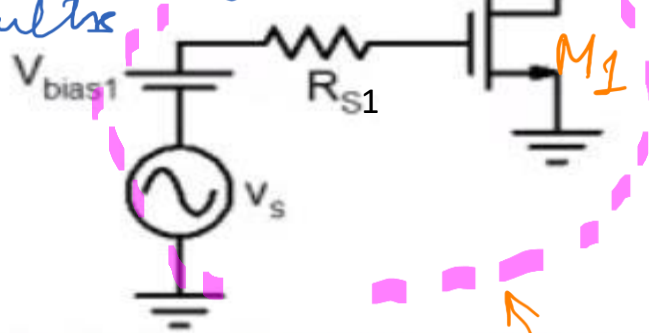
$$i_n = -\frac{g_m v_g}{1 + R_d / r_o}$$

$$R_n \cong \frac{1 + R_d / r_o}{g_m + g_{mb}}$$

# Cascode Amplifier

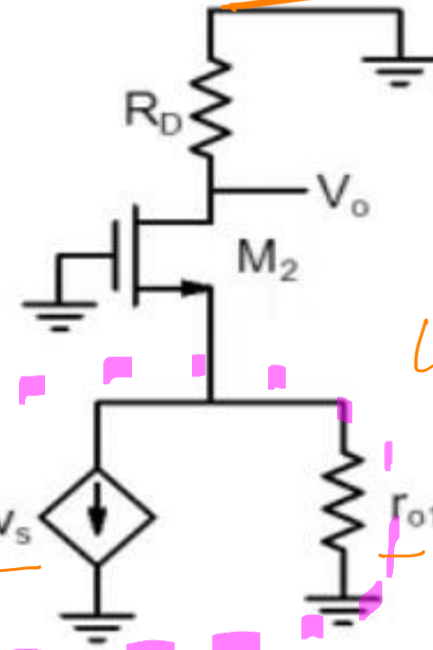
Method-1: Traditional way  $\rightarrow$  small-signal

Method-2: Use 2 useful Results



Let's calculate the Gain of this Amplifier

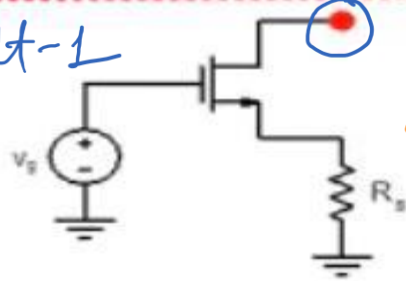
noy's eq



$$i_N \cong g_{m1} v_s$$

$$R_N \cong r_{o1}$$

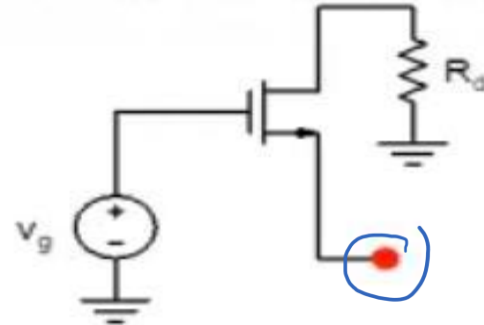
useful Result-1



$$i_n \cong \frac{g_m v_g}{1 + (g_m + g_{mb}) R_S}$$

$$R_n \cong r_o \times \{1 + (g_m + g_{mb}) R_S\}$$

useful Result-2



$$i_n = -\frac{g_m v_g}{1 + R_d / r_o} \quad R_n \cong \frac{1 + R_d / r_o}{g_m + g_{mb}}$$

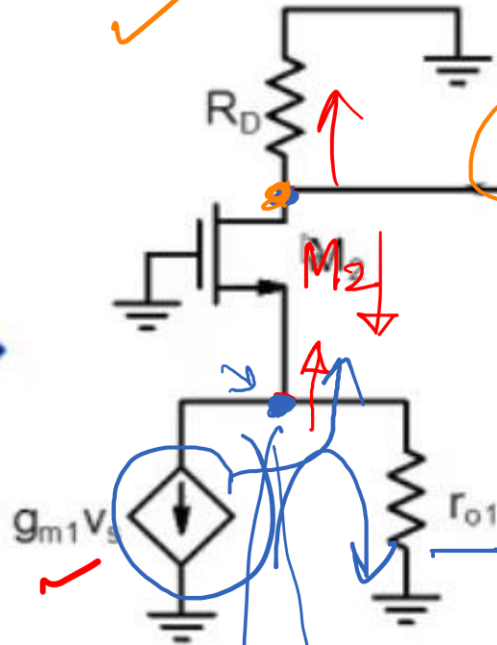
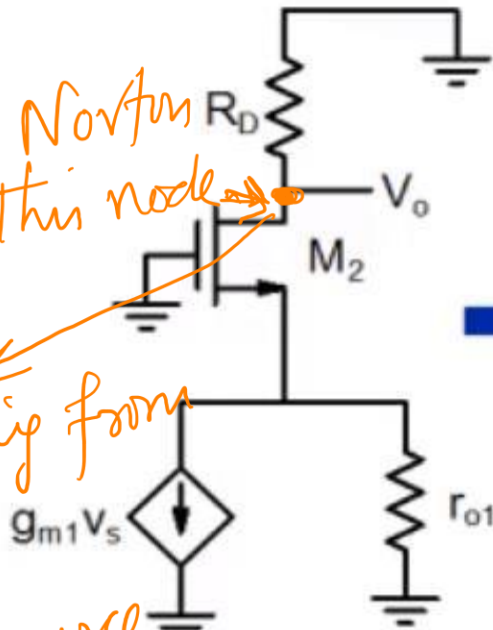
# Cascode Amplifier

Built Norton eq<sup>n</sup> at this node

The whole ckt looking from this node is a current source in parallel with  $R_{o1}$ .

$$i_n \cong \frac{g_m v_g}{1 + (g_m + g_{mb})R_S}$$

$$R_n \cong r_o \times \{1 + (g_m + g_{mb})R_S\}$$



now, Built Norton eq<sup>n</sup> at  $(V_o)$   
→ Find the Norton current →  $(I_N)$

gnd

→ Source of  $I_N$  is  $g_{m1} V_s$

$i_N \cong g_{m1} V_s$  → This current  $(g_{m1} V_s)$  has two choices

$$R_N = R_D \parallel r_{o2} (1 + (g_{m2} + g_{mb2})r_{o1}) \cong R_D$$

two choices  
→  $r_{o1}$   
→  $M_2$

flow into  $M_2$  and come out as  $I_N$

what is Resistance when we look into  $M_2$

$$i_n = -\frac{g_m v_g}{1 + R_d/r_o} \quad R_n \cong \frac{1 + R_d/r_o}{g_m + g_{mb}}$$

$$R_n \cong \frac{1}{g_{m2} + g_{mb2}}$$

→ Remember: The order of  $V_D$  and resistance looking into source  
 $\downarrow \approx M \Omega$   
 $\downarrow \approx k \Omega$

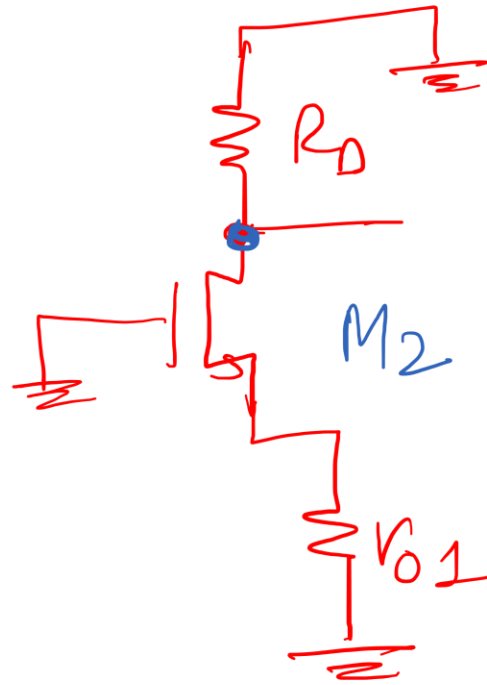
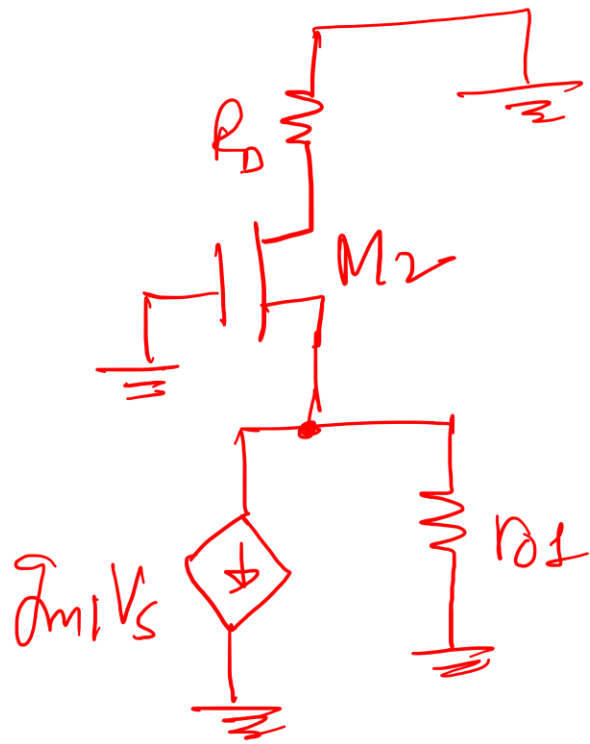
→ Therefore, the current will flow into  $M_2$

