

T.E./Insem.-623
T.E. (E & TC) (Semester - I)
ELECTROMAGNETICS
(2015 Pattern)

Time : 1 Hour]

[Max. Marks : 30

Instructions to the candidates:

- 1) Answer Q.1 or Q.2, Q.3 or Q.4, Q.5 or Q.6.
- 2) Neat diagrams must be drawn wherever necessary.
- 3) Figures to the right side indicate full marks.
- 4) Use of calculator is allowed.
- 5) Assume suitable data if necessary.

Q1) a) A uniform line charge of $4\mu\text{C}/\text{m}$ is located on the y axis. Find \vec{E} in Cartesian coordinates at P(3, 1, 2) if the charge extends from: **[6]**

- i) $-\infty < y < \infty$,
- ii) $-5 < y < 10$.

b) Derive an expression for the potential difference V_{AB} between point A and B, in presence of an uniform line charge with charge density ρ_L lying on entire Z-axis ($-\infty$ to ∞). **[4]**

OR

Q2) a) Using Gauss's Law, derive an expression for electric field intensity (\vec{E}) at point P in free space, due to infinite surface charge with charge density ρ_s , placed on entire $Z = 0$ plane. Consider point P towards positive side of $Z = 0$ plane. **[6]**

b) Four infinite uniform sheets of charge are located as follows $20\text{ pC}/\text{m}^2$ at $y=7$, $-8\text{ pC}/\text{m}^2$ at $y=3$, $6\text{ pC}/\text{m}^2$ at $y=-1$ and $-18\text{ pC}/\text{m}^2$ at $y=-4$.

Find \vec{E} at the point :**[4]**

- i) A (2, 6, -4),
- ii) B (0, 0, 0),
- iii) C (-1, -1.1, 5).

P.T.O.

Q3) a) Derive electrostatic boundary conditions for the boundary between two perfect dielectric materials. [6]

b) Let $\epsilon_{r1} = 2.5$ for $0 < y < 1$ mm, $\epsilon_{r2} = 4$ for $1 < y < 3$ mm, and ϵ_{r3} for $3 < y < 5$ mm. Conducting surfaces are present at $y = 0$ and $x = 5$ mm. Calculate the capacitance per square meter of surface area if : [4]

i) ϵ_{r3} is that of air;

ii) $\epsilon_{r3} = \epsilon_{r1}$;

iii) $\epsilon_{r3} = \epsilon_{r2}$;

iv) region 3 is silver.

OR

Q4) a) Derive an expression for energy stored in an electrostatic field in terms of \bar{D} & \bar{E} . [6]

b) Two extensive homogeneous isotropic dielectrics meet on plane $z = 0$. For $z > 0$, $\epsilon_{r1} = 4$ and $z < 0$, $\epsilon_{r2} = 3$. A uniform electric field $\bar{E}_1 = 5\hat{a}_x - 2\hat{a}_y + 3\hat{a}_z$ kV / m exists for $z \geq 0$. [4]

Find : i) \bar{E}_2 for $z \leq 0$;

ii) The angle which E_1 makes with the interface;

iii) The energy densitie (in J/m³) for $z > 0$.

Q5) a) i) Find \bar{H} in Cartesian components at P(2, 3, 4) if there is a current filament on the z axis carrying 8mA in the \bar{a}_z direction.

ii) Repeat if the filament is located at $x = -1, y = 2$. [6]

b) Write Maxwell's equation in point form and integral form for static electric and steady magnetic fields. [4]

OR

Q6) a) Let $\bar{H} = 15r\bar{a}_\phi$ mA / m.

i) Determine current enclosed by the circular path $r = 5$, $\theta = 25^\circ$, $0 \leq \phi \leq 2\pi$ by using line integral side of Stokes theorem.

ii) Determine current by surface integral side of Stokes theorem. [6]

b) State and prove Ampere Circuital Law. [4]

