

Lab 3 (8 Sep 2020)

Problem 1 [Karatsuba's algorithm] Write a program to read in two strings representing two binary numbers and to compute their product using Karatsuba's Divide and Conquer multiplication algorithm. You may assume that both the input strings have the same length.

Problem 2 [Counting Inversions]: An *inversion* in a sequence A of numbers is a pair of indices (i, j) such that $i < j$ and $A[i] > A[j]$. For e.g. the number of inversions in 1,3,9,8,5 is 3 while that in 4,10,8,2,1 is 8. Implement a $O(n \log n)$ *Divide and Conquer algorithm* to count the total number of inversions in an input sequence. You should verify that your output is correct by comparing it with the output of the naive program.

Problem 3 [Maximum sum sub-array]: Given an array A of integers write a program to return indices (i, j) ($0 \leq i < j \leq n-1$) such that the sum $A[i] + A[i+1] + \dots + A[j]$ is maximum for all sub-arrays. For e.g. if $A = [-2, 10, -4, 12, -9]$, then $i=1, j=3$ would give the maximal sum $(10 + (-4) + 12 = 18)$. Your algorithm should run in $O(n \log n)$ time.

Hint: Think of a divide-and-conquer strategy. You can implement a naive $O(n^2)$ algorithm to check the correctness of your divide-and-conquer algorithm.

Problem 4 [Selection Problem]: Implement the deterministic and randomized version of the Divide and Conquer selection algorithm.