

Average Speed :

$$* \text{ Avg. Speed} = \frac{\text{Total Distance}}{\text{Total Time}}$$

10. A person covers 18km/hr at 6km/hr, 16km at 8km/hr and 30km at 6km/hr. Then find average speed.

$$\Rightarrow \text{Avg. Speed} = \frac{18 + 16 + 30}{3 + 2 + 5}$$

$$= \frac{64}{10} \Rightarrow 6.4 \text{ km/hr}$$

11. A constant distance from A to B is covered by a man at 40km/hr. The person rides back the same distance at 30km/hr. Find avg. speed during the whole journey.

$$\Rightarrow \begin{array}{ccc} \leftarrow 30 & S_1 \\ A \rightarrow B & 40 & S_2 \end{array}$$

$$\Rightarrow \frac{2S_1 S_2}{S_1 + S_2} = \frac{2 \times 30 \times 40}{70}$$

[This will only work if two distances are equal.]

$$= \frac{2400}{70}$$

$$= 34.28 \text{ km/hr}$$

$$\Rightarrow 40 \times 163 = 6520$$

$$37 \times 162 = 5994$$

$$\therefore A + B + C = 6520 - 5994$$

$$2x + x + x - 9 = 526$$

$$3x - 9 = 526$$

$$3x = 535$$

$$\boxed{x = 178}$$

21. Out of three numbers, the first is twice the second and is half of the third. If average of three numbers is 56, the three numbers in order are:

$$\Rightarrow I = 2II = \frac{1}{2}III$$

$$\therefore \text{Ans} \Rightarrow 48, 24, 96$$

22. The average age of A and B is 20 years. If C were to replace A the average would be 19 and if C were to replace B the average would be 21. What are ages of A, B and C respectively?

$$\Rightarrow A + B = 40$$

$$B + C = 38$$

$$A + C = 42$$

$$\therefore 2(A + B + C) = 120$$

$$\therefore A + B + C = 60$$

$$40 + C = 60$$

$$\boxed{C = 20}$$

$$A = 40 - 20$$

$$\boxed{A = 20}$$

$$\boxed{B = 18}$$

14. A car travels t_1 hours at v_1 km/hr, t_2 hours at v_2 km/hr. What is the average speed.

$$\Rightarrow \text{Avg. Speed} = \frac{\text{Total Distance}}{\text{Total Time}}$$

$$S = \frac{D}{T}$$

$$D = S \times T \\ = \frac{v_1 t_1 + t_2 v_2}{t_1 + t_2}$$

mlb

A person runs the first $1/4^{\text{th}}$ of the distance at 8 km/hr, the next $3/5^{\text{th}}$ at 6 km/hr and remaining distance at 10 km/hr. Find his average speed.

$$\Rightarrow \frac{1}{4} \rightarrow 8 \quad \frac{3}{5} \rightarrow 6 \quad R = 10$$

$$TD = 480$$

$$\frac{1}{4} \times 480 = 120 \quad 8 \quad 15$$

$$\frac{3}{5} \times 480 = 288 \quad 6 \quad 48$$

$$72 \quad 10 \quad 7.2$$

$$\text{Avg. Speed} = \frac{480}{15 + 48 + 7.2} = \frac{480}{70.2} \Rightarrow 6.98$$

Averages

1. If a, b, c, d are five consecutive odd integers, then what is their average?

(a) $a+4$ (b) $(abcde)/5$ (c) $5(a+b+c+d+e)$

(d) $(4)a+8$ (e) None of these

⇒ 1, 3, 5, 7, 9

$$\text{Avg} = \frac{\text{Sum of obs.}}{\text{No. of obs.}} = \frac{25}{5} = 5$$

$$\therefore a+4 \text{ Ans}$$

2. The average of 8 numbers is 14. If 8 is subtracted from each given number, what will be the new average?

(a) 12 (b) 10 (c) 16 (d) 18 (e) None of these

⇒ +, -, ×, ÷

$A+$, $A-$, $A\times$, $A\div$

$$\therefore \text{Ans} \Rightarrow 14 - 8 = 12$$

23. The average temperature of Monday, Tuesday and Wednesday was 40° . The avg. of Tuesday, Wednesday and Thursday was 41° . That for Thursday being 49° , what was temperature of Monday?

$$\Rightarrow \begin{array}{r} M + T + W = 120 \\ - T + W + Th = 123 \\ \hline M - Th = -3 \end{array}$$

$$\therefore M - 49 = -3$$

$$M = 39^\circ$$

24. The average of Suresh's marks in English and History is 55. His average of marks in English and Science is 65. What is difference obtained b/w History and Science?

$$\Rightarrow \begin{array}{r} E + H = 110 \\ E + S = 130 \\ \hline H - S = 20 \end{array}$$

25. The average salary of the entire staff in a office is Rs 130 per month. The avg salary of officers is Rs 540 and that of non-officers is Rs 114. If the number of officers is 16, find the number of non-officers.

$$\Rightarrow \begin{array}{lll} A & N_1 & \bar{X}_1 \\ B & N_2 & \bar{X}_2 \\ C & N_3 & \bar{X}_3 \\ D & N_4 & \bar{X}_4 \end{array}$$

$$\Rightarrow \bar{X} = \frac{S}{N} \quad \left(\text{Avg} = \frac{\text{Sum}}{\text{No. of observations}} \right)$$

$$S = \bar{X} N$$

$$6 \times 22 = 132$$

$$\therefore 132 - (6 \times 7) \Rightarrow 132 - 42 = 90$$

$$\therefore \frac{90}{5} = 18 \text{ years}$$

19. (AMCAT)

