

Recursion - 1

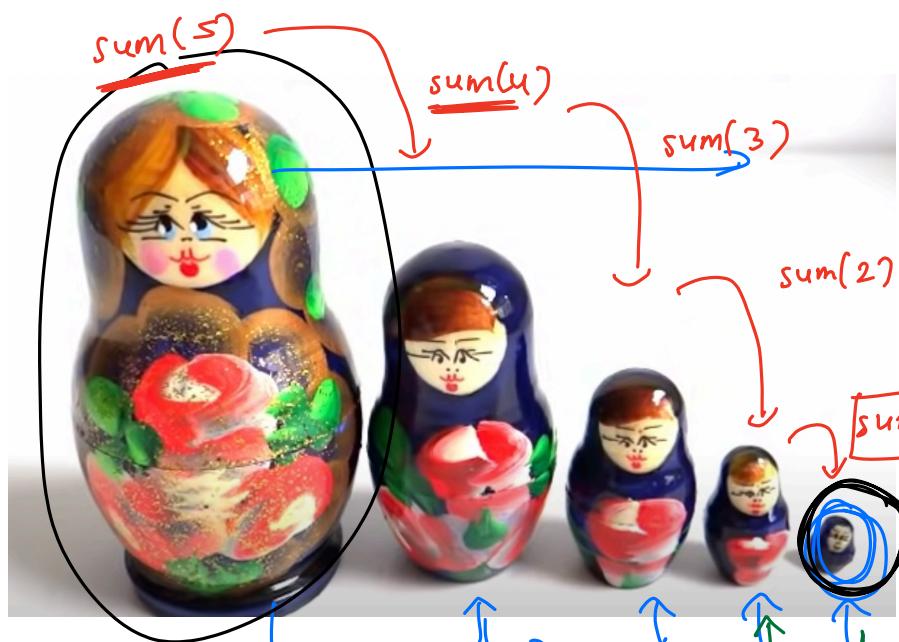
=> Python Refresher 4 -

Process on How to solve an Assignment Problem.

① What is recursion?

→ Merge sort } Adv-DFA
→ Trees }
→ Dynamic Prog. } Adv
→ Backtracking } DFA.

Video Clip => 3 observations



- 1) smaller dolls (subproblems)
- 2) Similar dolls (problem)
- 3) End doll (Base Condition)
- 4) ~~larger dolls~~

③ Stopping Condition

② Subproblems

Recursion => Solving a problem using smaller instances of the same problem.

(Q1) Sum of 1st N natural numbers. \Rightarrow Do it

using

recursion.

$$\text{sum}(3) = 1+2+3 = 6$$

$$\text{sum}(4) = \boxed{1+2+3} + 4 = 10 \Rightarrow \underline{\text{sum}(3) + 4}$$

$$\text{sum}(5) = \boxed{1+2+3+4} + 5 = 15 \Rightarrow \underline{\text{sum}(4) + 5}$$

Generalize the logic for N value

$$\text{sum}(N) = \text{sum}(N-1) + N$$

Steps of Recursion

→ Problem

① Assumption: Decide what you want your fn to do
 \Rightarrow Define the problem.

② Main Logic: Solving the assumption using subproblems.

③ Base Condition: When does the recursive function stop.

Steps of Recursion

- Problem
- ① Assumption: Decide what you want your fn to do
⇒ Define the problem.
 - ② Main Logic: Solving the assumption using subproblems.
 - ③ Base Condition: When does the recursive function stop.
- Given a num N, calc.
sum of 1st N numbers.

Calling the sum fn within itself.

```

def sum(N):
    if N == 1:
        return 1
    return sum(N-1) + N

```

→ Assumption.

→ Base Condition.

