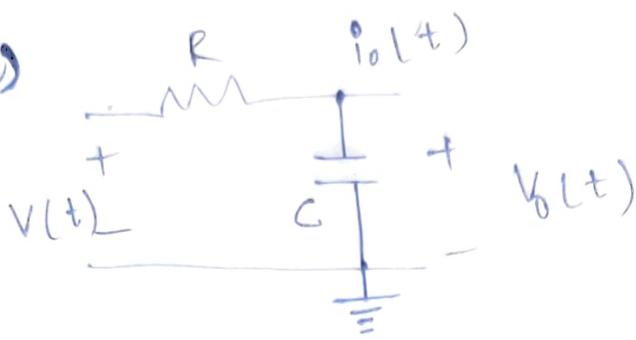
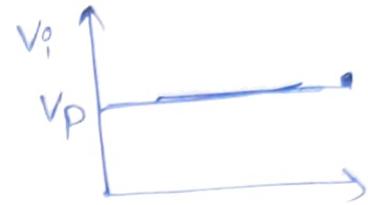


1.1(a)



input Voltage +



$$\frac{V_o}{V_{in}} = \frac{V_{out}}{V_{in}} = \frac{V_p - iR}{V_p}$$

$$Q = CV_o$$

$$i = C\frac{dV_o}{dt}$$

$$V_p - RC \frac{dV_o}{dt} = V_o$$

$$\int_0^t V_p - V_o = \int_0^t RC \frac{dV_o}{dt}$$

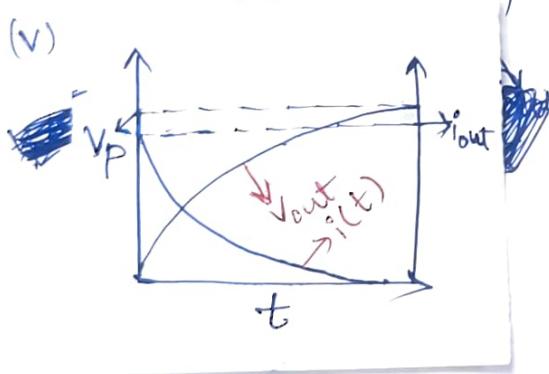
$$Q=0 \text{ at } t=0$$

$$\Rightarrow V_o = 0$$

$$\int_0^t \left[\frac{t}{RC} \right] = - \int_0^t \ln(V_p - V_o)$$

$$-\frac{t}{RC} = \ln \left(\frac{V_p - V_o}{V_p} \right) \Rightarrow e^{-t/RC} = 1 - \frac{V_o}{V_p}$$

$$V_o = V_p (1 - e^{-t/RC})$$



$$\text{Voltage across } R = \frac{V_{out}}{R}$$

$$i_{out} = \frac{V_i - V_o}{R} = \frac{V_p}{R} (e^{-t/RC})$$

Voltage divider

$$i(\omega) = \frac{V_{in}(\omega)}{R + \frac{1}{SC}}$$

$$V_{out}(\omega) = \frac{V_{in}(\omega) \left(\frac{1}{SC} \right)}{R + \frac{1}{SC}}$$

$$\frac{V_{out}}{V_{in}} = \frac{1}{1 + SRC} = H(\omega)$$

Pole:

$$H(\omega) = \infty$$

$$\frac{1}{1+SRC} = \infty$$

$$0 = 1 + SRC$$

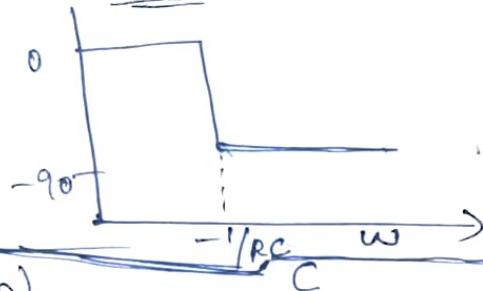
$$S = \frac{-1}{RC},$$

$$\text{for } \omega \ll \frac{1}{RC}$$

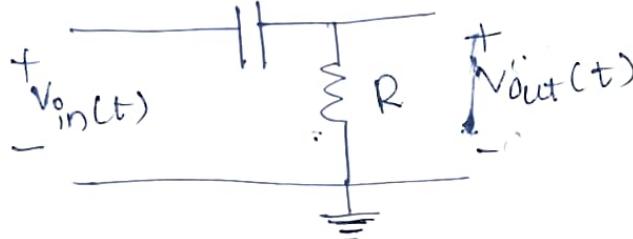
$$1 + SRC \approx 1$$

$$H(\omega) \approx 1$$

Phase



b)



$$V_{out} = iR$$

$$C V_c = Q$$

$$C(V_p - iR) = Q$$

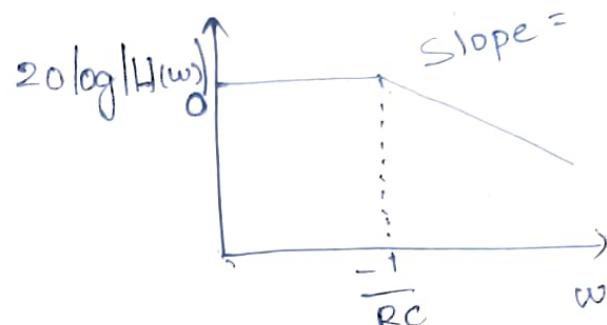
Zero:

$$H(\omega) = 0$$

$$\frac{1}{1+SRC} = 0$$

NO ZEROS.

$$|H(\omega)| = \frac{1}{\sqrt{1+(SRC)^2}}$$



Bodeplot

$$i = \frac{V_{out}}{R} = \frac{V_p}{R} e^{-t/RC}$$

$$C(V_p - V_o) = Q$$

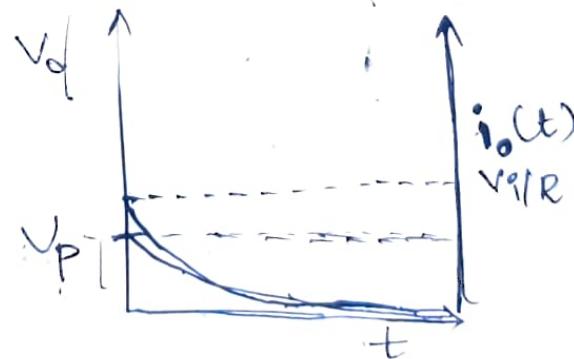
$$-C \frac{dV_o}{dt} = i$$

$$-RC \frac{dV_o}{dt} = iR = V_o$$

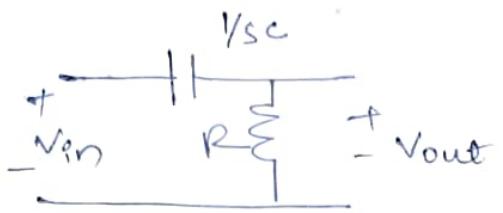
$$\frac{dV_o}{V_o} = \frac{dt}{-RC}$$

$$\ln(V_o) = \frac{t}{-RC} - t/RC$$

$$V_o = V_{pe}$$



frequency domain circuit

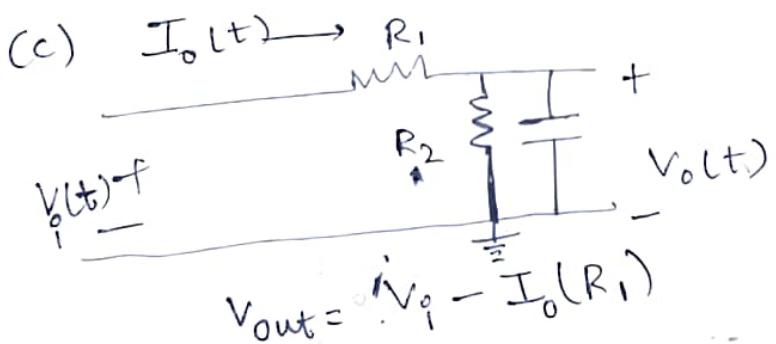
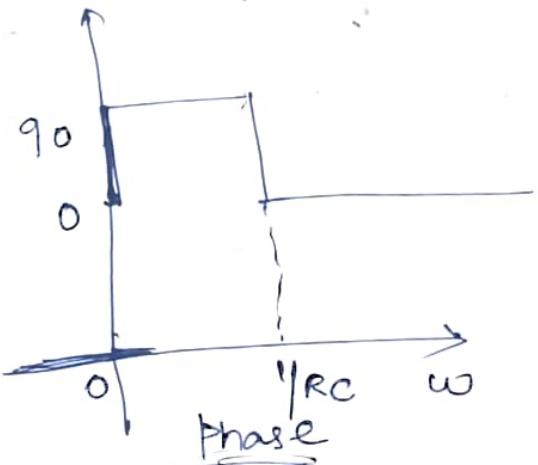
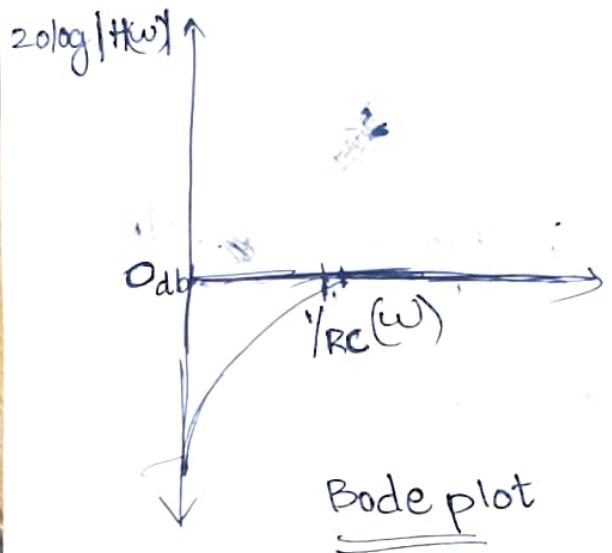