$$i_N \approx g_{m1} V_S$$

→ Now, let's find the Norton resistance at that node  
• Forget the ground

→ Resistance looking up  $\rightarrow R_D$

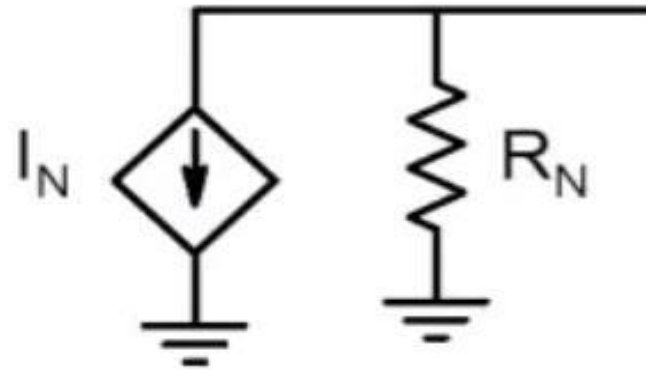
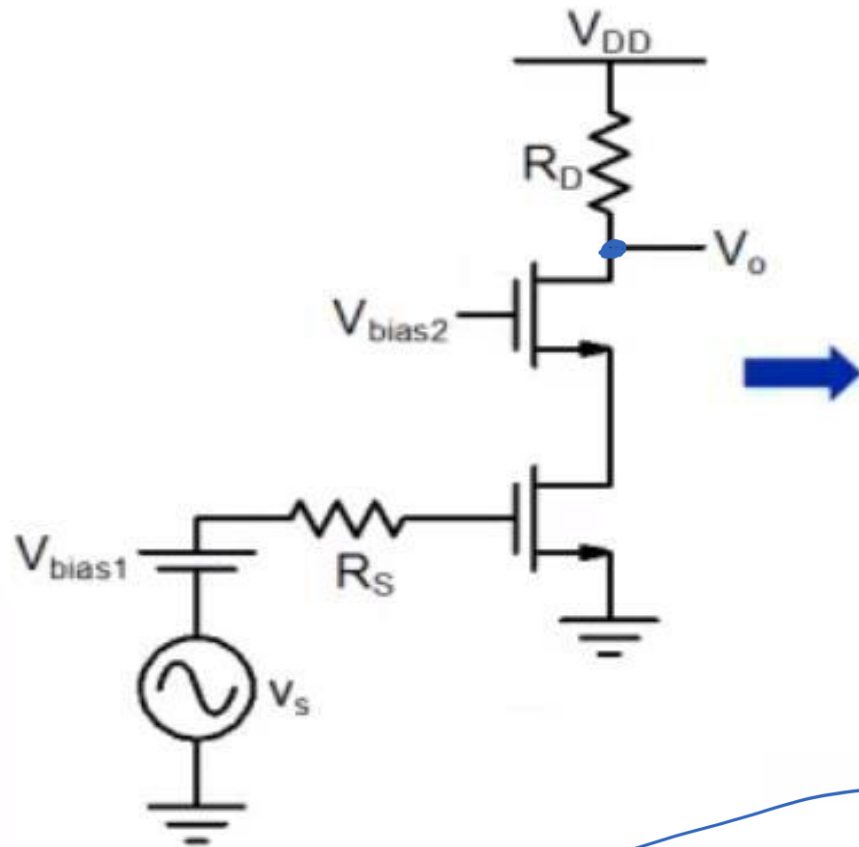
→ Resistance looking down  $\rightarrow$  short all sources



$$R_N \stackrel{\text{is}}{=} R_D \parallel \check{r}_{o2} (1 + (g_{m2} + g_{mb2}) \check{r}_{o1})$$

$$R_N \stackrel{\text{is}}{=} R_D$$

## Cascode Amplifier



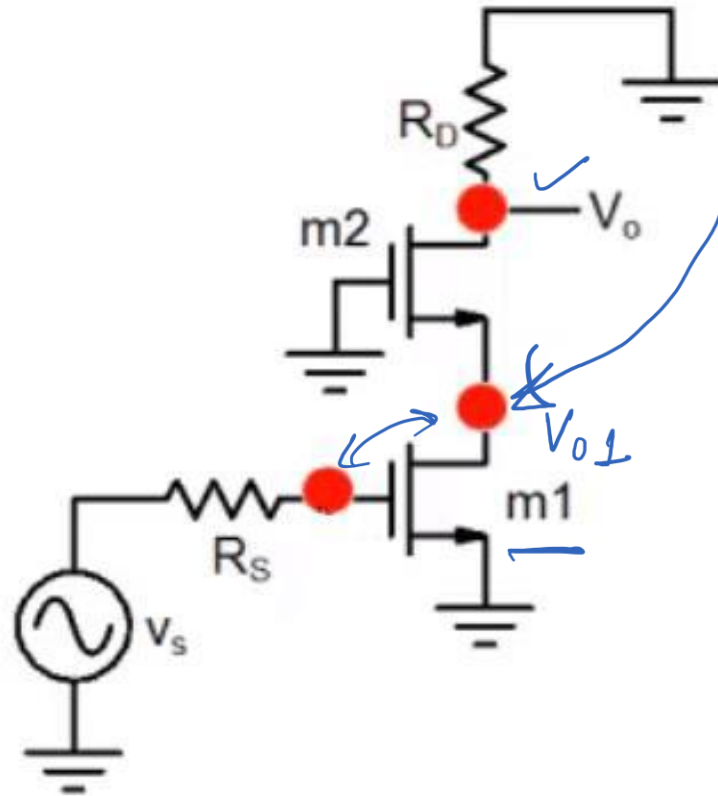
$$i_N \cong g_{m1} v_s$$

$$R_N \cong R_D$$

$\frac{v_o}{v_s} \cong -g_{m1} R_D$   
 $A_V \cong -g_{m1} R_D$  just like a CS amplifier

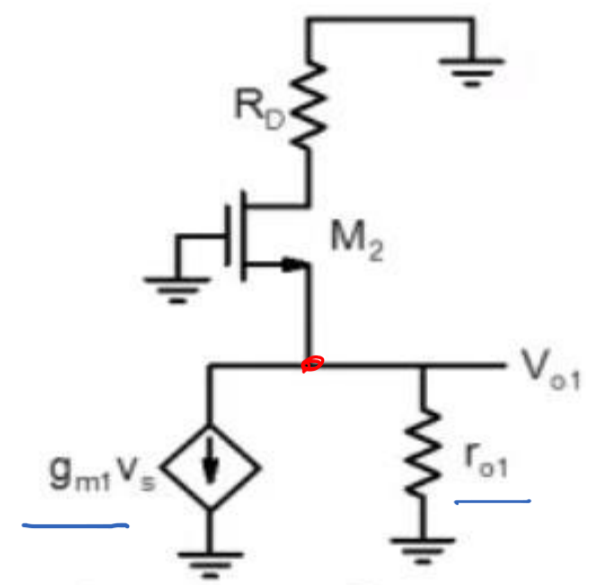
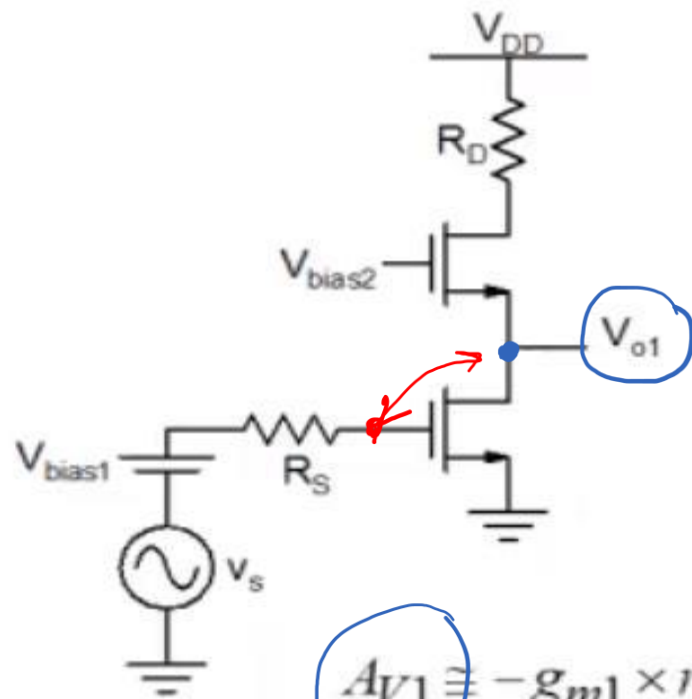
$$R_O \cong R_D$$

## Cascode Amplifier: Frequency Response



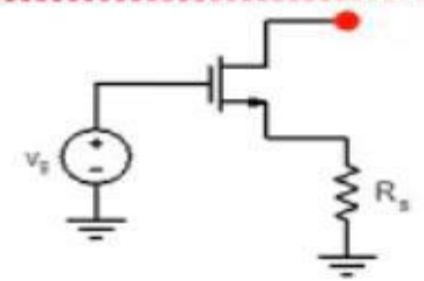
- Gain( $M_1$ ) will suffer from Miller effect
- Let's build a gain at  $V_{o1}$
- Build Norton eq<sup>n</sup>.





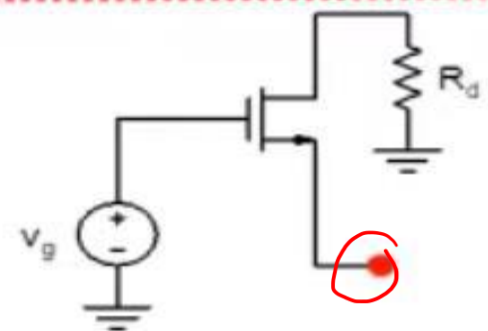
let's solve this

$$A_{V1} \cong -g_{m1} \times r_{o1} \parallel \left\{ \frac{1}{g_{m2} + g_{mb2}} \left( 1 + \frac{R_D}{r_{o2}} \right) \right\} \cong -\frac{g_{m1}}{g_{m2} + g_{mb2}}$$



$$i_n \cong \frac{g_m v_g}{1 + (g_m + g_{mb}) R_S}$$

$$R_n \cong r_o \times \{1 + (g_m + g_{mb}) R_S\}$$



$$i_n = -\frac{g_m v_g}{1 + R_d/r_o} \quad R_n \cong \frac{1 + R_d/r_o}{g_m + g_{mb}}$$

use useful Result -2

$$= \frac{1 + R_d / r_o}{g_{m2} + g_{mb2}}$$

$$R_N \triangleq r_{o1} \parallel \left\{ \frac{1}{g_{m1} + g_{mb2}} \right\} (1 + R_D / r_{o2})$$