The average age of husband and wife was 23 years when they were married 5 years ago. The average age of the husband, the wife and a child who was born during the interval is 20 years now. How old is child?

$$\Rightarrow H + W = 46 \quad 46 + 10$$

$$\therefore H + W + C = 60$$

$$56 + C = 60$$

$$\therefore \boxed{C = 4}$$

20. (AMCAT)

The avg. height of 40 students is 163 cm. On a particular day, three students A, B, C were absent and the average of remaining 37 students was found to be 162 cm. If A, B have equal heights and height of C be less than 2 cm of A, find the height of A.

$$x_c = \frac{N_1 \bar{x}_1 + N_2 \bar{x}_2}{N_1 + N_2}$$

$$130 = \frac{16 \times 540 + x(114)}{16 + x}$$

$$x = 410$$

26. A batsman in his 19 innings, missed a century by 2 runs and thereby increases his average by 3. What is his average after 19 innings.

$$\Rightarrow x + 3 = \frac{18x + 1 \times 98}{19} \quad \begin{array}{l} 1 \rightarrow 98 \\ 18 \rightarrow x \\ x_c = x + 3 \end{array}$$

$$19x + 57 = 18x + 98$$

$$x = 41$$

$$\therefore \text{Ans} \Rightarrow 41 + 3 = 44$$

27. In a coconut grove, $(x+2)$ trees yield 60 nuts per year per tree, x trees yield 120 nuts per year per tree and $(x-2)$ trees yield 180 nuts per year per tree. If the average yield per year per tree be 100, find x .

$$\Rightarrow 100 = \frac{60(x+2) + 120x + 180(x-2)}{x+2+x+x-2}$$

$$\boxed{x = 4}$$

12. A person divides his total route of journey into three equal parts and decide to travel the three parts with speeds of 20, 15, 10 km/hr. Find the avg speed.

$$\Rightarrow$$

60	20	3 hr
60	15	4 hr
60	10	6 hr

$$\therefore \text{Avg. Speed} = \frac{180}{13} \Rightarrow 13 \frac{1}{13} \text{ km/hr}$$

* Formula for 3 equal distances $\Rightarrow \frac{3S_1 S_2 S_3}{S_1 S_2 + S_2 S_3 + S_1 S_3}$

E-Limit

13. An aeroplane covers the four sides of square fields at speed of 200, 400, 600, 800 km/hr. Then what is average speed.

$$\Rightarrow$$

2400	200	12
2400	400	6
2400	600	4
2400	800	3

$$\text{Avg Speed} = \frac{4 \times 2400}{25}$$

$$= 384 \text{ km/hr}$$

16. The average age of three boys is 15 years. Their ages are in the ratio 3:5:7. Then the age of oldest is:

$$\Rightarrow 3 : \overset{\times 3}{\textcircled{5}} : 7$$

$$9 \quad 15 \quad 21$$

$\therefore \text{Ans} \Rightarrow 21 \text{ years}$

17. The population of town increased by 20% during the first year, by 25% during next year and 44% during third year. Find the average rate of increase during 3 years.

$$\Rightarrow \begin{array}{ccccccc} 100 & 120 & 25\% \times 120 & 150 & 44\% & 216 \\ & & = 25 \times 120 = 30 & & & \\ & & 100 & & & \end{array}$$

$$40 + 4 = 4(10\%) + 4(1\%) \quad [10\% \text{ of } 150 \text{ \& } 1\% \text{ of } 150]$$

$$\Rightarrow 4(15) + 4(1.5) = 60 + 6 \Rightarrow 66$$

$$\therefore \text{Ans} \Rightarrow \frac{116}{3} = 38\frac{2}{3}\%$$

- mp
18. The average age of a family of 6 members is 22 years. If the age of the youngest be 7 years, the average age of the family at the birth of youngest members was:

3. The average of x numbers is $3x$. If $x-1$ is subtracted from each given number, what will be the new average?

$$\Rightarrow 3x - (x-1)$$

$$\Rightarrow 3x - x + 1$$

$$= 2x + 1$$

4. The average of 40 numbers is 40.5. If each of the number is divided by 15, find the average of new set of numbers.

$$\Rightarrow \frac{40.5}{15} = 2.7$$

5. The average of 8 numbers is 21. If each number is multiplied by 8, find the average of new set of numbers.

$$\Rightarrow 21 \times 8 = 168$$

6. The average age of 24 students and the class teacher is 16 years. If the teacher's age is excluded, the average reduces by 1 year. What is the age of class teacher?

$$\Rightarrow S + T = 16$$

$$\begin{array}{r} \text{---} \quad \text{---} \quad \text{---} \quad T \\ 16 \ 16 \ 16 \quad 16 \\ 24 \times 1 = 24 \end{array}$$

$$\therefore 24 + 16 \Rightarrow 40 \text{ years}$$

7. The average age of 34 boys in a class is 14 years. If the teacher's age is included the average age of boys and the teacher becomes 15 years. What is the teacher's age?

$$\Rightarrow 34 \Rightarrow 14$$

$$34 + 15 \Rightarrow 49 \text{ years}$$

8. The avg. weight of 8 persons increases by 1.5 kg. If a person whose weight is 65 kg is replaced by a new person, what could be the weight of new persons?

$$\Rightarrow 1.5 \times 8 = 12$$

$$\therefore \text{Weight} = 65 + 12 = 77$$

9. In a class there are 24 boys whose avg. age is decreased by 3 months, when 1 boy aged 20 years is replaced by a new boy. Find the age of new boy

$$\Rightarrow 24 \times 3 = \frac{72}{12} \Rightarrow 6 \text{ years}$$

$$\therefore +20 - 6 = 14 \text{ years}$$