$$V_{out} = \frac{(R) V_{in}(\omega)}{R + \frac{1}{\omega C}}$$

$$\frac{V_{out}}{V_{in}} = H(\omega) = \frac{\omega C}{1 + \omega C}$$

Zeros: (i) $s=0 \Leftrightarrow (\omega C / 1 + \omega C) = 0$

Poles: (ii) $1 + \omega C = 0 \Rightarrow \omega = -1/R_C$



V_{out} at $t=0$

0



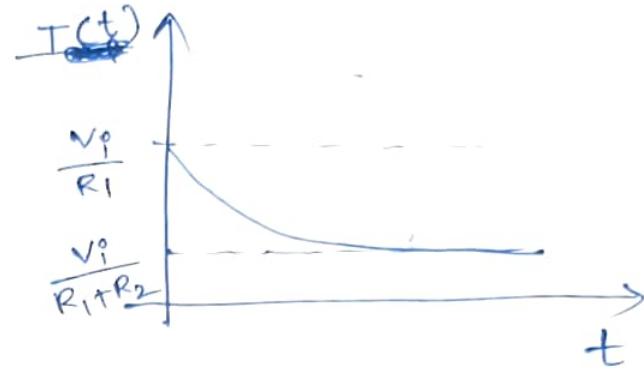
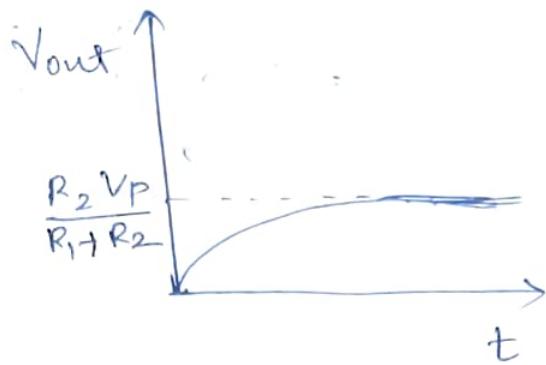
V_{out} at $t=\infty$

$R_2 \cdot V_p$

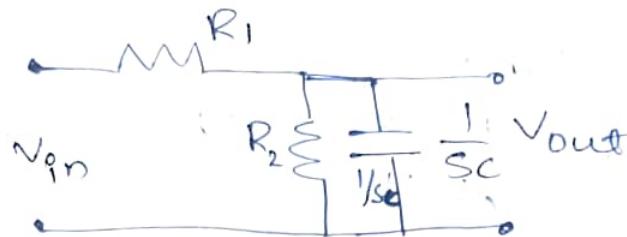


I_{out} at $t=\infty$ $\frac{V_p}{R_1 + R_2}$

$\bullet I_{out}$ at $t=0$ $\frac{V_i}{R_1}$



f domain ckt



$$\frac{\left(\frac{R_2}{R_2 + \frac{1}{sc}} \right) V_p}{\frac{R_2 \frac{1}{sc}}{R_2 + \frac{1}{sc}} + R_1} = V_{out}$$

$$\frac{V_{out}}{V_{in}} = \frac{R_2}{R_1 + R_2 + SR_1R_2C}$$

Poles: $H(j\omega) = \infty$

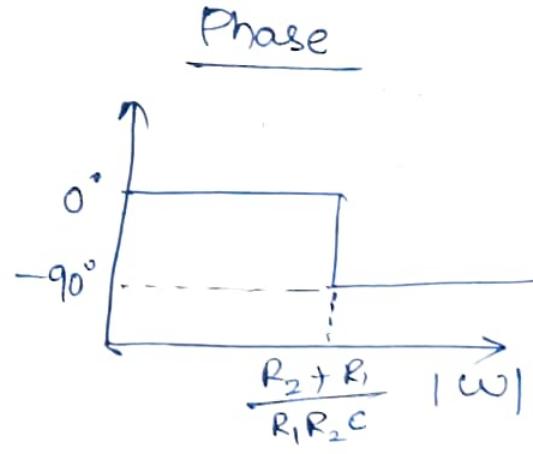
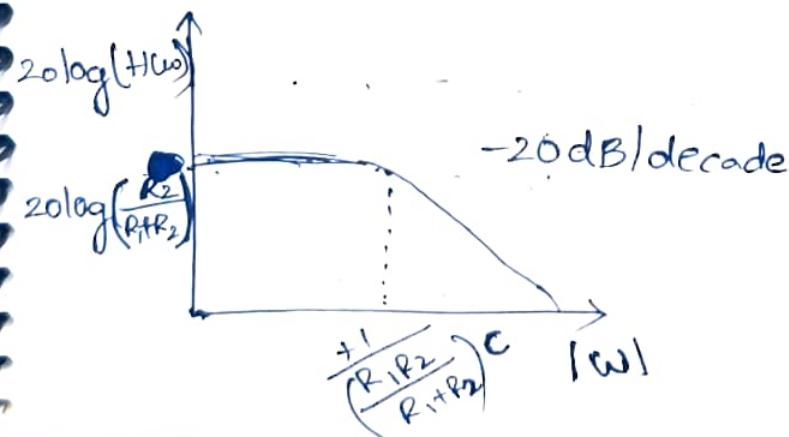
$$R_1 + R_2 + SR_1R_2C = 0$$

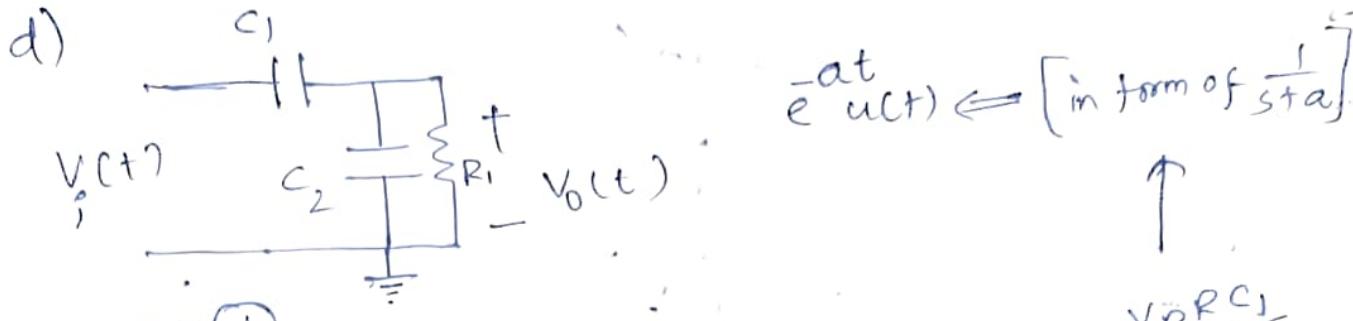
$$s = \frac{1}{\left(\frac{R_1R_2}{R_1 + R_2}\right)c} = -\frac{(R_2 + R_1)}{R_1R_2C}$$

Zeros:

$$H(j\omega) = 0$$

no zeroes





$e^{-at} u(t) \Leftrightarrow$ [in form of $\frac{1}{s+a}$] ↑

From ①

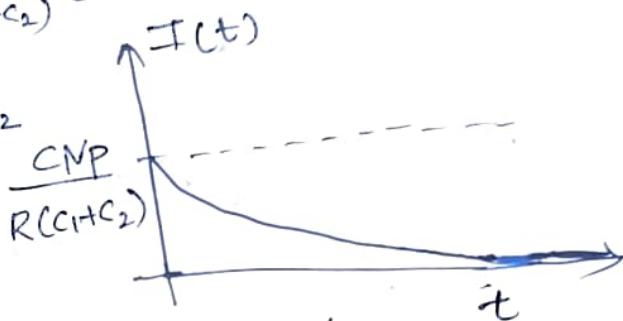
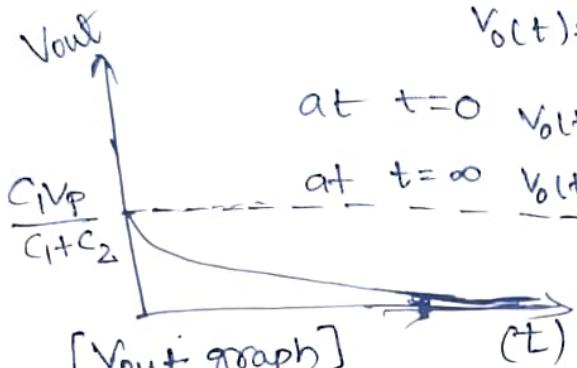
$$V_{out}(s) = \frac{V_p}{s} \cdot \frac{R s C_1}{R s C_1 + 1 + R C_2 s} = \frac{V_p C_1 R}{R s C_1 + R s C_2 + 1} = \frac{V_p R C_1}{\frac{1}{s} + R(C_1 + C_2)}$$