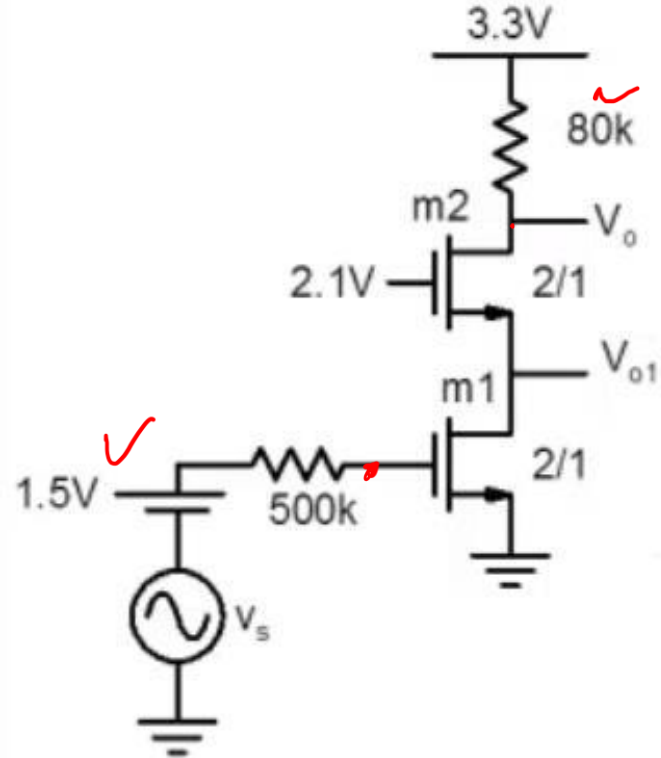
So, Net voltage develop at  $V_{o1} = I_N \cdot R_N$

$$V_{o1} = g_{m1} \cdot \check{V}_S * \underbrace{r_{o2} \parallel \left\{ \frac{1}{g_{m2} + g_{mb2}} \right\} (1 + R_D / r_{o2})}_{\text{---}}$$

$$\boxed{\frac{V_{o1}}{V_S} = \frac{g_{m1}}{g_{m2} + g_{mb2}}}$$

if both the MOS are identical, and if we ignore  $g_{mb2}$ , then  $A_V \leq 1$

## Example



$$I_{DSQ} = 25\mu A$$

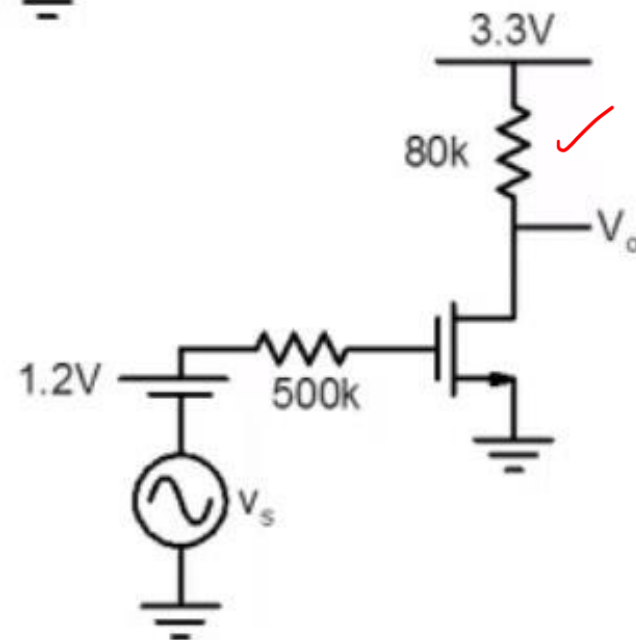
$$V_{sat1} = 0.5V$$

$$V_{o1}(dc) = 0.6V$$

$$V_o(dc) = 1.3V$$

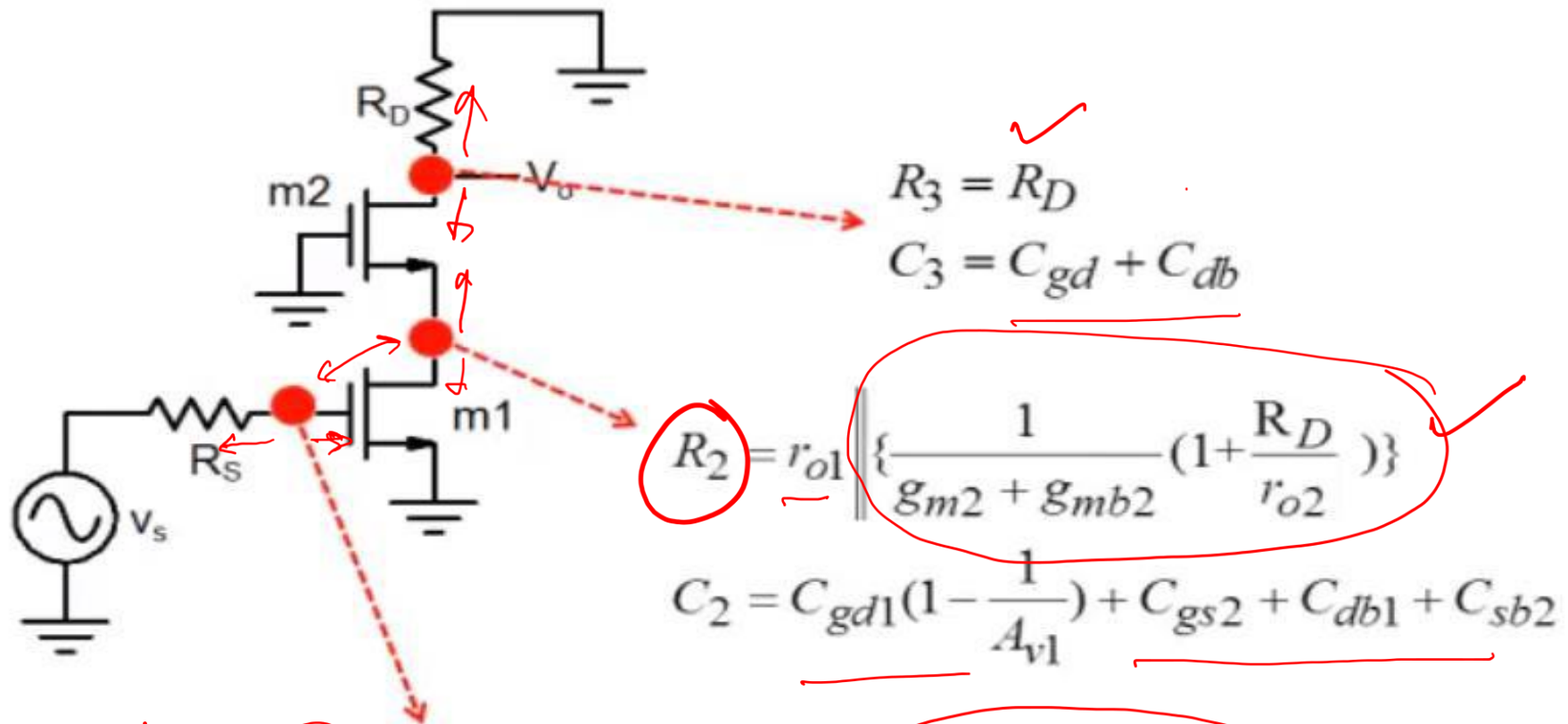
$$A_V = \frac{v_o}{v_s} = -8$$

$$A_{V1} = \frac{v_{o1}}{v_s} = -0.77$$



$$A_V = \frac{v_o}{v_s} = -8$$

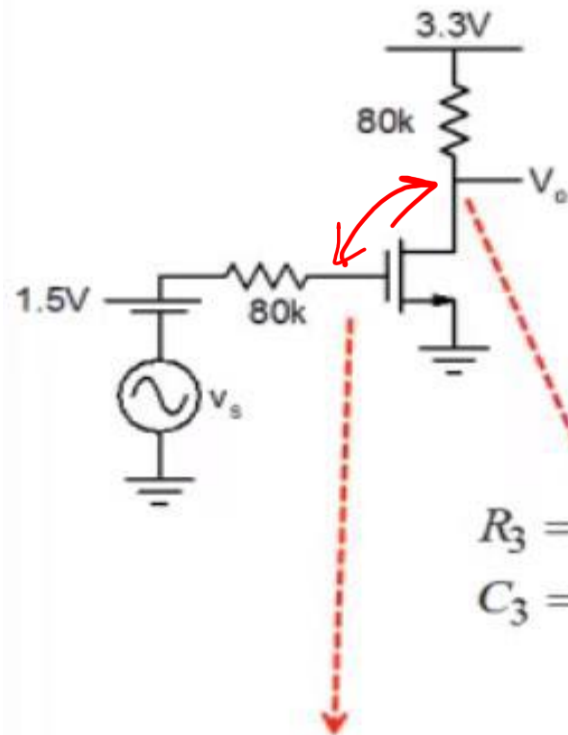
## Cascode Amplifier: Frequency Response



$$f_{3dB} \cong \frac{1}{2\pi \sum R_j C_j}$$

$R_3 C_3$

## Comparison-1



$$R_3 = R_D = 80k$$

$$C_3 = C_{gd} + C_{db} = 4.45 fF$$

$$R_1 = R_S$$

$$C_1 = C_{gs1} + C_{gd1}(1 - A_v)$$

$$= 4 + 3.6 = 7.6 fF$$

$$f_{3dB} \cong \frac{1}{2\pi \sum R_j C_j} = 166 MHz$$

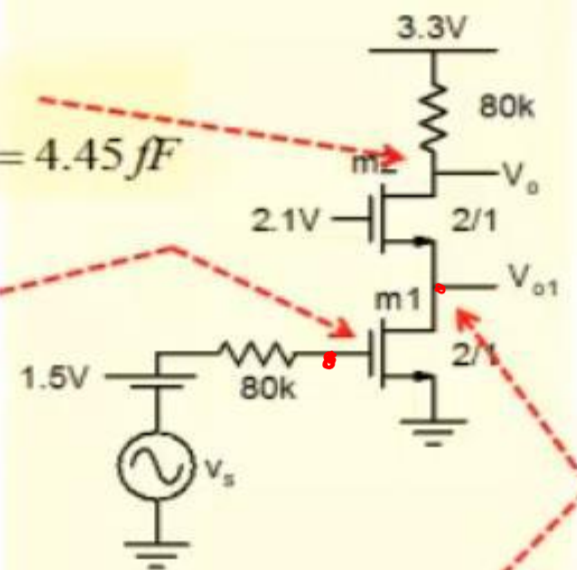
$$R_3 = R_D = 80k$$

$$C_3 = C_{gd} + C_{db} = 4.45 fF$$

$$R_1 = R_S$$

$$C_1 = C_{gs1} + C_{gd1}(1 - A_{v1})$$

$$= 4 + 0.8 = 4.8 fF$$



$$R_2 = r_{o1} \left\{ \frac{1}{g_{m2} + g_{mb2}} \left( 1 + \frac{R_D}{r_{o2}} \right) \right\} = 10k$$

