

[5460] - 591

T.E. (IT)

# THEORY OF COMPUTATION (2015 Pattern)

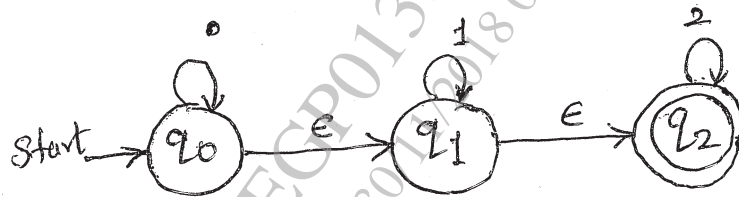
Time : 2½ Hours]

[Max. Marks : 70

Instructions to the candidates:

- 1) Answer Q.1 or Q.2, Q.3 or Q.4, Q.5 or Q.6, Q.7 or Q.8, Q.9 or Q.10.
- 2) Neat diagrams must be drawn wherever necessary
- 3) Figures to the right, indicate full marks
- 4) Assume suitable data, if necessary

**Q1)** a) Convert the NFA with  $\epsilon$  moves, for the following Transition Diagram, into its equivalent DFA. [8]



b) State properties & limitations of FSM. [2]

OR

**Q2)** a) Find the regular expression for the language [6]

- i) Consisting of all strings of a's & b's without any combination of double letters.
- ii) over  $\Sigma = \{a, b\}$  containing at least one 'a' & at least one 'b'.
- iii) Consisting of set of all strings that start with 'a' and do not have two consecutive 'b's.

b) Construct Transition Graph for the following regular expression. [4]

$$r = 1^* \cdot 0 \cdot 0 \cdot (0 + 1)^*$$

P.T.O.

- Q3) a)** Write a context free language (CFL) for the following CFG. [6]
- i)  $S \rightarrow OSO \mid A \mid \epsilon$   
 $A \rightarrow 1SO \mid \epsilon$
- ii)  $S \rightarrow aSc \mid A \mid \epsilon$   
 $A \rightarrow aAb \mid \epsilon$
- b) Eliminate  $\epsilon$  - productions from the given Grammar consisting of following productions [4]
- $S \rightarrow aSa \mid bSb \mid \epsilon$
- OR
- Q4) a)** Convert the following grammar G to GNF [8]
- $G = \{(A_1 A_2 A_3), (a, b), P, A_1\}$
- Where P consists of the following productions :
- $A_1 \rightarrow A_2 A_3$   
 $A_2 \rightarrow A_3 A_1 \mid b$   
 $A_3 \rightarrow A_1 A_2 \mid a$
- b) State applications of Context - free Grammar. [2]
- Q5) a)** Define PDA. Construct PDA that accepts the following language. [8]
- $L = \{a^n b^n \mid n > 0\}$
- Simulate for  $\omega = aaabb$
- b) Construct a PDA that accepts the following language. [8]
- $L = \{X, aXa, bXb, aaXaa, abXba, \dots\}$
- OR
- Q6) a)** Construct PM that multiplies two unary numbers write simulation for [10]
- i) aa.a  
 ii) aaa.aaa
- b) Give difference between PDA & PM. [6]
- Q7) a)** Design a TM that recognizes strings containing equal no. of 0's & 1's Write simulation for any two input strings. [9]
- b) Design a TM that recognizes binary palindromes. Write simulation for any two input strings. [9]

OR

- Q8)** a) Design TM that finds the Greatest Common Divisor (GCD) of two given numbers. Find GCD of 4 & 2. [12]  
b) Write short note on types of TM. [6]

- Q9)** a) Prove that.  
 $PCP = \{ \langle p \rangle \mid p \text{ is an instance of the Post Correspondence problem with a match} \}$ . [10]  
b) Write short note on p - class with examples. [6]

OR

- Q10)** a) Prove that following are decidable languages. [10]  
i)  $A_{NFA} = \{ \langle B, \omega \rangle \mid B \text{ is an NFA that accepts input string } \omega \}$   
ii)  $A_{REG} = \{ \langle R, \omega \rangle \mid R \text{ is a regular expression that generates string } \omega \}$   
b) Explain computational complexity with example. [6]