→ Main Logic

Sum(3) → sum(2) → sum(1) → sum(0) → sum(-1) ↴
Now we stop. -- --

(Q2) Factorial fact(N)
 $N = 5$

$$\begin{cases} 1 \times 10 = 10 \\ 0 + 10 = 10 \end{cases}$$

$$\text{fact}(5) = 5 \times 4 \times 3 \times 2 \times 1 = 120$$

$$\text{fact}(6) = 6 \times 5 \times 4 \times 3 \times 2 \times 1 = 720$$

$= 6 + \text{fact}(5)$

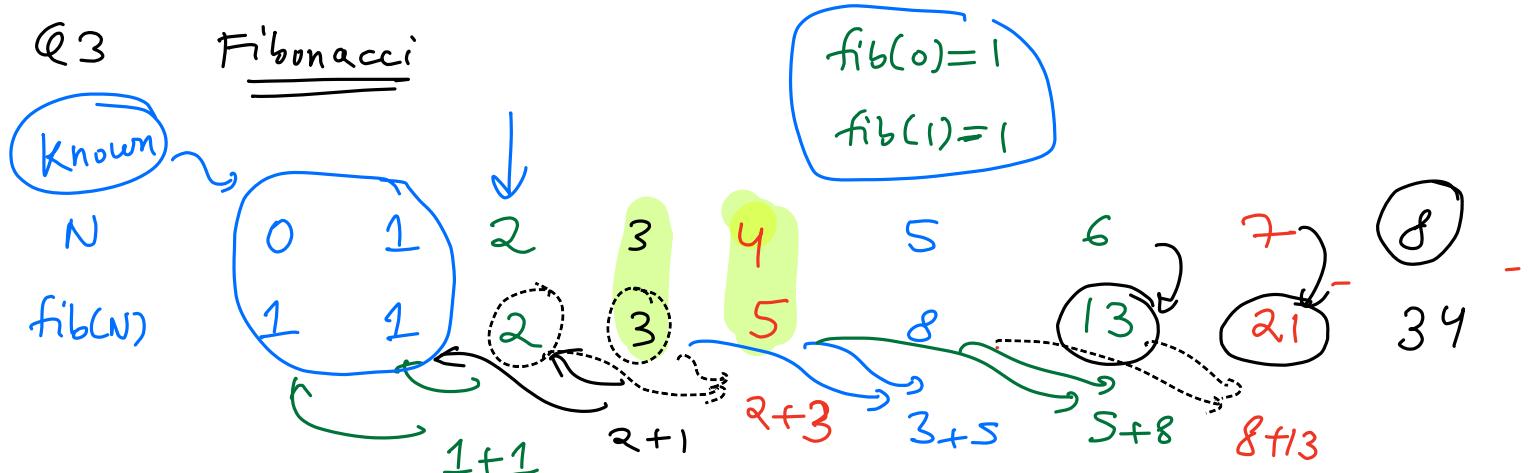
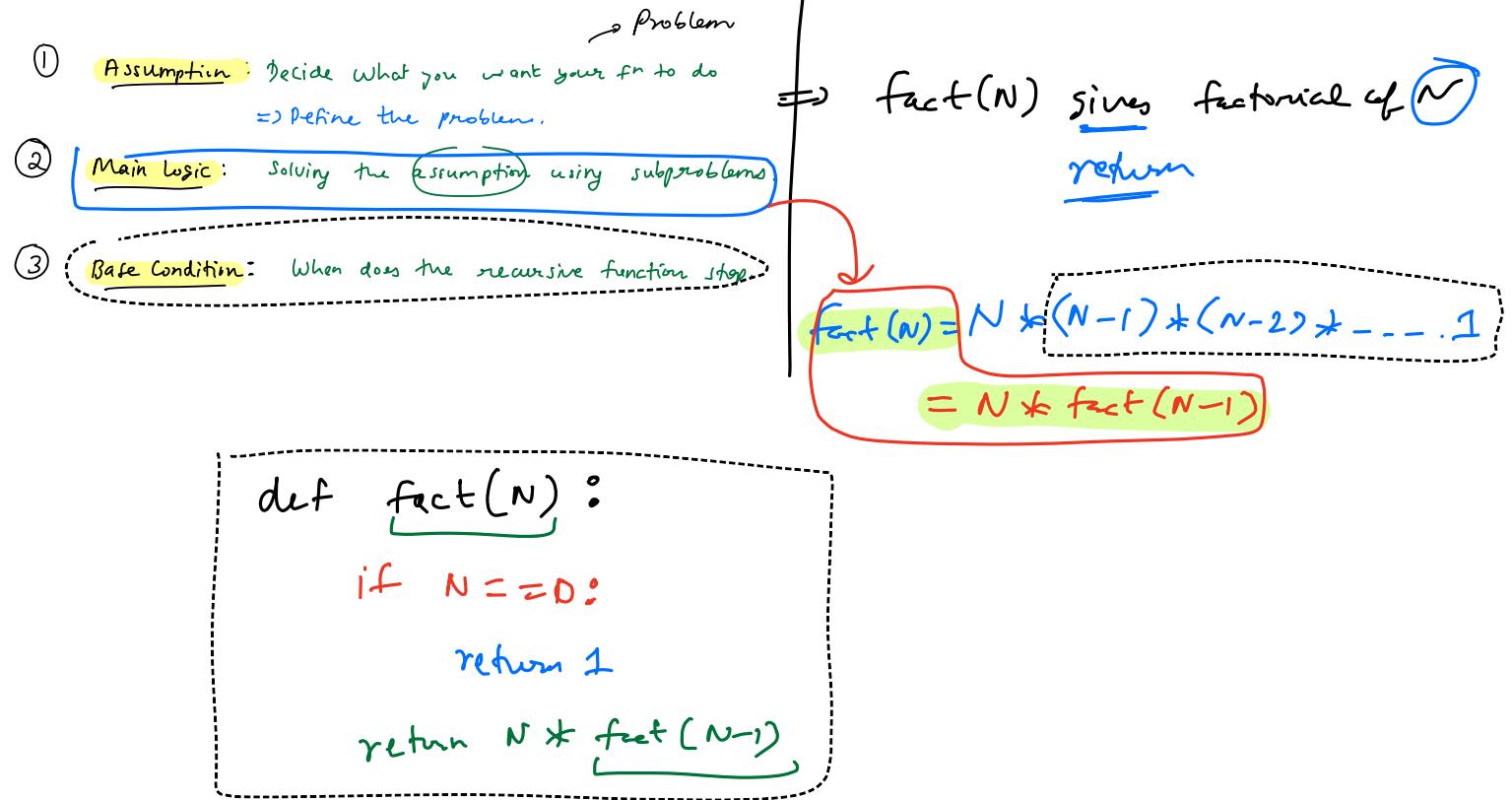
$$\text{fact}(2) = 2 \times 1 = 2$$