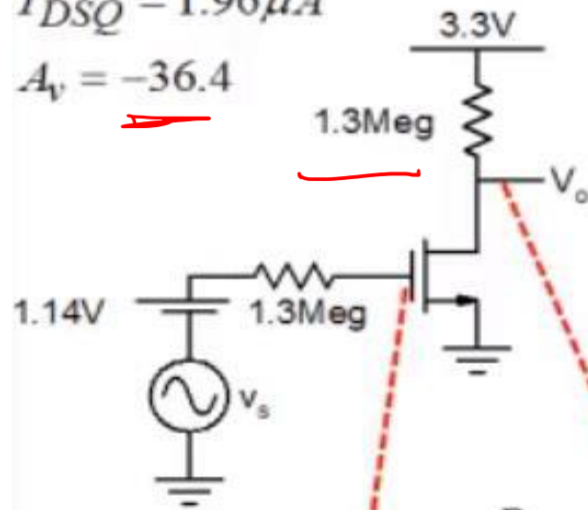
$$C_2 = C_{gd1} \left( 1 - \frac{1}{A_{v1}} \right) + C_{gs2} + C_{db1} = 12.8 fF$$

$$f_{3dB} \cong \frac{1}{2\pi \sum R_j C_j} = 183 MHz$$

## Comparison-2

$$I_{DSQ} = 1.96 \mu A$$

$$A_v = -36.4$$



$$R_1 = R_S$$

$$C_1 = C_{gs1} + C_{gd1}(1 - A_{v1})$$

$$= 4 + 0.8 = 4.8 fF$$

$$R_3 = R_D = 1300k$$

$$C_3 = C_{gd} + C_{db} = 4.4 fF$$

$$R_1 = R_S$$

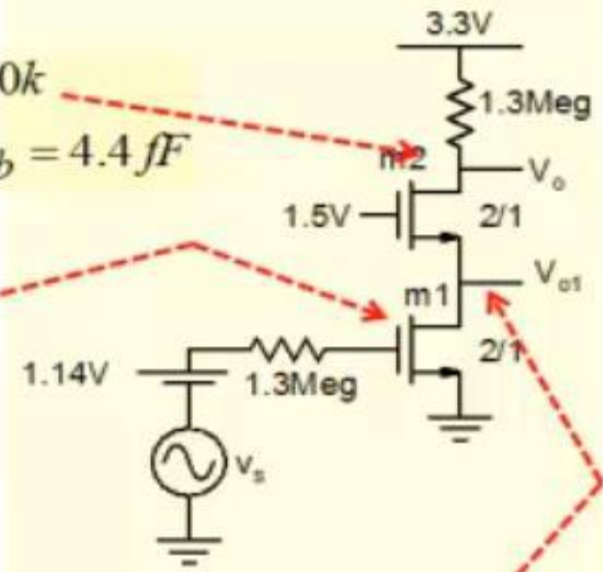
$$C_1 = C_{gs1} + C_{gd1}(1 - A_v)$$

$$= 4 + 15 = 19 fF$$

$$f_{3dB} \cong \frac{1}{2\pi \sum R_j C_j} = 5.24 MHz$$

$$R_3 = R_D = 1300k$$

$$C_3 = C_{gd} + C_{db} = 4.4 fF$$



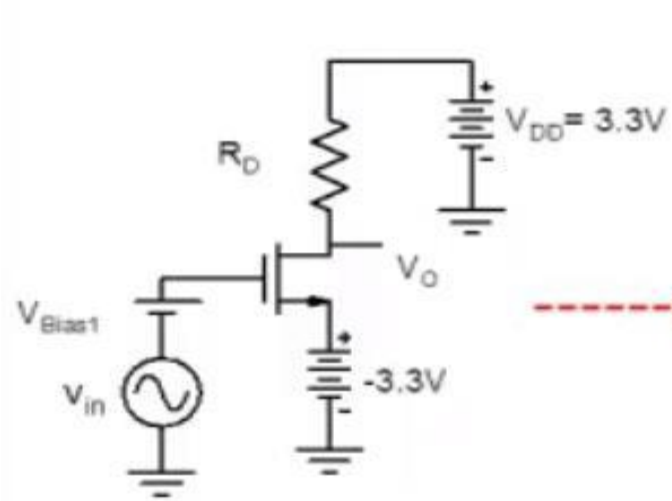
$$R_2 = r_{o1} \parallel \left\{ \frac{1}{g_{m2} + g_{mb2}} \left( 1 + \frac{R_D}{r_{o2}} \right) \right\} = 35.7k$$

$$C_2 = C_{gd1} \left( 1 - \frac{1}{A_{v1}} \right) + C_{gs2} + C_{db1} + C_{sb2} = 12.8 fF$$

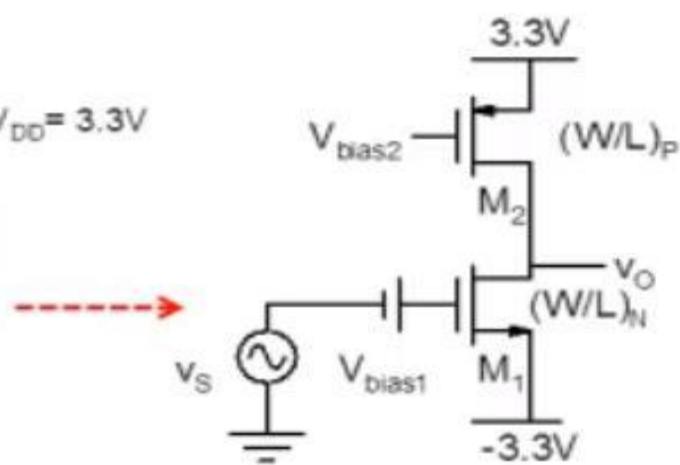
$$f_{3dB} \cong \frac{1}{2\pi \sum R_j C_j} = 12.8 MHz$$