Inverse Laplace

$$V_o(t) = \frac{V_p R C_1}{R(C_1 + C_2)} e^{-\frac{t}{R(C_1 + C_2)}} + \dots \quad ②$$

$$\text{at } t=0 \quad V_o(t) = \frac{C_1 V_p}{C_1 + C_2}$$

$$\text{at } t=\infty \quad V_o(t) = 0$$



[Vout graph]

Applying f-domain Ckt

$$V_{out} = V_{in} \cdot \frac{\frac{R}{sC_2}}{\frac{R+1/sC_2}{sC_1 + \frac{R}{sC_2}}} = V_{in} \cdot \frac{1}{1 + \frac{RC_2 s + 1}{R s C_1}} \quad - ①$$

$$\frac{V_{out}}{V_{in}} = \frac{R s C_1}{1 + R s (C_1 + C_2)} = H(w)$$

Zeroes:

$$\frac{R s C_1}{1 + R s (C_1 + C_2)} = 0$$

$$s = 0$$

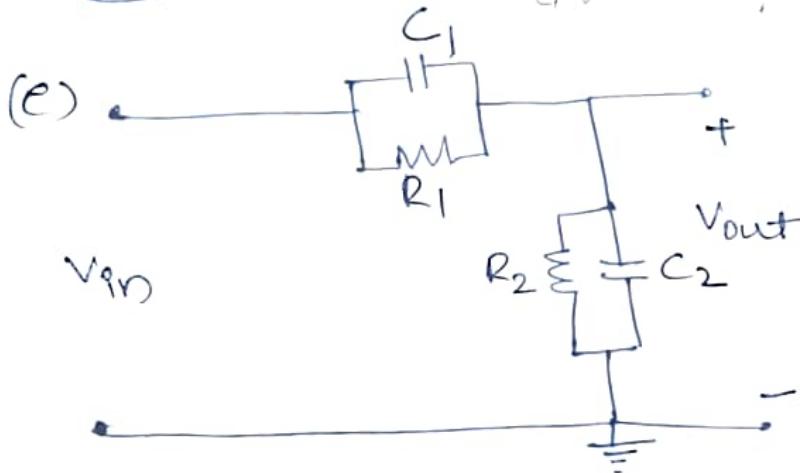
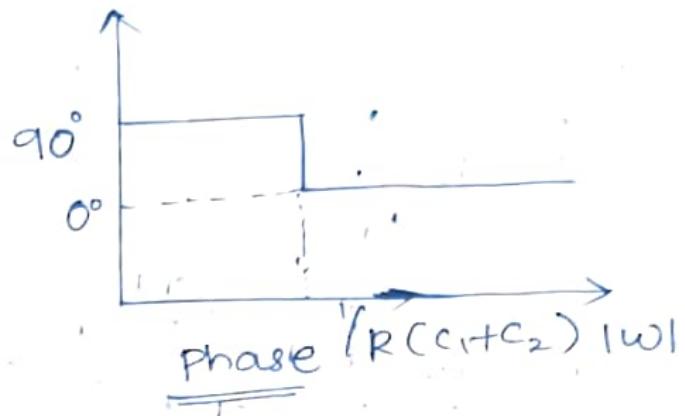
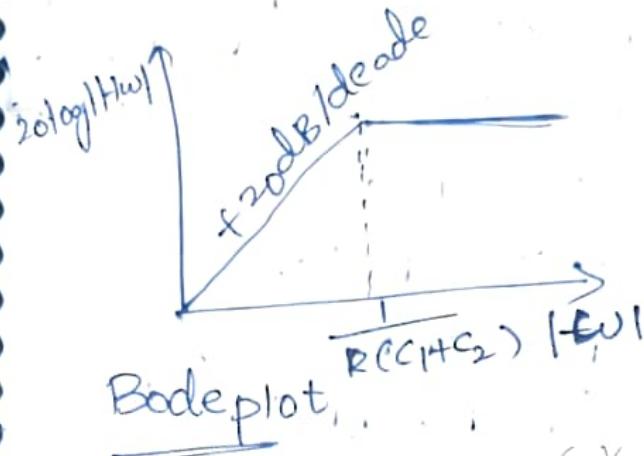
Poles:

$$H(w) \rightarrow \pm \infty$$

$$\frac{R s C_1}{1 + R s (C_1 + C_2)} \geq \infty$$

$$1 + R s (C_1 + C_2) = 0$$

$$s = -\frac{1}{R(C_1 + C_2)}$$



at $t = 0^+$

both capacitors are shorted then there's a path with no resistance, no opposing to e^\ominus Path so, huge amount of e^\ominus flowed through them and charged instantaneously

So, here charge is conserved bcz. no charges flowed through resistors at the start

$$C_1 V_1 = C_2 V_2$$

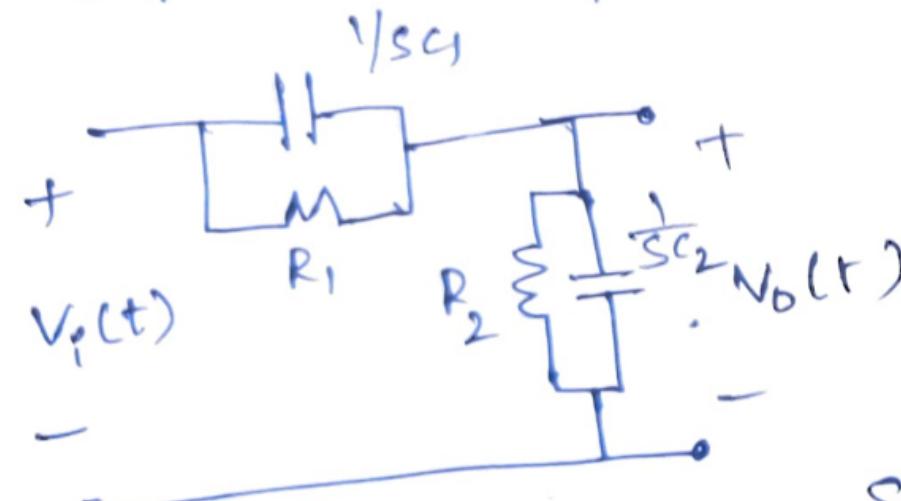
$$V_1 + V_2 = V_o$$

$$V_o = V_2 = \frac{C_1 V_o}{C_1 + C_2} \quad \text{at } t = 0^+$$

$t = \infty$
finally both charged completely then act as open capacitors
and voltage divided among resistors switches

$$V_o = \frac{R_2 V_o}{R_1 + R_2}$$

Laplace transformed circuit



$$\frac{N_o}{V_p} = \frac{\frac{R_2}{SC_2}}{R_2 + \frac{1}{SC_2}} + \frac{\frac{R_1}{SC_1}}{R_2 + \frac{1}{SC_2}}$$

$$\frac{V_1 R_2}{R_2 + R_1} = \frac{M_1 C_1}{C_1 + C_2}$$

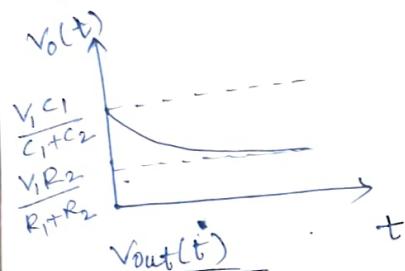
$$\text{Zero, } s = \frac{-1}{R_1 C_1}$$

$$H(s) = \frac{R_2}{R_1 + R_2} + \frac{SR_1 R_2 C_1}{R_1 + R_2} \left(\frac{1}{s} - \frac{R_2 + SR_1 R_2 C_1}{R_1 + R_2 + SR_1 R_2 (C_1 + C_2)} \right)$$

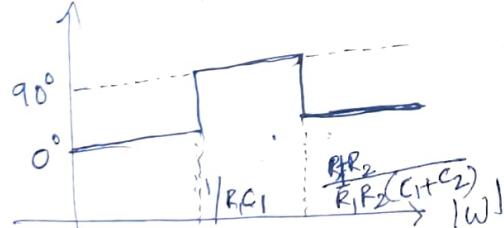
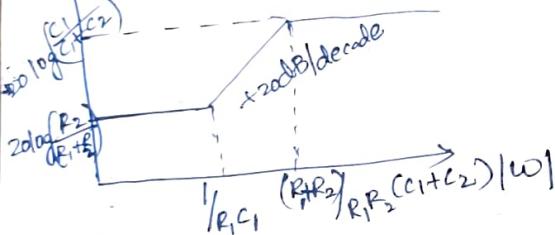
$$\frac{R_2 + SR_1 R_2 C_1}{R_1 + R_2 + SR_1 R_2 (C_1 + C_2)}$$

if Voltage is less than initial
Voltage then capacitors
discharged

if $R_1 C_1 > R_2 C_2$

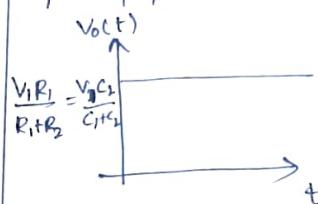


Bode Plot



if equal then there was no
change in the capacitors
from initial conditions

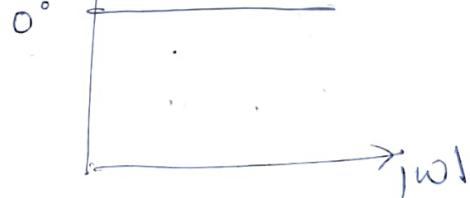
if $R_1 C_1 = R_2 C_2$



$$20 \log \left(\frac{R_2}{R_1 + R_2} \right) = 20 \log \left(\frac{C_2}{C_1 + C_2} \right)$$