$$\text{fact}(3) = 3 + 2 \times 1 = 6$$

$= 3 + \text{fact}(2)$

$$\text{fact}(1) = 1$$

$$\text{fact}(0) = 1$$



$$\text{fib}(8) = \text{fib}(7) + \text{fib}(6)$$

$$\text{fib}(5) = \text{fib}(4) + \text{fib}(3) = 5 + 3 = 8.$$

$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$

$$= 21 + 13$$

$$= 34$$

```

def fib(N):      # return Nth fib.
    if N==0 Or N==1:
        return 1
    return fib(N-1) + fib(N-2)

```

Steps of Recursion

- ① Assumption: Decide what you want your fn to do
→ Problem
⇒ Define the problem.
- ② Main Logic: Solving the assumption using subproblems.
- ③ Base Condition: When does the recursive function stop.

Flow of

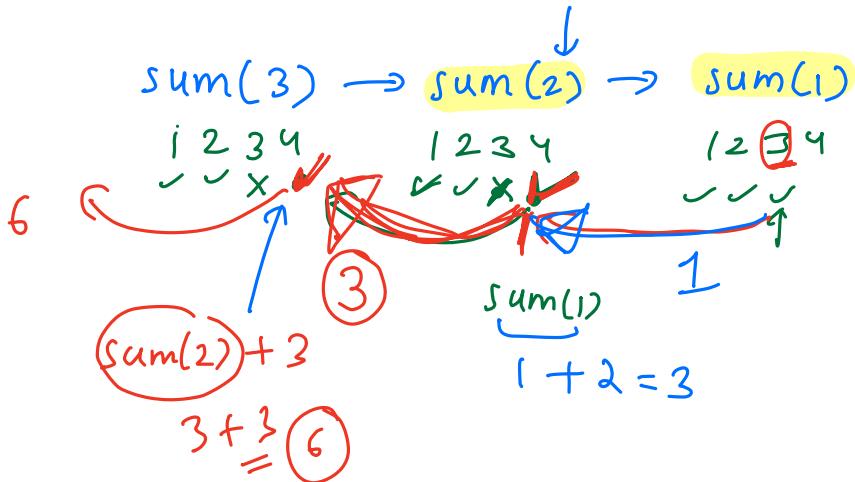
Recursion.

```

1 → def sum(N):
2   →     if N==1:
3   →         return 1
4   →     return sum(N-1) + N

```

→ Assumption.
} Base Condition
⇒ Main Logic



print 1-N
↳ 1, 2, 3, ..., N
→ Using rec.

