Seat	
No.	

[5057]-2042

S.E. (E&TC/Electronics) (First Semester)

EXAMINATION, 2016

SIGNALS AND SYSTEMS

(2015 **PATTERN**)

Time: Two Hours

Maximum Marks: 50

- **N.B.** :— (i) Attempt Q. 1 or Q. 2, Q. 3 or Q. 4, Q. 5 or Q. 6 and Q. 7 or Q. 8.
 - (ii) Figures to the right indicate full marks.
 - (iii) Neat diagrams must be drawn wherever necessary.
 - (iv) Assume suitable data, if necessary.
- 1. (a) Find whether the following signals are energy or power and find the corresponding value: [4]

$$x(t) = (\frac{1}{2})^n \cdot u[n]$$

(b) Find the convolution between :

[4]

$$x[n] = \{1, 1, 1, 1\}$$
 and

$$h[n] = \{1, 1, 1, 1\}$$

(c) Find odd and even components of the signal: [4]

$$x[n] = u[n] - u[n-4].$$

2. (a) An analog signal is given by the equation :

 $x(t) = 2 \sin 400\pi t + 10 \cos 1000\pi t$.

It is sampled at sampling frequency 1000 Hz.

- (i) What is the Nyquist rate for the above signal?
- (ii) What is the Nyquist interval of the signal? [2]
- (b) Find the convolution between:

$$x(t) = u(t)$$
 and

$$h(t) = u(t-2)$$

using graphical method.

(c) Check whether the following signal is periodic or non-periodic.

If periodic, find period of the signal: [4]

[6]

$$x(t) = \cos(n / 8) \cdot \cos(n\pi / 8).$$

- 3. (a) State and explain the properties of Continuous Time Fourier Series. [6]
 - (b) Determine the transfer function and impulse response for the system described by the differential equation shown below for zero initial conditions:

$$d / dt [y(t)] + 3 y(t) = x(t)$$
.

4.	(a)	Draw	the	magnitude	and	phase	spectrum	of	the	signal	: [6]		
$x(t) = 5\cos(2\pi 10t + 30) - 10\cos(2\pi 20t + 60).$													

(b) Find the Fourier transform of the signal : [6] $x(t) = \sin \omega_c t. u(t).$

- **5.** (a) State and prove convolution property of Laplace transform. [6]
 - (b) Find the initial and final value of: [7]

$$X(s) = 5s + 50 / s(s + 5)$$
.

Or

6. (a) Find the Laplace transform of the given signal and draw its ROC:

$$x(t) = -e^{at}u(-t).$$

(b) Find the inverse Laplace transform of: [7]

$$X(s) = 3s + 7 / (s^2 - 2s - 3).$$

- 7. (a) List the properties of auto correlation and cross correlation for energy signals. [6]
 - (b) A perfect die is thrown. Find the probability that: [7]

P.T.O.

- (i) You get even number.
- (ii) You get a perfect square.

- **8.** (a) List the properties of probability. Explain conditional probability with an example and formula. [6]
 - (b) A three digit message is transmitted over a noisy channel having a probability of error as P(E) = 2/5 per digit. Find and draw the CDF. [7]