

# Equations Governing P-N Junction and Diode Models

## 1. Built-in Potential ( $V_{bi}$ ):

$$V_{bi} = (kT / q) * \ln(N_A * N_D / n_i^2)$$

## 2. Depletion Region Width ( $W$ ):

$$W = \sqrt{(2 * \epsilon / q) * ((N_A + N_D) / (N_A * N_D)) * (V_{bi} - V)}$$

## 3. Depletion Width on Each Side:

$$\text{P-side: } W_p = W * (N_D / (N_A + N_D))$$

$$\text{N-side: } W_n = W * (N_A / (N_A + N_D))$$

## 4. Electric Field ( $E$ ):

$$E_{max} = q * N_A * W_p / \epsilon = q * N_D * W_n / \epsilon$$

## 5. Capacitance of the Junction ( $C_j$ ):

$$C_j = \epsilon * A / W$$

$$\text{For reverse bias: } C_j = C_0 / \sqrt{1 + V_R / V_{bi}}$$

## 6. Diode Current Equation:

$$I = I_S * (\exp(qV / kT) - 1)$$

## 7. Continuity Equation:

$$\text{For holes: } (d(p)/dt) = (1/q) * \text{div}(J_p) + G - R$$

$$\text{For electrons: } (d(n)/dt) = (1/q) * \text{div}(J_n) + G - R$$

## 8. Diffusion Lengths:

$$L_p = \sqrt{D_p \cdot \tau_p}, L_n = \sqrt{D_n \cdot \tau_n}$$

#### 9. Diffusion Current and Drift Current:

$$\text{Electron diffusion: } J_{n\_diff} = q \cdot D_n \cdot (d(n)/d(x))$$

$$\text{Hole diffusion: } J_{p\_diff} = q \cdot D_p \cdot (d(p)/d(x))$$

$$\text{Electron drift: } J_{n\_drift} = q \cdot \mu_n \cdot n \cdot E$$

$$\text{Hole drift: } J_{p\_drift} = q \cdot \mu_p \cdot p \cdot E$$

#### 10. Ideal Diode Equation:

$$I = I_S \cdot (\exp(qV / kT) - 1)$$

#### 11. Dynamic Resistance ( $r_d$ ):

$$r_d = n \cdot V_T / I$$

Where  $V_T = kT / q$  (~26mV at room temperature)

#### 12. Power Dissipation:

$$P = I \cdot V$$