Body effect is ignored

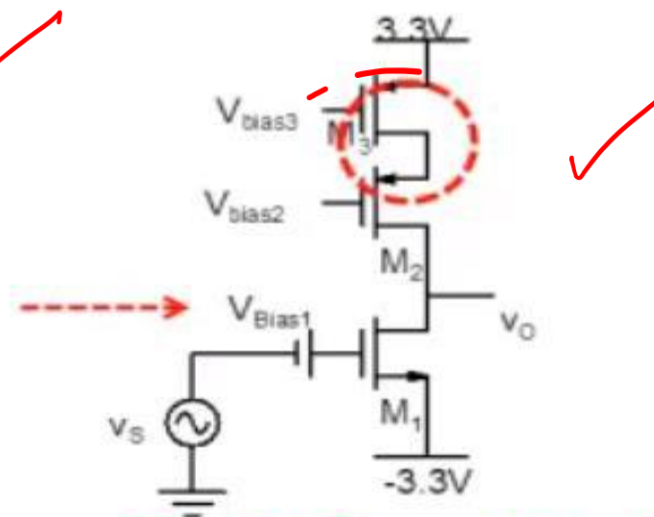




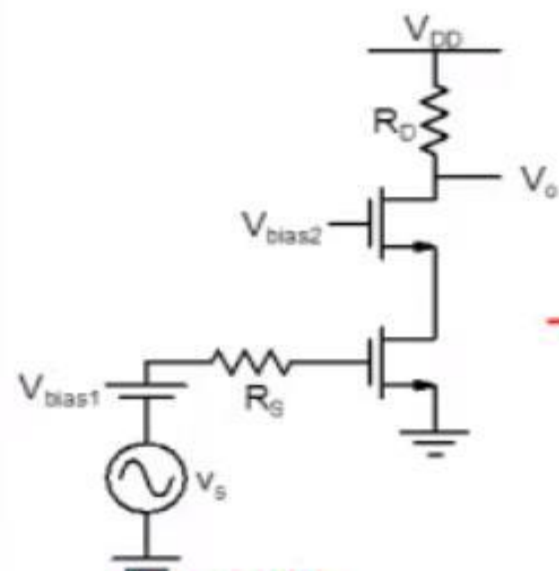
**CS amplifier**



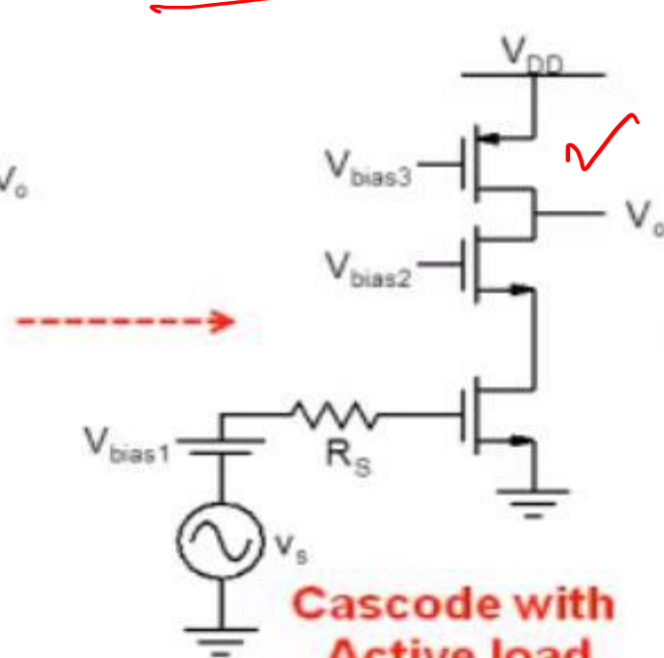
**CS with Active Load**



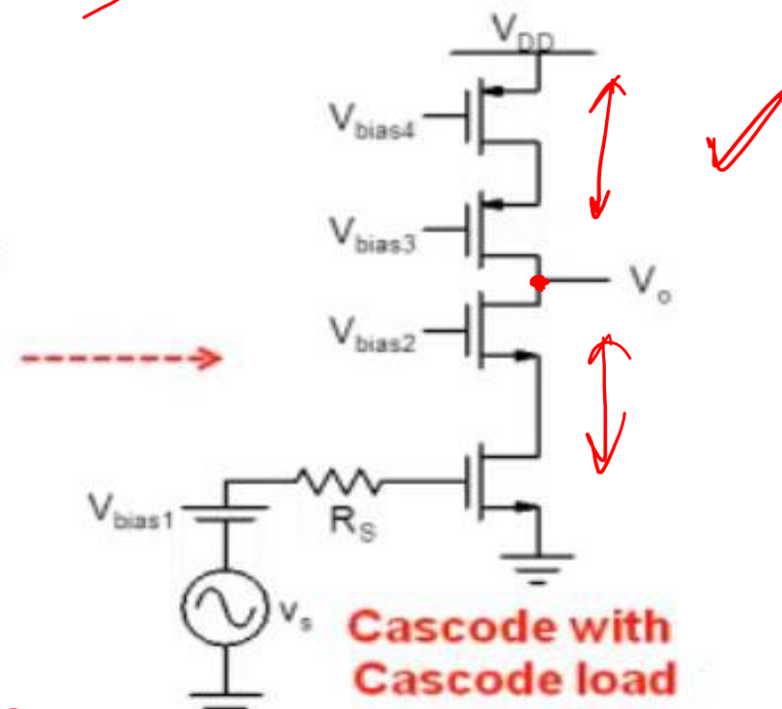
**CS with Cascode Load**



**Cascode with Resistive load**



**Cascode with Active load**

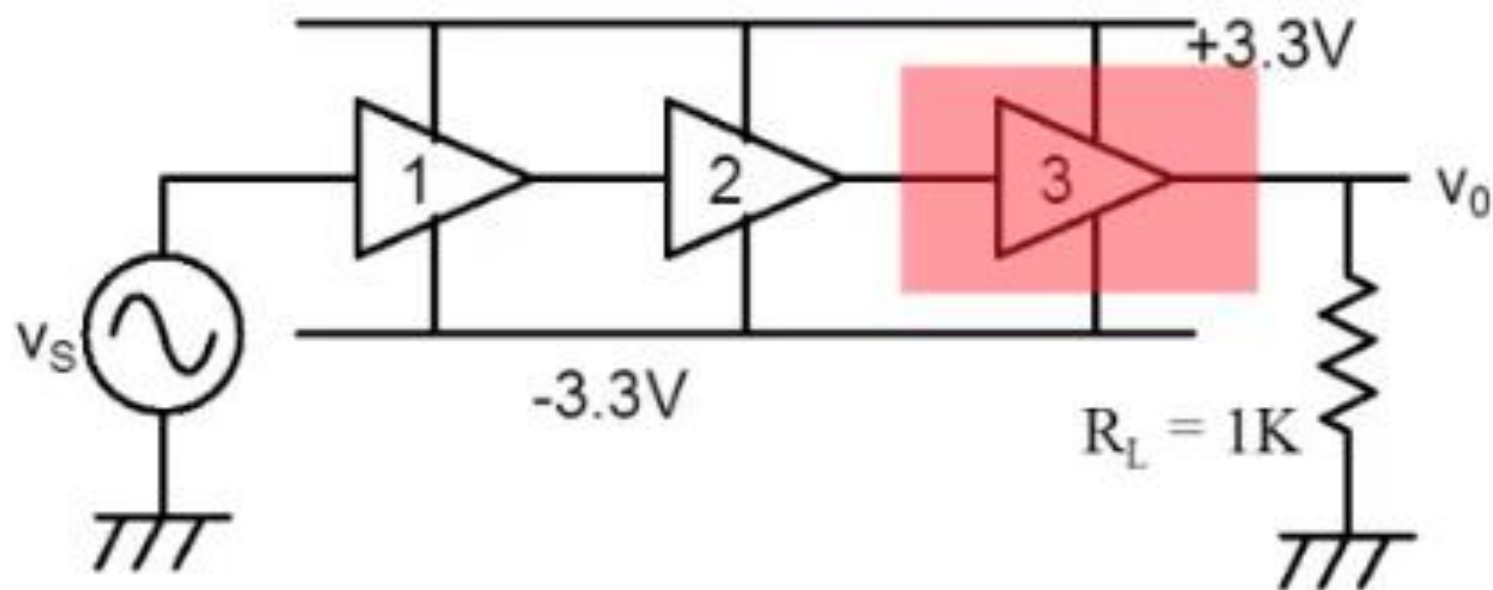


**Cascode with Cascode load**

## Common Drain Amplifier



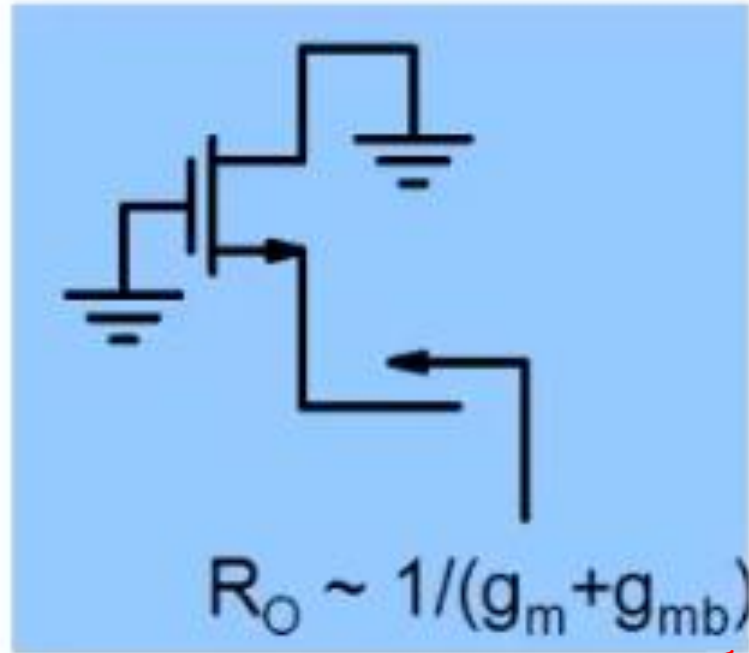
Why do we want one more amplifier configuration?



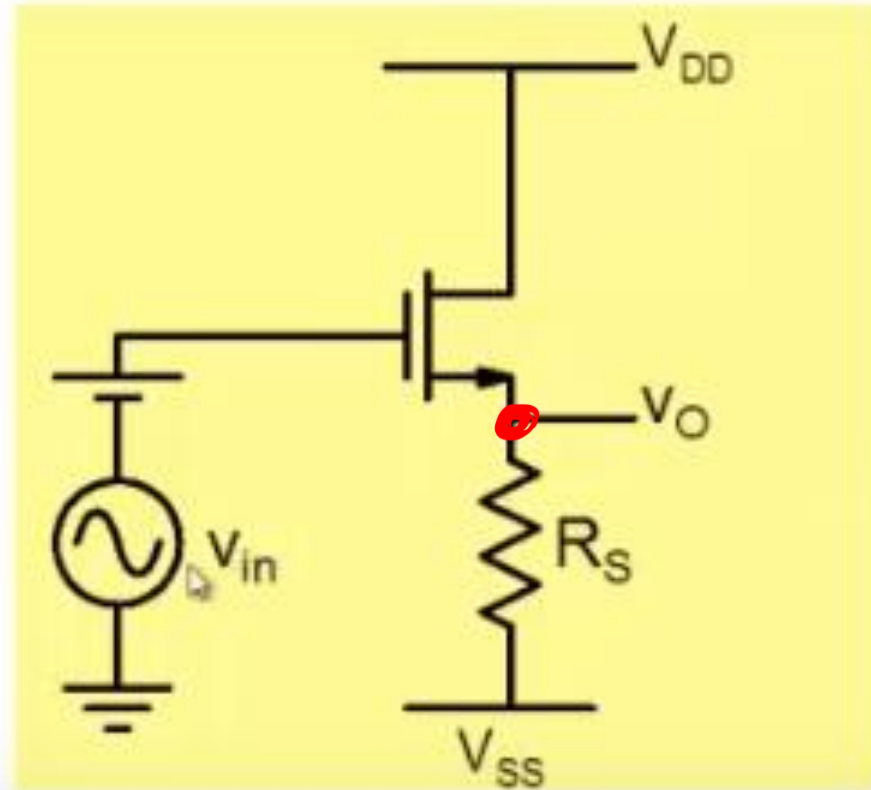
Low output Resistance;  
Rail-to-Rail voltage swing;      Low distortion  
High efficiency

## Strategy for obtaining Low output resistance

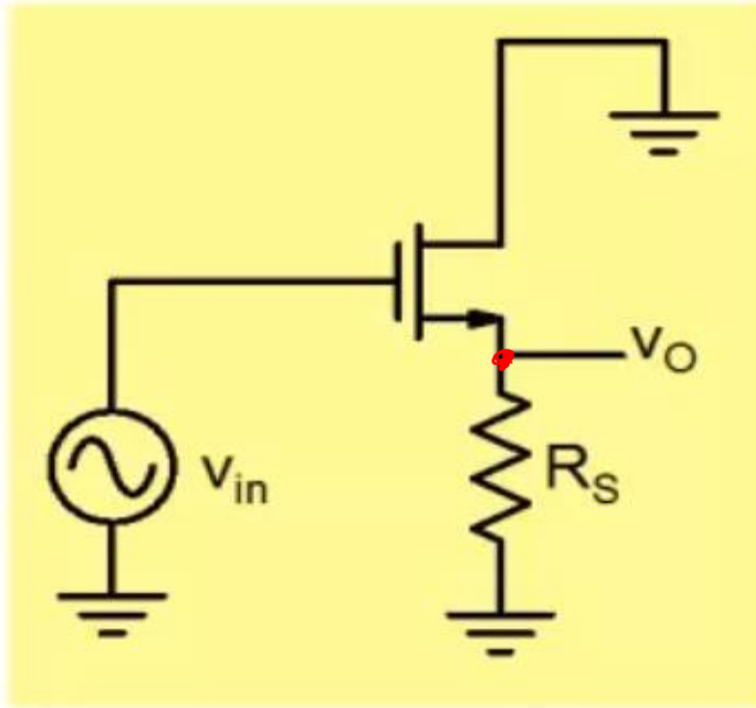
Resistance looking into source is small !