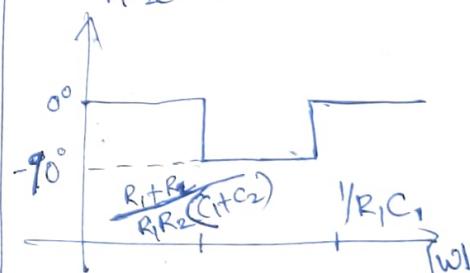
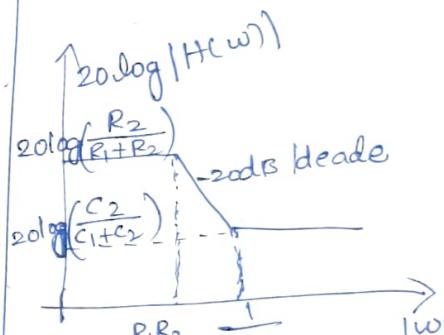
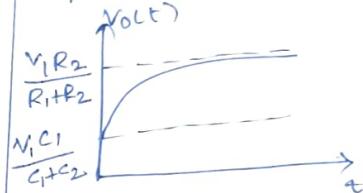
$$\frac{1}{R_1 C_1} = \frac{R_1 + R_2}{R_1 R_2 (C_1 + C_2)}$$

Phase (zero)

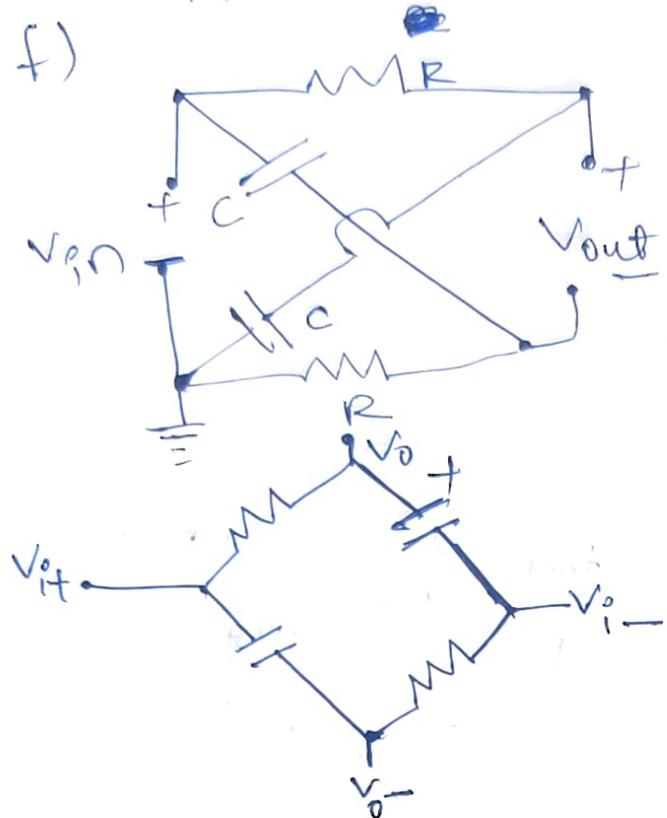


if it was greater then
the capacitors have
further charged

if $R_1 C_1 < R_2 C_2$



f)



$$t=0 \rightarrow \text{closed switch} \Rightarrow \text{shorted}$$
$$t=\infty \rightarrow \text{open switch} \Rightarrow \text{open}$$

at $t=0^+$ as capacitors they act as closed

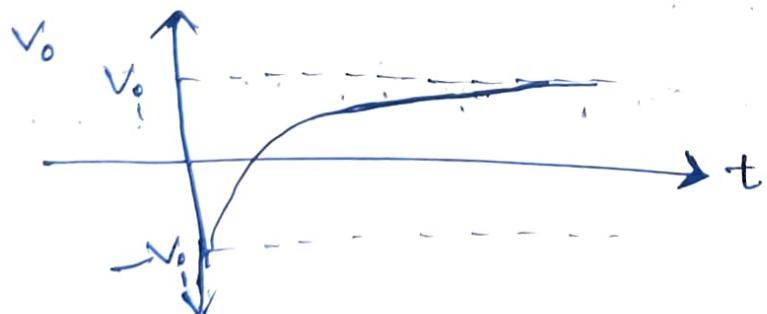
switches then

$$V_o = -V_i \text{ at } t=0^+$$

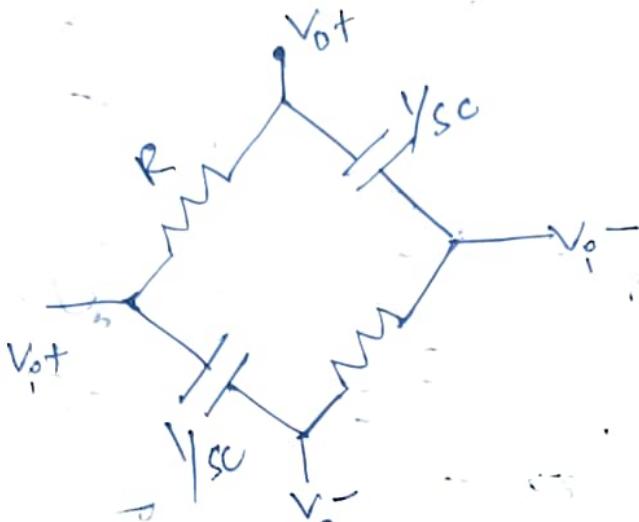
at $t=\infty$

the capacitors are charged and act as open

switches then, $V_o = V_i$ at $t=\infty$



Laplace applied circuit



$$i_{\text{total}} = \frac{2V_p}{(R + \frac{1}{SC})} = \frac{2V_p}{R + \frac{1}{SC}}$$

$$i(\frac{1}{SC}) - i(R) = V_o$$

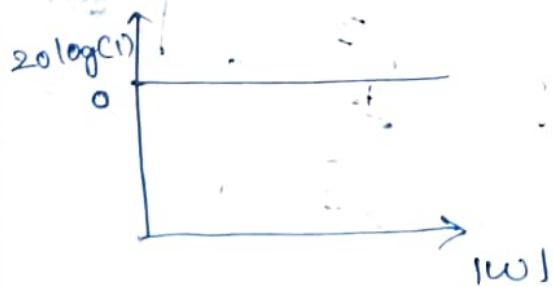
$$\frac{\left(\frac{1}{SC} - R\right)}{\left(\frac{1}{SC} + R\right)} V_p = V_o$$

$$\frac{V_o}{V_p} = \frac{(1 - SRC)}{(1 + SRC)} = H(\omega)$$

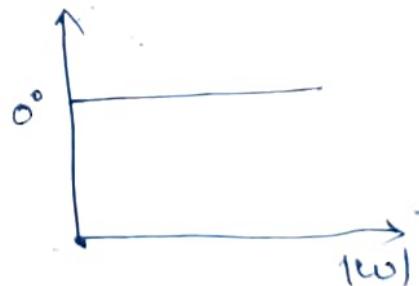
$$\text{Zero} = \frac{1}{RC}, \text{Pole} = \frac{-1}{RC}$$

$$\omega \ll \frac{1}{RC} \quad SRC \ll 1$$

$$H(\omega) = 1$$



Bode plot



phase

i in one branch

$$i_b = \frac{V_p}{R + \frac{1}{SC}}$$

2.1

cut in Voltage:- The voltage at which the diode starts conducting significant amount of current

→ approx 430 mV

knee - voltage :- at which slope of the IV graph increases in the forward bias, here stronger conduction starts

⇒ approx
↓
⇒ 600 mV

reverse saturation current:- the small amount of current flown in reverse bias

∴ - 2.52 nA

incremental diode resistance)- resistance of the diode from IV graph

$$\frac{\Delta V}{\Delta I} = \frac{620 - 560}{0.1 - 0.9} = 18 \Omega$$

2.2

Half wave rectifier

- * given sine wave as input contains both +ve and -ve cycles, the cycle decides the direction of current in circuit
- * only passes half of the input wave, according diode orientation with respect to voltage sine and +ve or -ve

2.3 Full Wave rectifier

- * A full-wave rectifier converts AC to DC by allowing both halves of the AC input to pass through the same direction. It uses two diodes arranged to conduct during both positive and -ve cycles of the input sine wave.
- * During the +ve half cycle, diodes conduct and allow current to flow in one direction, during the negative half-cycle, the diodes reverse and still allow current in same direction.

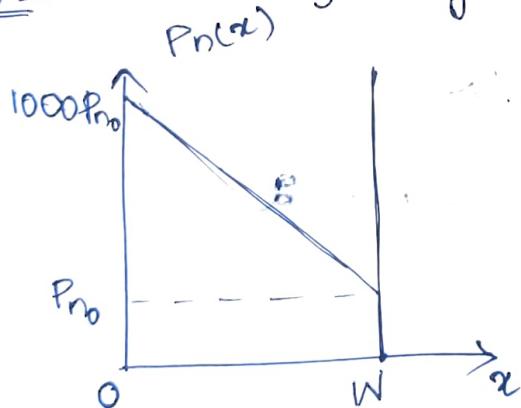
3.1

Yes, During the preparation of doped semi-conductors kirchoff's current law is applicable

KCL is a process of conservation of charge here while in the process of doping. The injected carriers contribute to the current, but total current at the injecting point is remains conserved because carriers move in theory by produces an output current that is equal to input current

In both n-type and p-type the current associated with the injected carriers is balanced by the current due to other charge carriers, by maintaining the principle of charge conservation.
Hence KCL Remains valid during process of injecting carriers in doping.

