

Started on	Thursday, 17 September 2020, 10:20 AM
State	Finished
Completed on	Thursday, 17 September 2020, 10:49 AM
Time taken	29 mins 22 secs
Marks	11/20
Grade	6 out of 10 (55%)

Question **1**

Incorrect

Mark 0 out of 2

Which of the following statements are TRUE?

Select one or more:

- ☒  $n^{0.1} = \Omega((\log n)^8)$
- ✓
- ☒  $n^{1.01} = O(n \log^2 n)$
- ✗
- ☒  $2^n = \Theta(2^{n+1})$
- ✓
- ☒  $\log 2n = \Omega(\log 3n)$
- ✓

Your answer is incorrect.

The correct answers are:  $n^{0.1} = \Omega((\log n)^8)$

,  $\log 2n = \Omega(\log 3n)$

,  $2^n = \Theta(2^{n+1})$

Question **2**

Incorrect

Mark 0 out of 1

If  $f(n) = n^{1/2}$  and  $g(n) = 5^{\log_2 n}$ , then

Select one or more:

- ☐ None of the others
- ☒  $f(n) = O(g(n))$
- ✓
- ☐  $f(n) = o(g(n))$
- ☐  $f(n) = \Omega(g(n))$

Your answer is incorrect.

The correct answers are:  $f(n) = O(g(n))$

,  $f(n) = o(g(n))$

Question **3**

Incorrect

Mark 0 out of 1

If  $\sum_{i=0}^n i^2 = X$  then X is

Select one or more:

- ☒  $o(n^4)$
- ✓
- ☐  $\Theta(n^3)$
- ☐  $\Theta(n^2)$
- ☐  $\Omega(n^3)$

Your answer is incorrect.

The correct answers are:  $\Theta(n^3)$

,  $o(n^4)$

Question **4**

Incorrect

Mark 0 out of 1

If  $C(n)$  denotes the worst case runtime and  $D(n)$  denotes the average case runtime of an algorithm, then which of the following is always true?

Select one or more:

- ☒  $C(n) = o(D(n))$
- ✗
- ☐  $C(n) = \Theta(D(n))$
- ☒  $C(n) = \Omega(D(n))$
- ✓
- ☐ None of the others

Your answer is incorrect.

The correct answer is:  $C(n) = \Omega(D(n))$

Question **5**

Incorrect

Mark 0 out of 1

What is the runtime of the following procedure?

 $\text{foo}(n)$ 

if  $(n \leq 2)$  then return 1 else return  $\text{foo}(\sqrt{n})$

Select one or more:

☒  $O(n)$ 

✗

☐  $O(\log n)$ ☐  $O(\log \log n)$ ☐  $O(1)$ 

Your answer is incorrect.

The correct answer is:  $O(\log \log n)$

Question **6**

Correct

Mark 1 out of 1

“In every instance of the [Stable Matching Problem](#), there is a [stable matching](#) containing a pair  $(m, w)$  such that  $m$  is ranked first on the preference list of  $w$  and  $w$  is ranked first on the preference list of  $m$  “

Select one:

☐ True☒ False ✓

The correct answer is 'False'.

Question **7**

Correct

Mark 1 out of 1

The runtime of the Gale Shapley algorithm for an input instance consisting of  $n$  men and  $n$  women is

Select one or more:

☐  $O(n \log n)$ ☒  $O(n^2)$ 

✓

☐ None of the others☐  $O(n)$ 

Your answer is correct.

The correct answer is:  $O(n^2)$

Question **8**

Correct

Mark 1 out of 1

“In every Stable Marriage problem instance, there always exists a [stable matching](#) where for every matched pair  $(m, w)$ , it is true that both  $m$  and  $w$  do not have the other as their least preferred partner.”

Select one:

- ☐ True
- ☒ False ✓

The correct answer is 'False'.

Question **9**

Correct

Mark 2 out of 2

Consider the [Stable Matching](#) problem with  $n$  men and  $n$  women, where for some value  $k$ , where  $1 \leq k \leq n$ , there are  $k$  good men and  $k$  good women. So there are  $n - k$  bad men and  $n - k$  bad women. Everyone would rather marry any good person than any bad person. That is, any person's preference list, the first  $k$  entries are the good people of the opposite gender (in some order), and the next  $n - k$  entries are of the bad people of the opposite gender (in some order).

For this scenario which of the following statements are TRUE?

Select one or more:

- ☒ In every [stable matching](#), every good man is married to a good woman ✓
- ☒ In every [stable matching](#), every bad man is married to a bad woman ✓
- ☐ There may exist some stable matchings where a good man is married to a bad woman
- ☐ There may exist some stable matchings where a bad man is married to a good woman

Your answer is correct.

