

**CS201c Programming Evaluation 3**  
**Instructor: Apurva Mudgal**  
**Topic: String matching using hashing**  
**Due Date: Nov 3, 2019 by 11:59 pm**

**Problem description.**

*Input Format:*

The first line is a single positive integer  $n$ .

The second line contains a bit string  $x$  of length exactly  $n$ .

The third line contains a second positive integer  $m$ .

This is followed by  $m$  lines, with  $p$ -th ( $1 \leq p \leq m$ ) line containing four positive integers  $i_p$ ,  $j_p$ ,  $k_p$ , and  $l_p$  between 1 and  $n$ :

```
i_1 j_1 k_1 l_1
i_2 j_2 k_2 l_2
.
.
.
i_m j_m k_m l_m
```

*Output Format:*

The output consists of  $m$  lines.

The  $p$ -th line has the single integer 1 if and only if substring  $x[i_p \dots j_p]$  is equal to substring  $x[k_p \dots l_p]$ . Otherwise, the  $p$ -th line has the single integer 0.

*Note.* You can use a randomized algorithm i.e., your C++ program can have a random supply of random bits using `srand()` and `rand()` functions. *Be sure to initialize your random number generator with a fresh seed using `srand()` at the start of your C++ program.*

*Hint.* Find an efficient randomized, hashing scheme for substrings such that two unequal substrings can have the same hash value only with some maximum probability.

**Requirements:**

1. *Running time.* Worst-case time taken by your C++ program should be  $O((n+m) \log_2(n))$  in the RAM model.

2. *Probability of giving a correct answer.* Further, for each  $1 \leq p \leq m$ , your C++ should satisfy the following condition:

$$\Pr [\text{the } p\text{-th line of your output is correct}] \geq 1 - (1/n)$$

3. You cannot use any in-built libraries (including standard template library). All data structures should be implemented in C++ from scratch.
4. **Collaboration is not permitted on this assignment. Your submitted code should be completely your own.**

**See section titled ``Honor Code'' in course outline already shared with you.**

**Example.**

Sample Input.

```
10
1011011011
6
1 4 7 10
2 5 7 10
2 4 5 7
2 4 8 10
3 7 6 10
1 5 6 10
```

Correct Sample Output.

```
1
0
1
1
1
0
```

*Note.* Since your C++ code is randomized, you are allowed to make an error on each output with probability at most  $\frac{1}{n} = 0.167$ .