3.2



$$N_D = 10^{16} \text{ cm}^{-3} \quad \text{to find } J_{\text{diff}}, \alpha$$

$$W = 5 \mu\text{m}$$

$$n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$$

$$\frac{dp}{dx} = \frac{(1000-1)P_{no}}{W} = \frac{999P_{no}}{W} \quad \text{from graph}$$

$$(N_D)(P_{no}) = n_i^2 \quad (\text{by book})$$

$$10^{16} \times P_{n_0} = 2.25 \times 10^{20}$$

$$P_{n_0} = 2.25 \times 10^4 \text{ cm}^{-3}$$

$$J_{\text{diff}} = \frac{I}{A} = D_p \frac{dP}{dx} \cdot q$$

$$\left[k = 1.38 \times 10^{-23} \text{ J K}^{-1}, T = 300 \text{ K}, q = 1.6 \times 10^{-19} \text{ C} \right]$$

$$\frac{D_p}{\text{el}p} = \frac{kT}{q} \quad (\text{Einstein relation}) \quad \left[\begin{array}{l} \text{el}p \text{ in semi-conductors} \\ \mu_{\text{el}p} = 450 \text{ cm}^2/\text{Vs} \end{array} \right]$$

$$D_p = (26 \text{ m}^2)(450 \text{ cm}^2/\text{Vs})$$

$$D_p = 11.6 \text{ cm}^2/\text{s} \quad (10 \text{ cm}^2/\text{s} \text{ approx})$$

[Converted into SI]

$$J = 11.6 \times 10^{-4} \cdot \frac{(999) \times 2.25 \times 10^4}{5 \times 10^{-6}} \times 1.6 \times 10^{-19} \times 10^6$$

$$J = 8343.6 \times 10^{-4+4+6-19+6} \text{ A/m}^2$$

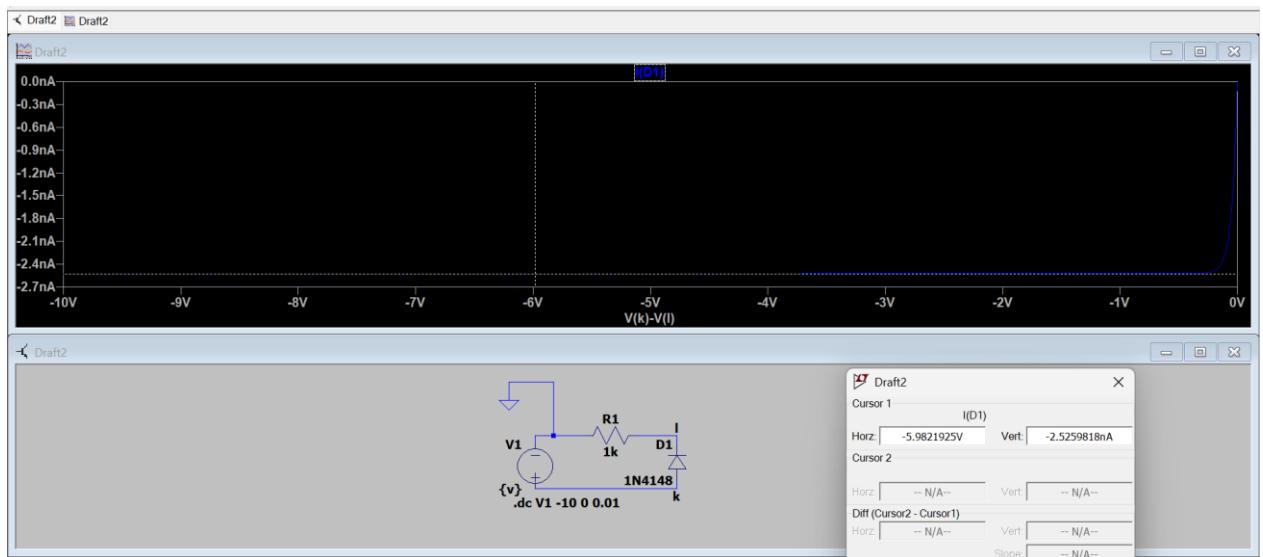
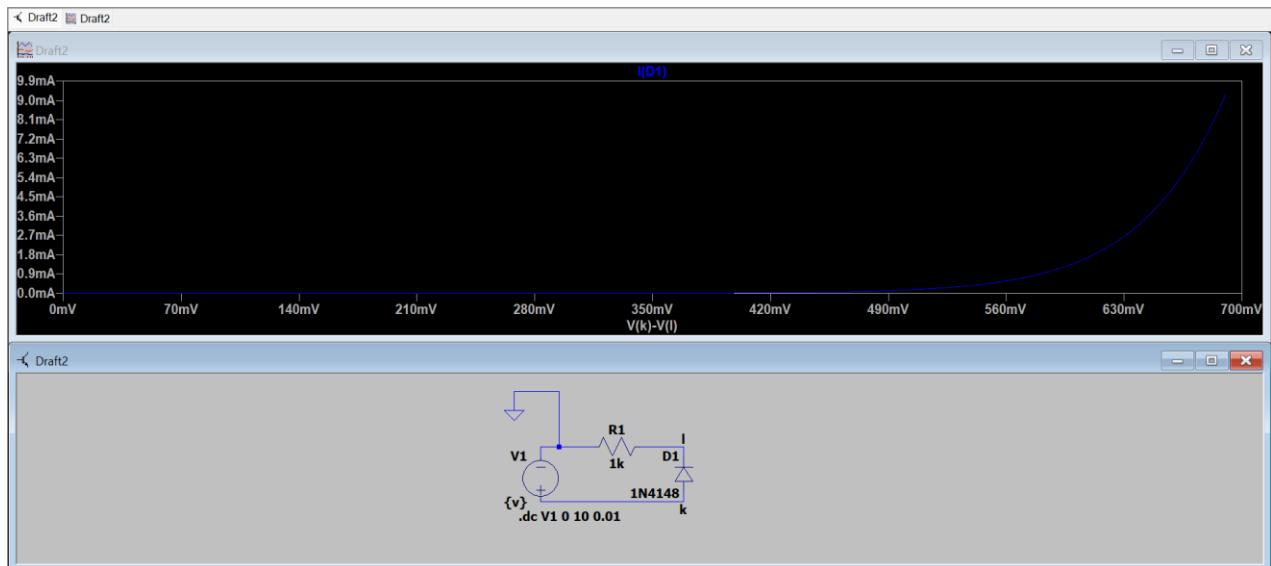
$$J = 8343.6 \times 10^{-7}$$

$$J = 8.3 \times 10^3 \times 10^{-7} \times 10^{-4} \text{ A/cm}^2$$

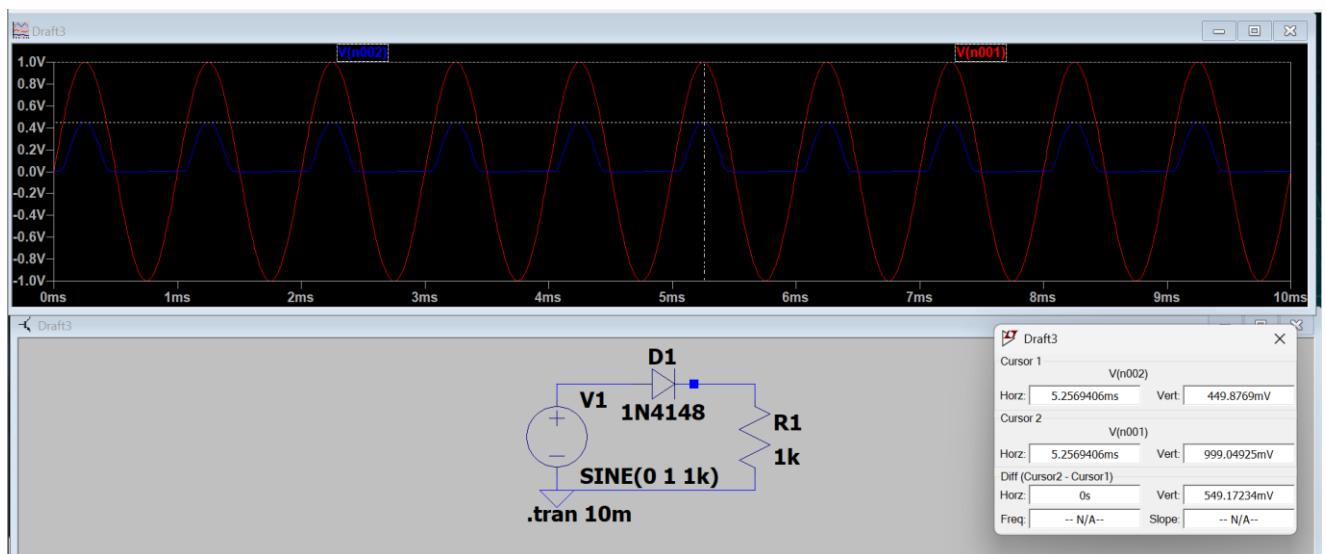
$$J = 8.3 \times 10^{-8} \text{ A/cm}^2 = 8.36 \text{ nA/cm}^2$$