Apply input at gate, take output at Source

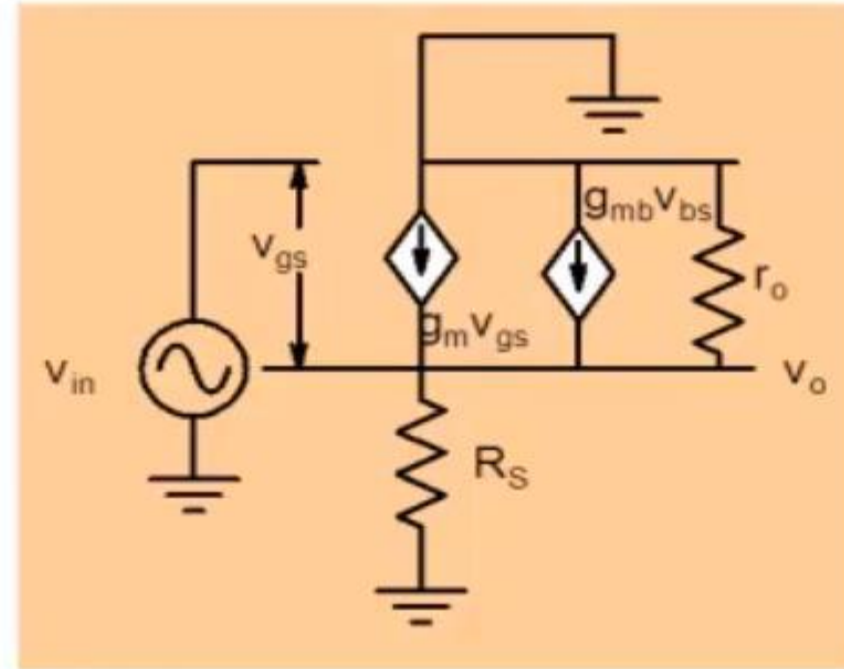


## Small Signal Analysis



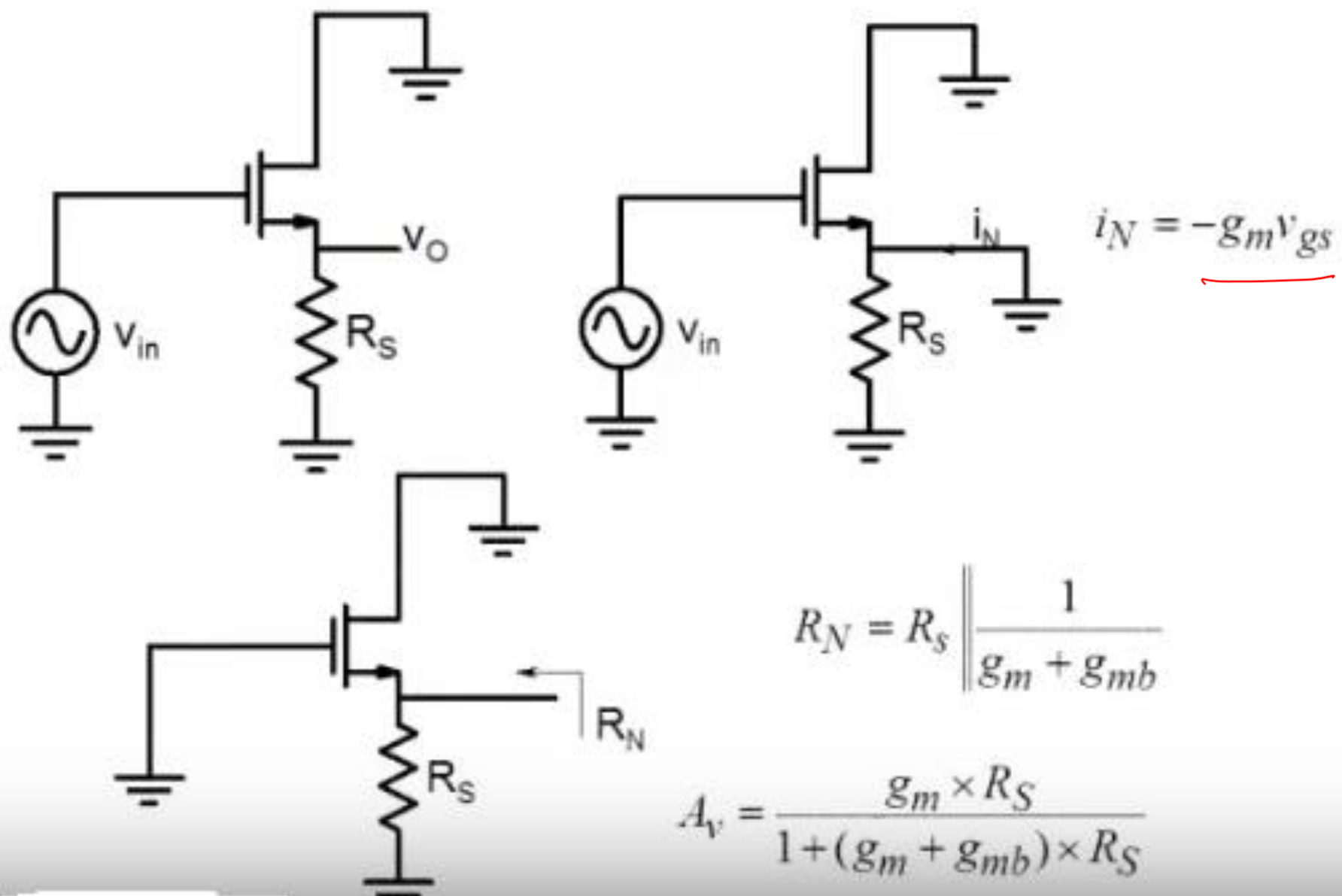
$$A_v = \frac{g_m R_S \parallel r_o}{1 + (g_m + g_{mb}) R_S \parallel r_o}$$

Gain is less than unity !

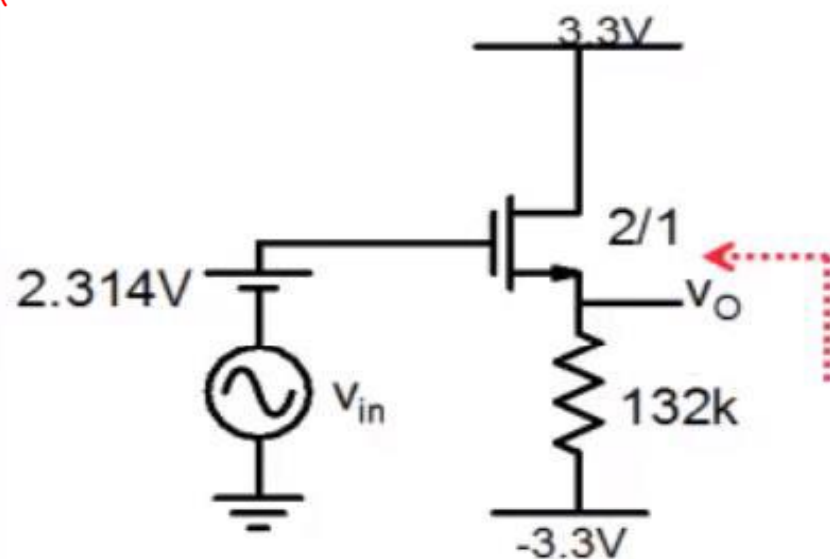


$$R_o = R_S \parallel \frac{1}{g_m + g_{mb}} \cong \frac{1}{g_m + g_{mb}}$$

Output resistance is low !



## Example:



$$V_{Bias} = V_{GSQ} + I_{DSQ}R_S + V_{SS}$$

$$I_{DSQ} = \frac{\beta_N}{2} (V_{GSQ} - V_{THN})^2 [1 + \lambda_n V_{DSQ}]$$

$$V_{THN} = V_{THN0} + \gamma (\sqrt{2\phi_F + V_{SBQ}} - \sqrt{2\phi_F})$$

$$V_{SBQ} = I_{DSQ}R_S ; V_{DSQ} = V_{DD} - I_{DSQ}R_S - V_{SS}$$

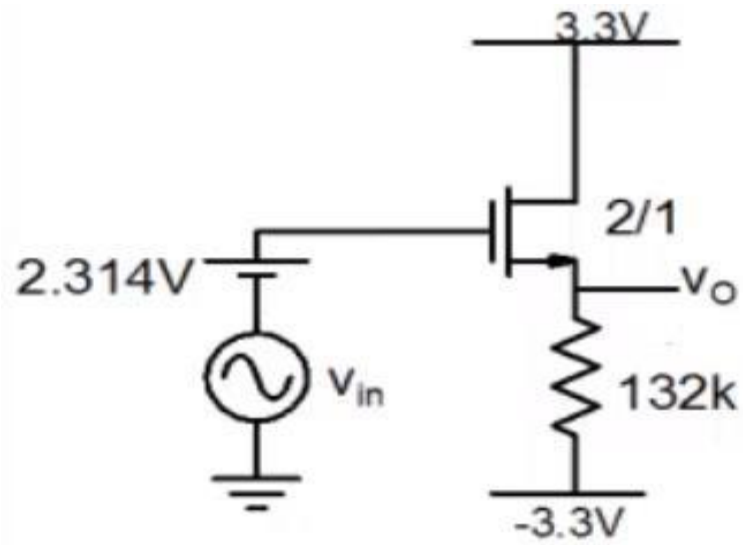
$$I_{DSQ} = 25\mu A \quad V_{SBQ} = 3.3V \Rightarrow V_{THN} = 1.8V ; V_{GSQ} = 2.314V \quad V_{DSQ} = 3.3V$$

$$g_m = 100\mu A/V ; g_{mb} = 17.5\mu A/V ; r_o = 4M\Omega$$

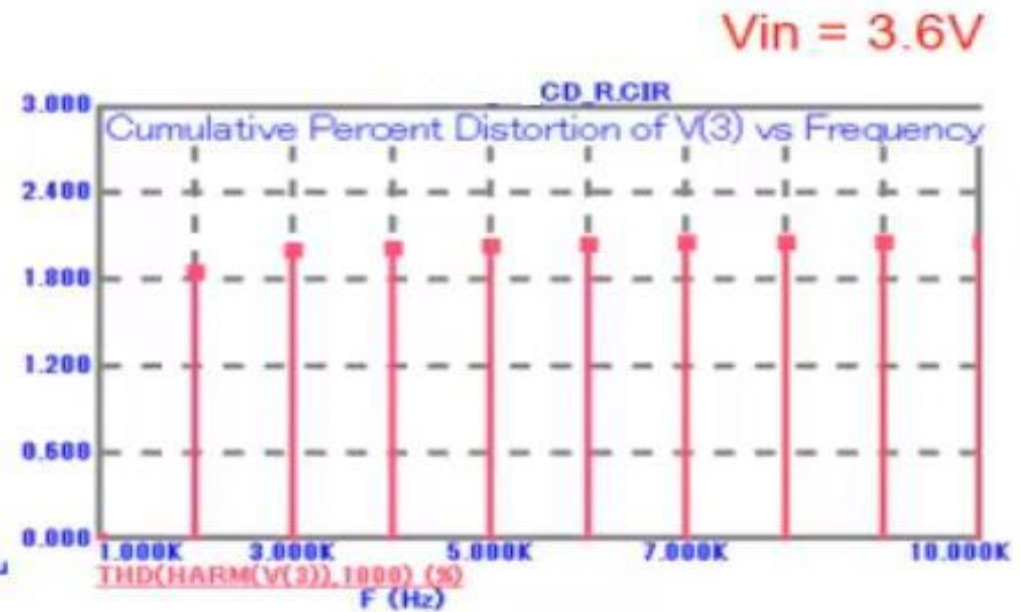
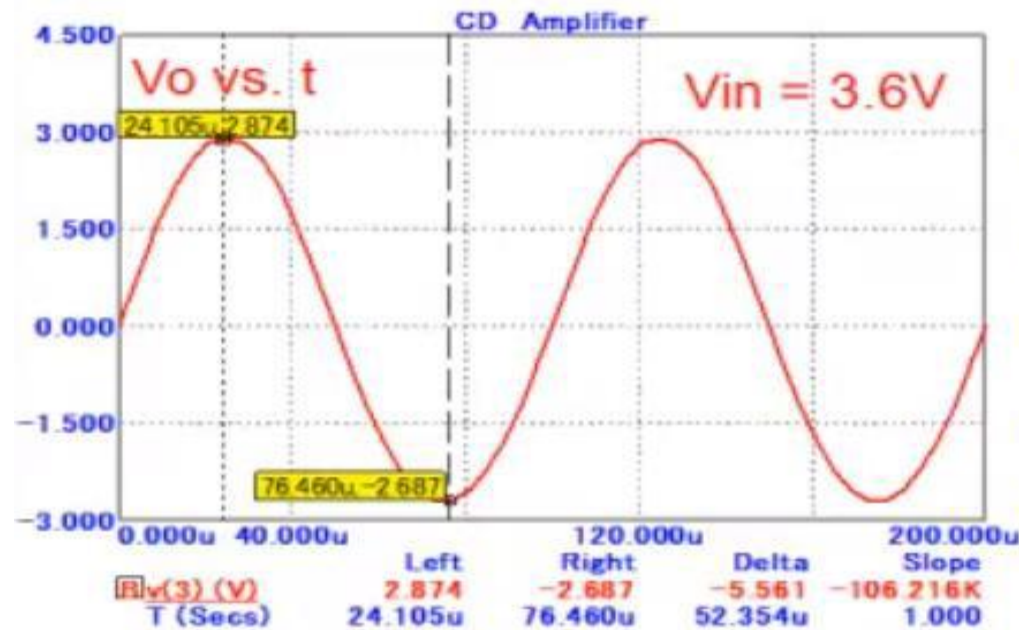
$$A_v = \frac{g_m R_S}{1 + (g_m + g_{mb})R_S} = 0.8$$