Python Tutor code visualizer: v + pythontutor.com/render.html#mode=display

Python Tutor: Visualize code in Python, JavaScript, C, C++, and Java

```
Python 3.6
(known limitations)

1
2 def fact(n): # assumption
3     if n == 0: # base condition
4         return 1
5     return n * fact(n - 1) # main logic
6
7 print(fact(3))
```

[Edit this code](#)

→ line that just executed
→ next line to execute

<< First < Prev Next > Last >>

Step 15 of 18

[Customize visualization](#)

Print output (drag lower right corner to resize)

Frames Objects
Global frame function
fact fact(n)

fact

n 3

Wait on S line

fact

n 2

Wait on line S

fact

n 1

Wait on line S

fact

n 0

Return value

1

Base

$f(3) \rightarrow f(2) \rightarrow f(1) \rightarrow f(0)$

1

$f(3) \rightarrow f(2) \rightarrow f(1) \rightarrow f(0)$

1

Python 3.6
(known limitations)

```
1
2 def fact(n): # assumption
3     if n == 0: # base condition
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Step 15 of 18

[Customize visualization](#)

Print output (drag lower right corner to resize)

Frames Objects
Global frame function
fact fact(n)

fact

n 3

Wait on S line

fact

n 2

Wait on line S

fact

n 1

Wait on line S

fact

n 0

Return value

1

Base

$f(3) \rightarrow f(2) \rightarrow f(1) \rightarrow f(0)$

1

$f(3) \rightarrow f(2) \rightarrow f(1) \rightarrow f(0)$

1

Target: Confident
in writing
recursive codes.

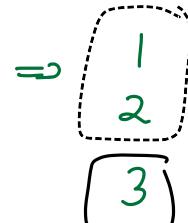
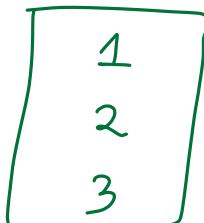
(Q4)

Print Increasing

Given N , print nums from 1 to N using recursion.

$N=3$

Output

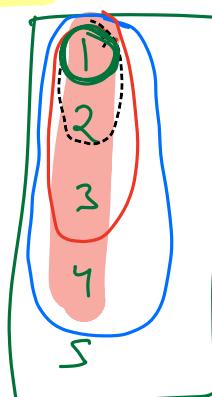


inc(2)
print(3)

$N=5$

Output

inc(5)



def inc(5):

 inc(4)

 print(5)

 inc(3)

 print(4)

 inc(2)

 print(3)

 inc(1)

 print(2)

Base

inc(5)

def inc(n):

 if n==1:

 print(1)

 inc(n-1)

 print(n)

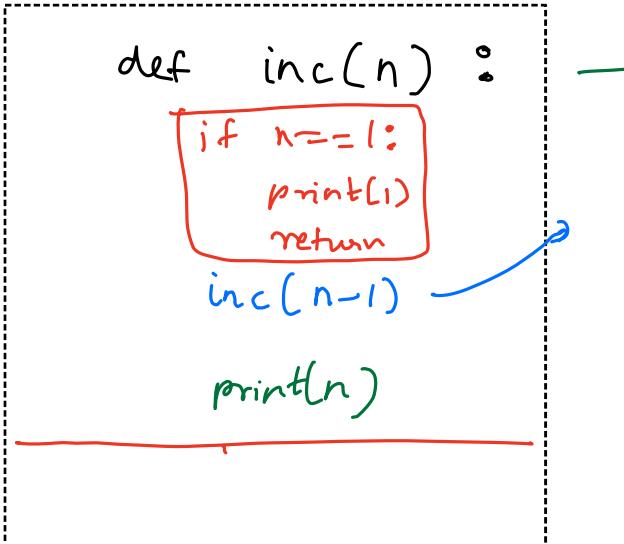
print from 1 to n in inc.order

my subordinate

print from 1 to (n-1)

inc(5) → inc(4) → inc(3) → inc(2) → inc(1) → inc(0) → inc(-1)

inc(-n)
↓



Python 3.6
(known limitations)