$$J = 83.4 \text{ nA/cm}^2$$

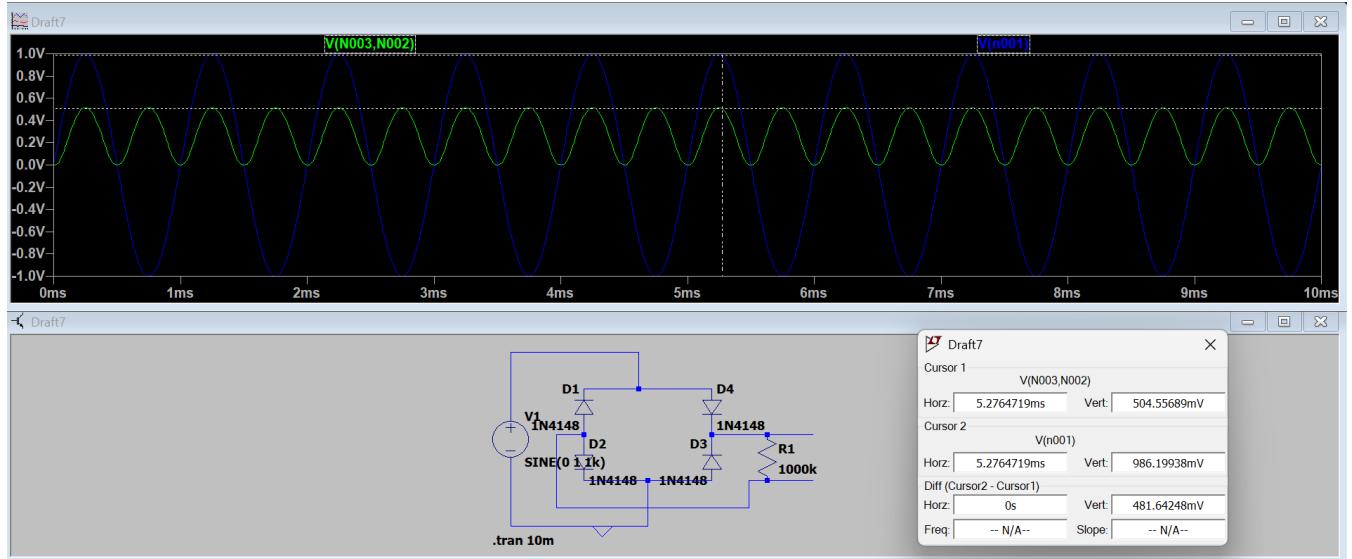
2.1



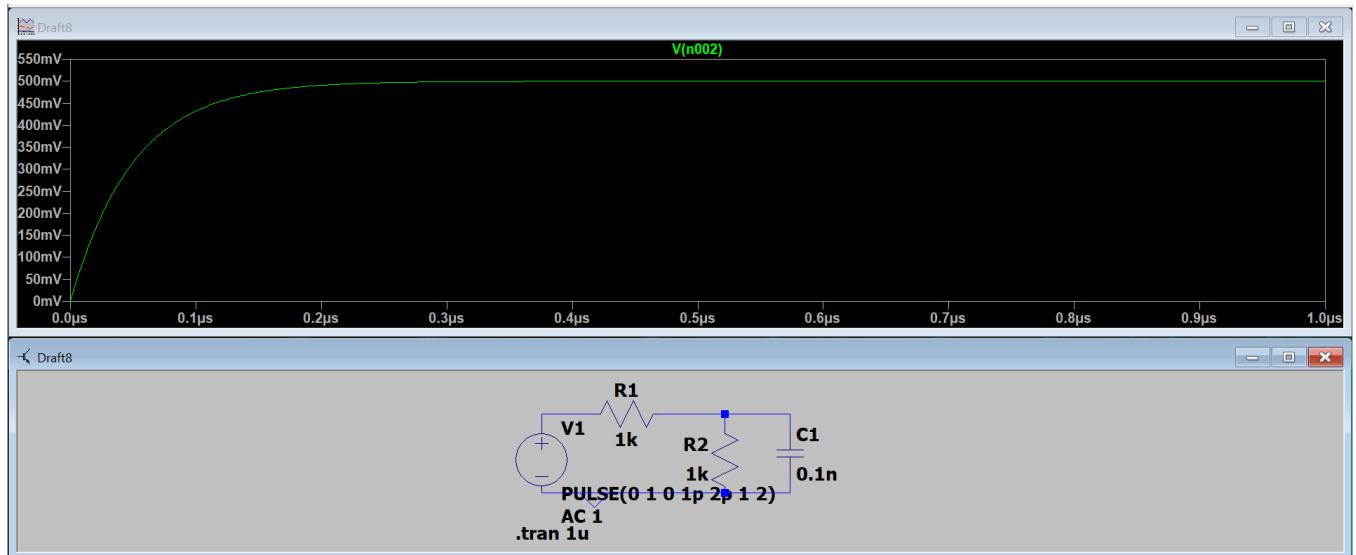
2.2

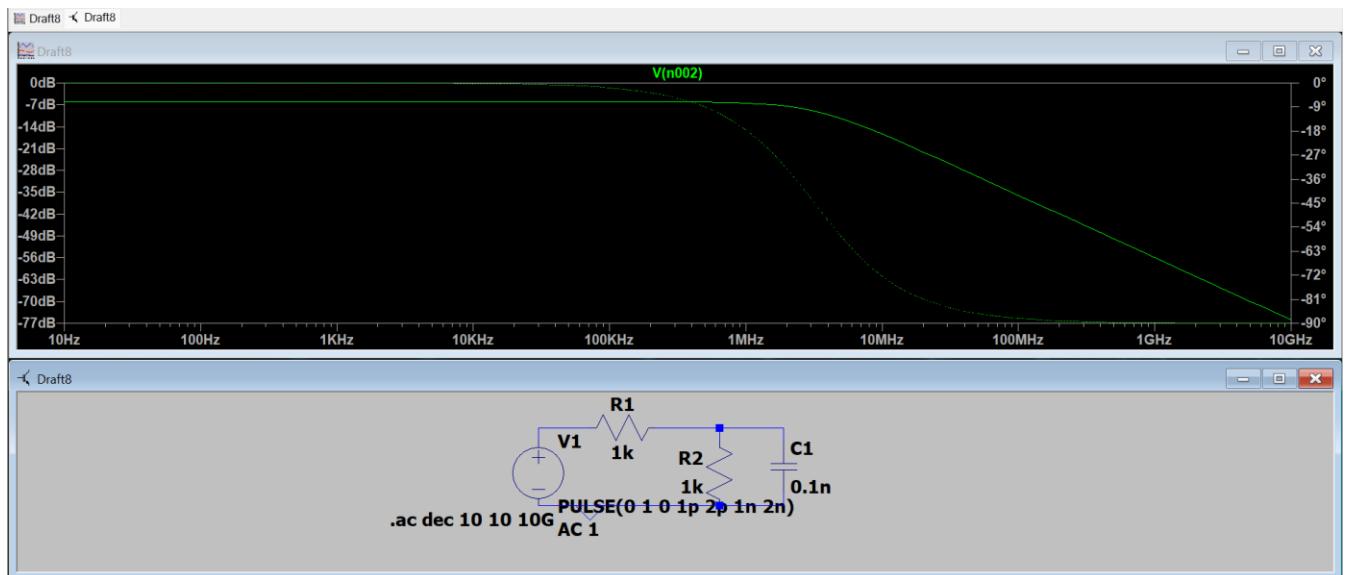


2.3

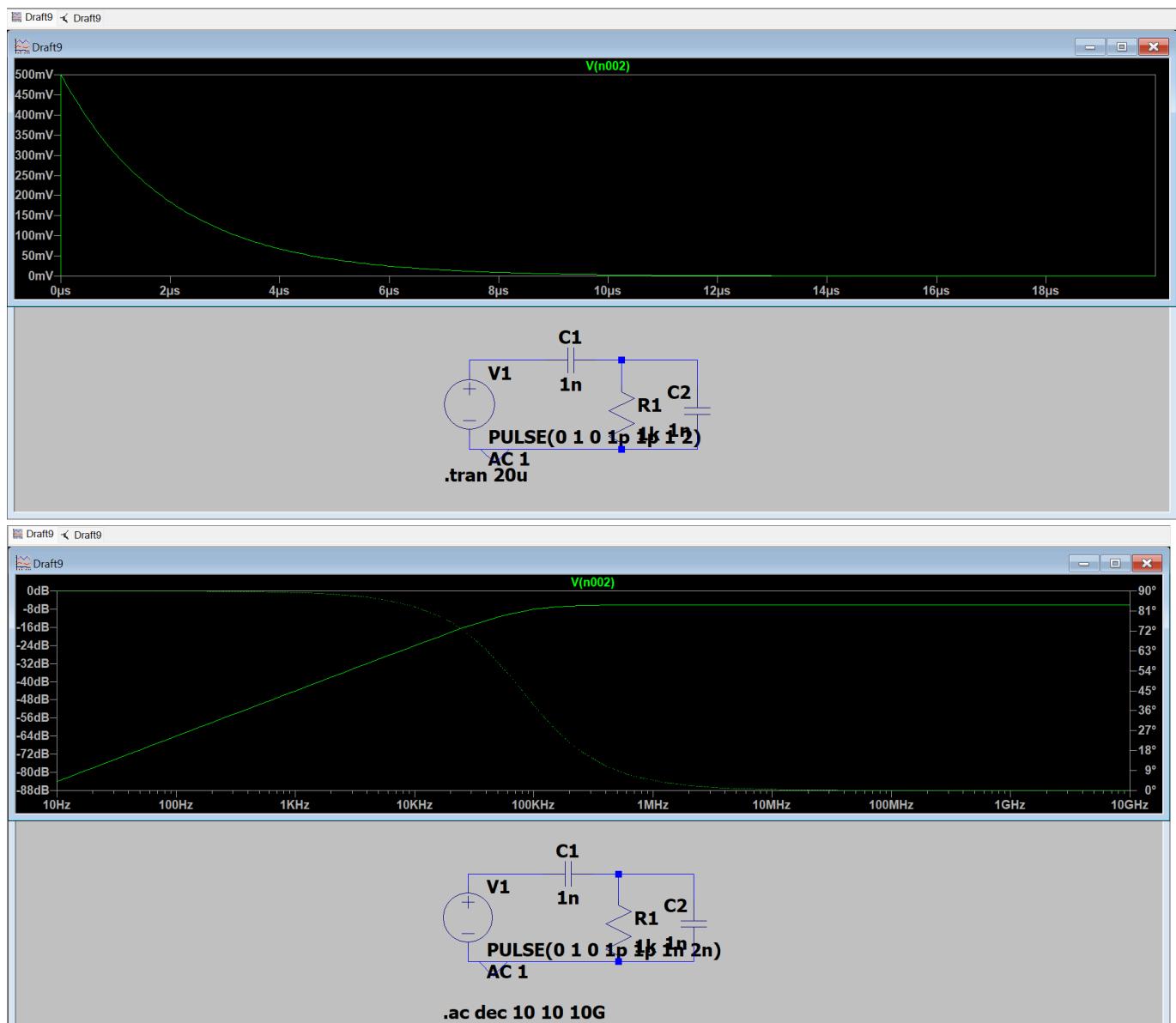