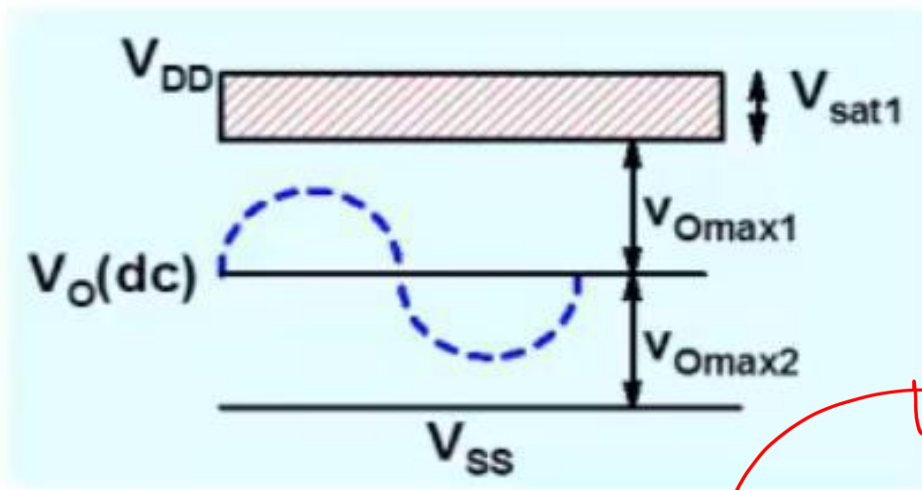
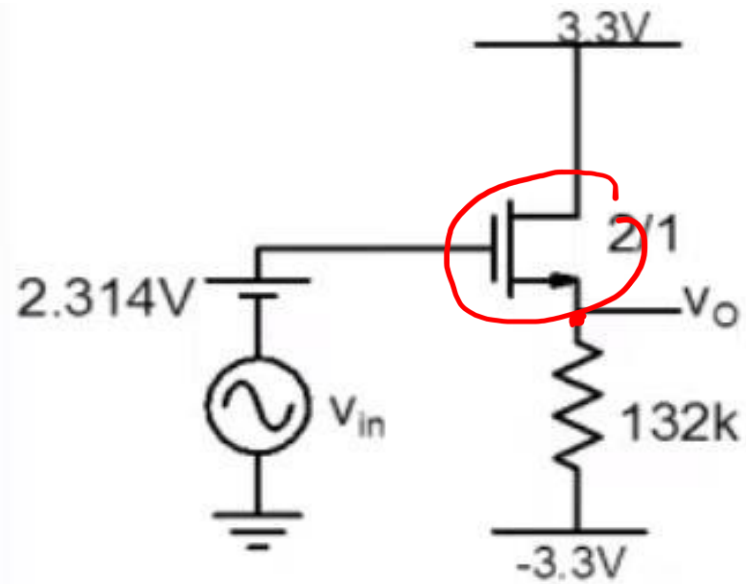
$$R_o = R_S \parallel \frac{1}{g_m + g_{mb}} \sim 8k$$



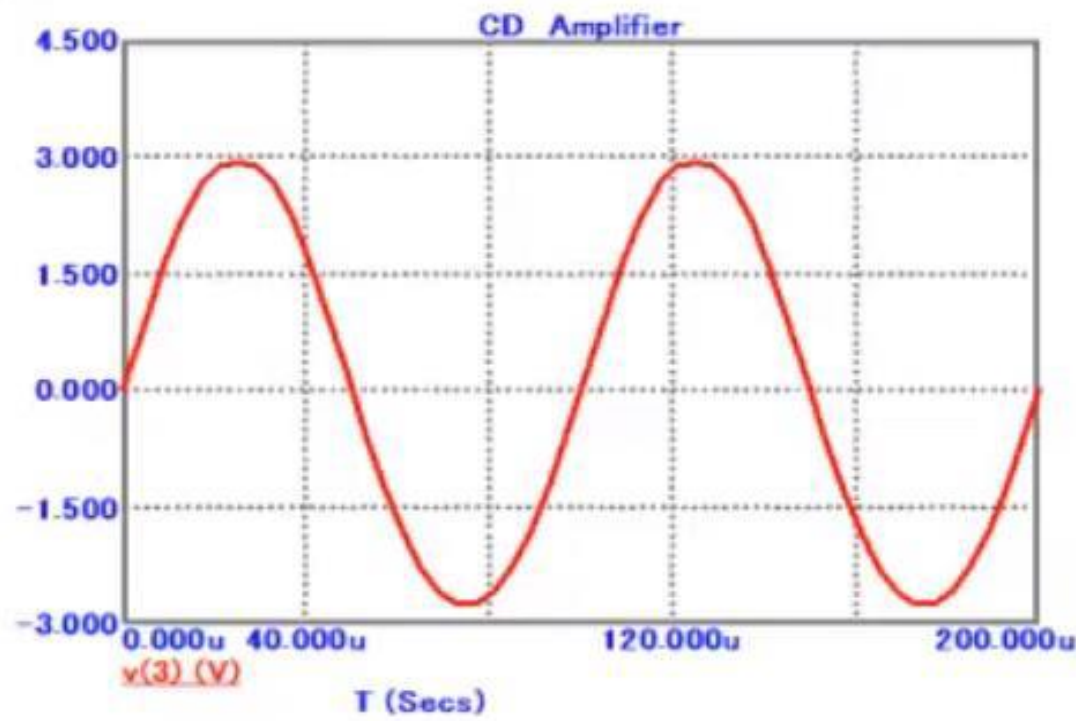


CD amplifier has good linearity and thus less prone to harmonic distortion



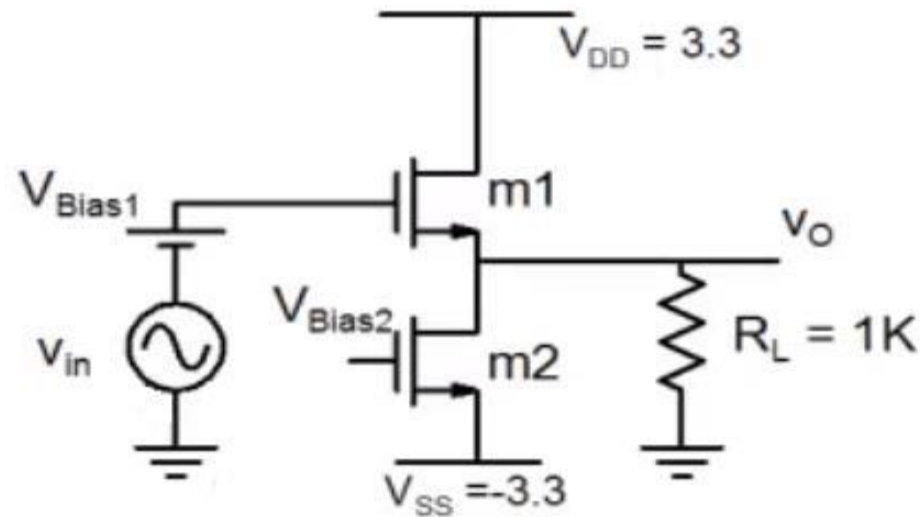


Voltage swing limited by current



## Example

$$I_{DSQ} = 3.3mA$$



$$\frac{W_1}{L_1} = \frac{200}{1}; V_{GS1} = 2.389V; V_O = 0V$$

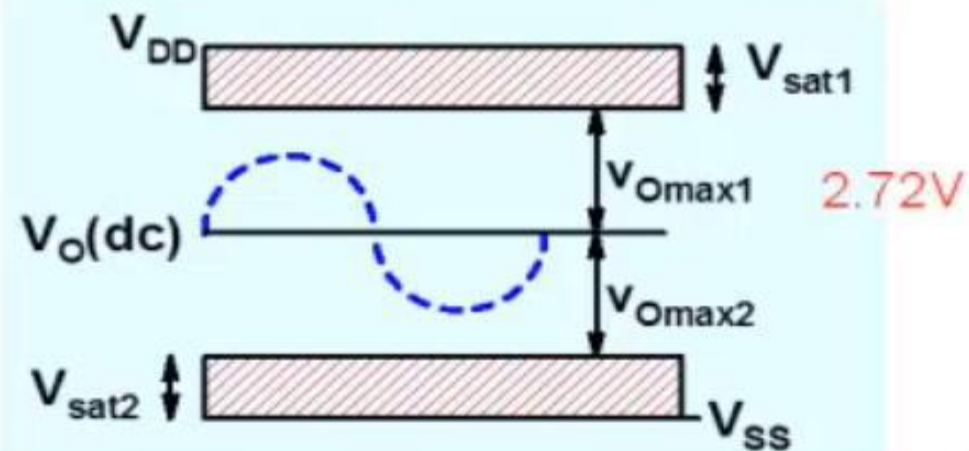
$$\frac{W_2}{L_2} = \frac{200}{1}; V_{GS2} = 1.575V$$