```

1 def inc(n): # assumption
2     if n == 1: # base case
3         print(1)
4     ↗ return # main logic below
5     # does return None
6     inc(n - 1)
7     print(n)
8
9 inc(5)

```

[Edit this code](#)

line that just executed
next line to execute

<< First < Prev Next > > Last >

Step 19 of 27

Customize visualization

Print output (drag lower right corner to resize)

1

Frames Objects

Global frame inc ↗ function inc(n)

inc n 5

inc n 4

inc n 3

inc n 2

inc n 1 Return value None

HW: Print from N to 1 using recursion

→ Do your assignments on recursion.

Recap

⇒ Problem Solving Session on Sat, Sep 10, 9pm

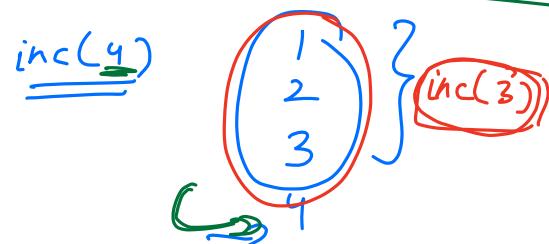
Time Complexity + Python Refresher + Sorting

- least solved ones
- You have mentioned on Slack.

1 hr / 2hr / 3hr

Doubts

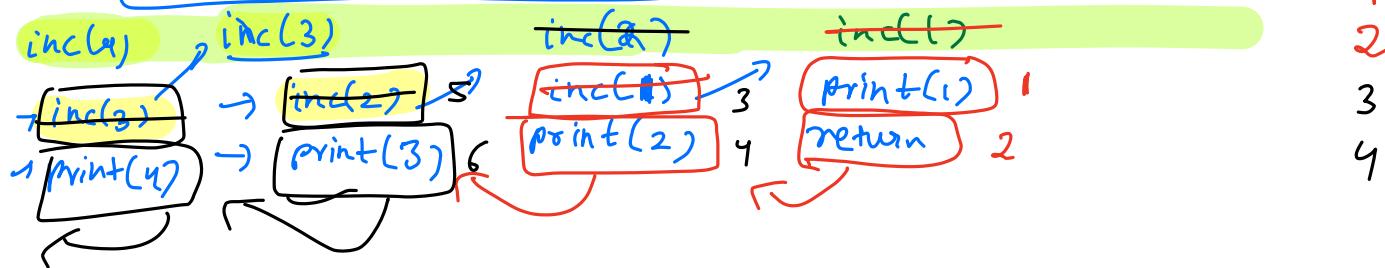
- ① Inc. Print (Return)
→ ② Flow of sum function



```
1 def inc(n):  
2     if n==1:  
3         print(n)  
4         return  
5     inc(n-1)  
6     print(n)
```

print from 1 to n

print from 1 to (n-1)



A screenshot of a Python debugger showing the execution of `inc(5)`. The code is:

```

def inc(n):
    if n == 1:
        print(1)
        return 5
    x = inc(n - 1)  # variable x: Literal[5] | None
    print("----", x)
    print(n)
    return

```

The current frame is `[8] inc(5)`. The stack trace shows:

- 1
- 5
- None
- 3
- None
- 4
- None
- 5

Annotations include:

- `x = inc(n - 1)` highlighted with a yellow box.
- `print("----", x)` highlighted with a yellow box.
- `return` highlighted with a yellow box and labeled "by default".
- `dark statement is return.` handwritten note.
- `inc(5)` at the top with a green arrow pointing down to `inc(4)`.
- `inc(4)` with a green arrow pointing down to `inc(3)`.
- `inc(3)` with a green arrow pointing down to `inc(2)`.
- `inc(2)` with a green arrow pointing down to `inc(1)`.
- `inc(1)` with a green arrow pointing down to `print(1)`.
- `print(1)` with a green arrow pointing down to `return`.
- `return` with a green arrow pointing down to the next frame.
- `Output` on the right with a green arrow pointing down to the stack trace.
- `x = None` handwritten note near `x` in the code.
- `None` handwritten note near the first `None` in the stack trace.
- `5` handwritten note near the last `5` in the stack trace.
- `2` handwritten note near the second `None` in the stack trace.

```

Python 3.6
(known limitations)

1 def sum(N):
2     if N == 1:
3         return 1
4
5     return sum(N - 1) + N
6
7 print(sum(4))

```

[Edit this code](#)

→ line that just executed
→ next line to execute

[<< First](#) [< Prev](#) [Next >](#) [Last >>](#)

Done running (18 steps)

[Customize visualization](#)