1.2 (c)

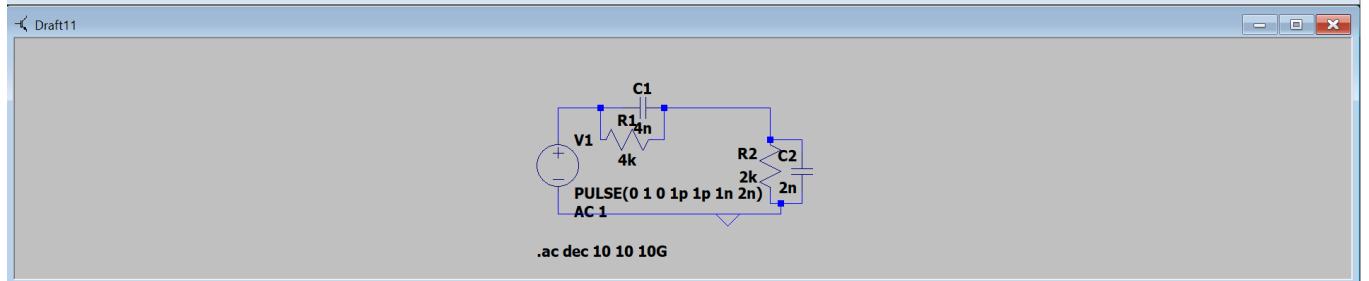
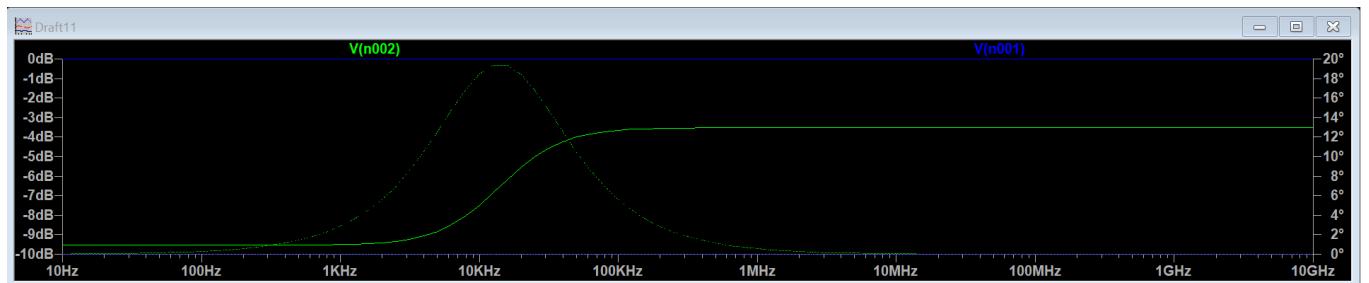
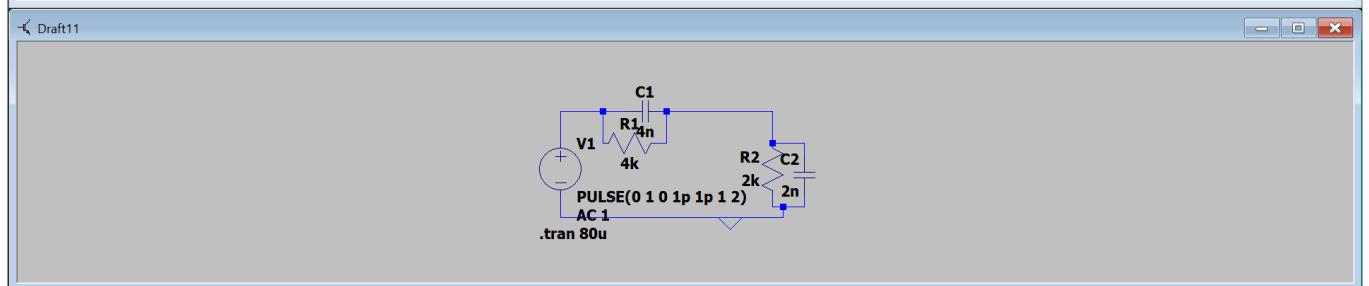
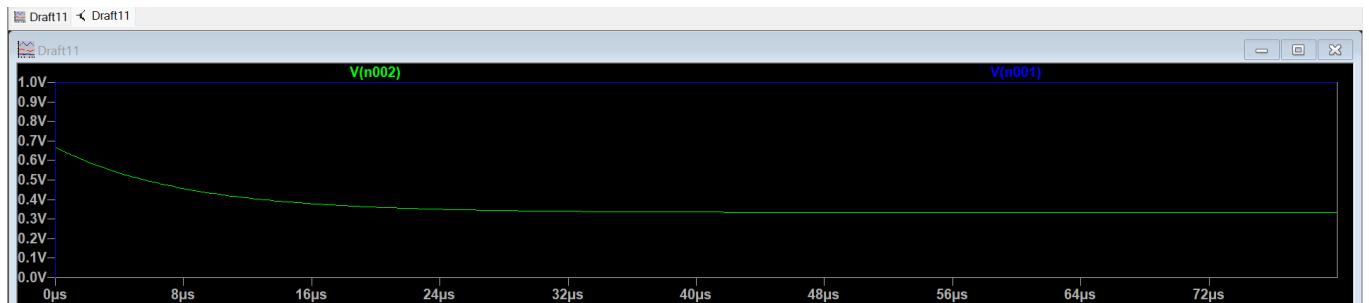