$$\Rightarrow V_{bias2} = -1.725V$$

$$V_{sat} = 0.575V$$

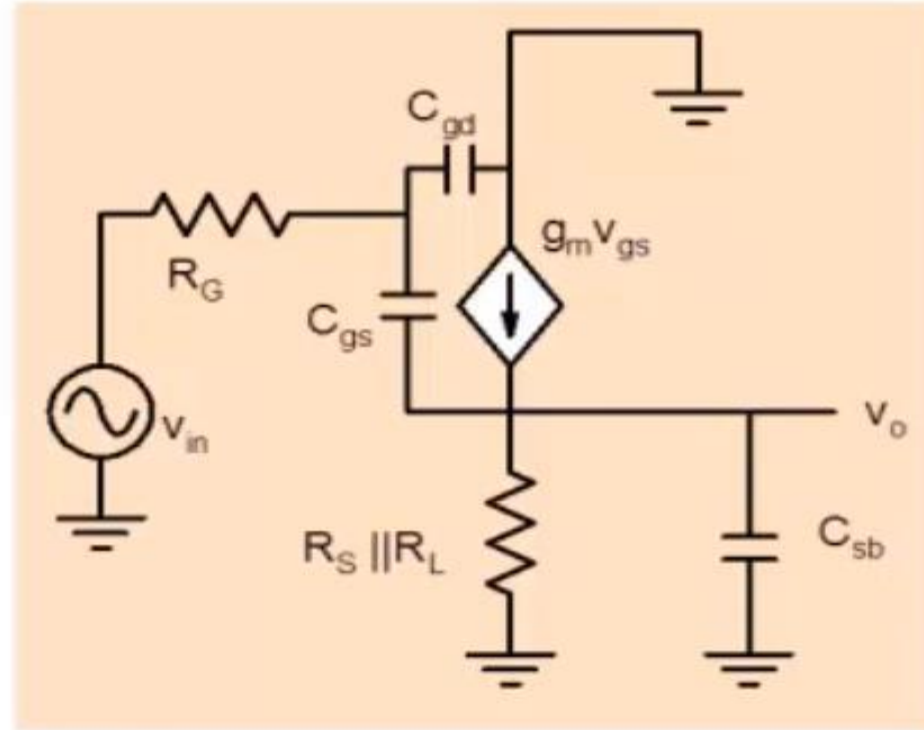
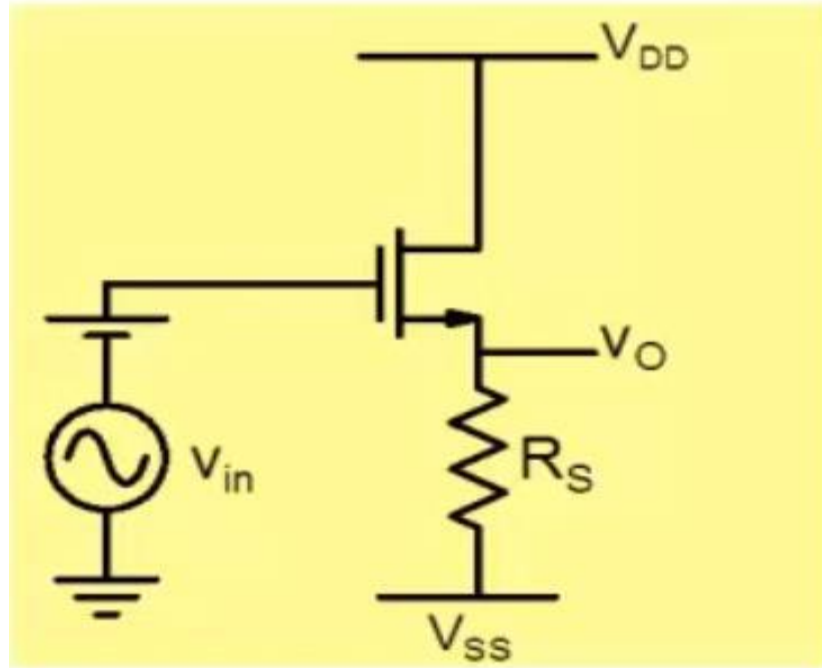
$$A_v = \frac{g_m R_L}{1 + (g_m + g_{mb}) R_L} = 0.79$$

$$R_o = \frac{1}{g_m + g_{mb}} \sim 74\Omega$$





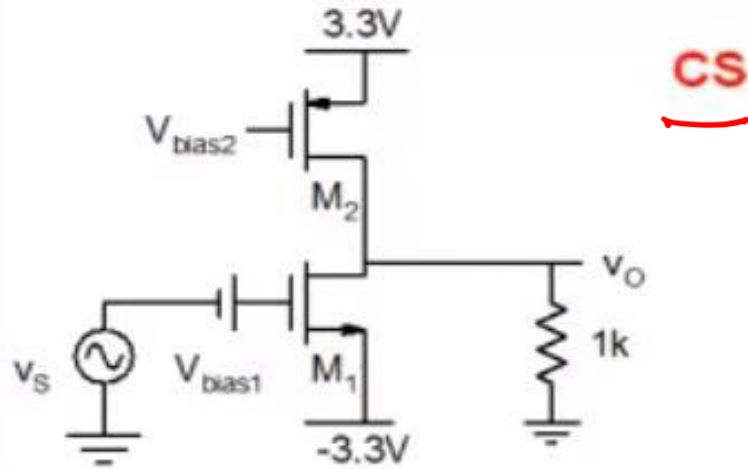
## Frequency Response



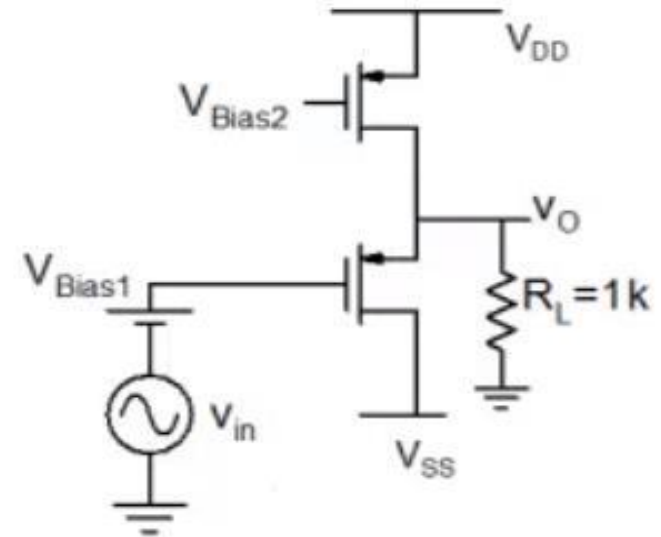
$$f_{3dB} = \frac{1}{2\pi \sum \tau_j}$$

$$\tau_j = R_j C_j$$

## Summary



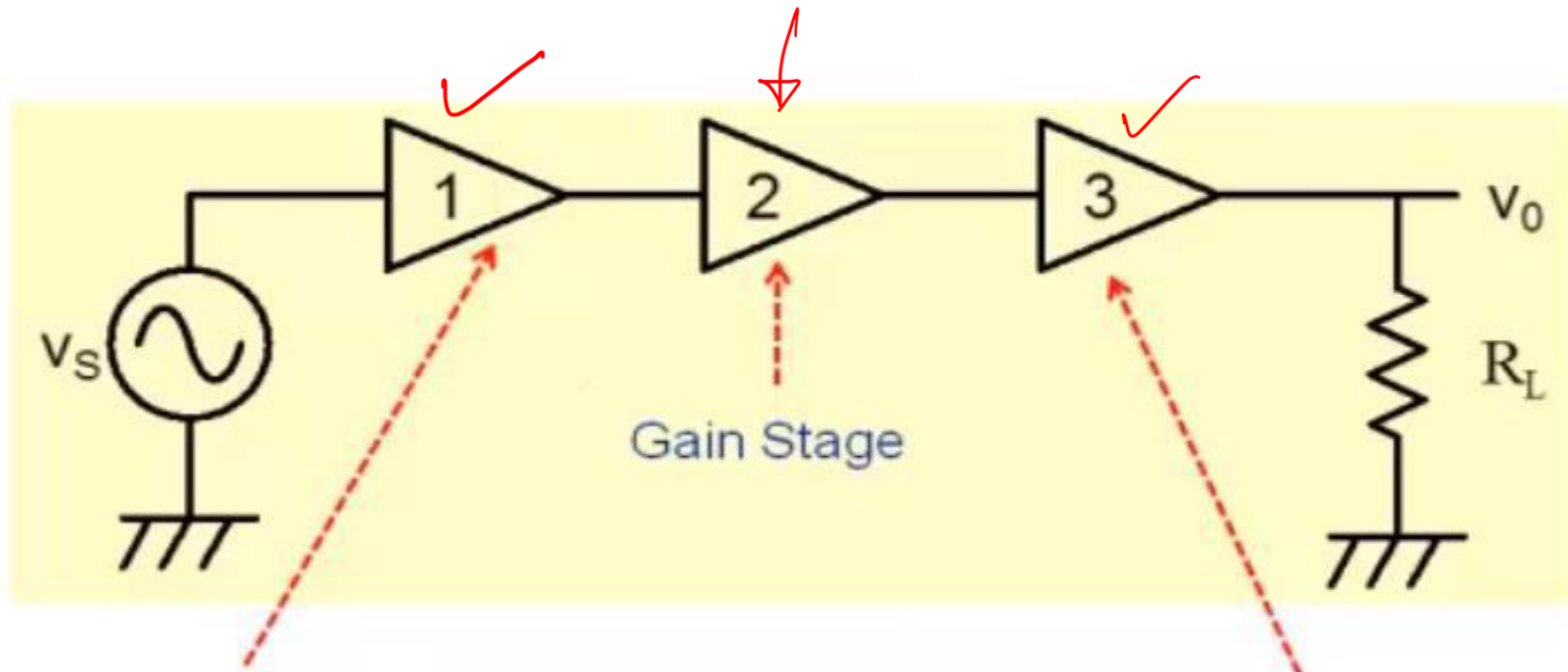
1. Low Output resistance requires large bias current
2. Rail-to-rail output swing
3. Frequency response suffers from Miller's effect and is inferior.



1. Significantly Lower Output resistance can be obtained at same value of bias current
2. Swing lower by about a  $V_T$  drop
3. Good frequency response

Efficiency limited to  $< 25\%$  for both the stages

## Principle of Division of labor !



Specialize in input resistance

Specialize in output resistance and power delivery