The correct answers are: In every [stable matching](#), every good man is married to a good woman, In every [stable matching](#), every bad man is married to a bad woman

Question **10**

Correct

Mark 1 out of 1

A worst valid partner of a person  $p$  is

Select one or more:

- ☐ None of the others
- ☐ The person  $p'$  of the opposite gender who is least preferred by  $p$ .
- ☐ The last person  $p'$  to whom  $p$  proposes in the Gale-Shapley algorithm.
- ☒ The least preferred person  $p'$  of the opposite gender such that there is a [stable matching](#) containing the pair  $(p, p')$  ✓

Your answer is correct.

The correct answer is: The least preferred person  $p'$  of the opposite gender such that there is a [stable matching](#) containing the pair  $(p, p')$

Question **11**

Correct

Mark 1 out of 1

Suppose you have to choose between the following two algorithms:

- Algorithm A solves problems of size  $n$  by recursively solving two subproblems of size  $n - 1$  and then combining the solutions in constant time.
- Algorithm B solves problems of size  $n$  by dividing them into nine subproblems of size  $n/3$ , recursively solving each subproblem, and then combining the solutions in  $O(n^2)$  time.

Which of the following statements are true?

Select one or more:

- ☐ None of the others
- ☐ Runtimes of algorithm A and B are  $O(n^2)$  and  $O(n^2 \log n)$  respectively; A is the faster algorithm
- ☒ Runtimes of algorithm A and B are  $O(2^n)$  and  $O(n^2 \log n)$  respectively; B is the faster algorithm
- ✓
- ☐ Runtimes of algorithm A and B are  $O(2^n)$  and  $O(n^2)$  respectively; B is the faster algorithm

Your answer is correct.

The correct answer is: Runtimes of algorithm A and B are  $O(2^n)$  and  $O(n^2 \log n)$  respectively; B is the faster algorithm

Question **12**

Incorrect

Mark 0 out of 1

How many lines, in asymptotic notation, does the following program print? Assume  $n$  is a power of 2.

```
function foo( $n$ )  
  if  $n > 1$ :  
    print("still going")  
    foo( $n/2$ )  
    foo( $n/2$ )
```

Select one or more:

- ☒  $\Theta(n^2)$
- ✗
- ☐ None of the others
- ☐  $\Theta(n \log n)$
- ☐  $\Theta(n)$

Your answer is incorrect.

The correct answer is:  $\Theta(n)$

Question **13**

Not answered

Marked out of 1

Recall that in the linear time selection algorithm, we picked our pivot  $x$  to be an approximate median of the sequence  $A$ . Suppose we instead picked  $x$  to be any arbitrary element of the sequence  $A$ . Then which of the following statements are True?

Select one or more:

- ☐ The modified algorithm is still correct
- ☐ The modified algorithm no longer has a linear worst case runtime.
- ☐ The modified algorithm is incorrect
- ☐ None of the others
- ☐ The modified algorithm still has a linear worst case runtime.

Your answer is incorrect.

The correct answers are: The modified algorithm is still correct, The modified algorithm no longer has a linear worst case runtime.


Question **14**

Correct

Mark 1 out of 1

While merging two sorted lists of size  $m$  and  $n$  into a single sorted list of size  $m+n$ , the number of comparisons is

Select one or more:

- ☐  $O(n)$
- ☒  $O(m + n)$
- 
- ☐  $O(\log m + \log n)$
- ☐  $O(m)$

Your answer is correct.

The correct answer is:  $O(m + n)$

Question **15**

Incorrect

Mark 0 out of 1

A collection of  $n$  strings, where each string has  $n$  characters, is sorted using Mergesort. What is the worst case runtime of this procedure? Strings are sorted based on the lexicographic order

Select one or more:

- ☐  $O(n \log n)$
- ☐  $O(n^2 \log n)$
- ☐ None of the above.
- ☒  $O(n^2)$



Your answer is incorrect.

The correct answer is:  $O(n^2 \log n)$

Question **16**

Correct

Mark 1 out of 1

The recurrence relation for the runtime of the Tower of Hanoi problem is

Select one or more:

☐  $T(n) = 2T(n - 1) + O(n)$

☐  $T(n) = 2T(n/2) + O(1)$

☒ None of the others ✓

☐  $T(n) = 2T(n - 2) + O(1)$

Your answer is correct.

The correct answer is: None of the others

Question **17**

Correct

Mark 1 out of 1

What is the number of moves to solve the Tower of Hanoi problems for  $n$  disks?

Select one or more:

☒  $2^n - 1$



☐  $2^n$

☐  $n^2 - 1$

☐  $n^2$

Your answer is correct.

The correct answer is:  $2^n - 1$

Question **18**

Correct

Mark 1 out of 1

What is the asymptotic runtime of the following piece of code?

```
void foo() {  
    int i,j;  
    for (i=1;i<n;i++)  
        for(j=1;j<log(i);j++)  
            print("running foo")  
}
```

Select one or more:

☐  $O(\log n)$ ☐  $O(n^2 \log n)$ ☐  $O(n)$ ☒  $O(n \log n)$ 

Your answer is correct.

The correct answer is:  $O(n \log n)$

[◀ Lab Test 1](#)[Jump to...](#)