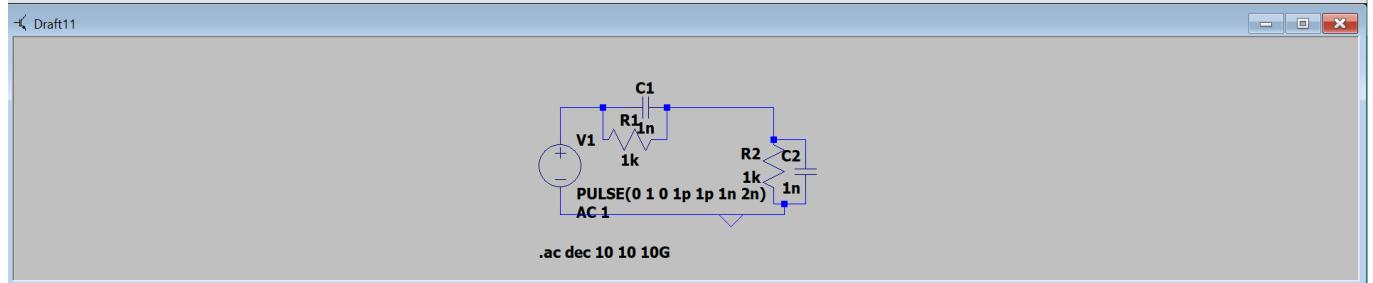
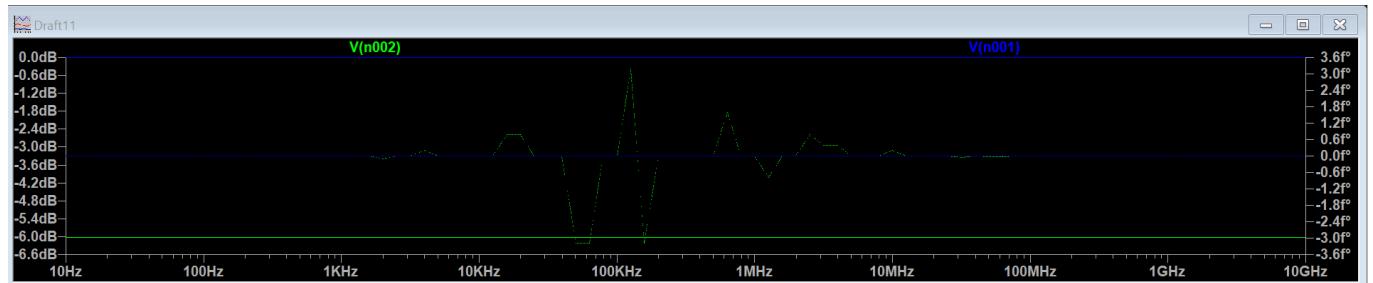
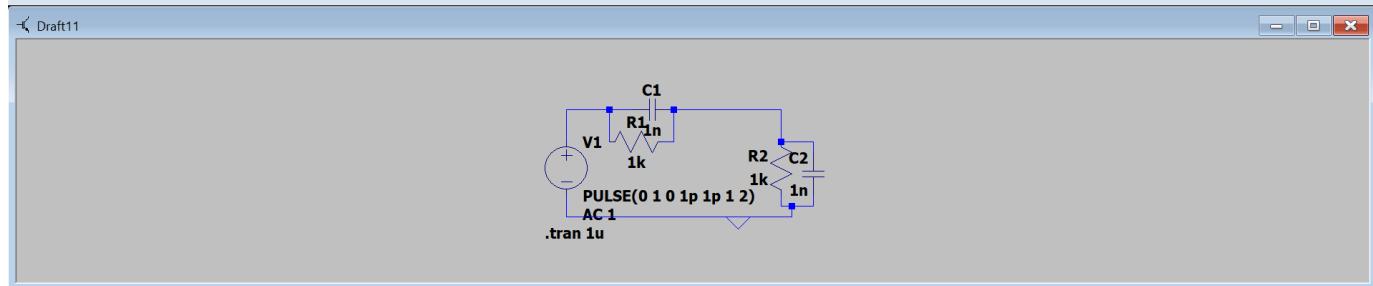
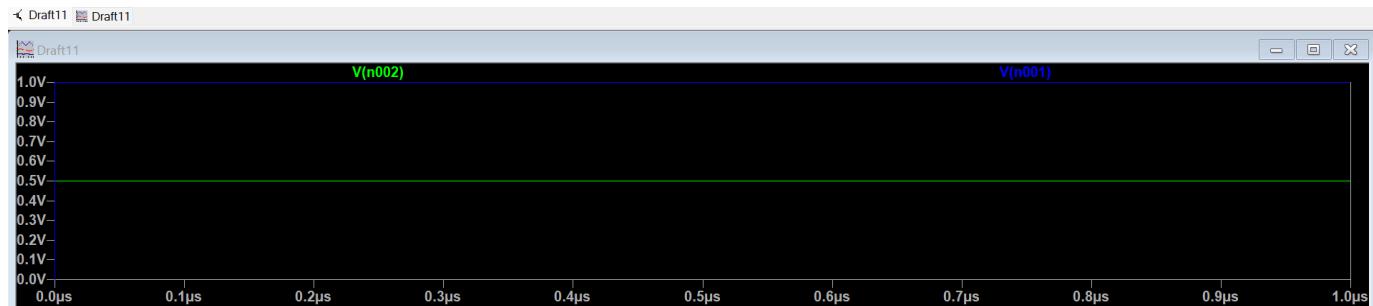
1.2 (d)



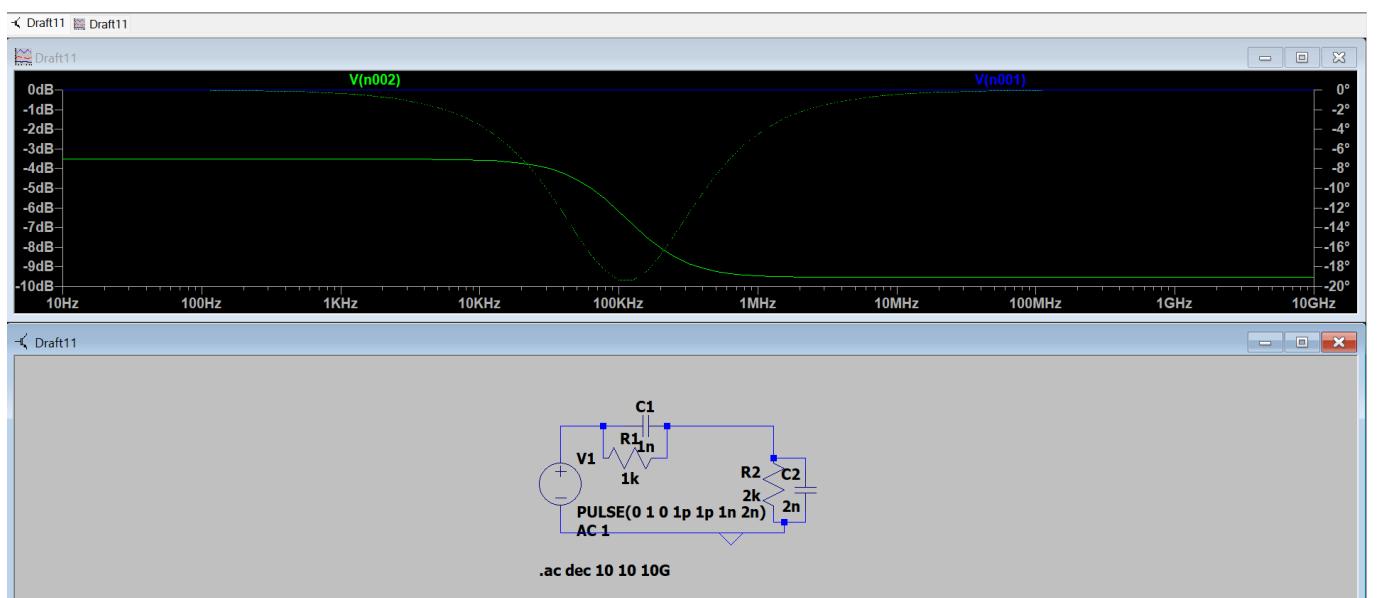
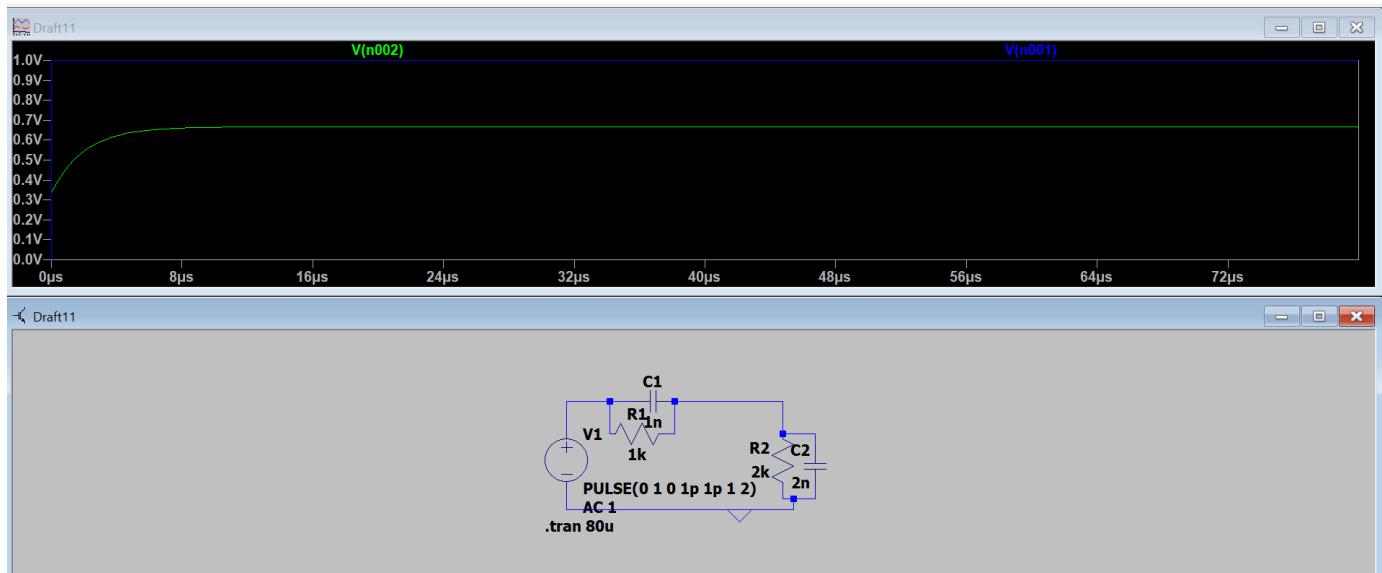
1.2 (e) R1C1>R2C2



1.2 (e) $R_1C_1=R_2C_2$



1.2 (e) R1C1<R2C2



1.2 (f)

